Fundamentals of Physics

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2 Motion Along a Straight Line

2.1 Position, displacement, and average velocity

Magnitude
$$\Rightarrow \Delta x_1 - x_2$$

Average velocity $\Rightarrow v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1}$
Magnitude $\Rightarrow \frac{\text{total distance}}{\Delta t}$

2.2 Instantaneous velocity and speed

Instantaneous velocity
$$\Rightarrow \lim_{\Delta t \to 0} \frac{\Delta x}{\Delta t} = \frac{\mathrm{d}x}{\mathrm{d}t}$$

2.3 Acceleration

Average acceleration
$$\Rightarrow a_{\text{avg}} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t}$$

Acceleration at a point $\Rightarrow a = \frac{\mathrm{d}v}{\mathrm{d}t}$

 \star If the signs of the velocity and acceleration of a particle are the same, the speed of the particle increases. If the signs are opposite, the speed decreases.

2.4 Constant acceleration

The following five equations describe the motion of a particle with constant acceleration.

Nr	Equation	Missing quantity
1	$v = v_0 + at$	$x-x_0$
2	$x - x_0 = v_0 t + \frac{1}{2} a t^2$	v
3	$v^2 = v_0^2 + 2a(x - x_0)$	t
4	$x - x_0 = \frac{1}{2}(v_0 + v_t)t$	a
5	$x - x_0 = vt - \frac{1}{2}at^2$	v_0

2.5 Free-fall acceleration

* The free-fall acceleration near Earth's surface is $a = -g = -9.8 \text{ m/s}^2$, and the magnitude of the acceleration is $g = 9.8 \text{ m/s}^2$. Do not substitute -9.8 m/s^2 for g.

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2.6 Graphical integration in motion analysis

• On a graph of acceleration a versus time t, • On a graph of velocity v versus time t, the the change in the velocity is given by:

$$v_1 - v_0 = \int_{t_0}^{t_1} a \, dt. \qquad x_1 - x_0 = \int_{t_0}^{t_1} v \, dt,$$

3 Vectors

3.1 Vectors and their components

- Vector has magnitude and direction.
- Scalar quantities that can are fully described by a magnitude (a numerical value alone), without any direction.
- Vector sum (resoultant) are the product from adding two or more vecotrs.

$$\vec{s} = \vec{a} + \vec{b},$$

$$\vec{a} + \vec{b} = \vec{b} + \vec{a}$$
 (commutative law)
$$(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$$
 (associative law)
$$\vec{d} = \vec{a} - \vec{b} = \vec{a} + (-\vec{b})$$
 (vector subtraction)

A component of a vector is the projection of a vector on an axis.

Finding the components:
$$a_x = a \cos \theta$$
 and $a_y = a \sin \theta$

If we know a vectors \boldsymbol{a}_x and \boldsymbol{a}_y and want magnitude or angle we can use:

$$a = \sqrt{a_x^2 + a_y^2}$$
 and $\theta = \tan^{-1}(\frac{a_y}{a_x})$

3.2 Unit vectors, adding vectors by components

Unit vector - is a vector with magnitude of exactly 1.

$$r_x = a_x + b_x$$

$$\vec{r} = \vec{a} + \vec{b} \quad r_y = a_y + b_y$$

$$r_z = a_z + b_z$$

We can write a vector \vec{a} in terms of unit vectors as: $\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$

3.3 Multiplying vectors

There are two ways of multiplying vectors, one way produces a scalar (scalar product) and the other way produces a new vector (vector product):

Feature	Scalar product (dot)	Vector product (cross)
Symbol	$ec{A}\cdotec{B}$	$ec{A} imesec{B}$
Result	Scalar (number)	Vector
Formula	$AB\cos\theta$	$AB\sin\theta$
Component form	$A_x B_x + A_y B_y + A_z B_z$	$(A_yB_z - A_zB_y, A_zB_x - A_xB_z, A_xB_y - A_yB_x)$

4 Motion in two and three dimentions

4.1 Position and displacment

Position vector - a vector that extends from a reference point (usually the origin) to the particle.

• Unit vector notation: $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$

• Particle's displacement: $\Delta \vec{r} = \vec{r}_2 - \vec{r}_1$

• Alternative form: $\Delta \vec{r} = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}$ $= \Delta x \,\hat{i} + \Delta y \,\hat{j} + \Delta z \,\hat{k}$

4.2 Average velocity and instantaneous velocity

• If a particle undergoes a displacment $\Delta \vec{r}$ in time interval Δt , it's average velocity \vec{v}_{avg} for that time interval is: $\vec{v}_{avg} = \frac{\Delta \vec{r}}{\Delta t}$.

• As Δt is shrank to 0, $\vec{v_{avg}}$ reaches a limit called either the velocity or the instantenious velocity \vec{v} : $\vec{v} = \frac{d\vec{r}}{dt} = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$

 \star The direction of the instantaneous velocity \vec{v} of a particle is always tangent to the particles path at the particles position.

4.3 Average acceleration and instantanious acceleration

• If a particle's velocity changes from $\vec{v_1}$ to $\vec{v_2}$ in time interval Δt , it's average acceleration during Δt is:

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$$\vec{a}_{avg} = \frac{\vec{v}_2 - \vec{v_1}}{\Delta t} = \frac{\Delta \vec{v}}{\Delta t}$$

4.4 Projectile motion

When you throw an object at an angle:

- It moves forward at a constant horizontal speed.
- It moves up and then down because of gravity pulling it downward.
- The path it follows is a parabola.
- \star In projectile motion, the horizontal motion and the vertical motion are independent of each other; that is, neither motion affects the other.

The vertical motion of a projectile is governed by the following kinematic equations:

$$v_y = v_0 \sin \theta_0 - gt,$$
 $v_y^2 = (v_0 \sin \theta_0)^2 - 2g(y - y_0).$

The trajectory (path) of a particle in projectile motion is parabolic and is given by

$$y = (\tan \theta_0)x - \frac{gx^2}{2(v_0 \cos \theta_0)^2}$$
, if x_0 and y_0 are zero.

The equations of motion for the particle (while in flight) can be written as

$$x - x_0 = (v_0 \cos \theta_0)t,$$
 $y - y_0 = (v_0 \sin \theta_0)t - \frac{1}{2}gt^2,$

The particle's horizontal range R, which is the horizontal distance from the launch point to the point at which the particle returns to the launch height, is

$$R = \frac{v_0^2}{q} \sin 2\theta_0.$$

 \star The horizontal range R is maximum for a launch angle of 45°.

4.5 Uniform circular motion

$$a = \frac{v^2}{r}$$
 (centripetal acceleration), $T = \frac{2\pi r}{v}$ (period).

4.6 Relative motion in one dimention

In relative motion, two reference frames moving at constant velocity measure different velocities for the same particle but the same acceleration. The relationship between the measured velocities is

$$\vec{v}_{PA} = \vec{v}_{PB} + \vec{v}_{BA},$$

and since the frames move at constant velocity,

$$\vec{a}_{PA} = \vec{a}_{PB}$$
.

* Observers on different frames of reference that move at constant velocity relative to each other will measure the same acceleration for a moving particle.

4.7 Relative motion in two dimentions

In two-dimensional relative motion, two reference frames moving at constant velocity measure different velocities for a particle but the same acceleration. The relationship between the measured velocities is

$$\vec{v}_{PA} = \vec{v}_{PB} + \vec{v}_{BA},$$

and since the frames move at constant velocity,

$$\vec{a}_{PA} = \vec{a}_{PB}$$
.

5 Force and motion - I

5.1 Newton's first and second laws

- * Newton's First Law: If no *net* force acts on a body ($\vec{F}_{net} = 0$), the body's velocity cannot change; that is, the body cannot accelerate.
- * An inertial reference frame is one in which Newton's laws hold.
- * Newton's Second Law: The net force on a body is equal to the product of the body's mass and its acceleration.
 - The law can be written as:

$$\vec{F}_{\text{net}} = m\vec{a}$$
 (Newton's second law).

• In component form:

$$F_{\text{net},x} = ma_x, \qquad F_{\text{net},y} = ma_y, \qquad F_{\text{net},z} = ma_z.$$

 \star The acceleration component along a given axis is caused *only by* the sum of the force components along that *same* axis, and not by force components along any other axis.

5.2 Some particular forces

$$F_g = mg$$
.

* The weight W of a body is equal to the magnitude F_g of the gravitational force on the body.

$$W = mg$$
 (weight),

* When a body presses against a surface, the surface (even a seemingly rigid one) deforms and pushes on the body with a normal force \vec{F}_N that is perpendicular to the surface.

5.3 Applying Newton's laws

* Newton's Third Law: When two bodies interact, the forces on the bodies from each other are always equal in magnitude and opposite in direction.

$$F_{BC} = F_{CB}$$
 (equal magnitudes)

6 Force and motion - II

6.1 Friction

Two types of friction:

- Static frictional force Prevents motion when a body is at rest. Is written as $\vec{f_s}$.
- Kinetic frictional force What friction becomes when sliding begins. Is written as \vec{f}_k .

Properties of friction:

- 1. If a body does not move, the static frictional force \vec{f}_s balances the component of the applied force that is parallel to the surface.
- 2. The maximum static friction is given by

$$f_{s,\max} = \mu_s F_N,$$

where μ_s is the coefficient of static friction and F_N is the normal force.

3. Once the body starts sliding, the frictional force becomes kinetic and is given by

$$f_k = \mu_k F_N$$

where μ_k is the coefficient of kinetic friction.

6.2 The drag force and terminal speed

When a body moves through a fluid, it experiences a drag force \vec{D} opposing its motion. The drag magnitude depends on the relative speed v and is given by

$$D = \frac{1}{2}C\rho Av^2,$$

where C is the drag coefficient, ρ is the fluid density, and A is the cross-sectional area.

At terminal velocity, the drag force equals the gravitational force, and the speed becomes constant:

$$v_t = \sqrt{\frac{2F_g}{C\rho A}}.$$

6.3 Uniform Circular Motion

 \star A centripetal force accelerates a body by changing the direction of the body's velocity without changing the body's speed.

A particle moving in a circle of radius R at constant speed v has a centripetal acceleration directed toward the center:

$$a = \frac{v^2}{R}.$$

This acceleration is caused by a net centripetal force of magnitude

$$F = \frac{mv^2}{R},$$

where m is the particle's mass.

7 Kinetic energy

7.1 Kinetic Energy

The kinetic energy K associated with the motion of a particle of mass m and speed v, where v is well below the speed of light, is

$$K = \frac{1}{2}mv^2$$
 (kinetic energy).