Load Required Packages

```
In [2]:
        import os, sys
        import pandas as pd
        import scipy.io
        import numpy as np
        from scipy.spatial.distance import pdist
        import time
        import math
        import keras
        import matplotlib.pyplot as plt
        from tensorflow.keras.models import Sequential
        from sklearn import ensemble
        from sklearn.metrics import accuracy_score, make_scorer, classification_report
        from statistics import mean
        from sklearn.ensemble import GradientBoostingClassifier
        import PIL
        from PIL import Image
        from scipy.io import loadmat
        from sklearn.model_selection import train_test_split, cross_validate,GridSearc
        hCV
        from keras.layers import Dense, Activation, Flatten, Input, Dropout
        from keras.layers import BatchNormalization
        from keras.models import Model
        from keras import initializers
        from keras.optimizers import Adam
        from keras.utils import to categorical
```

Using TensorFlow backend.

Part I Baseline Model: GBM

1. Provide directories for training/testing images.

2. Train/Test Split Feature Extraction

```
In [16]: info = pd.read csv(train label path)
         # read mat file and store coordinates in mat
         m = []
         for idx in info['Index']:
             file = "%04d.mat"%(idx)
             m.append( scipy.io.loadmat( os.path.join( train_pt_dir, file ) ))
         mat = [x[[i for i in x.keys() if not i in [' header ', ' version ', ' glo
         bals__']][0]] for x in m]
         c = np.array([pdist(x) for x in mat[0:]])
In [17]: train idx, test idx = train test split(info['Index'], test size=0.2, random st
         ate=123)
In [18]: | start time test=time.time()
         train_features=np.array([pdist(mat[i-1]) for i in train_idx ])
         print("baseline train features extracting takes %s seconds" % round((time.time
         () - start time test),3))
         start time train=time.time()
         test_features=np.array(([pdist(mat[i-1]) for i in test_idx ]))
         print("base line test features extracting takes %s seconds" % round((time.time
          () - start time train),3))
         train labels=info.emotion idx[train idx-1]
         test labels=info.emotion idx[test idx-1]
         print(train features.shape,train labels.shape)
         baseline train features extracting takes 0.121 seconds
         base line test features extracting takes 0.027 seconds
         (2000, 3003) (2000,)
```

3. Train a Baseline GBM model with training features and responses

```
In [63]: | #baseline GBM
          baseline = GradientBoostingClassifier(learning rate=0.1, n estimators=100,max
          depth=3, min samples split=2, min samples leaf=1, subsample=1,max features='sq
          rt', random state=10)
          start_time=time.time()
          baseline.fit(train_features, train_labels)
          print("training model takes %s seconds" % round((time.time() - start time),3
          ))
          predictors=list(train_features)
          print('Accuracy of the GBM on test set: {:.3f}'.format(baseline.score(test_fea
          tures, test labels)))
          start time1 = time.time()
          pred=baseline.predict(test_features)
          print("testing model takes %s seconds" % round((time.time() - start time1),3))
          print(classification_report(test_labels, pred))
         training model takes 66.134 seconds
         Accuracy of the GBM on test set: 0.440
         testing model takes 0.044 seconds
                        precision
                                      recall
                                             f1-score
                                                          support
                     1
                             0.50
                                        0.56
                                                  0.53
                                                               18
                     2
                                                               19
                             0.65
                                        0.68
                                                  0.67
                     3
                             0.40
                                        0.56
                                                               25
                                                  0.47
                     4
                             0.50
                                        0.52
                                                  0.51
                                                               21
                     5
                             0.58
                                        0.61
                                                  0.59
                                                               18
                     6
                             0.63
                                        0.46
                                                  0.53
                                                               26
                     7
                                                               20
                             0.40
                                        0.50
                                                  0.44
                     8
                             0.73
                                                  0.71
                                        0.69
                                                               16
                     9
                             0.78
                                        0.56
                                                  0.65
                                                               25
                    10
                             0.45
                                        0.45
                                                  0.45
                                                               20
                    11
                             0.41
                                        0.50
                                                  0.45
                                                               24
                    12
                             0.44
                                        0.25
                                                  0.32
                                                               32
                    13
                             0.12
                                        0.17
                                                  0.14
                                                               24
                    14
                             0.54
                                        0.57
                                                  0.55
                                                               23
                    15
                             0.59
                                        0.45
                                                  0.51
                                                               22
                    16
                             0.73
                                        0.73
                                                  0.73
                                                               22
                    17
                             0.37
                                        0.42
                                                  0.39
                                                               26
                    18
                             0.31
                                        0.23
                                                  0.26
                                                               22
                    19
                             0.23
                                                               23
                                        0.22
                                                  0.22
                    20
                             0.17
                                        0.30
                                                  0.21
                                                               20
                             0.46
                    21
                                        0.32
                                                  0.38
                                                               34
                    22
                             0.25
                                        0.20
                                                  0.22
                                                               20
              accuracy
                                                  0.44
                                                              500
                                                              500
                             0.47
                                        0.45
                                                  0.45
             macro avg
```

4. Parameter tuning

weighted avg

0.44

0.44

500

0.46

4.1 parameter tuning Learning_rate,n_estimator

4.2 Tuning Max_depth, Min_samples_split

```
In [10]: #param_test2 = {'max_depth':range(1,16,2), 'min_samples_split':range(2,102,2
0)}
    #tuning2 = GridSearchCV(estimator = GradientBoostingClassifier(learning_rate=
0.05, n_estimators=500, max_features='sqrt', subsample=1, random_state=10),
    #param_grid = param_test2, scoring='accuracy',n_jobs=4,iid=False, cv=5)
    #tuning2.fit(train_features,train_labels)
    #tuning2.cv_results_, tuning2.best_params_, tuning2.best_score_
```

4.3 Parameter Tuning:min_samples_split,min_samples_leaf

4.4 Parameter Tuning Max_features

4.5 Parameter Tuning Subsample

5. Final Parameter set at: learning_rate=0.05, n_estimators=500,max_depth=5,min_samples_split=62, min_samples_leaf=30,random_state=10,max_features='sqrt',subsample=1.0

```
In [19]:
         baseline tune=GradientBoostingClassifier(learning rate=0.05, n estimators=500,
          max depth=5,min samples split=62, min samples leaf=30,random state=10,max feat
          ures='sqrt',subsample=1.0)
          start time=time.time()
          baseline tune.fit(train features, train labels)
          print("training model takes %s seconds" % round((time.time() - start_time),3
          ))
          predictors=list(train features)
          print('Accuracy of the GBM on test set: {:.3f}'.format(baseline_tune.score(tes
          t features,test labels)))
          start_time1 = time.time()
          pred=baseline_tune.predict(test_features)
          print("testing model takes %s seconds" % round((time.time() - start_time1),3))
          print(classification report(test labels, pred))
         training model takes 282.097 seconds
         Accuracy of the GBM on test set: 0.486
         testing model takes 0.358 seconds
                        precision
                                     recall f1-score
                                                         support
                     1
                             0.57
                                       0.72
                                                  0.63
                                                              18
                     2
                             0.70
                                       0.84
                                                              19
                                                  0.76
                     3
                             0.41
                                       0.52
                                                  0.46
                                                              25
                     4
                             0.43
                                       0.57
                                                  0.49
                                                              21
                     5
                             0.57
                                       0.72
                                                  0.63
                                                              18
                     6
                             0.72
                                       0.50
                                                  0.59
                                                              26
                     7
                             0.58
                                       0.55
                                                  0.56
                                                              20
                     8
                             0.75
                                       0.75
                                                  0.75
                                                              16
                    9
                             0.80
                                       0.64
                                                  0.71
                                                              25
                    10
                             0.41
                                       0.45
                                                  0.43
                                                              20
                             0.48
                                                  0.56
                                                              24
                    11
                                       0.67
                    12
                             0.44
                                       0.34
                                                  0.39
                                                              32
                    13
                             0.22
                                       0.21
                                                  0.21
                                                              24
                    14
                             0.52
                                       0.65
                                                  0.58
                                                              23
                    15
                             0.61
                                       0.50
                                                  0.55
                                                              22
                                                              22
                    16
                             0.80
                                       0.73
                                                  0.76
                    17
                             0.29
                                                              26
                                       0.31
                                                  0.30
                    18
                             0.26
                                       0.23
                                                  0.24
                                                              22
                    19
                             0.26
                                       0.26
                                                  0.26
                                                              23
                    20
                             0.24
                                       0.30
                                                  0.27
                                                              20
                    21
                             0.52
                                       0.38
                                                  0.44
                                                              34
                    22
                             0.38
                                       0.15
                                                  0.21
                                                              20
             accuracy
                                                  0.49
                                                             500
                             0.50
                                       0.50
                                                  0.49
            macro avg
                                                             500
```

Increase accuracy from 0.440 to 0.486 after tuning

0.49

weighted avg

0.49

0.48

500

Part II Advanced Model: Densely-connected Neural Networks

Procedure

BatchNorm -> Densely-connected NN -> ReLu -> Dropout -> BatchNorm -> Densely-connected NN -> ReLu -> Dropout -> Densely-connected NN -> ReLu -> Dropout -> Densely-connected NN -> ReLu -> Densely-connected NN -> Softmax -> Output

1. Provide directories for training/testing images.

```
In [3]: """
    Path
    """
    DATA_PATH = "../data/train_set"
    POINTS_FOLDER = os.path.join(DATA_PATH, "points")
    LABELS_FOLDER = DATA_PATH
```

2. Train/Test Split Feature Extraction

```
In [4]: def read labels():
            labels_df = pd.read_csv(os.path.join(LABELS_FOLDER, 'label.csv'))
            labels_df = labels_df.loc[:,['emotion_idx','emotion_cat','type']]
            return labels df
        def read_points():
            files = [file for file in os.listdir(POINTS FOLDER) if file.endswith('.ma
        t')]
            files.sort()
            face points = np.zeros((len(files), 78, 2))
            for index, filename in enumerate(files):
                face_points_dict = loadmat(os.path.join(POINTS_FOLDER, filename))
                face_points[index] = face_points_dict.get('faceCoordinatesUnwarped',
         face_points_dict.get('faceCoordinates2'))
            return face points
        points = read_points()
        labels = read labels()
        ### train test split
        X_points_train, X_points_test, y_train, y_test = train_test_split(points,label
        s,test_size=0.2, random_state=666)
        ### Feature Extraction time on training set:
        feature training start = time.time()
        X_train = np.zeros((X_points_train.shape[0], 3003))
        for i in range(X points train.shape[0]):
            current = X points train[i]
            X_train[i,] = pdist(current)
        feature training end = time.time()
        y_train = y_train['emotion_idx']
        y_train = to_categorical(y_train)[:,1:]
        print("Feature Extraction time on training set:","%s seconds"%(feature_trainin
        g_end - feature_training_start))
        ### Feature Extraction time on test set:
        feature test start = time.time()
        X_test = np.zeros((X_points_test.shape[0], 3003))
        for i in range(X_points_test.shape[0]):
            current = X points test[i]
            X_test[i,] = pdist(current)
        feature_test_end = time.time()
        y test = y test['emotion idx']
        y_test = to_categorical(y_test)[:,1:]
        print("Feature Extraction time on test set:","%s seconds"%(feature_test_end -
        feature test start))
```

Feature Extraction time on training set: 0.0984201431274414 seconds Feature Extraction time on test set: 0.026224851608276367 seconds

3. Train model

```
In [5]: input shape = [3003]
        input layer = Input(input shape)
        x = BatchNormalization(momentum = 0.88)(input layer)
        x = Dense(22*10,activation='relu',kernel initializer=initializers.glorot norma
        1(seed=4))(x)
        x = Dropout(0.25)(x)
        x = BatchNormalization()(x)
        x = Dense(22*8,activation='relu',kernel_initializer=initializers.glorot_normal
        (seed=4))(x)
        x = Dropout(0.25)(x)
        x = Dense(22*4,activation='relu',kernel_initializer=initializers.glorot_normal
        (seed=4))(x)
        x = Dropout(0.25)(x)
        x = Dense(22*2,activation='relu',kernel_initializer=initializers.glorot_normal
        (seed=4))(x)
        output_layer = Dense(22,activation='softmax',kernel_initializer=initializers.g
        lorot normal(seed=4))(x)
        model2 = Model(input_layer,output_layer)
```

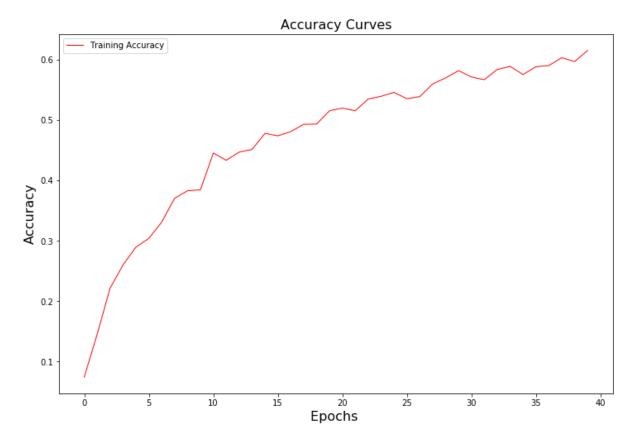
```
In [6]: start_time = time.time()
    model2.compile(loss='categorical_crossentropy',optimizer = Adam(lr=0.001),metr
    ics=['accuracy'])
    model_history = model2.fit(X_train,y_train,epochs = 40,validation_data=[X_test
    ,y_test])
    print("training model takes %s seconds" % round((time.time() - start_time),3
    ))
```

```
Train on 2000 samples, validate on 500 samples
Epoch 1/40
2000/2000 [============== ] - 11s 6ms/step - loss: 3.0909 - ac
curacy: 0.0745 - val loss: 2.8831 - val accuracy: 0.1280
Epoch 2/40
2000/2000 [============== ] - 3s 2ms/step - loss: 2.7894 - acc
uracy: 0.1450 - val loss: 2.5699 - val accuracy: 0.1820
Epoch 3/40
2000/2000 [================ ] - 3s 2ms/step - loss: 2.4786 - acc
uracy: 0.2215 - val loss: 2.1691 - val accuracy: 0.2880
Epoch 4/40
2000/2000 [============== ] - 4s 2ms/step - loss: 2.2981 - acc
uracy: 0.2600 - val loss: 2.0427 - val accuracy: 0.3080
2000/2000 [============== ] - 4s 2ms/step - loss: 2.1345 - acc
uracy: 0.2895 - val loss: 1.8898 - val accuracy: 0.3800
Epoch 6/40
2000/2000 [============== ] - 4s 2ms/step - loss: 2.0055 - acc
uracy: 0.3040 - val loss: 1.8210 - val accuracy: 0.3620
Epoch 7/40
uracy: 0.3310 - val_loss: 1.7562 - val_accuracy: 0.3840
Epoch 8/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.8543 - acc
uracy: 0.3705 - val_loss: 1.6571 - val_accuracy: 0.4320
Epoch 9/40
2000/2000 [================ ] - 3s 2ms/step - loss: 1.7891 - acc
uracy: 0.3830 - val_loss: 1.6187 - val_accuracy: 0.4100
Epoch 10/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.8106 - acc
uracy: 0.3845 - val_loss: 1.6062 - val_accuracy: 0.4460
Epoch 11/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.6791 - acc
uracy: 0.4455 - val loss: 1.5587 - val accuracy: 0.4740
Epoch 12/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.6583 - acc
uracy: 0.4335 - val_loss: 1.5786 - val_accuracy: 0.4380
Epoch 13/40
2000/2000 [============ ] - 3s 2ms/step - loss: 1.6121 - acc
uracy: 0.4470 - val_loss: 1.5002 - val_accuracy: 0.4920
Epoch 14/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.5910 - acc
uracy: 0.4515 - val_loss: 1.5508 - val_accuracy: 0.4800
Epoch 15/40
uracy: 0.4780 - val loss: 1.5120 - val accuracy: 0.5020
Epoch 16/40
2000/2000 [=========== ] - 3s 2ms/step - loss: 1.5371 - acc
uracy: 0.4740 - val_loss: 1.4611 - val_accuracy: 0.4800
Epoch 17/40
2000/2000 [=============== ] - 4s 2ms/step - loss: 1.5343 - acc
uracy: 0.4810 - val_loss: 1.4801 - val_accuracy: 0.5060
Epoch 18/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.4862 - acc
uracy: 0.4930 - val_loss: 1.4538 - val_accuracy: 0.5200
Epoch 19/40
2000/2000 [============ ] - 3s 2ms/step - loss: 1.4885 - acc
```

```
uracy: 0.4935 - val loss: 1.4841 - val accuracy: 0.5020
Epoch 20/40
2000/2000 [================ ] - 3s 1ms/step - loss: 1.4582 - acc
uracy: 0.5155 - val loss: 1.4644 - val accuracy: 0.4960
Epoch 21/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.4012 - acc
uracy: 0.5200 - val loss: 1.5052 - val accuracy: 0.4720
Epoch 22/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.3938 - acc
uracy: 0.5155 - val loss: 1.4515 - val accuracy: 0.5200
Epoch 23/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.3690 - acc
uracy: 0.5350 - val loss: 1.3926 - val accuracy: 0.5120
Epoch 24/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.3682 - acc
uracy: 0.5395 - val loss: 1.3942 - val accuracy: 0.5260
Epoch 25/40
2000/2000 [============== ] - 5s 2ms/step - loss: 1.3361 - acc
uracy: 0.5460 - val loss: 1.4021 - val accuracy: 0.5360
Epoch 26/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.3434 - acc
uracy: 0.5355 - val loss: 1.4091 - val accuracy: 0.5220
Epoch 27/40
2000/2000 [============== ] - 3s 2ms/step - loss: 1.3059 - acc
uracy: 0.5390 - val_loss: 1.4268 - val_accuracy: 0.5260
Epoch 28/40
2000/2000 [================ ] - 4s 2ms/step - loss: 1.2742 - acc
uracy: 0.5600 - val_loss: 1.4122 - val_accuracy: 0.5260
Epoch 29/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.2681 - acc
uracy: 0.5700 - val_loss: 1.3886 - val_accuracy: 0.5200
Epoch 30/40
2000/2000 [============ ] - 4s 2ms/step - loss: 1.2435 - acc
uracy: 0.5820 - val loss: 1.4358 - val accuracy: 0.5220
Epoch 31/40
2000/2000 [=============== ] - 4s 2ms/step - loss: 1.2800 - acc
uracy: 0.5715 - val_loss: 1.3830 - val_accuracy: 0.5280
Epoch 32/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.2505 - acc
uracy: 0.5670 - val_loss: 1.3526 - val_accuracy: 0.5280
Epoch 33/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.2514 - acc
uracy: 0.5840 - val_loss: 1.3533 - val_accuracy: 0.5260
Epoch 34/40
2000/2000 [============ ] - 3s 1ms/step - loss: 1.1825 - acc
uracy: 0.5890 - val loss: 1.3739 - val accuracy: 0.5300
Epoch 35/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.2138 - acc
uracy: 0.5755 - val_loss: 1.4148 - val_accuracy: 0.5480
Epoch 36/40
2000/2000 [============== ] - 4s 2ms/step - loss: 1.1915 - acc
uracy: 0.5885 - val loss: 1.3319 - val accuracy: 0.5320
Epoch 37/40
2000/2000 [============== ] - 3s 2ms/step - loss: 1.1862 - acc
uracy: 0.5905 - val_loss: 1.3199 - val_accuracy: 0.5440
Epoch 38/40
2000/2000 [================ ] - 3s 2ms/step - loss: 1.1417 - acc
```

```
In [7]: fig, ax = plt.subplots(figsize=[12,8])
    ax.plot(model_history.history['accuracy'],'r',linewidth=1.0, label = 'Training
    Accuracy')
    ax.legend()
    plt.xlabel('Epochs ',fontsize=16)
    plt.ylabel('Accuracy',fontsize=16)
    plt.title('Accuracy Curves',fontsize=16)
```

Out[7]: Text(0.5, 1.0, 'Accuracy Curves')



4. Test accuracy

5. Predicted label

```
In [9]:
        predict DATA PATH = "../data/test set predict"
        POINTS FOLDER = os.path.join(predict DATA PATH, "points")
        predict_points = read_points()
        predict start = time.time()
        X_predict = np.zeros((predict_points.shape[0], 3003))
        for i in range(predict_points.shape[0]):
            current = predict points[i]
            X_predict[i,] = pdist(current)
        predict_end = time.time()
        print("Feature Extraction time on test set:","%s seconds"%(predict_end - predi
        ct start))
        Feature Extraction time on test set: 0.17246484756469727 seconds
```

```
In [27]: | y_predict = []
         for i in model2.predict(X_predict):
             y_predict.append(np.argmax(i) + 1)
In [12]: | df advance = pd.DataFrame(data = y predict)
         df advance.to csv('../output/baseline prediction.csv')
In [25]: df_baseline = pd.DataFrame(data = baseline_tune.predict(X_predict))
         df baseline.to csv('../output/baseline prediction1.csv')
```