

# Summary

## Learned Skills

1. Applied calibration and preformat in experiment, fixed pile up.
2. Set up the NLOS simulation from scratch: considering noise, windowing effect, Lambertian shading, vignetting.
3. Utilized the simulation to explore the effect of FoV size, exposure time, non-confocal geometry, pulse width, depth resolution.

## Contribution

1. Developed stitch method for SPAD array FoV. (W5, W9)
2. Developed interpolation method for camera shooting from an angle. (W11)
3. Implemented 2-stage RSD for non-planar wall, added mask, shading and correct phase, and verified the algorithm on real data. (W13-21)

# W0: Experiment Setup



$$\frac{\text{average power}}{\text{repetition rate}} \times \frac{1}{h\nu} \times \left( \frac{20\text{cm} \times 20\text{cm}}{2\pi(1.5\text{m})^2} \right)^2 \times \frac{80\text{cm} \times 80\text{cm}}{2\pi(1.5\text{m})^2}$$

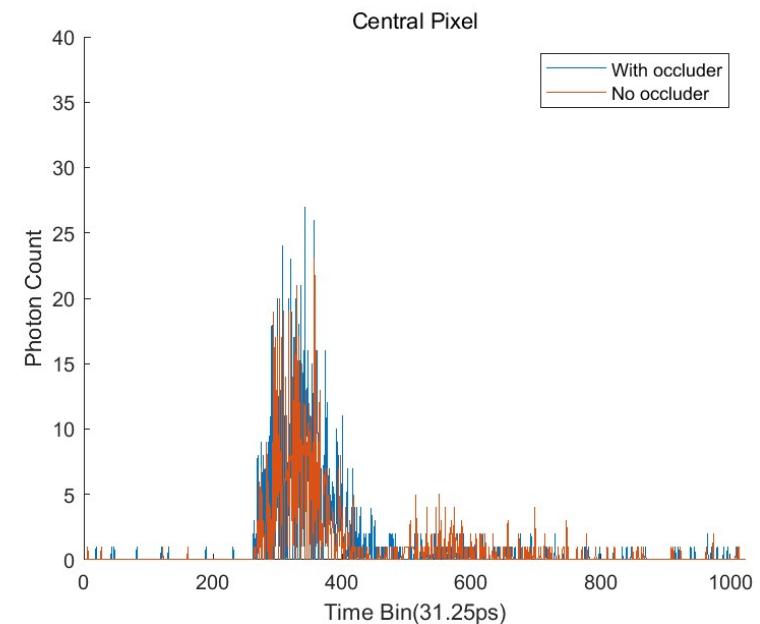
1W, 500k, 440nm

FoV size

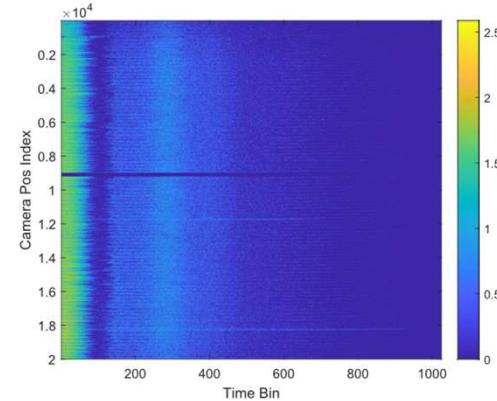
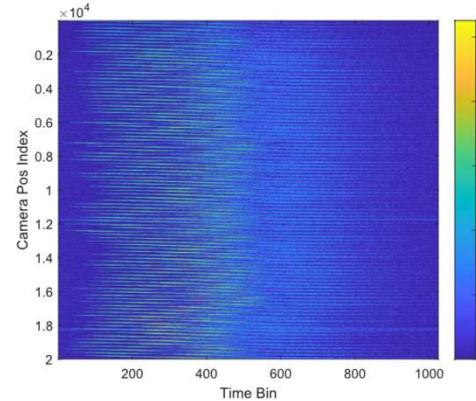
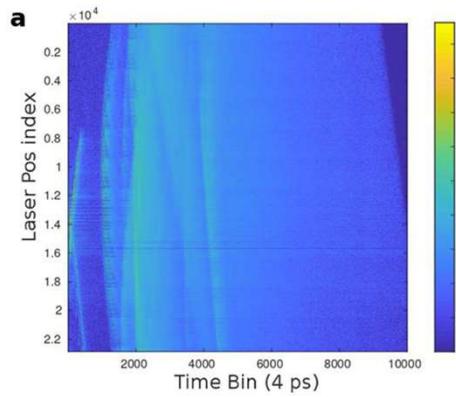
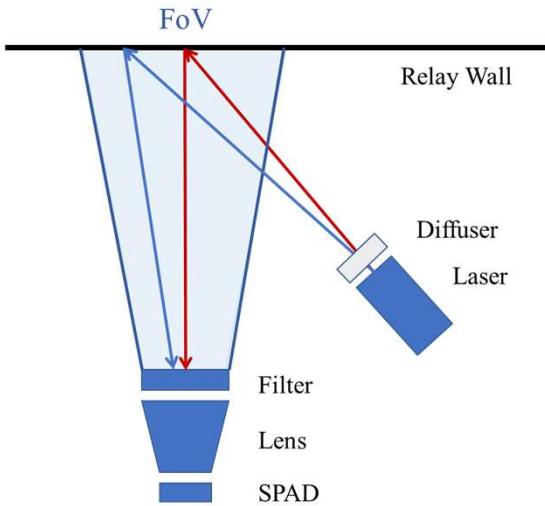
Object size

Got SPAD and laser work;  
Estimated photon count.

There was annoying first bounce,  
although laser point was out of FoV.



# W1: 3D Reconstruction of FoV



Nat19. Liu et.al

Raw

Calibrated

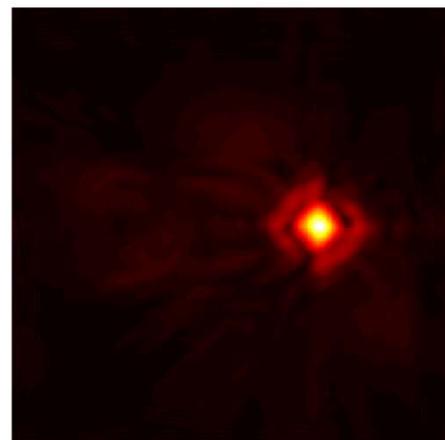
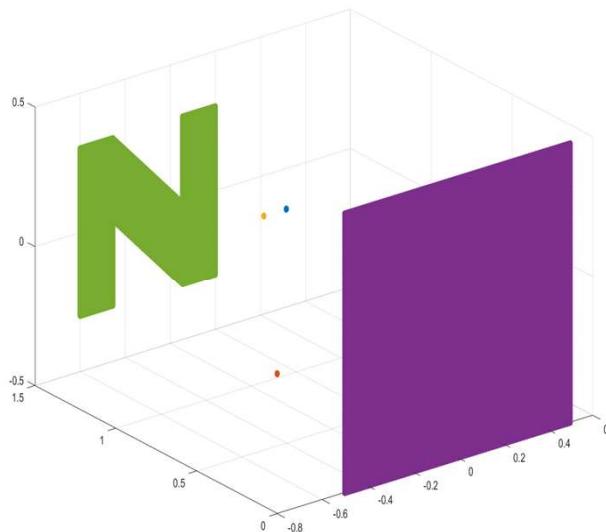
- Calibrated the SPAD array pixels;
- Got RSD algorithm work.

No hyperbola due to small FoV.

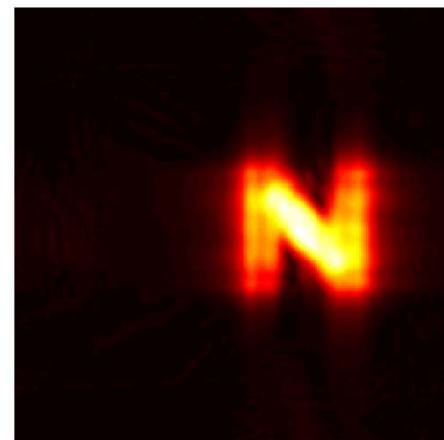
## W2: FoV Simulation

- Set up simulation from scratch;
- Decided how large the FoV should be.

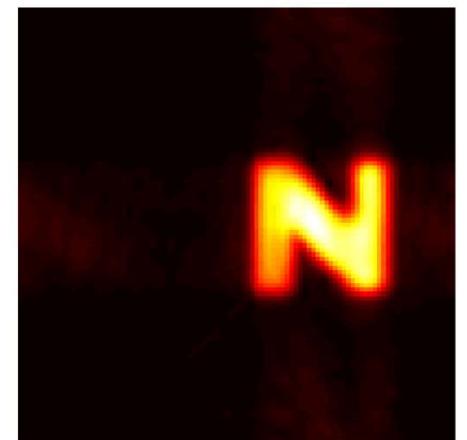
Ignored the noise.



FoV 0.5m\*0.5m



FoV 1m\*1m



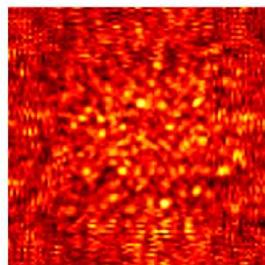
FoV 2m\*2m

# W3: Exposure Time Simulation

- Added Poisson & Gaussian noise in simulation to decide exposure time;
- Tried LPF to compensate.

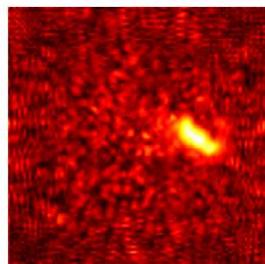
Back projection method messed up.

Exposure Time: 0.1ms  
Peak: 263

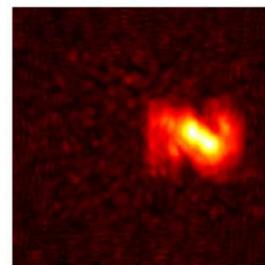


About 1.6s per pixel in our experiment setup (detection rate etc,), 40 readouts add up, it can take several hours labor ☺

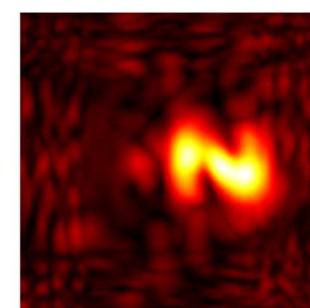
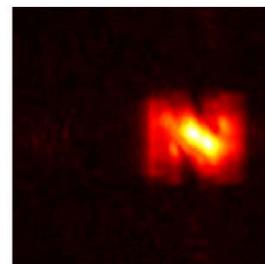
Exposure Time: 1ms  
Peak: 2288



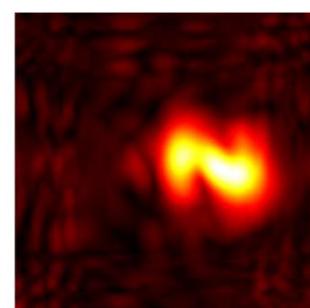
Exposure Time: 10ms  
Peak: 2.2e4



Exposure Time: 100ms  
Peak: 2.1e5



$$\text{Lambda} = \\ 12 * \text{sampling\_spacing}$$

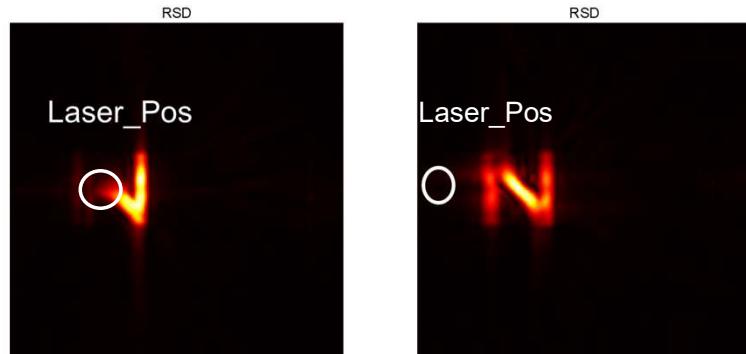


Add LPF

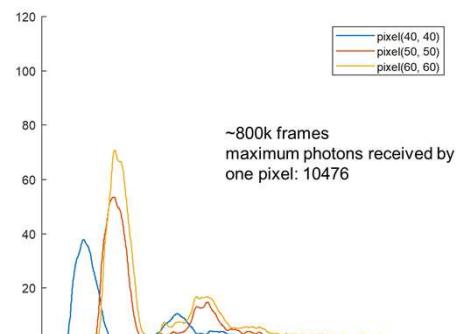
# W4: Non-confocal Geometry

How to choose the laser position is tricky in this experimental setup.

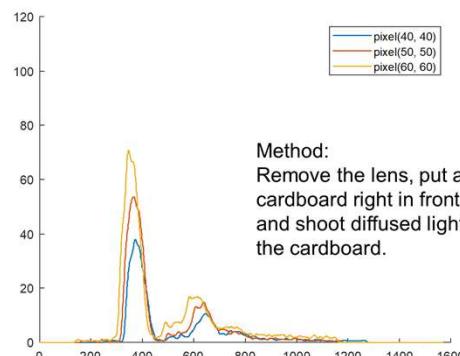
- Explored about the geometry;
- Figured out problem of BP: Laplacian filter;
- Preformatted the experimental data.



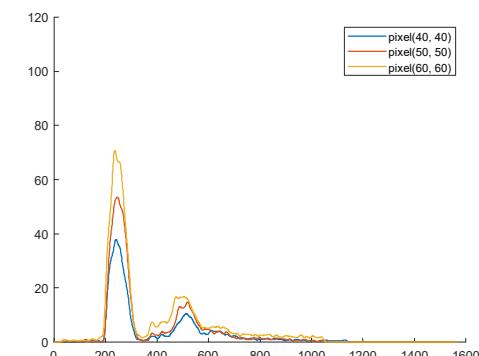
Can't block first bounce, pile up effect.



Raw



Calibrated



Preformatted

# W5: Stitch Method for FoV

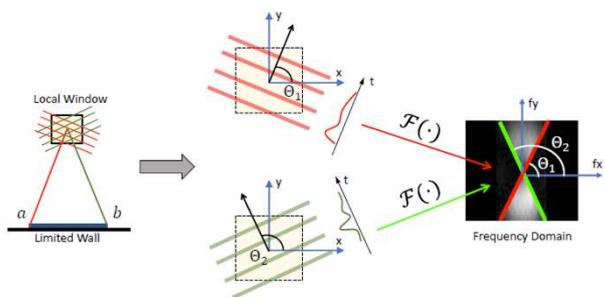
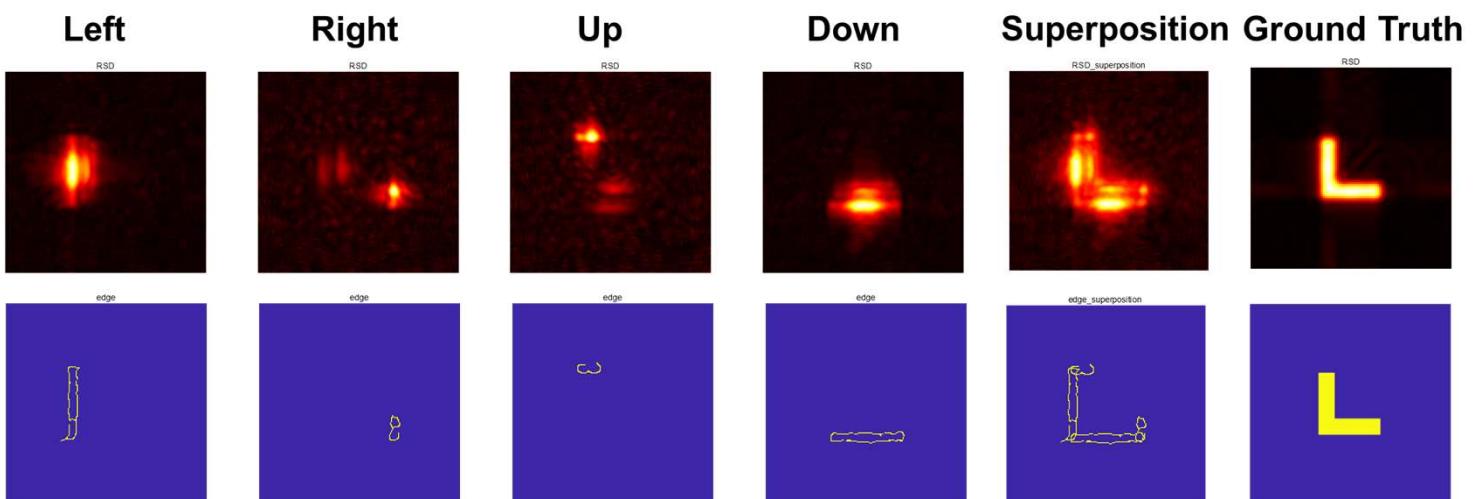
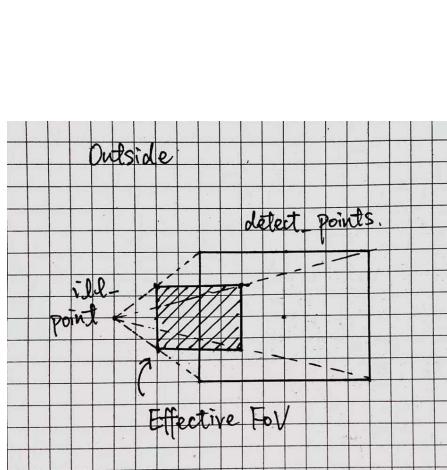
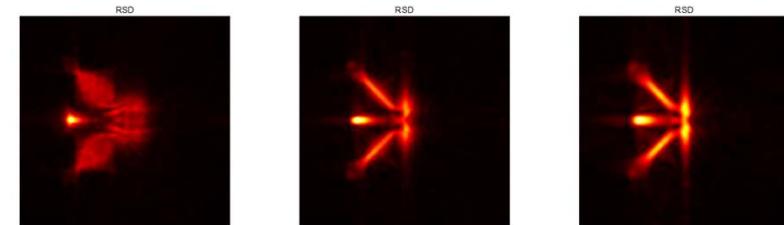


Figure 5. Fourier slice theorem and cone generation.

- Did theoretical analysis;
- Stitched FoV: edge detection + superposition.

Detected artifact for close objects.

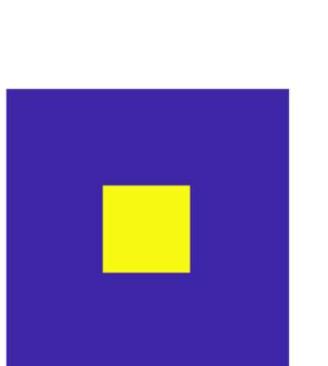
**Ground Truth       $z = 0.5m$        $z = 1m$        $z = 1.5m$**



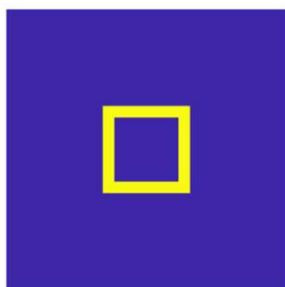
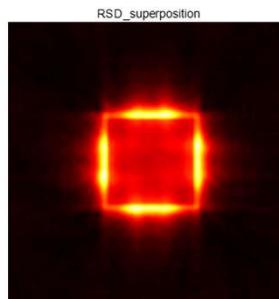
# W6: Fill-in for Stitch Method

Worked out the difference between box and frame.

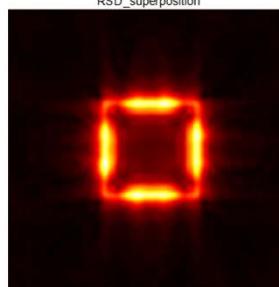
Simulation went wrong: windowing effect detected.



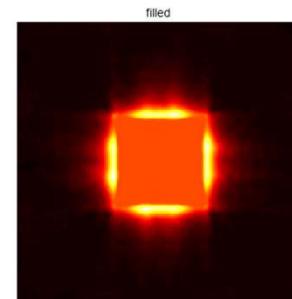
superposition



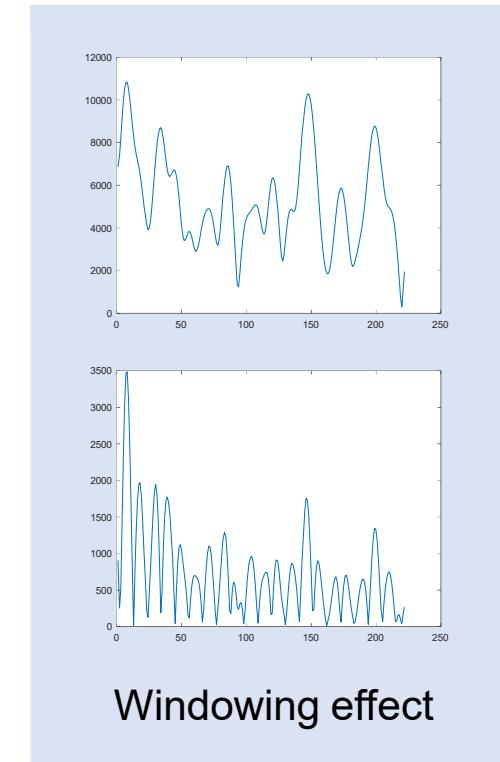
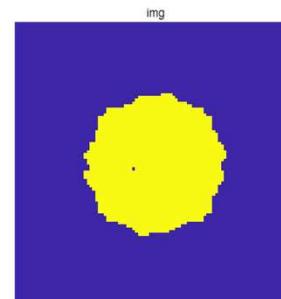
RSD\_superposition



2D filling



3D threshold



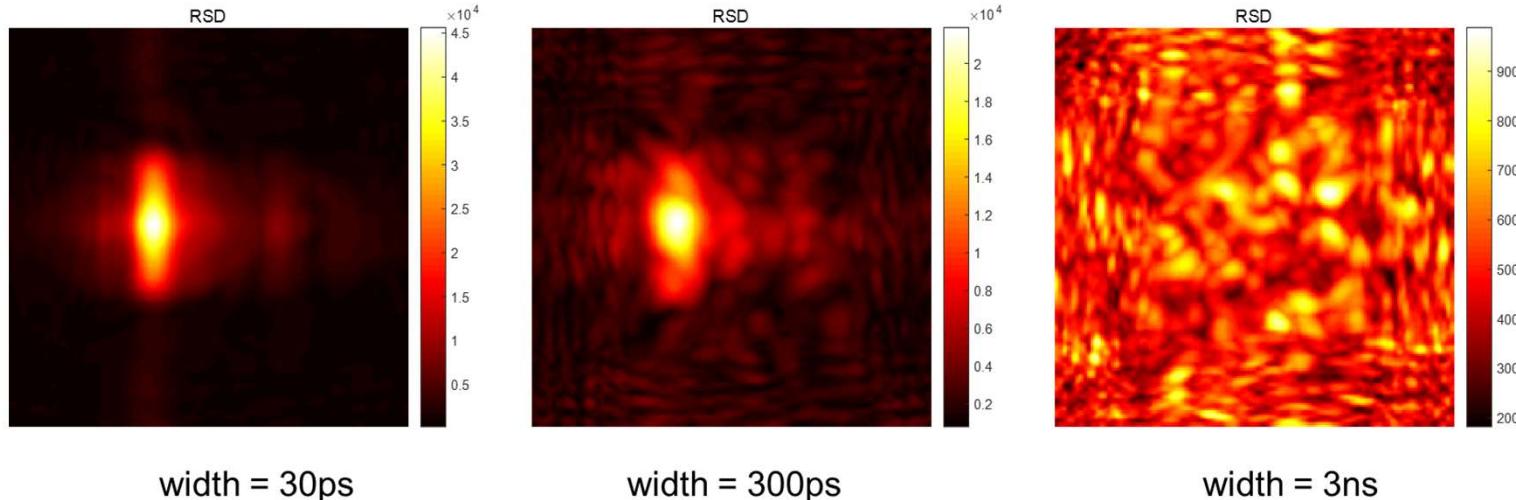
Windowing effect

# W7: Pulse Width Simulation

Gaussian Function, width = FWHM =  $2.355\sigma$   
Fix  $\lambda = 8\text{cm}$

Fixed windowing effect.

Compensation & deconvolution for long pulse width failed.



width = 30ps

width = 300ps

width = 3ns

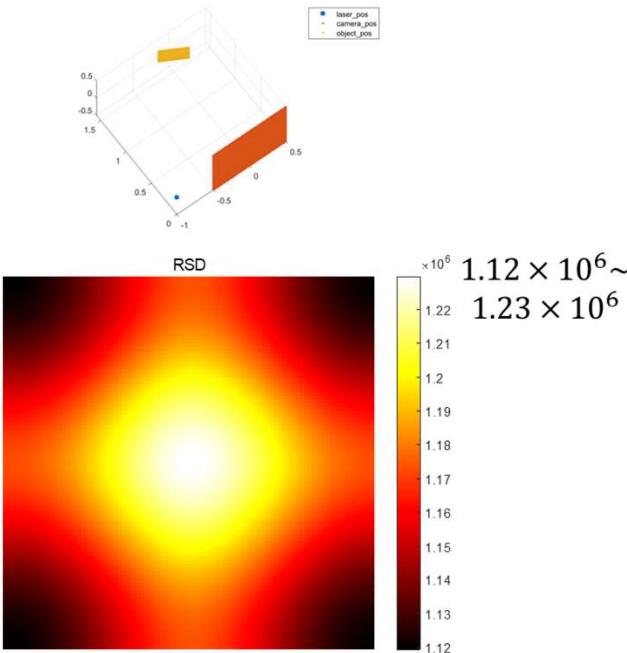
Phasor Freq\_cutoff  $\propto 1/\text{length} \propto 1/\text{wavelength}$

$\Rightarrow \text{wavelength} > \alpha(\text{constant}) * \text{width}$

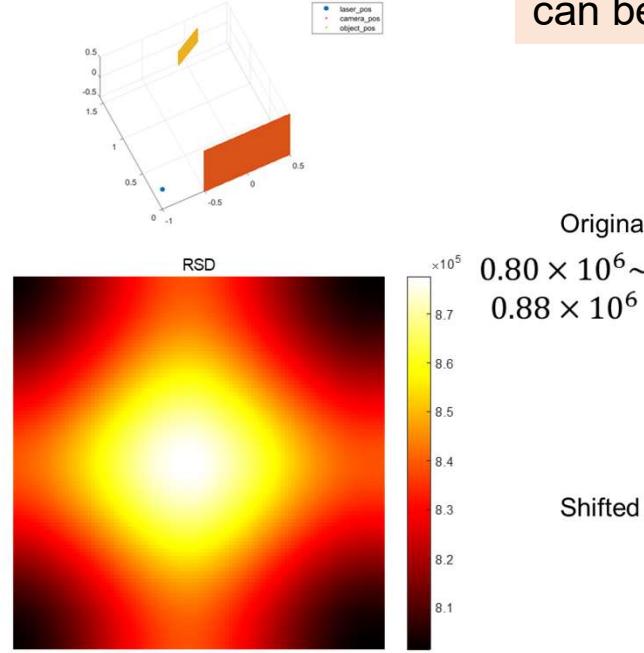
# W8: Tilted Object Simulation

- Tested more scenes using 3ns laser;
- Figured out the reason for sharp edges in reconstruction: padding of aperture.

Raw



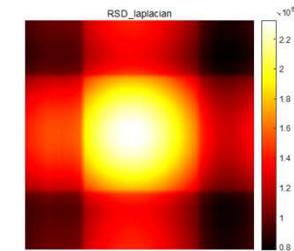
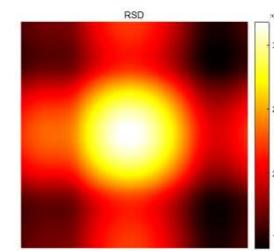
Tilted



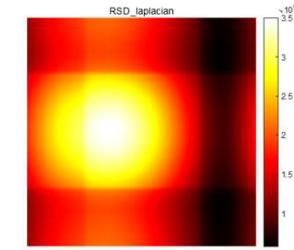
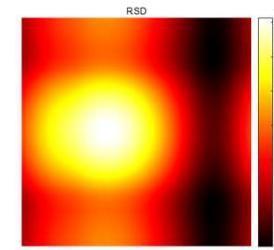
Same shape, just dimmer.

Confirmed that there's hardly any shape can be reconstructed with 3ns laser.

Original

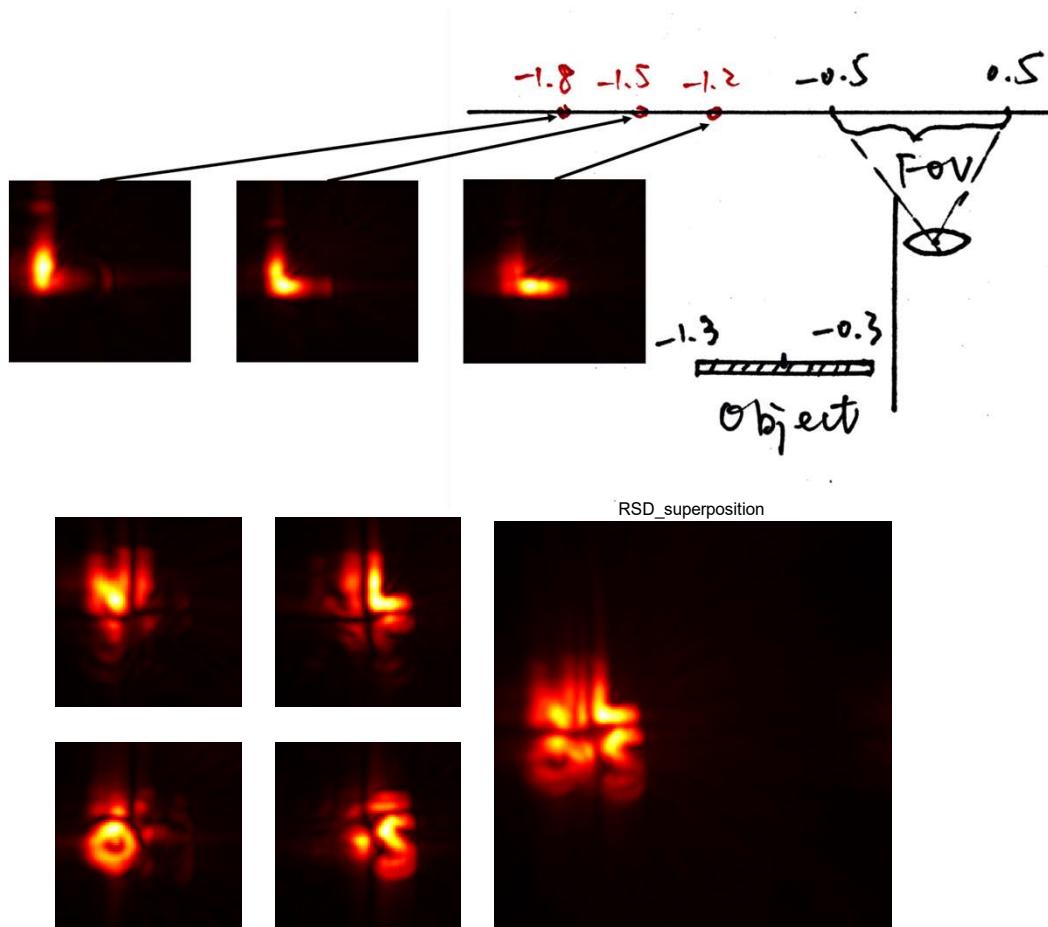


Shifted

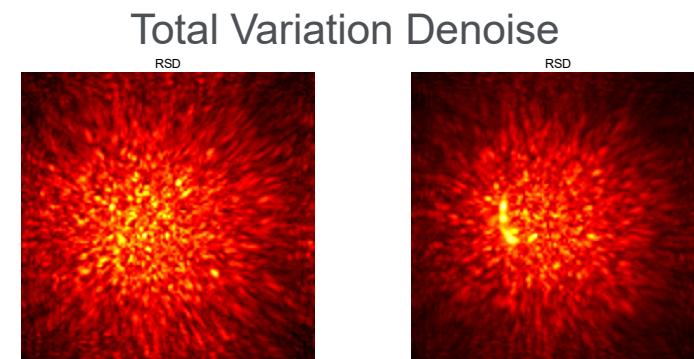
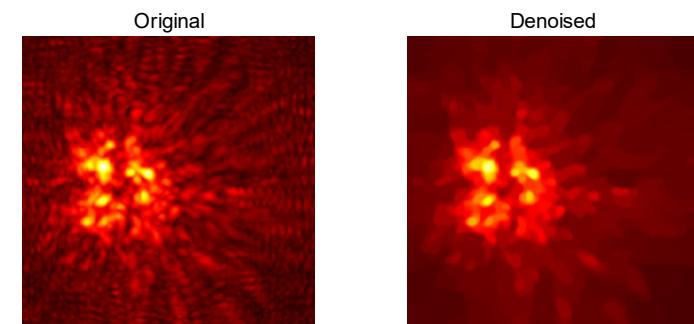


Sharp edges in RSD Laplacian due to padding

# W9: Stitch Method for FoV



- Added Lambertian shading to simulation;
- Stitched the reconstruction of different laser points;
- Tried different denoise method.

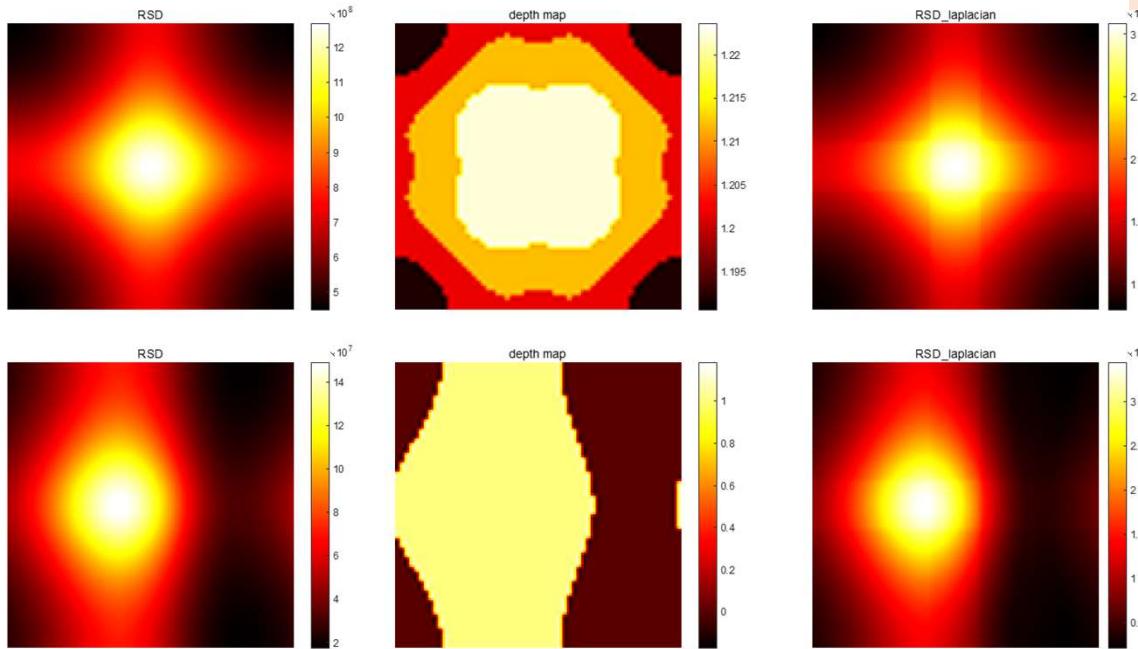


Deconvolution Denoise

# W10: Depth Map Reconstruction

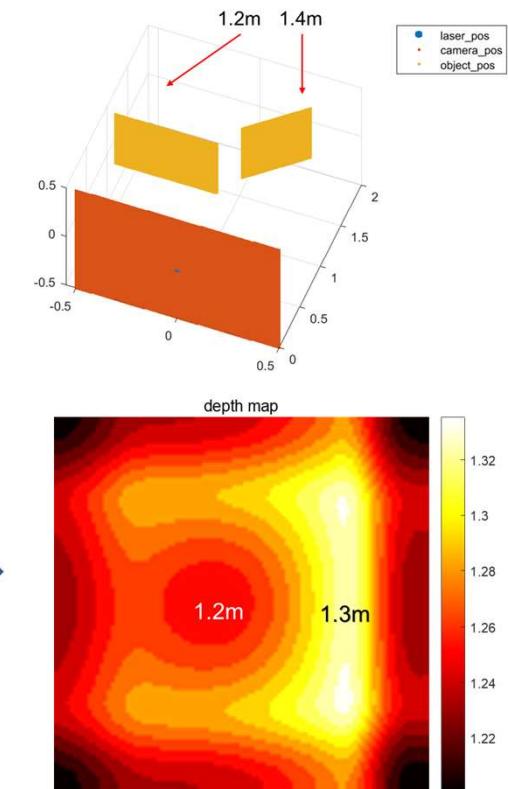
Explored the depth resolution.

Better than axial resolution but distorted too.



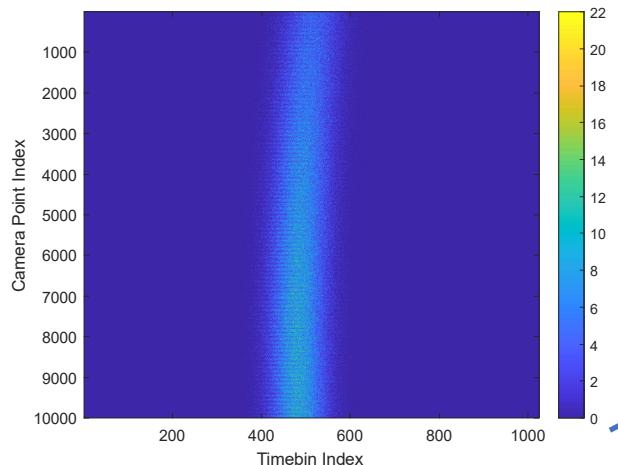
## Depth Map Features

1. Very Uniform – **Good Resolution**
2. The edges depend on denoise threshold (intensity map) – **Can't help reconstruct shape (axial resolution)**

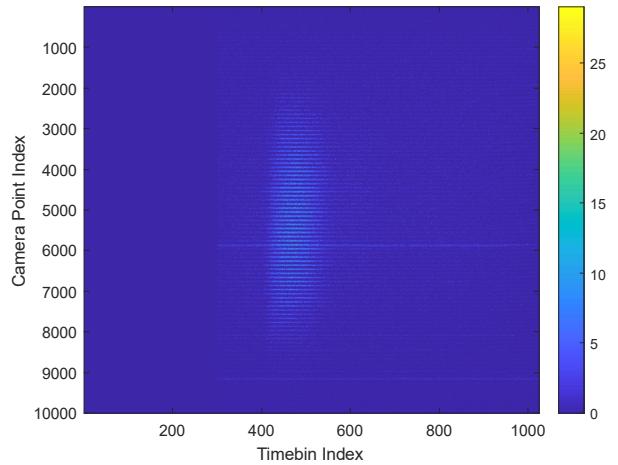


# W11: Fix pile up & Interpolation

Simulation

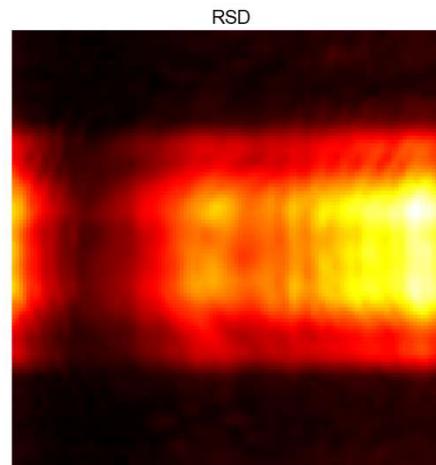


Experiment

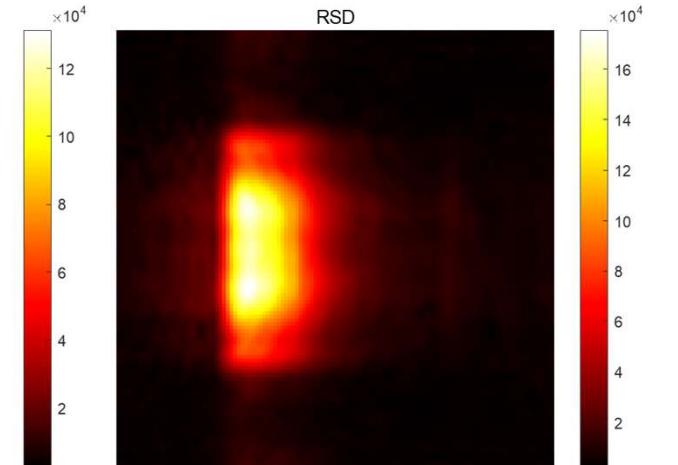


- Fixed the pile up in experiment calibration;
- Verified interpolation method for camera seeing from an angle.

Strong vignetting



No interpolation

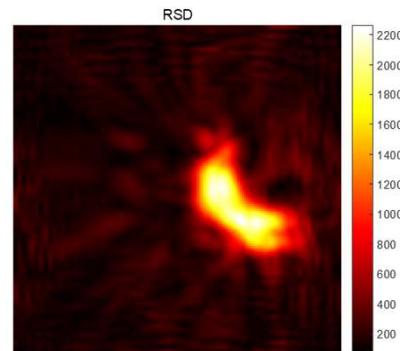
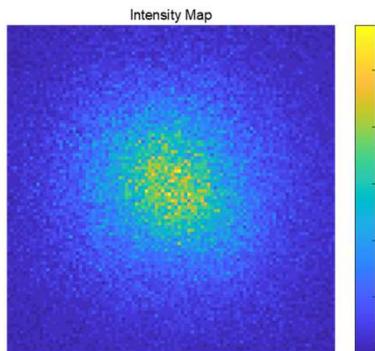
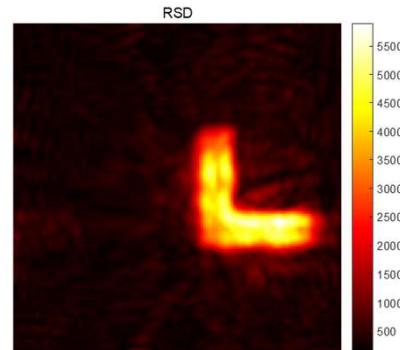
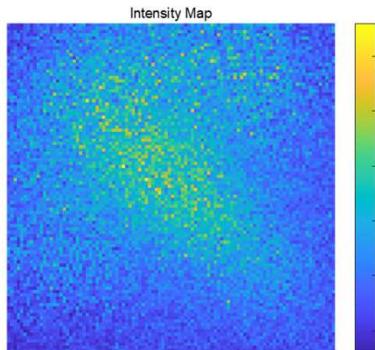


With interpolation

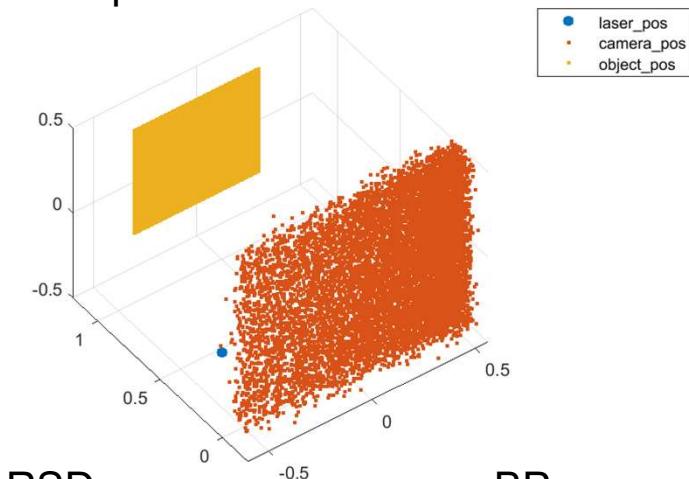
# W12: Vignetting Simulation

- Added vignetting to simulation;
- Tested non-planar scene.

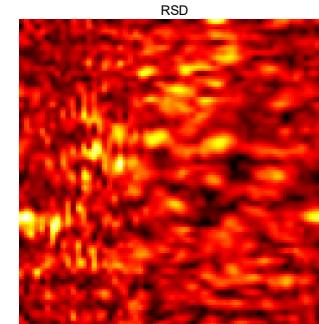
First Row: without vignetting  
Second Row: with vignetting



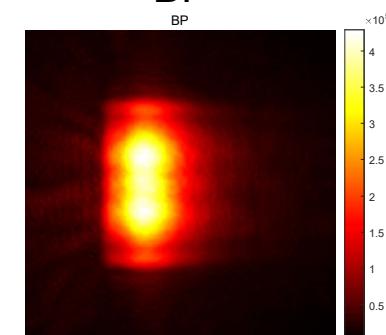
Non-planar scene



RSD

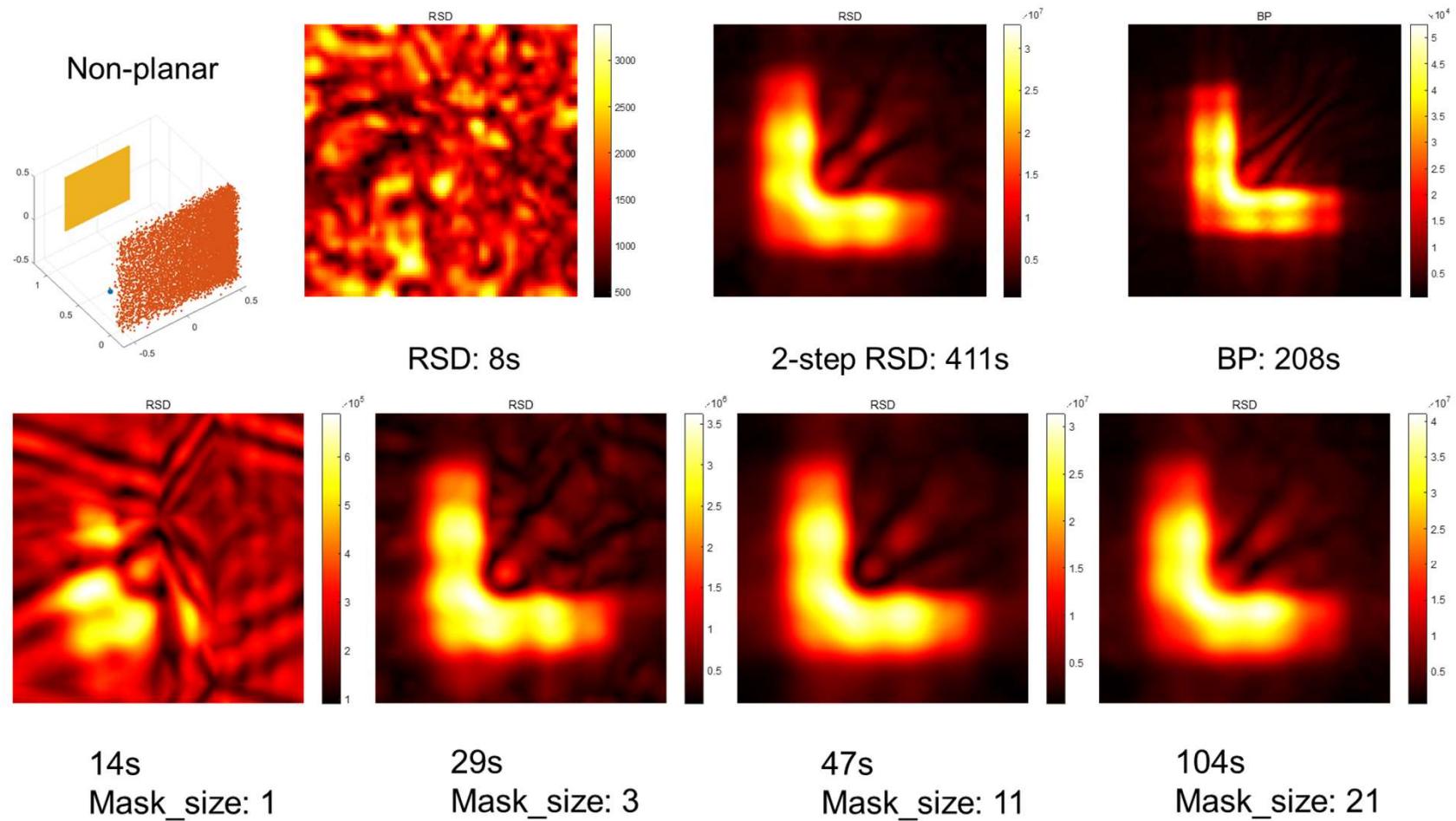


BP



# W13: 2-stage RSD Simulation

- Implemented 2-stage RSD in simulation;
- Tested the effect of mask size.

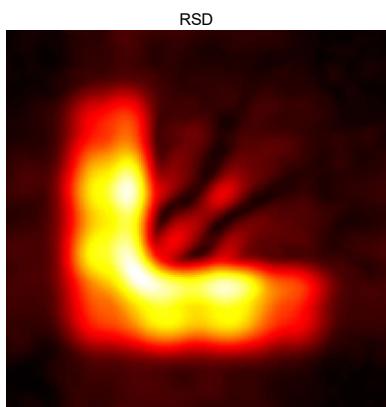


# W14: Padding in 2-stage RSD

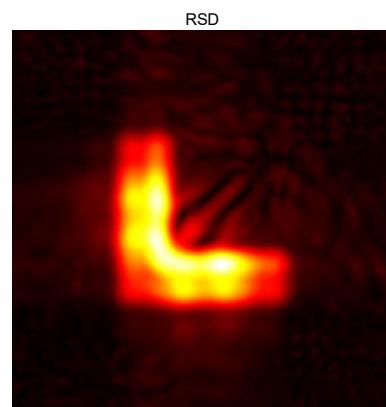
Compared two different ways of padding aperture in 2-stage RSD.

Tried geometry parameter pre-calculate to accelerate but failed (large variable need long load time).

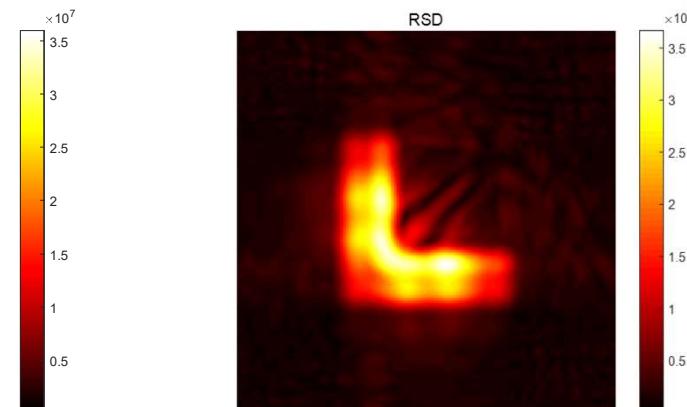
Non-planar



411s  
1m Aperture



1126s  
First step propagate  
to 1.5m Aperture



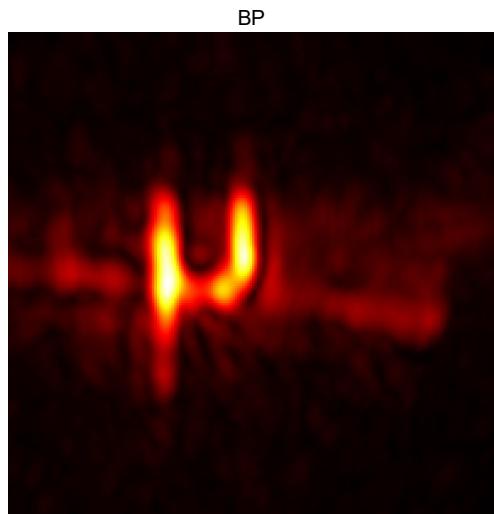
494s  
First step zero padding to  
1.5m Aperture

Zero padding is fine and fast for objects smaller than the sampling plane  
The first propagation plane should be **larger than the sampling plane**

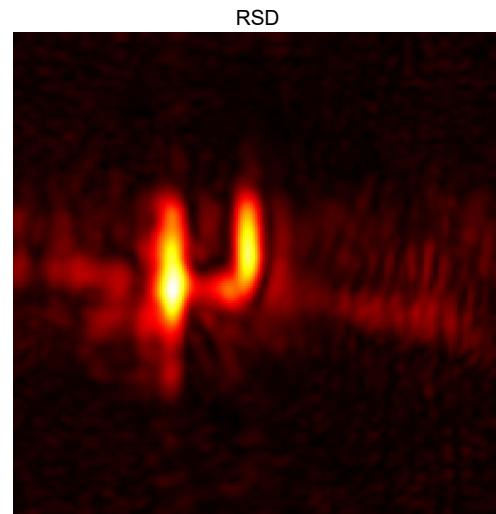
# W15: Real Data 2-stage RSD

Verified the 2-step RSD on real fan-on dataset.

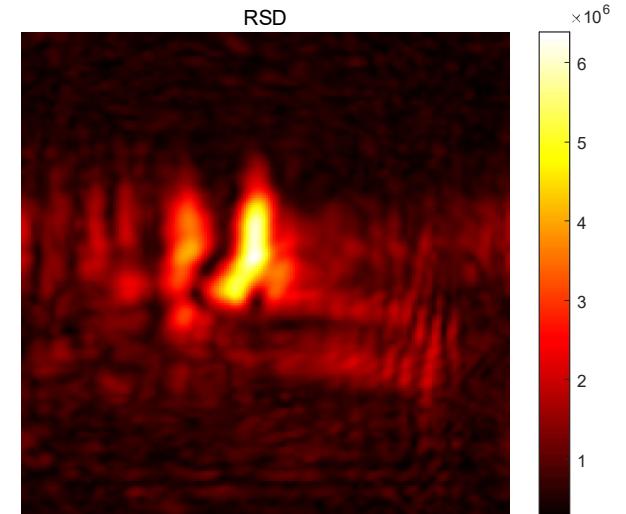
8cm virtual wavelength, 2m\*2m\*1m 3D reconstruction, spacing 2cm



803s  
BP



403s  
Fist propagate to z=0.3m plane

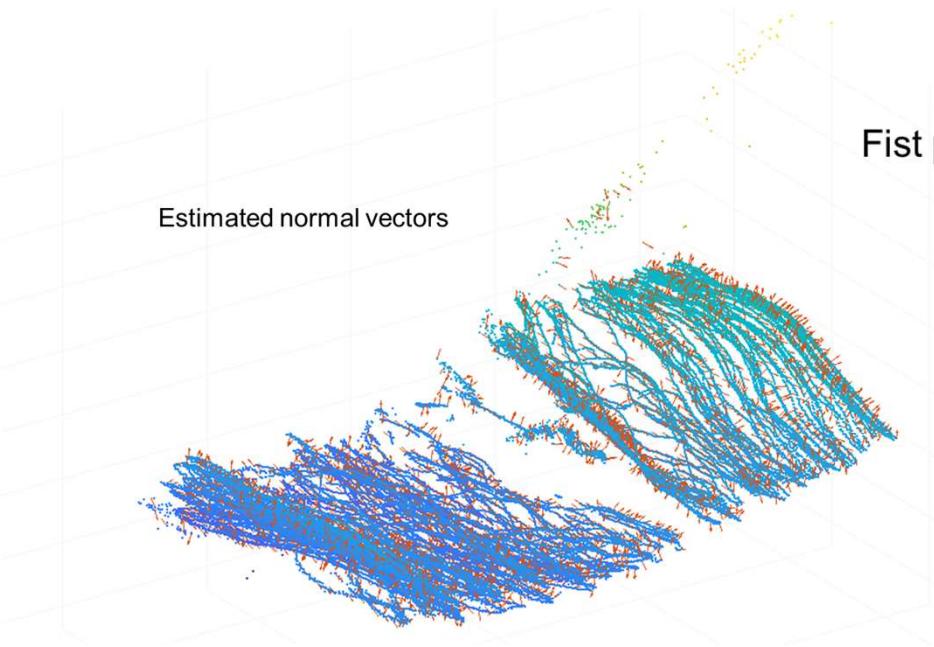


424s  
Fist propagate to z=0.1m plane

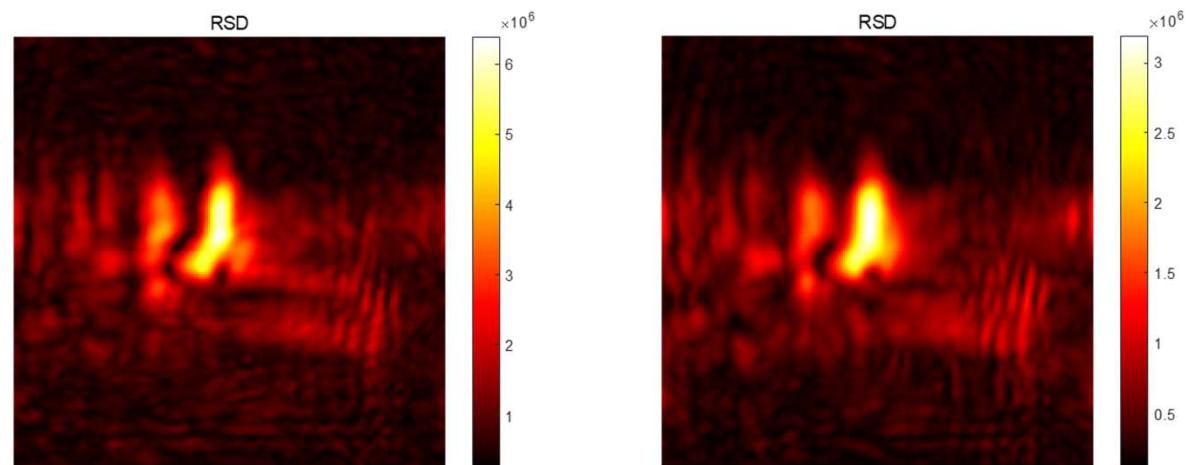
# W16: Shading in RSD

Tried to find out the reason for degrade of closer intermediate plane.

The cos factor didn't change much.



Fist propagate to z=0.1m plane



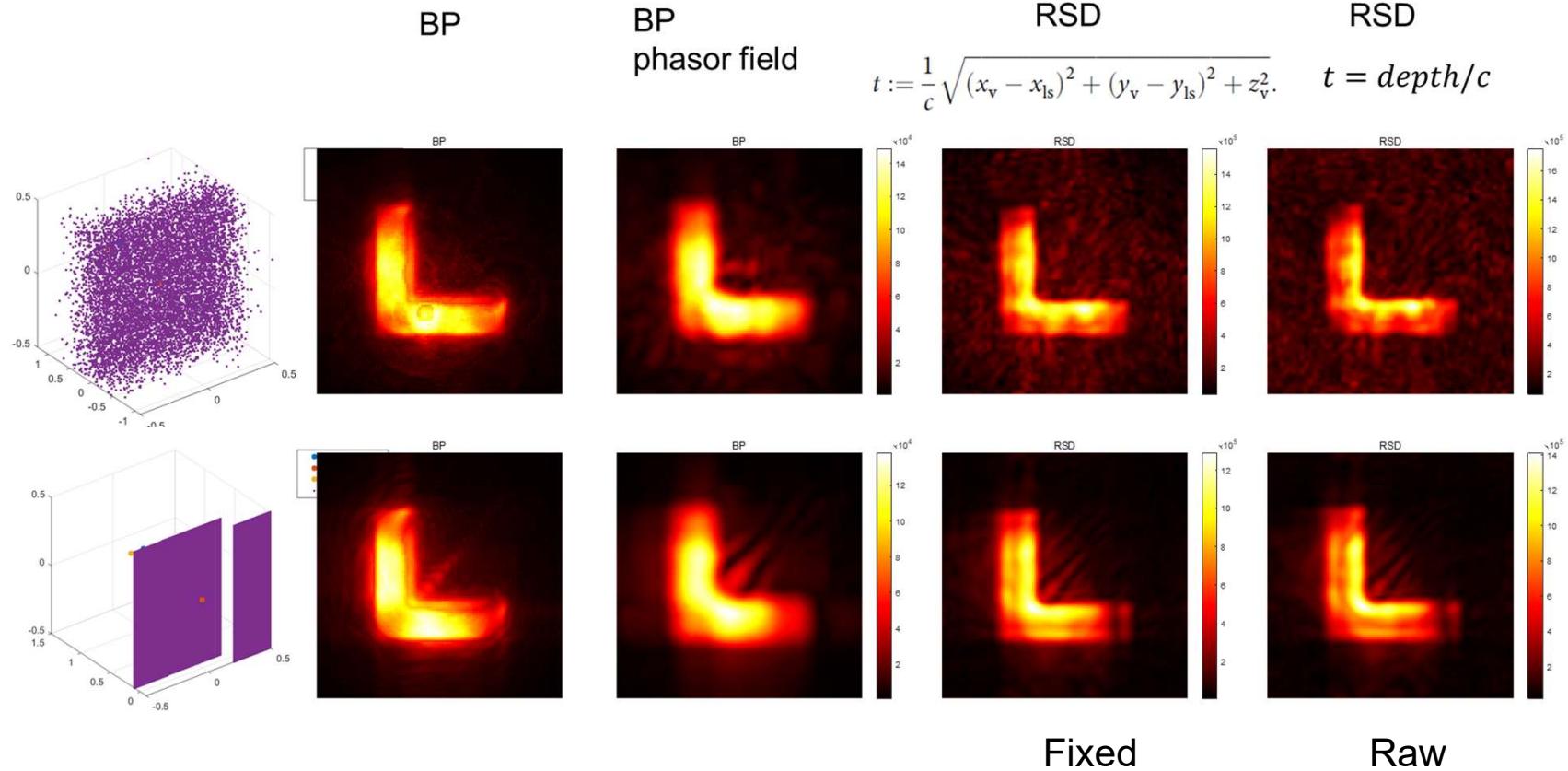
## 3.5.2 The Rayleigh-Sommerfeld Diffraction Formula

Let the Green's function  $G_-$  be substituted for  $G$  in Eq. (3-23). Using (3-35), it follows directly that

$$U_I(P_0) = \frac{1}{j\lambda} \iint_{S_1} U(P_1) \frac{\exp(jkr_{01})}{r_{01}} \cos(\vec{n}, \vec{r}_{01}) ds \quad (3-40)$$

# W17: Correct Phase RSD

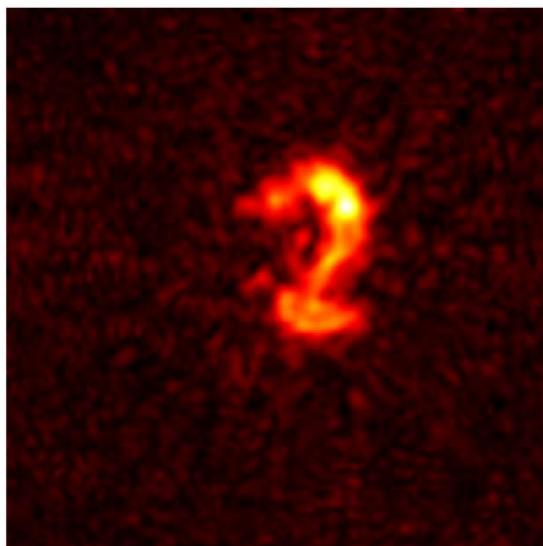
Found an issue regarding the open-source RSD implementation: the phase is approximated. Fixed it.



# W18: Planar Verification

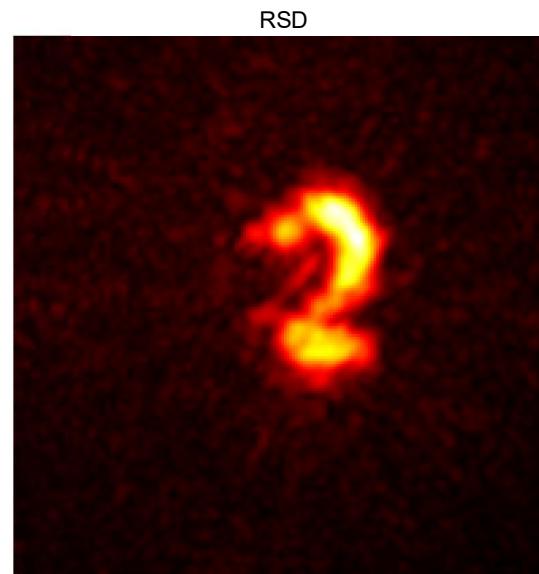
Verified the 2-stage algorithm on planar dataset measured by Yimeng.

RSD, 6s



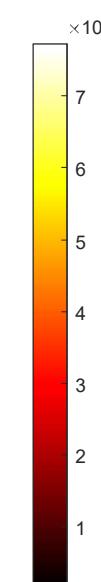
Generated position

2-stage RSD, 79s

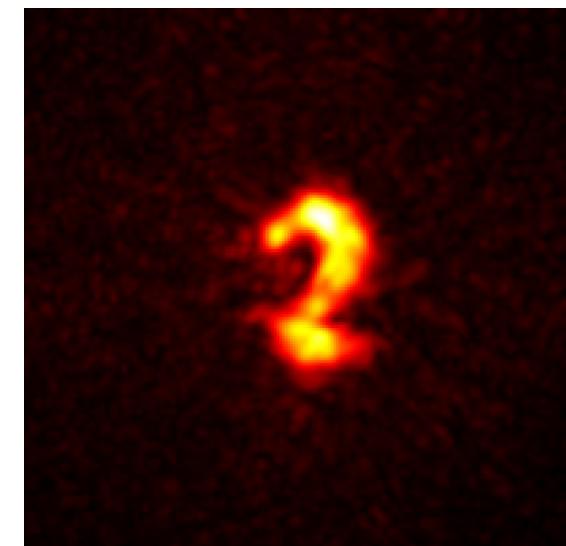


Generated position

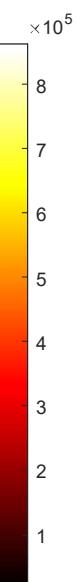
RSD



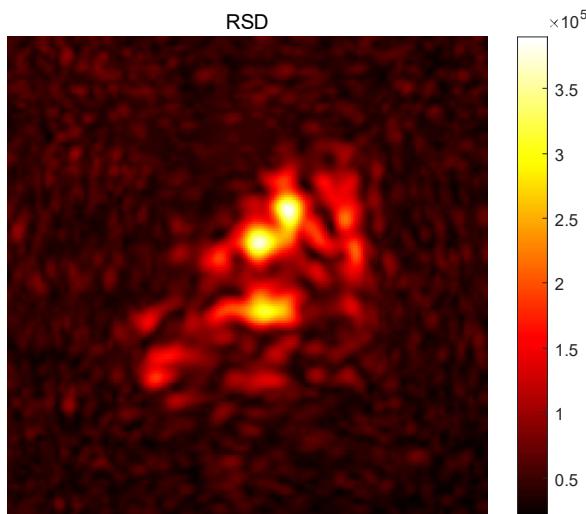
RSD



Measured position



# W19: Non-planar Verification

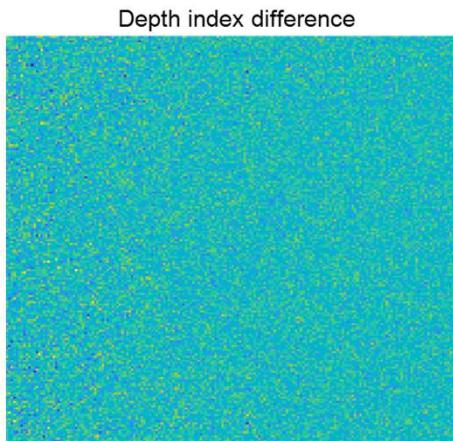


- Verified the 2-stage algorithm on non-planar dataset measured by Yimeng;
- Checked the credibility of first-bounce measurement by applying different filters to see how the peaks change.

Non-planar dataset is too noisy.

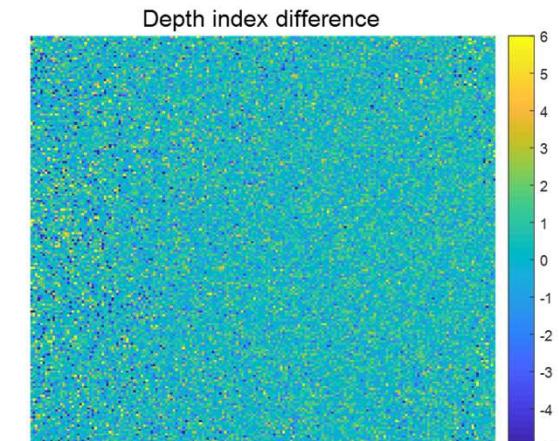
## First bounce validity

Planar Case



Max total photon count: 7412  
Standard deviation: 0.99

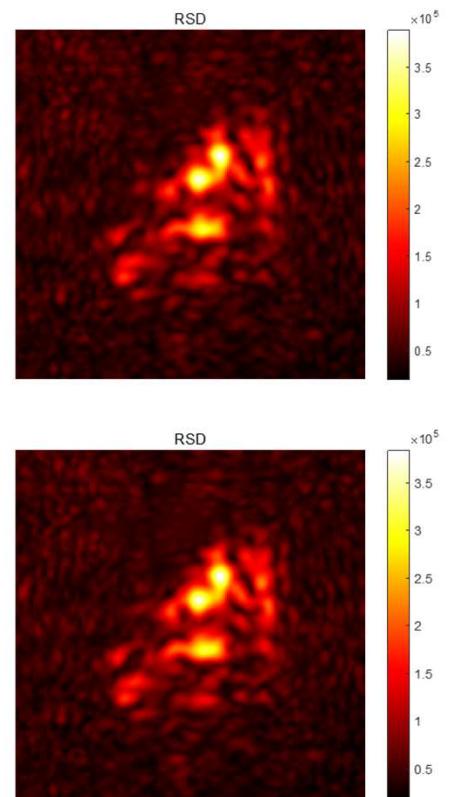
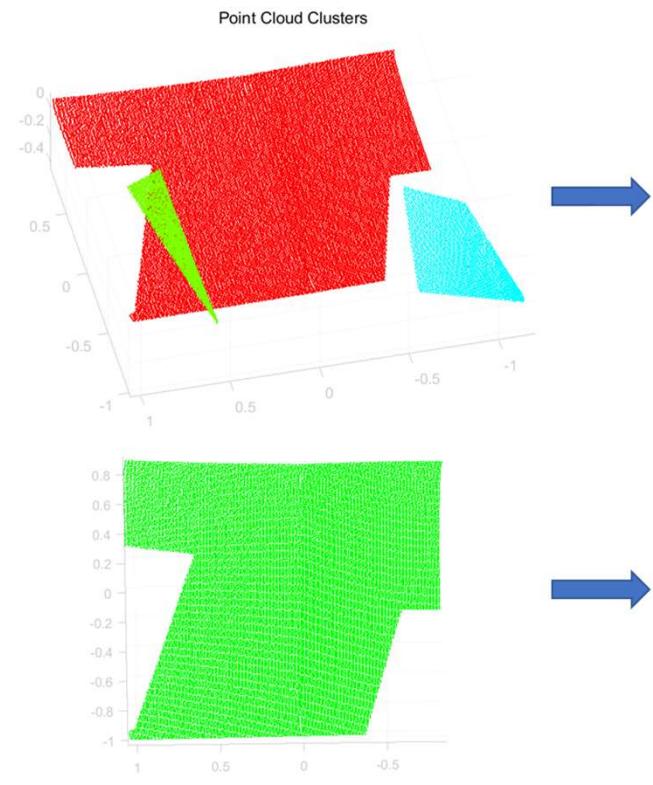
Non-planar Case



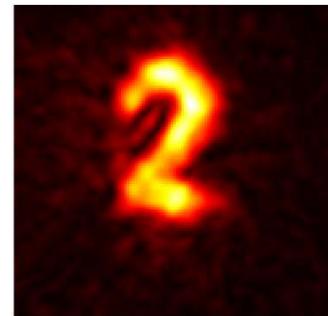
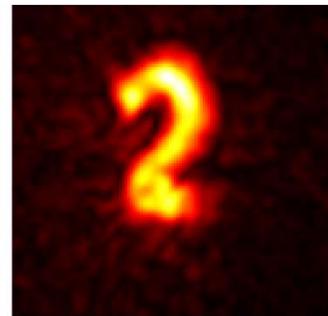
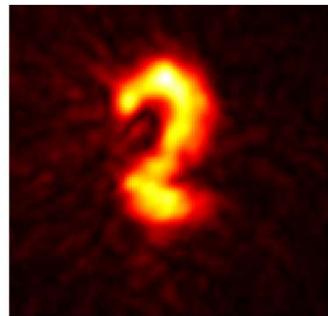
Max total photon count: 2473  
Standard deviation: 4.25

# W20: Non-planar Debug

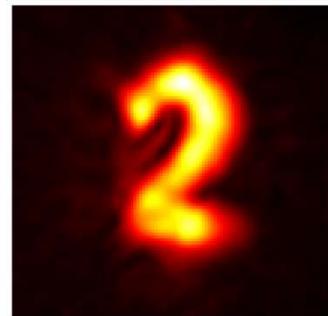
Applied point cloud segmentation to test whether the non-planar positions are measured correctly. It seems they are.



# W21: Stitch SPADs



9 SPADs in total



Combined the results of different SPADs in the array to test whether the SPADs' positions are measured correctly. It seems they are.

Yet two of them are strange.

