

# Depth and thickness of tectonic tremor in the northeastern Olympic Peninsula

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## Key Points:

- We use seismic data from small-aperture arrays in the Olympic Peninsula, Washington and tremor epicenters determined previously by a multibeam backprojection method.
- We compute the depth of the tremor source from estimates of S minus P times determined from stacking horizontal-to-vertical cross-correlations of seismic data.
- Tremor is located close to the plate boundary in a region no more than 2-3 kilometers thick.

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## Abstract

Tectonic tremor has been explained as a swarm of low-frequency earthquakes, which are located on a narrow fault at the plate boundary. However, due to the lack of clear impulsive phases in the tremor signal, it is difficult to determine the depth of the tremor source and the distance of the source to the plate interface with great precision. The thickness of the tremor region is also not well constrained. The tremor may be located on a narrow fault as the low-frequency earthquakes appear to be, or distributed over a few kilometers wide low shear-wave velocity layer in the upper oceanic crust, which is thought to be a region with high pore-fluid pressure. Lag times of peaks in the cross-correlation of the horizontal and vertical components of tremor seismograms, recorded by small-aperture arrays in the Olympic Peninsula, Washington, are interpreted to be S minus P times. Tremor depths are estimated from these S minus P times using epicenters from a previous study using a multibeam backprojection method. The tremor is located close to the plate boundary in a region no more than 2-3 kilometers thick and is very close to the depths of low-frequency earthquakes. The tremor is distributed over a wider depth range than the low-frequency earthquakes. However, due to the uncertainty on the depth, it is difficult to conclude whether the source of the tremor is located at the top of the subducting oceanic crust, in the lower continental crust just above the plate boundary, or in a narrow zone at the plate boundary.

## 1 Introduction

Tremor is a long (several seconds to many minutes), low amplitude seismic signal, with emergent onsets, and an absence of clear impulsive phases. Tectonic tremor has been explained as a swarm of small, low-frequency earthquakes (LFEs) (Shelly et al., 2007), that is small magnitude earthquakes ( $M \sim 1$ ) where frequency content (1-10 Hz) is lower than for ordinary small earthquakes (up to 20 Hz). The source of the LFEs is located on or near the plate boundary, and their focal mechanisms represent shear slip on a low-angle thrust fault dipping in the same direction as the plate interface (Ide et al., 2007; Royer & Bostock, 2014). The polarization of tremor in northern Cascadia is also consistent with slip on the plate boundary in the direction of relative plate motion (Wech & Creager, 2007). Due to the lack of clear impulsive phases in the tremor signal, it is difficult to determine the depth of the tremor source with the same precision. In subduction zones such as Nankai and Cascadia, tectonic tremor observations are spatially and temporally correlated with geodetically observed slow slip (Obara, 2002; Rogers & Dragert, 2003). Due to this correlation, these paired phenomena have been called Episodic Tremor and Slip (ETS).

The occurrence of tremor seems to be linked to low effective normal stress or high fluid pressure near the location of the tremor. Indeed, Shelly et al. (2006) have observed a high P-wave to S-wave velocity ratio in the subducting oceanic crust near the location of the LFEs in western Shikoku, Japan. In Cascadia, Audet et al. (2009) have computed teleseismic receiver functions in Vancouver Island, and analyzed the delay times between the forward-scattered P-to-S, and back-scattered P-to-S and S-to-S conversions at two seismic reflectors identified as the top and bottom of the oceanic crust. It allowed them to compute the P-to-S velocity ratio of the oceanic crust layer and the S-wave velocity contrast at both interfaces. The very low Poisson's ratio of the layer could not be explained by the mineral composition, and they interpreted it as evidence for high pore-fluid pressure. The link between tremor and high pore fluid pressure is also supported by the influence of tidal cycles on the variations of tremor occurrence. Nakata et al. (2008) noticed that tremor swarms often exhibit occurrences with a periodicity of about 12 or 24 h, and concluded that they are probably related to Earth tides. Their occurrence is also well correlated with time evolution of Coulomb failure stress (CFS) and CFS rate. However, tremor occurrences are advanced by a few hours relative to CFS, from which they conclude that a simple Coulomb threshold model is not sufficient to explain tremor occurrence. This discrepancy can be explained by using a rate- and state-dependent fric-

tion law. Thomas et al. (2009) have also observed that tremor occurrence on the deep San Andreas fault are correlated with small, tidal shear stress changes. They explain it by a very weak fault zone with low effective normal stress, probably due to near-lithostatic pore pressures at the depth of the tremor source region.

Two scenariii could explain the generation of tectonic tremor by highly pressured fluids (Shelly et al., 2006). A first possibility is that tremor is generated by the movement of fluids at depth, either by hydraulic fracturing or by coupling between the rock and fluid flow. The accompanying slip could be triggered by the same fluid movement that generates the tremor or, alternatively, the fluid flow could be a response to changes in stress and strain induced by the accompanying slip. The second possibility is that tremor is generated by slow otherwise aseismic shear slip on the plate interface as slip locally accelerates owing to the effects of geometric or physical irregularities on the plate interface. Fluids would then play an auxiliary role, altering the conditions on the plate interface to enable transient slip events, without generating seismic waves directly.

The source of the fluids could be the dehydration of hydrous minerals within the subducting oceanic crust (Shelly et al., 2006). Fagereng and Diener (2011) computed the equilibrium mineral assemblages at different P-T conditions, and compared it to the P-T path of the subducting oceanic crust in Shikoku and Cascadia. They noted that for most of the P-T path, there are no dehydration reactions and the slab remains fluid-absent, except for depths between 30 and 35 km for Shikoku, and depths between 30 and 40 km for Cascadia, where the mineral model predicts significant water release. These depth ranges coincide with the depth range where tremor has been observed. They concluded that abundant tremor activity requires metamorphic conditions where localized dehydration occurs during subduction, which explains why the generation of tectonic tremor is restricted to a small range of depth along the plate boundary. In subduction zones where dehydration reactions are more widely distributed, there would be a more diffuse pattern of tremor activity that would be harder to detect.

Large amounts of fluids could be available at the fore-arc mantle corner. First, the bending of the subducting plate at the ocean trench may introduce water in the upper oceanic mantle, resulting in extensive serpentinization (Hyndman et al., 2015). Second, the serpentinization of the fore-arc mantle corner may decrease the vertical permeability of the boundary between the oceanic plate and the overriding continental crust while keeping a high permeability parallel to the fault. It would thus channel all the fluid up-dip in the subducting oceanic crust, and explain the sharp velocity contrast observed by Audet et al. (2009) on top of the oceanic crust layer. At greater depth, the large volume reduction and water release accompanying eclogitization in the subducted oceanic crust, and the large volume expansion accompanying serpentinization in the mantle wedge, could increase the permeability of the plate boundary through fracture generation. A possible cause of ETS events could thus be periodic cycles of steady pore-fluid pressure build-up from dehydration of subducted oceanic crust, fluid release from fracturing of the interface during ETS, and subsequent precipitation sealing of the plate boundary (Audet et al., 2009).

Whereas the position of the subduction zone ETS does not seem to coincide with a specific temperature or dehydration reaction (Peacock, 2009), there seems to be a good coincidence between the location of the fore-arc mantle corner, and the location of ETS (Hyndman et al., 2015). The generation of slow slip and tectonic tremor could then be related to the presence of quartz in the overriding continental crust. Using receiver functions of teleseismic body waves, and data from the literature, Audet and Bürgmann (2014) observed that the recurrence time of slow earthquakes increases linearly with the  $V_p / V_s$  ratio of the forearc crust. They also noticed that along a margin-perpendicular profile from northern Cascadia, the  $V_p / V_s$  ratio of the forearc, and the recurrence time of ETS events, decrease with increasing depth. Likewise, Hyndman et al. (2015) pointed out that the deep fore-arc crust has a very low Poisson's ratio (less than 0.22), and that the only mineral with a very low Poisson's ratio is quartz (about 0.1), which led them to conclude that there may be a significant amount of quartz (about 10% by volume)

in the deep fore-arc crust above the fore-arc mantle. Audet and Bürgmann (2014) explained the presence of quartz in the forearc by the enrichment of forearc minerals in fluid-dissolved silica derived from the dehydration of the down-going slab. As the solubility of silica increases with temperature, fluids generated at depth and rising up the subduction channel should be rich in silica (Hyndman et al., 2015).

Quartz veins have indeed been observed in exhumed subduction zones. For instance, Fagereng et al. (2014) have studied an exhumed shear zone representing the subduction megathrust before its incorporation into the accretionary prism. They focused their study on a 30 m high by 80 m long cliff exposure where foliation has developed as a result of shearing along the subduction thrust interface. They identified two groups of quartz veins, foliation-parallel veins, and discordant veins, that must have formed for an extended time before, during, and after foliation development. They interpret the foliation-parallel veins as having been formed by viscous shear flow, and note that the shear strain rate due to the flow may be high enough to accommodate a slow slip strain rate of  $10^{-9} s^{-1}$ , for a typical subduction thrust thickness of 30 m (Rowe & Moore, 2013). They interpret the discordant veins as having been formed by brittle deformation caused by locally elevated fluid pressure. The size of the structures where brittle deformation is observed (meters to hundreds of meters) is compatible with the size of the asperity rupturing during an LFE. Tremor and slow slip may thus be a manifestation of brittle-viscous deformation in the shear zone.

However, several constraints remain to be explained. Audet and Bürgmann (2014) estimated that the fluid flux required for the formation of quartz veins was two orders of magnitude greater than the fluid production rates estimated from the dehydration of the slab. They hypothesized that silica-saturated fluids may originate from the complete serpentinization of the mantle near the wedge corner. They suggested that higher temperature and quartz content at depth may lead to faster dissolution - precipitation processes and more frequent slip events. Their model could also explain the global variation in recurrence time, with mafic silica-poor regions having longer ETS recurrence times than felsic silica-rich regions.

Moreover, the zone with high low Poisson's ratio observed by Hyndman et al. (2015) has a large vertical extent (about 10 kilometers). If the whole zone is associated with quartz deposition and tectonic tremor generation, we should also observe a large vertical distribution of the source of the tremor. Kao et al. (2006) have used a Source Scanning Algorithm to detect and locate tremor, and have indeed located tremor in the continental crust, with a wide depth range of over 40 km. They noted that this wide depth range could not arise from either analysis uncertainties or a systematic bias in the velocity model they used. Uncertainties on the location of the tremor have been estimated by Ide (2012) at about 1.5 km in epicenter and 4.5 km in depth. A follow-up study by Kao et al. (2009) gave a thickness of the tremor zone of 5-10 km. This depth range is inconsistent with the depth of the LFEs, which have been located on a thin band at or near the plate interface with a rupture mechanism that corresponds to the thrust dip angle (Ide et al., 2007). In the Olympic Peninsula, LFE families have been identified and located by Chestler and Creager (2017a, 2017b), and all LFE families were located near the plate interface. Further study is thus needed to narrow the uncertainty on the depth of the source of the tremor, and verify whether tremor occurs in a wider zone than LFEs.

Several methods have been developed to detect and locate tectonic tremor or LFEs using the cross-correlation of seismic signals. The main idea is to find similar waveforms in two different seismic signals, which could correspond to a single tremor or LFE recorded at two different stations, or two different tremors or LFEs with the same source location but occurring at two different times and recorded by the same station. A first method consists in comparing the envelopes of seismograms at different stations (Obara, 2002; Wech & Creager, 2008), or directly the seismograms at different stations (Rubin & Armbruster, 2013). For instance, Wech and Creager (2008) computed the cross-correlations of envelope seismograms for a set of 20 stations in western Washington and southern Van-

couver Island. Then, they performed a grid search over all possible source locations to determine which one minimizes the difference between the maximum cross-correlation and the value of the correlogram at the lag time corresponding to the S-wave travel time difference between two stations.

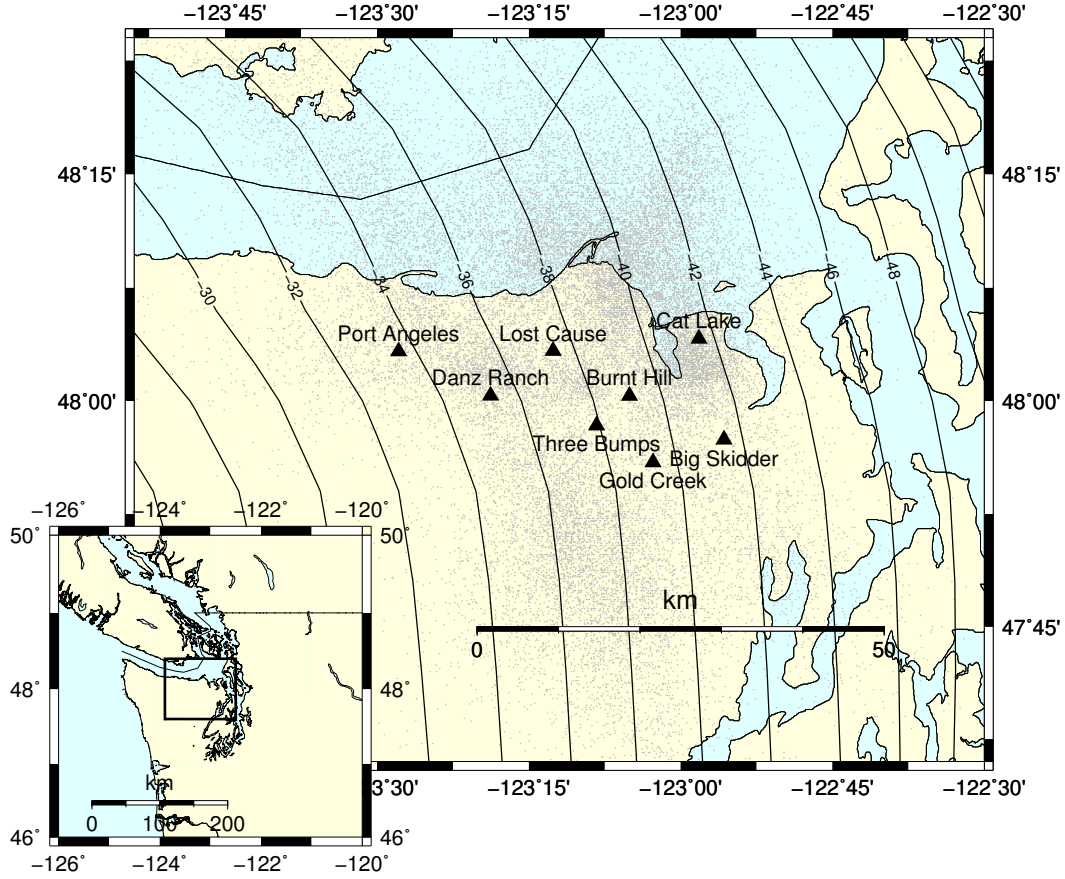
A second method is based on the assumption that repeating tremor or LFEs with sources located nearby in space will have similar waveforms (Bostock et al., 2012; Royer & Bostock, 2014; Shelly et al., 2006, 2007). For instance, Bostock et al. (2012) looked for LFEs by computing autocorrelations of 6-second long windows for each component of 7 stations in Vancouver Island. They then classified their LFE detections into 140 families. By stacking all waveforms of a given family, they obtained an LFE template for each family. They extended their templates by adding more stations and computing cross-correlations between station data and template waveforms. They used P- and S-travel-time picks to obtain a hypocenter for each LFE template. By observing the polarizations of the P- and S-waveforms of the LFE templates, they computed focal mechanisms and obtained a mixture of strike slip and thrust mechanisms, corresponding to a compressive stress field consistent with thrust faulting parallel to the plate interface. Further study showed that the average double couple solution is generally consistent with shallow thrusting in the direction of plate motion (Royer & Bostock, 2014).

Finally, a third method uses seismograms recorded across small-aperture arrays (Ghosh et al., 2010a; La Rocca et al., 2009). For instance, La Rocca et al. (2009) stacked seismograms over all stations of the array for each component, and for three arrays in Cascadia. They then computed the cross-correlation between the horizontal and the vertical component, and found a distinct and persistent peak at a positive lag time, corresponding to the time between P-wave arrival on the vertical channel and S-wave arrival on the horizontal channels. Using a standard layered Earth model, and horizontal slowness estimated from array analysis, they computed the depths of the tremor sources. They located the sources near or at the plate interface, with a much better depth resolution than previous methods based on seismic signal envelopes, source scanning algorithm, or small-aperture arrays. They concluded that at least some of the tremor consisted in the repetition of LFEs as was the case in Shikoku. A drawback of the method was that it could be applied only to tremor located beneath an array, and coming from only one place for an extended period of time.

In this study, we extend on the method used by La Rocca et al. (2009) using the cross-correlation between horizontal and vertical components of seismic recordings to estimate the depth of the source of the tectonic tremor, and the depth extent of the region from which tremor originates. If indeed tremor is made of swarms of LFEs, and both represent the regions of deformation during ETS events, we would expect the thickness of the tremor to be the same as the thickness of the LFEs. If not, tremor may be occurring where LFEs are harder to detect because they are either smaller in amplitude, or spread out over continuous space and not as clearly repeating.

## 2 Data

The data were collected during the 2009-2011 Array of Arrays experiment. Eight small-aperture arrays were installed in the northeastern part of the Olympic Peninsula, Washington. The aperture of the arrays was about 1 km, and station spacing was a few hundred meters. Arrays typically had ten 3-component seismometers, augmented by an additional 10 vertical-only sensors during the 2010 ETS event. The arrays were around 5 to 10 km apart from each other (Figure 1). Most of the arrays recorded data for most of a year, between June 2009 to September 2010, and captured the main August 2010 ETS event. The arrays also recorded the August 2011 ETS event with a slightly reduced number of stations. Ghosh et al. (2012) used a multibeam backprojection (MBBP) technique to detect and locate tremor. They bandpass filtered the vertical component between 5 and 9 Hz and divided the data into one-minute-long time windows. They performed beam forming of vertical component data in the frequency domain at each ar-



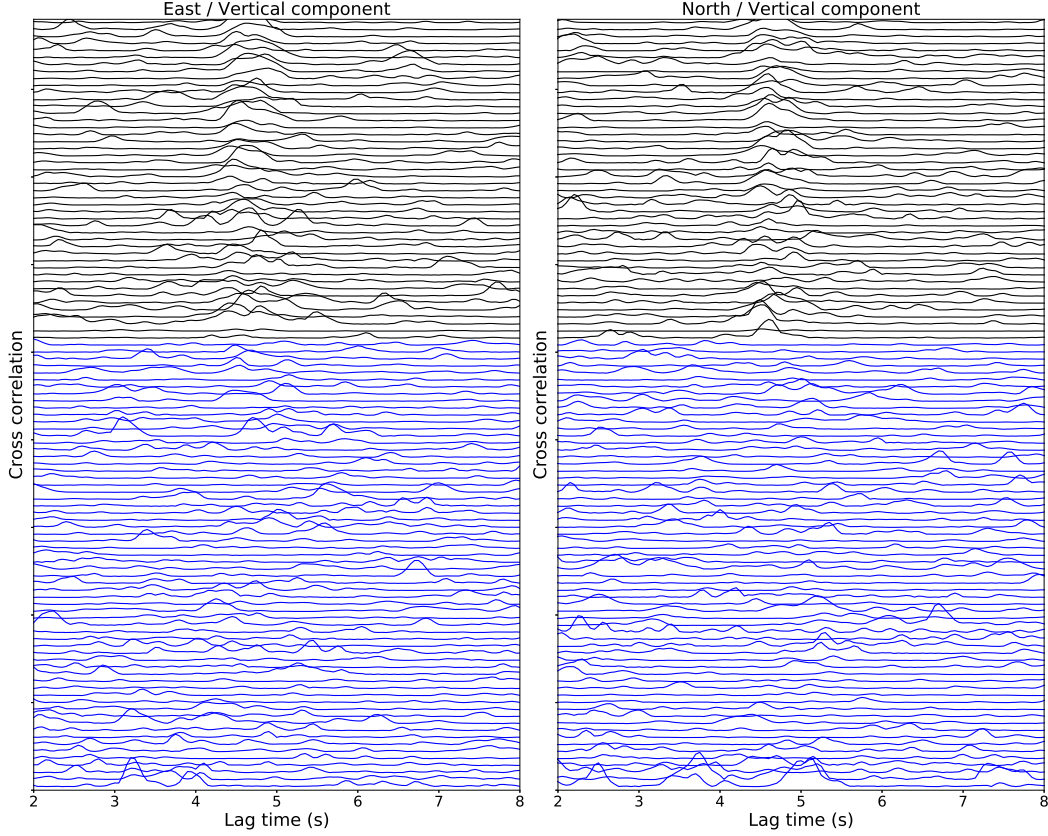
**Figure 1.** Map showing the location of the eight arrays (black triangles) used in this study and tremor locations (grey dots) located using these arrays (Ghosh et al., 2012). Inset shows the study area with the box marking the area covered in the main map. Contours represent a model of the depth of the plate interface (McCrory et al., 2006).

ray to determine the slowness vectors, and backprojected the slownesses through a 3-D wavespeed model (Preston et al., 2003) to locate the source of the tremor for each time window. This produced 28902 tremor epicenters for one-minute-long time windows during June, 2009 - September, 2010 and 5600 epicenters during August - September, 2011.

### 3 Method

For each array, and every 5 km by 5 km grid cell located within 25 km, we analyze the one-minute-long time windows corresponding to all the tremor epicenters located within the grid cell. For each three-component seismic station and each channel, we detrended the data, tapered the first and last 5 seconds with a Hann window, removed the instrument response, bandpass filtered between 2 and 8 Hz, and resampled the data to 20 Hz. All these preprocessing operations were done with the Python package obspy. For each seismic station and each one-minute-long time window, we cross correlated the vertical component with the East-West component and with the North-South component. Then, we stacked the cross correlation functions over all the seismic stations of the array. We call this stack  $S_{ij}(\tau)$  for time lag  $\tau$ , the  $i$ -th channel ( $i=1$  or  $2$  for the North or





**Figure 2.** Envelopes of the stacked cross-correlation functions for the Big Skidder array for the 110 one-minute long time windows when tremor was detected in a 5 km by 5 km grid cell located 7 kilometers southwest of the array. Top shows time windows (black) that fit the stack well. Bottom shows time windows (blue) that do not fit the stack well. Left panel is the cross-correlation of the EW component with the vertical component, and right panel is the cross-correlation of the NS component with the vertical component. The cross-correlation functions have been cut between 2 and 8 seconds to focus on the time lags around the peaks.

East channel) and the  $j$ -th one-minute-long time window for a given epicenter grid/array pair. At each step of this method we experimented with a linear stack, a  $n$ th-root stack, and a phase-weighted stack (Schimmel & Paulssen, 1997) and found that the phase-weighted stack worked best. So, all the stacks discussed here used the phase-weighted method. Figure 2 shows an example of the envelopes of  $S_{ij}(\tau)$  for the Big Skidder array for the 110 one-minute-long time windows when tremor was detected in the 5 km by 5 km grid cell located 7 kilometers southwest of the array. For all time windows, there is a primary peak in the envelopes of the cross-correlation  $S_{ij}(\tau)$  at  $\tau = 0s$  (not shown in the Figure). Additionally, for about 40% of the time windows, we also see a secondary peak in the envelopes of the cross-correlation  $S_{ij}(\tau)$  at about  $\tau = 4.5s$ . As the energy of the P-waves is expected to be higher on the vertical component, and the energy of the S-waves to be higher on the horizontal components, we interpret this peak to correspond to the time lag between the arrival of the direct P- and S-waves.

Only about half of the envelopes of the cross-correlation functions have a distinct peak that coincides with the peak in the stacked cross-correlation. The other cross-correlation functions show either a distinct peak at another time lag, or no clearly visible peak. This

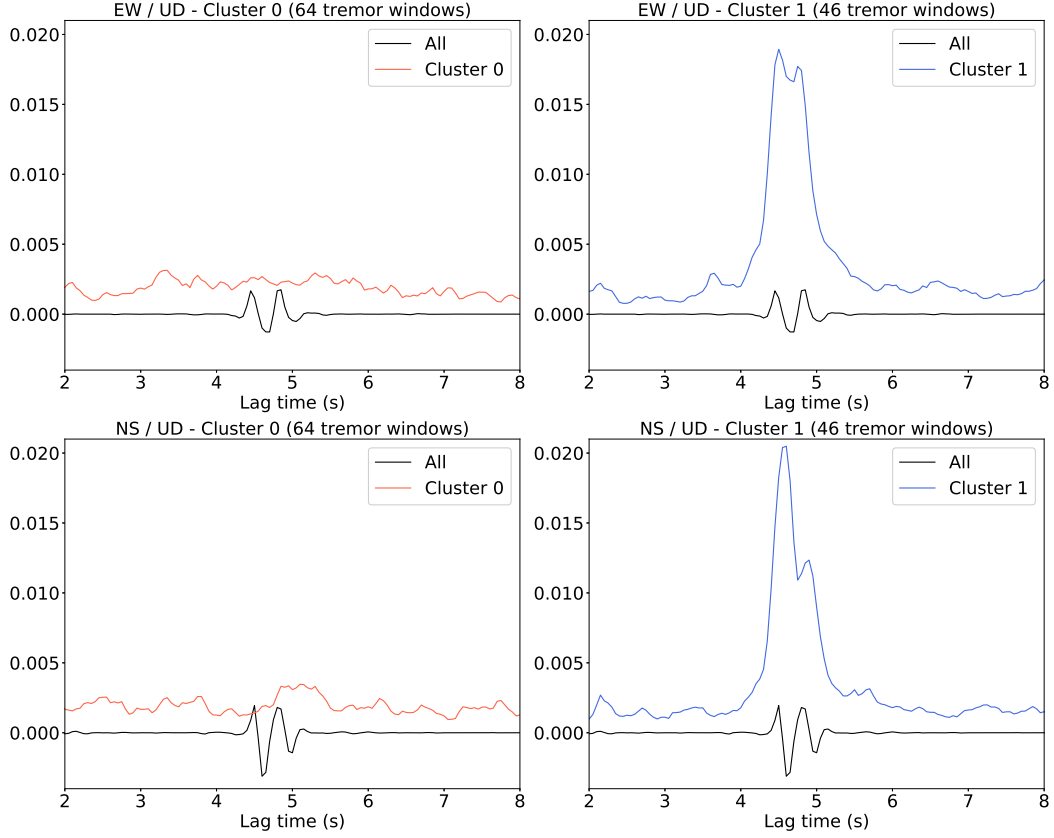
may be either because the tremor epicenter was mislocated, or because the signal-to-noise ratio is too low.

In the following, we are only interested in the value of the stacks for time lags close to the secondary peak, and not in the entire time window for which we have computed the cross-correlation. To determine which time window to look at, we compute the theoretical value of the time lag between the P- and S-wave arrivals if the source was located on the plate boundary. We then look for the timing  $\tau_{kl}$  of the absolute value of the stack in a time window starting 1 second before and ending 1 second after the theoretical time lag.  $k$  and  $l$  take values between 1 and 3 depending on whether the method used for the stacking of the stations and the stacking of the time windows is a linear stack, a  $n$ th-root stack or a phase-weighted stack. We thus have 9 possible values for the timing of the secondary peak. We define  $T_{min} = \min_{k=1,2,3;l=1,2,3} \tau_{kl} - 1$  and  $T_{max} = \max_{k=1,2,3;l=1,2,3} \tau_{kl} + 1$ , and we limit the rest of our analysis to the time window  $[T_{min}; T_{max}]$ .

To improve the signal-to-noise ratio of the peak in the stacked cross-correlation, we divided the one-minute-long time windows into two clusters, the ones that match the stacked cross-correlations well, and the ones that do not. In order to do the clustering, we stacked the stacked cross-correlation functions,  $S_{ij}(\tau)$ , over all the one-minute-long time windows to obtain  $S_i(\tau)$ . For each one-minute time window  $j$  we cross-correlated  $S_i(\tau)$  with  $S_{ij}(\tau)$  to obtain  $S_{ij}^c(\tau)$ . We want to verify whether the waveform  $S_{ij}(\tau)$  around the secondary peak matches well with the stack  $S_i(\tau)$ . We thus look for the maximum of the absolute value of the stack  $S_i(\tau)$  between one second before and one second after the theoretical time lag between P- and S-wave arrival if the source was on the plate boundary. We call the time lag corresponding to this maximum  $\tau_{max}$ . Then for the cross-correlation between  $S_{ij}(\tau)$  and  $S_i(\tau)$ , we keep only the values of lag times  $\tau$  between one second before and one second after  $\tau_{max}$ . For each  $i$  and  $j$  we determine 3 numbers from  $S_{ij}^c(\tau)$ : its value at zero lag time, its maximum absolute value and the time lag at which it takes its maximum absolute value, and we determine one number from  $S_{ij}(\tau)$ : the ratio of its maximum absolute value  $S_{ij}(\tau_{max})$  to its rms. We considered lag times  $\tau$  from 12 to 14 seconds to compute the value of the rms of the  $S_{ij}(\tau)$ . Each one-minute-long time window is thus associated with eight values of quality criteria, four for each of the the East and North channels. We then classified each one-minute-long time window into two different clusters, based on the value of these criteria, using a K-means clustering algorithm (function `sklearn.cluster.KMeans` from the Python library `SciKitLearn`). The K-means procedure is as follows: We choose to have 2 clusters, then we arbitrarily choose a center for each cluster. We put each one-minute-long time window into the cluster to which it is closest (based on the values of the eight criteria). Once all one-minute-long time windows have been put in a cluster, we recompute the mean of the eight criteria for each cluster, and iterate the procedure until convergence. On average, about 35% of the time windows fit well with the stack and are kept in the first cluster, while 65% do not fit well with the stack and are removed. For each cluster, we then stacked the envelopes of the cross-correlation functions over all the one-minute-long time windows belonging to that cluster using a phase-weighted stack. We tried using more than 2 clusters, but it did not improve the final stack of the best cluster. Figure 3 shows the stack of the envelopes of the  $S_{ij}(\tau)$  over the time windows  $j$  that correspond to cluster 0 (red) and cluster 1 (blue). The clustering has greatly improved the amplitude of the peak for cluster 1, and made the peak nearly disappear for cluster 0.

We did this analysis for grid cells located in a 50 km by 50 km area centered on each of the eight arrays. We thus consider up to  $11 * 11 * 8 = 968$  values of the time lag between the direct P-wave and S-wave. We assumed that the epicenter is at the center of the grid and determined the depth that satisfies that epicenter and the observed S-minus-P time. The velocity models are taken from the 3D velocity model from Merrill et al. (2020). For each array, we looked for the closest grid point (in terms of latitude and longitude) in the 3D model by Merrill et al. (2020) and used the corresponding layered model of compressional and shear wave speeds to compute the tremor depth. We thus used 8 different 1D velocity models corresponding to the 8 arrays. This allows us





**Figure 3.** Stack of the cross-correlation functions over all the 110 time windows from Figure 2. The black line is the stack  $S_i(\tau)$  over all time windows of the stack of cross-correlation functions over all stations within the array. The red line on the left panels is the stack over all the time windows in cluster 0 of the envelopes of the stack of cross-correlation functions over stations within the array. This corresponds to time windows that do not fit well with the stack. The blue lines on the right panels are the same as the red lines, except it uses time windows in cluster 1 (which contains the time windows that fit well with the stack). Top panels are the cross-correlation of the EW component with the vertical component, and bottom panels are the cross-correlation of the NS component with the vertical component. The stacked cross-correlation function has been cut between 2 and 8 seconds to focus on the time lags around the peak.

to take into account the substantial variations of the Poisson's ratio in the East-West direction.

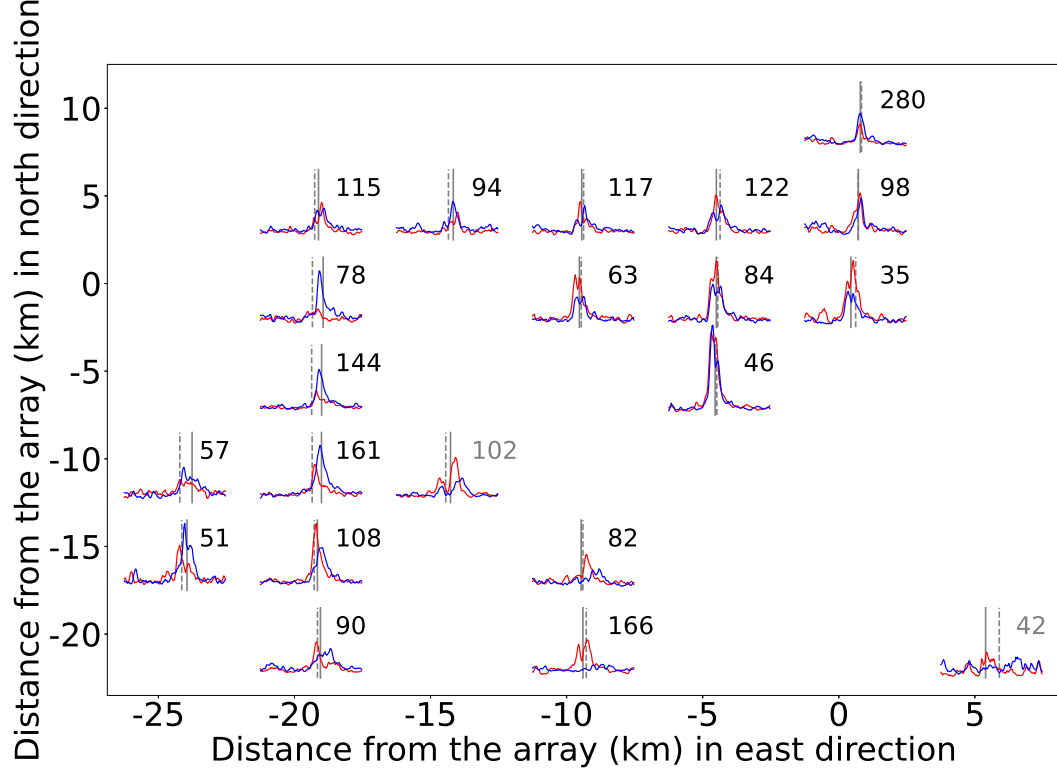
We verify that using the expected value of the time lag between P- and S-wave arrival if the source was located on the plate boundary does not introduce bias in the analysis. The highest peak in the absolute value of the phase-weighted stack of the cross-correlation functions  $S_i(\tau)$  within our defined window  $[T_{min}; T_{max}]$  is the same as the highest peak between 3 and 8 seconds for every array / tremor grid except for one (the grid cell located about 7 km south-east of the Burnt Hill array) so using the theoretical S-P time as a guide to define the time window has very little or no effect on the final travel-time observation.

## 4 Results

To obtain robust results, we limit our analysis to grid cells where there are at least 30 one-minute-long time windows in the best cluster. We assumed that the location of the tremor source is fixed during the one-minute-long time window where we compute the cross-correlation of the seismic signal. However, during an ETS event, rapid tremor streaks have been observed to propagate up-dip or down-dip at velocities ranging on average between 30 and 110 km/h (Ghosh et al., 2010b), which corresponds to a maximum source displacement of 0.9 km updip or downdip during the 30 seconds duration before and after the middle of the time window. The change in predicted S-minus-P time caused by changing source location by 0.9 km in the up- or down-dip direction is small for tremor along strike from the array or in the down dip direction. However, the change in this lag time for tremor sources up-dip from the arrays exceeds one quarter of the dominant period of the tremor signal (period = 0.33 s) for tremor sources more than 18 km updip from an array. Thus, tremors beyond 18 km updip of an array may not add coherently during rapid tremor migrations. This method works best if the P-wave is cleanly recorded on the vertical component and the S-wave on the horizontals, so generally speaking the results are more robust for near vertical ray paths.

Finally, the data from some of the arrays are very noisy, which makes it hard to see a signal emerging when stacking over the one-minute-long time windows. We chose to keep only the locations for which the ratio between the maximum value of the stack of the envelopes of the cross-correlation functions to the root mean square is higher than 5. We compute the root mean square in cluster 1 for a time lag between 12 and 14 s because we do not expect any reflected wave to arrive that late after a direct wave. The corresponding stack of the envelopes of the cross-correlation functions are shown in Figure 4 for the East-West component and the North-South component. The grey dashed vertical line shows the theoretical time lag between the arrival of the direct P-wave and the arrival of the direct S-wave using the corresponding 1D velocity model for this array and the plate boundary model from Preston et al. (2003), the grey solid line corresponds to the moment centroid of the stack. There is a good agreement between the timing of the centroid and the theoretical time lag for most of the locations of the source of the tremor.

To compute the depth, we select the EW or the NS component with the larger maximum value of the peak. We focus on the part of the stack of the envelopes of the cross-correlation functions located between 2 seconds before and 2 seconds after the time lag  $\tau_{max}$  corresponding to the secondary peak obtained earlier. We computed the moment centroid of this part of the stack and assumed that it was equal to the time lag between the arrivals of the direct P-wave and the direct S-wave. We then computed the corresponding depth of the source of the tremor for all the locations of the source of the tremor. To verify the effect of the width of the time window for which we compute the moment centroid, we compute the centroid and the corresponding depth of the source for widths equal to 2 seconds, 4 seconds, and 6 seconds. We compute the variations in depths when decreasing the width from 4 seconds to 2 seconds. 87% of the differences in depth are under 2 kilometers. The median difference is 0.064 km, so there is no bias towards shall-



**Figure 4.** Stack of the envelopes of the cross-correlation signals for different positions of the tremor source relative to the Big Skidder array showing the cross-correlation between the East-West and the vertical components (red lines) and between the North-South and vertical components (blue lines). The theoretical S-minus-P times (grey dashed line for the Preston model) are generally in good agreement with the centroids in cross-correlation functions (grey solid line). The location of the tremor varies from west to east (left to right) and from south to north (bottom to top). The numbers next to each graph indicate the number of one-minute-long time windows in the best cluster. For clarity, we plotted only the part of the cross-correlation signal corresponding to time lags between 2 and 8 seconds.

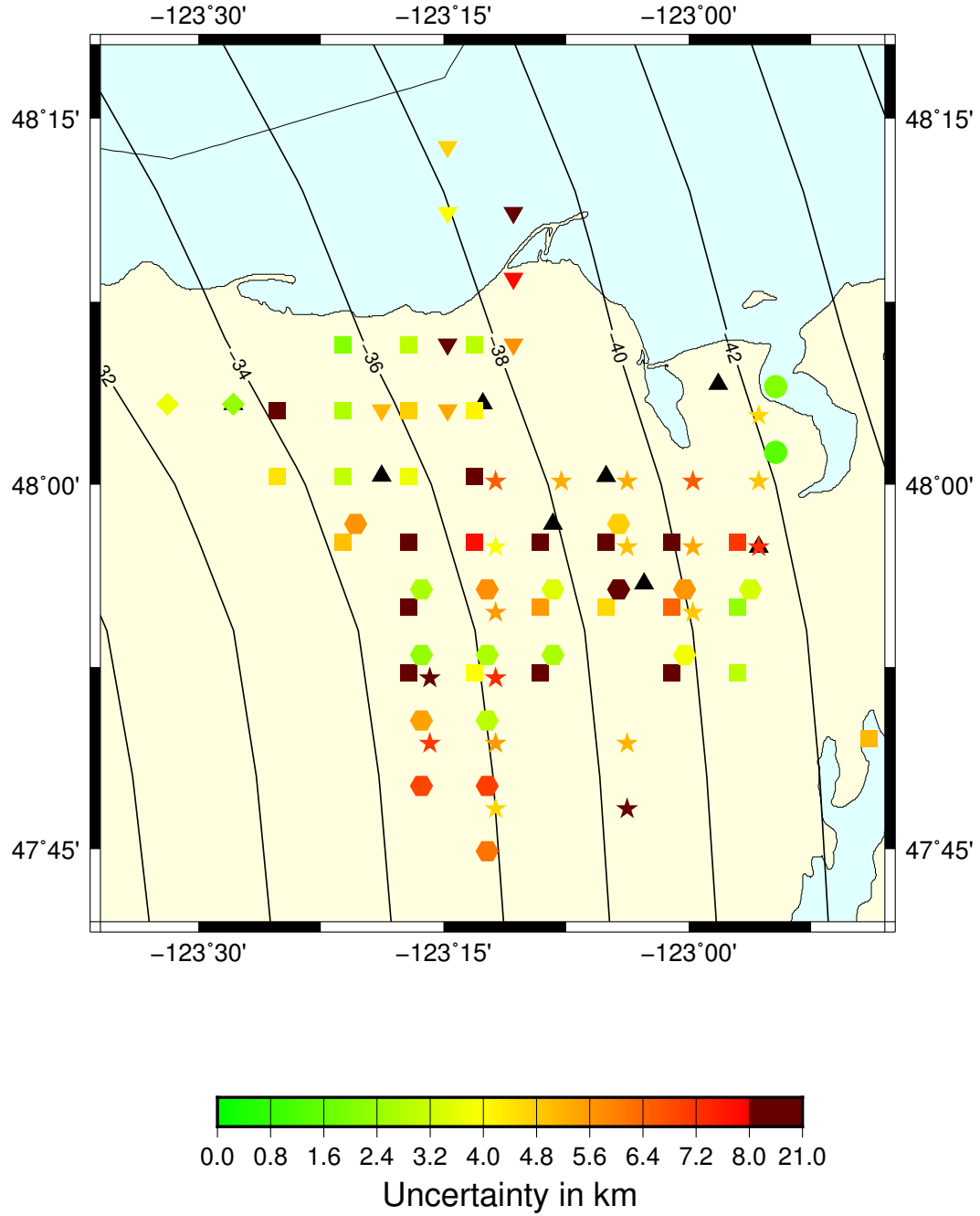
lower or deeper depths when we decrease the width of the time window. When we compute the variations in depths when increasing the width from 4 seconds to 6 seconds, 84% of the differences in depth are under 2 kilometers and the median difference is 0.054 km. We did the same analysis for the eight arrays of the experiment and each of the tremor-location grid points. The corresponding stacks of the envelopes are shown in Figures S1 to S7 in the supplementary material. For the two arrays Cat Lake and Lost Cause, there are very few source-array locations that have both enough tremor and a high ratio between the peak and the root mean square. Moreover, for the locations where we have a peak, the peak is often not very clear and stretched along the time axis. We did not use data from these two arrays. For the Port Angeles array, there is only a clear peak for a near vertical incidence of the seismic waves. We choose to keep this array in the analysis in order to have two additional data points in the westernmost region of the study area.

To estimate the uncertainty on the depth of the source of the tremor, we computed the width of the stack of the envelopes of the cross-correlation functions at half the maximum of the peak. We then computed the associated depth difference using the 1D velocity model. As we computed the envelopes of the cross-correlation functions before stacking, the peak is large and also the associated uncertainty on the depth. Nevertheless, about 75% of the data points have an uncertainty under 8km (Figure 5). The uncertainties are higher for the Burnt Hill array, and are almost always lower than 8km for the five other arrays. We tried different stacking methods, both for the stacking of the correlation functions over all the seismic stations of a given array, and for the stacking of the envelopes of those stacks over the one-minute-long time windows when tremor is detected. We experimented with a linear stack, a  $n$ th-root stack, and a phase-weighted stack, and found that using a phase-weighted stack for both the stacking over the stations and the stacking over one-minute-long time windows gave the lower uncertainty on the tremor depth.

In the following, we kept only the data points for which the maximum amplitude of the stack is higher than 0.05. Figures 6 and 7 show respectively a map and three cross-sections of the depth of the source of the tremor. Figure 8 shows a map of the distance between the source of the tremor and the plate boundary from the Preston model, alongside with the depth of the low-frequency earthquake families observed by Sweet et al. (2019) and Chestler and Creager (2017a, 2017b). There is a good agreement between the depth of the source of the tremor, the depth of the low-frequency earthquake families, and the depth of the plate boundary. On the cross-section figures, we compare the distance of the source of the tremor to the plate boundary for different locations of the cross-section. We note that the depth of the tremor matches well the depth of the low-frequency earthquakes.

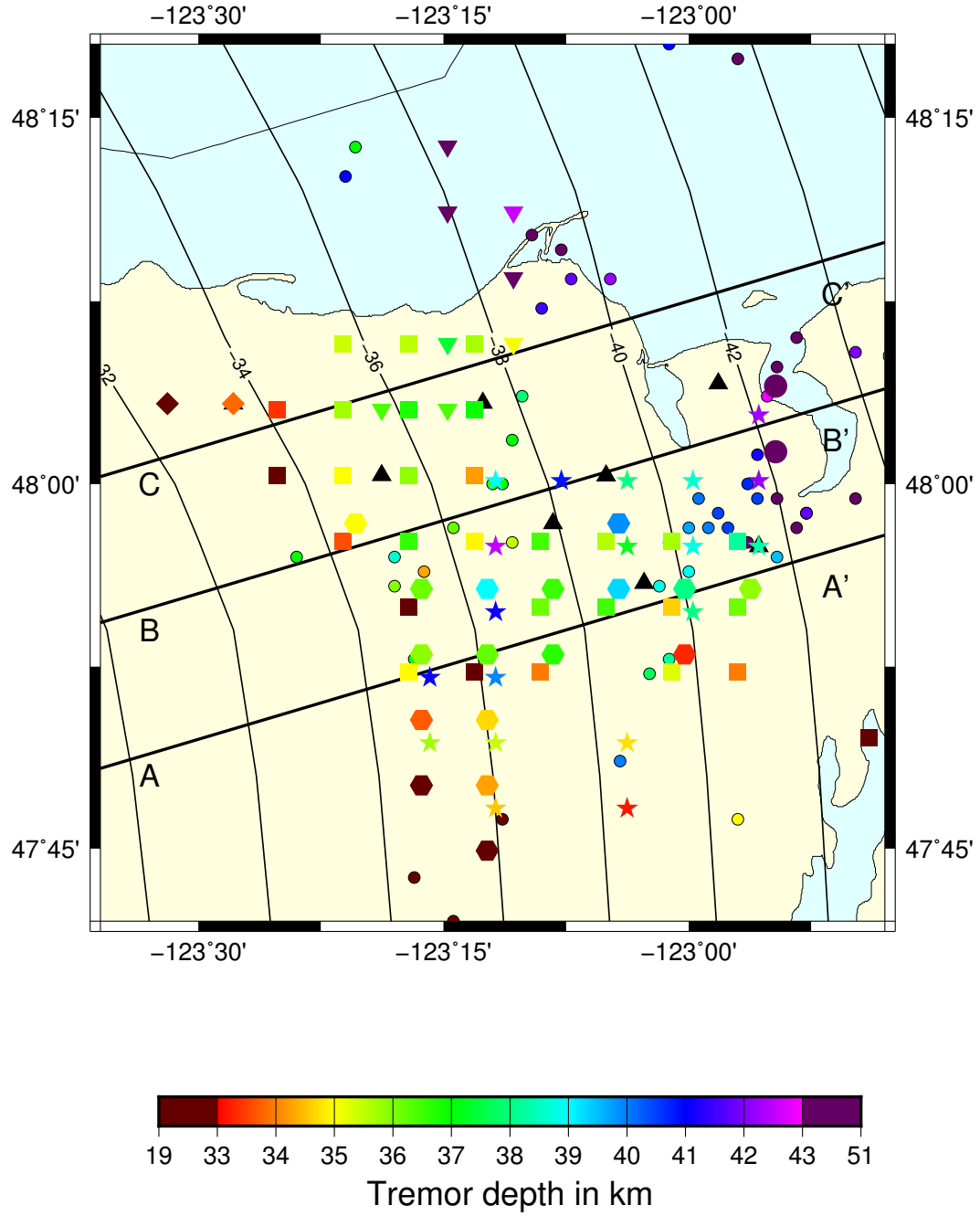
## 5 Discussion

Previous studies have shown evidence for seismic anisotropy near the slab interface (Nikulin et al., 2009) and in the overriding continental crust (Cassidy & Bostock, 1996). If the source of the tremor is located in or under the anisotropic layer, the time lag between the arrival of the direct P-wave and the arrival of the direct S-wave could be different depending on whether we consider the East-West component or the North-South component. To verify whether possible anisotropy could affect our results, we computed the time difference between the timing of the maximum of the stack of the envelopes of the stacked cross-correlation functions between the East-West component and the vertical component, and between the North-South component and the vertical component. We also computed the associated difference in depth of the source of the tremor (see Figure 9) for all arrays and all locations of the tremor. The difference in time is generally less than 0.25 s while the difference in depth is generally less than 2 kilometers, which is similar to the uncertainty on the tremor depth. As the time difference between the East-West component and the North-South component due to anisotropy is expected to vary depending on the relative position of the array compared to the source of the tremor, we also plotted the time difference as a function of the distance from source to array, and

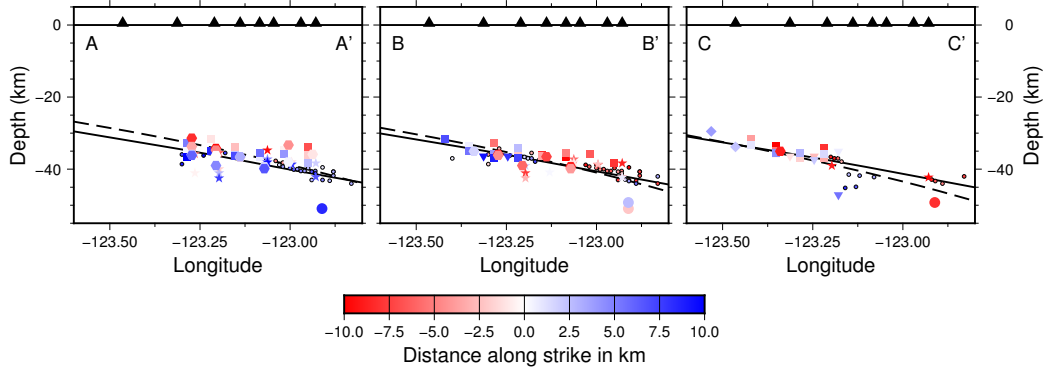


**Figure 5.** Map of the uncertainty on the depth of the tremor based on the width of the stack of the envelopes of the cross-correlation functions for arrays Burnt Hill (squares), Big Skidder (stars), Danz Ranch (inverted triangles), Gold Creek (large circles), Port Angeles (diamonds), and Three Bumps (hexagons).





**Figure 6.** Map of the depth of the source of the tremor and of the low-frequency earthquake families (small filled circles) identified by Sweet et al. (2019) and Chestler and Creager (2017a, 2017b). The three black lines indicate the positions of the cross-sections shown in Figure 7. Tremor depths are from arrays Burnt Hill (squares), Big Skidder (stars), Danz Ranch (inverted triangles), Gold Creek (large circles), Port Angeles (diamonds), and Three Bumps (hexagons)

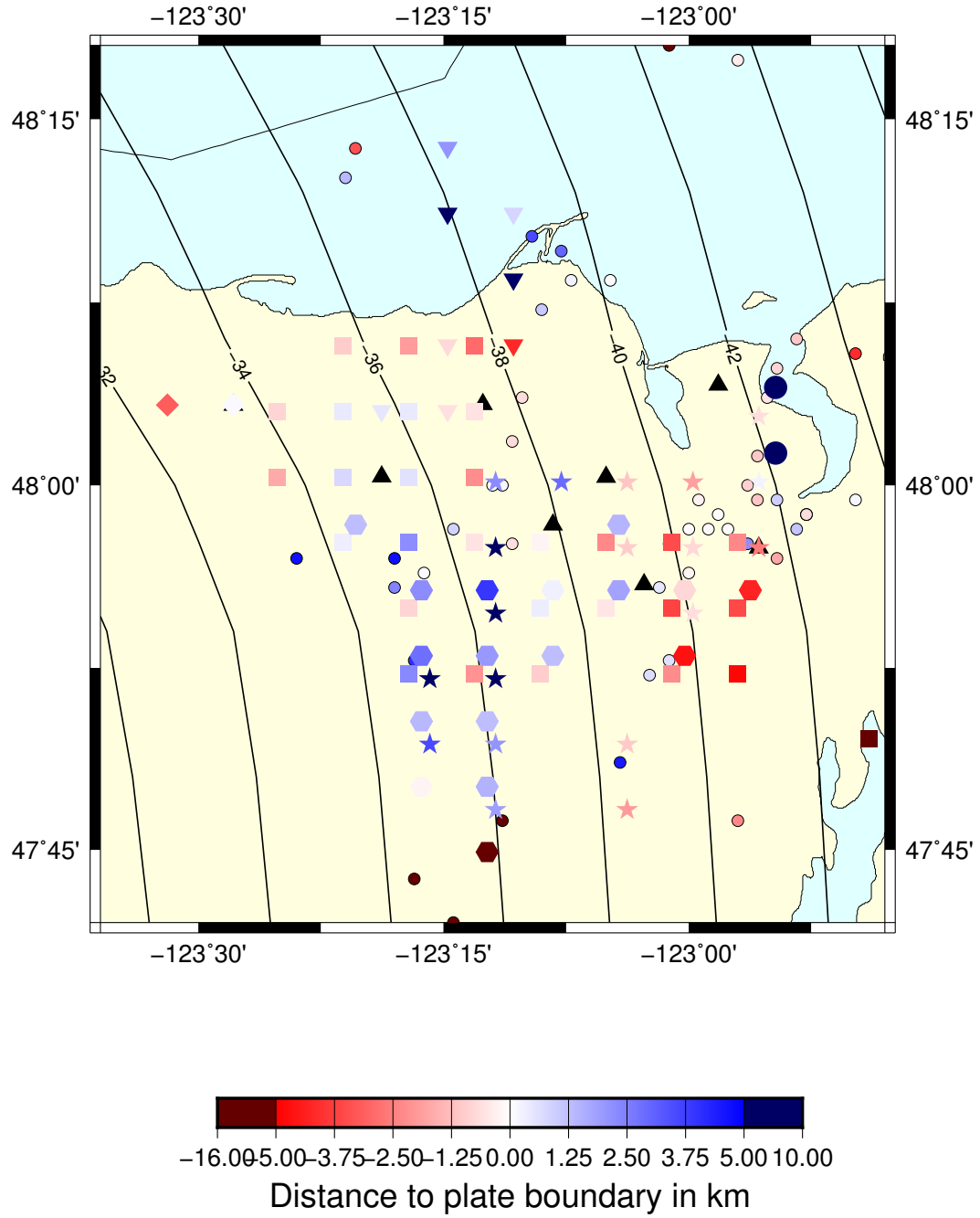


**Figure 7.** Cross-sections showing depth of the tremor and of the low-frequency earthquake families (small filled circles) identified by Sweet et al. (2019) and Chestler and Creager (2017a, 2017b) for cross sections A-A', B-B', and C-C' shown in Figure 6. The black line corresponds to the plate boundary profile of McCrory et al. (2006) along the southern most black line shown on Figure 6, and the dashed line to the plate boundary profile of Preston et al. (2003). The color bar shows the distance of the tremor and the low-frequency earthquakes along the strike. Only tremor and low-frequency earthquakes less than 10 km away from the profile line are shown. Tremor depths are from arrays Burnt Hill (squares), Big Skidder (stars), Danz Ranch (inverted triangles), Gold Creek (large circles), Port Angeles (diamonds), and Three Bumps (hexagons).

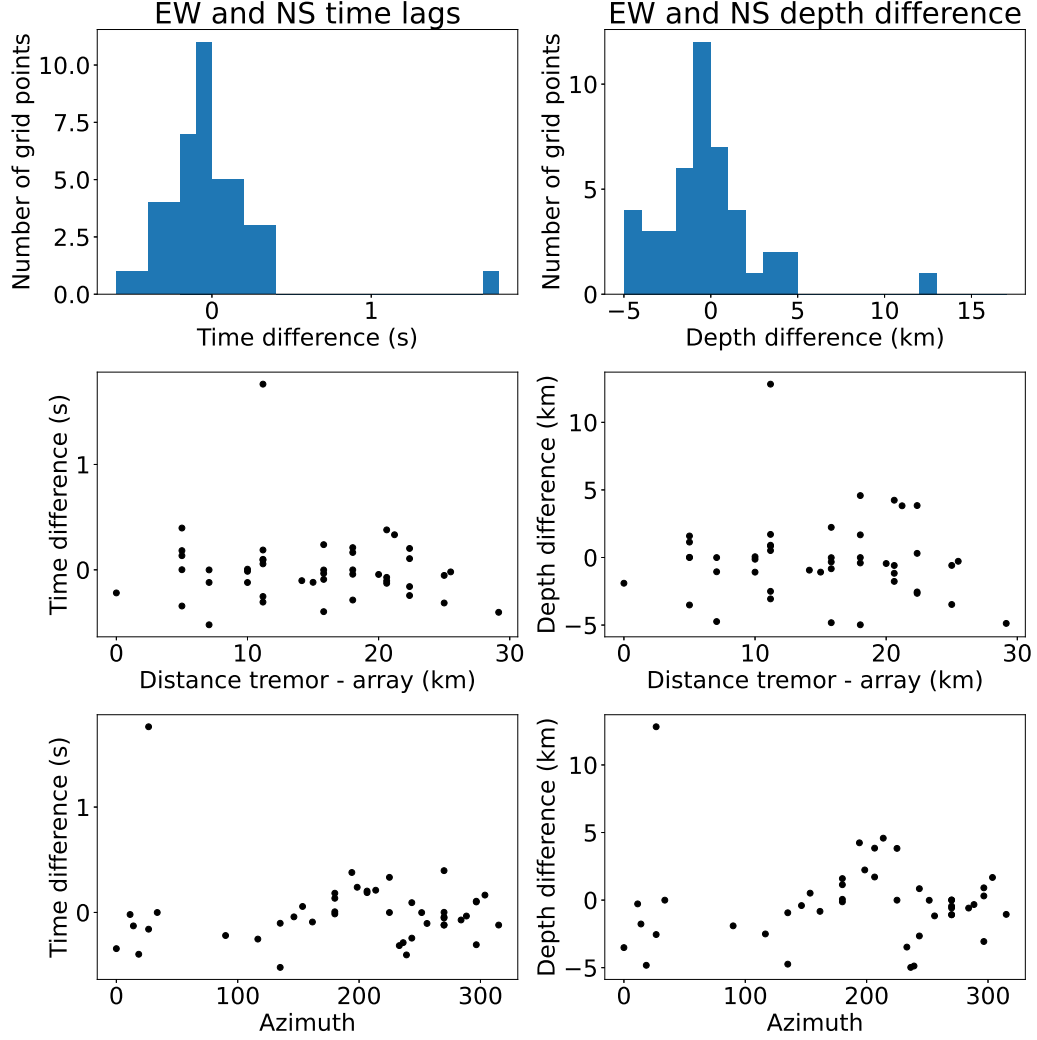
as a function of the azimuth, as well as the corresponding depth difference (Figure 9). The time difference does not increase with the distance from the source to the array, and there is no seismic path orientation that gives bigger time difference. Thus, seismic anisotropy does not seem to have a significant effect on the time lags between the arrival of the direct P-wave and the arrival of the direct S-wave, and can be neglected. Nikulin et al. (2009) observed anisotropy in the low-velocity layer beneath station GNW, located in the eastern Olympic Peninsula, south of the eight seismic arrays used in this study. If the tremor is located above the low-velocity layer, we do not expect this source of seismic anisotropy to introduce a significant effect on our measured time lags. Nikulin et al. (2009) locate the low-velocity layer above the plate boundary, in the lower continental crust, which is shallower than the location given by Bostock (2013), who locates the low-velocity layer in the upper oceanic crust. However, even if a low-velocity layer with 5 % anisotropy is located in the lower continental crust as indicated by Nikulin et al. (2009), the resulting difference in time lags should not be more than a few tenths of a second, and the resulting difference in depth should not be more than 2 kilometers. Cassidy and Bostock (1996) observed anisotropy in the continental crust, especially in the upper 20 kilometers to the north of our arrays. However, the anisotropy resulted in time delays of the seismic waves of no more than 0.32s for deep earthquakes (40-60 km depth) and not more than 0.20s for shallow earthquakes (15-30 km depth). The corresponding difference in tremor depth is similar to the uncertainty.

Several approximations have been made to compute the tremor depth. First, we stacked over all the tremor in 5km by 5km grid cell. The depth difference corresponding to epicentral tremor locations at the center versus the edge of a cell varies from about 1 to 2 km for cells near the array to cells 25 km from an array. Second, the  $V_p / V_s$  ratio is not very well known. A variation of about 1% of the  $V_p / V_s$  ratio used to compute the depth would lead to a variation of about 1-1.5 km of the corresponding tremor depth (Figure 10).

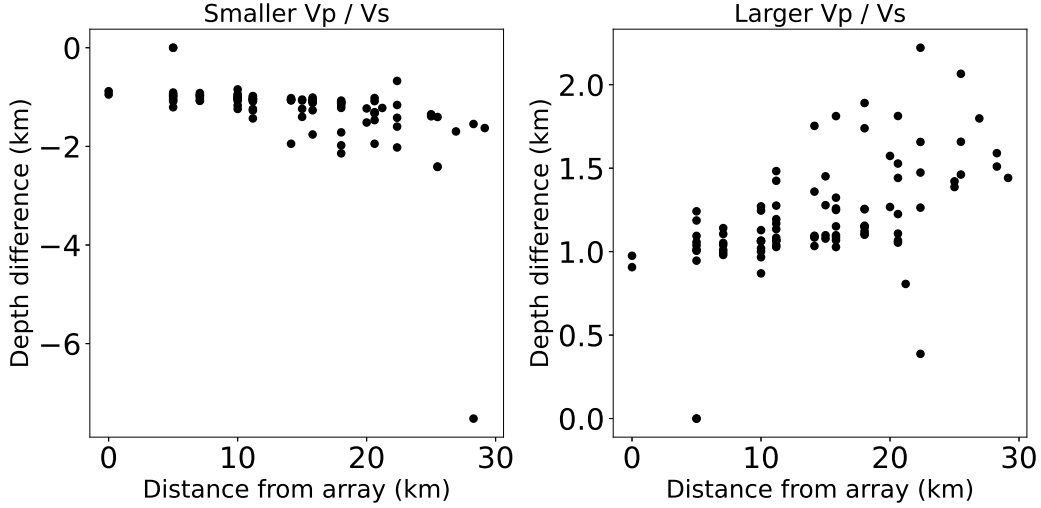
As proposed by Kao et al. (2009), the source of the tremor could be distributed inside a layer that is 15 or more kilometers thick. We have assumed that all the tremor within a given grid cell originate from the same depth, and averaged over all the data



**Figure 8.** Map of the distance between the plate boundary (from the Preston model) of the tremor and of the low-frequency earthquake families (filled circles) identified by Sweet et al. (2019) and Chestler and Creager (2017a, 2017b)). Tremor located below the plate boundary is blue, and above is red. Tremor depths are from arrays Burnt Hill (squares), Big Skidder (stars), Danz Ranch (inverted triangles), Gold Creek (large circles), Port Angeles (diamonds), and Three Bumps (hexagons).



**Figure 9.** Left: S-minus-P times measured from envelopes of cross-correlation functions on the East-West component minus those from the North-South component. Right: Corresponding difference in inferred tremor depths. These are plotted as histograms (top), versus epicentral distance between tremors and arrays (middle) and tremor to array azimuth. There is no systematic signal that might be caused by anisotropy.

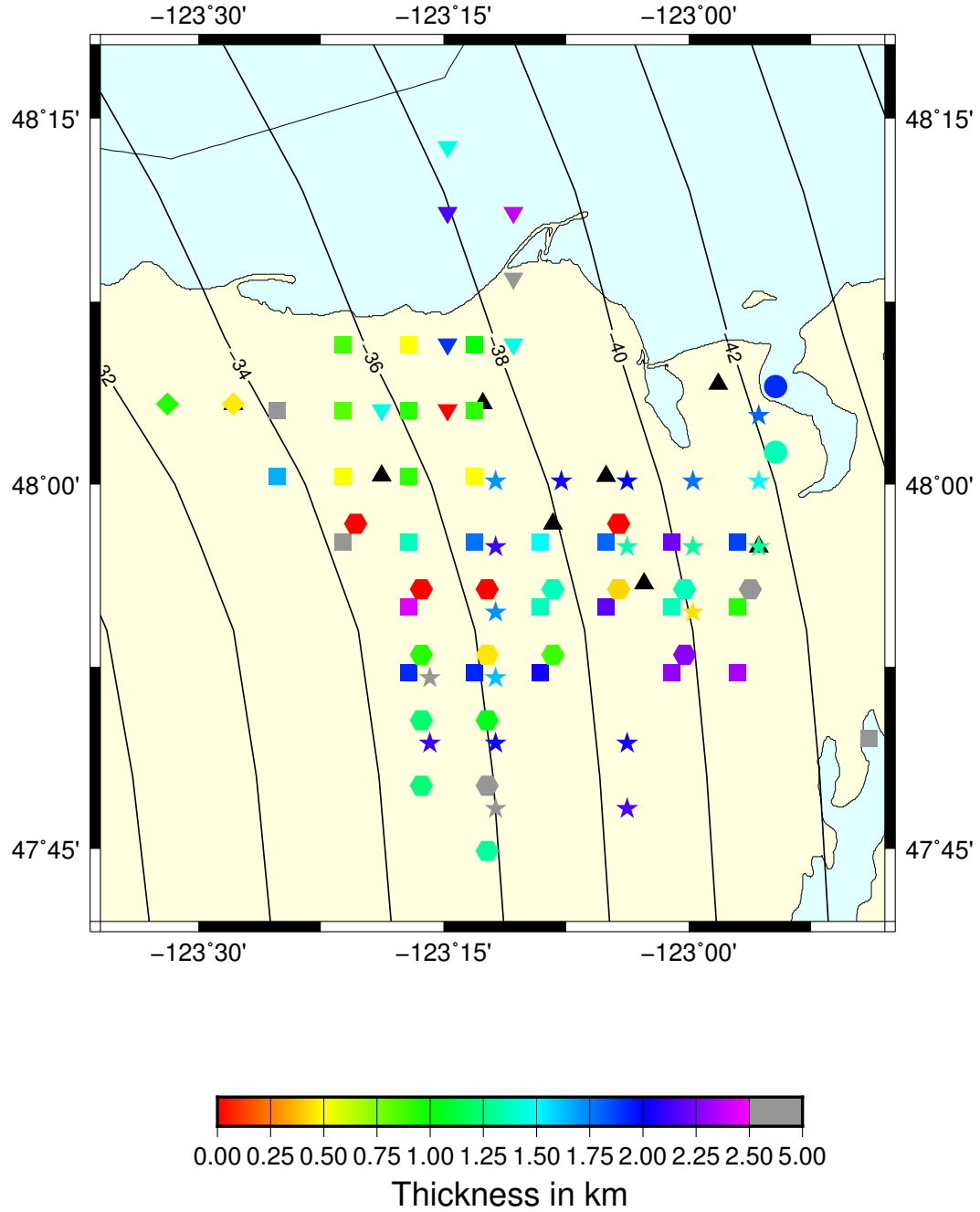


**Figure 10.** Variations of the depth of the tremor and we decrease the  $V_p / V_s$  ratio of 1% (left) and when we increase the  $V_p / V_s$  ratio of 1% (right). A change in the  $V_p / V_s$  ratio corresponds to a change in the theoretical time lag between direct P-wave and direct S-wave if the source is located on the plate boundary. Thus, it changes the time interval over which we compute the centroid of the stacked envelopes, and thus the time lag we use to compute the depth.

to get the tremor depth. However, instead of being located on the same plane near the plate boundary, the tremor may be scattered over a layer surrounding the plate boundary. To compute the thickness of this layer, for each location of the array and the source of the tremor, we computed for each one-minute-long time window for which the cross-correlation function matches well the stacked cross-correlation the time lag between the time corresponding to the maximum absolute value for the cross-correlation function and the time corresponding to the maximum absolute value for the stacked cross-correlation. We thus obtained a distribution of time lags and the corresponding distribution of depths, and we tried to estimate the scale of the interval over which the depths vary. An example of time lags distribution is shown in Figure S8 of the supplementary material. Using the standard deviation could lead to overestimate the width of the interval, and the corresponding thickness of the tremor layer, as the standard deviation is very sensitive to outliers. Instead, we use the Qn estimator of Rousseeuw and Croux (1993), which is a more robust estimator of scale, similar to the median absolute deviation (MAD). Qn is equal to the  $k$ th order statistic of the  $\binom{n}{2}$  interpoint distances where  $n$  is the number of points, and  $k = \binom{h}{2}$  with  $h = \lceil \frac{n}{2} \rceil + 1$  and  $\lceil x \rceil$  denote the integer part of  $x$ . As the MAD, the Qn estimator is not very sensitive to outliers, and it has the advantage of being suitable for asymmetric distributions, contrary to the MAD, which attaches equal importance to positive and negative deviations from the median. We then used the scale of the interval over which the tremor depth varies as an estimate of the thickness of the tremor layer (see Figure 11). The average thickness of the tremor zone is about 1.6 km, while nearly all the values of the thickness are less than 3km, which is substantially lower than the depth extent from Kao et al. (2009). The smallest values for the thickness are about 0.8-2 kilometers.

Another way of estimating the thickness of the tremor zone is to fit a plane with a linear regression from all the values of the depth and compute the residuals from the





**Figure 11.** Map of the thickness of the tremor layer estimated from scatter of individual 1-minute tremor windows. Tremor widths are from arrays Burnt Hill (squares), Big Skidder (stars), Danz Ranch (inverted triangles), Gold Creek (large circles), Port Angeles (diamonds), and Three Bumps (hexagons).

**Table 1.** Summary of distances to plate boundary

|                                    | Median     | MAD      | Qn       |
|------------------------------------|------------|----------|----------|
| Tremor depth - Preston depth       | - 0.207 km | 2.623 km | 1.313 km |
| Tremor depth - McCrory depth       | - 0.850 km | 2.429 km | 1.390 km |
| LFE families depth - Preston depth | - 0.189 km | 1.312 km | 0.871 km |
| LFE families depth - McCrory depth | - 0.495 km | 1.805 km | 0.988 km |

regression (Figure 12). The Qn estimator of scale (Rousseeuw & Croux, 1993) for the error between the tremor depth and the fitted plane is only 1.3 km.

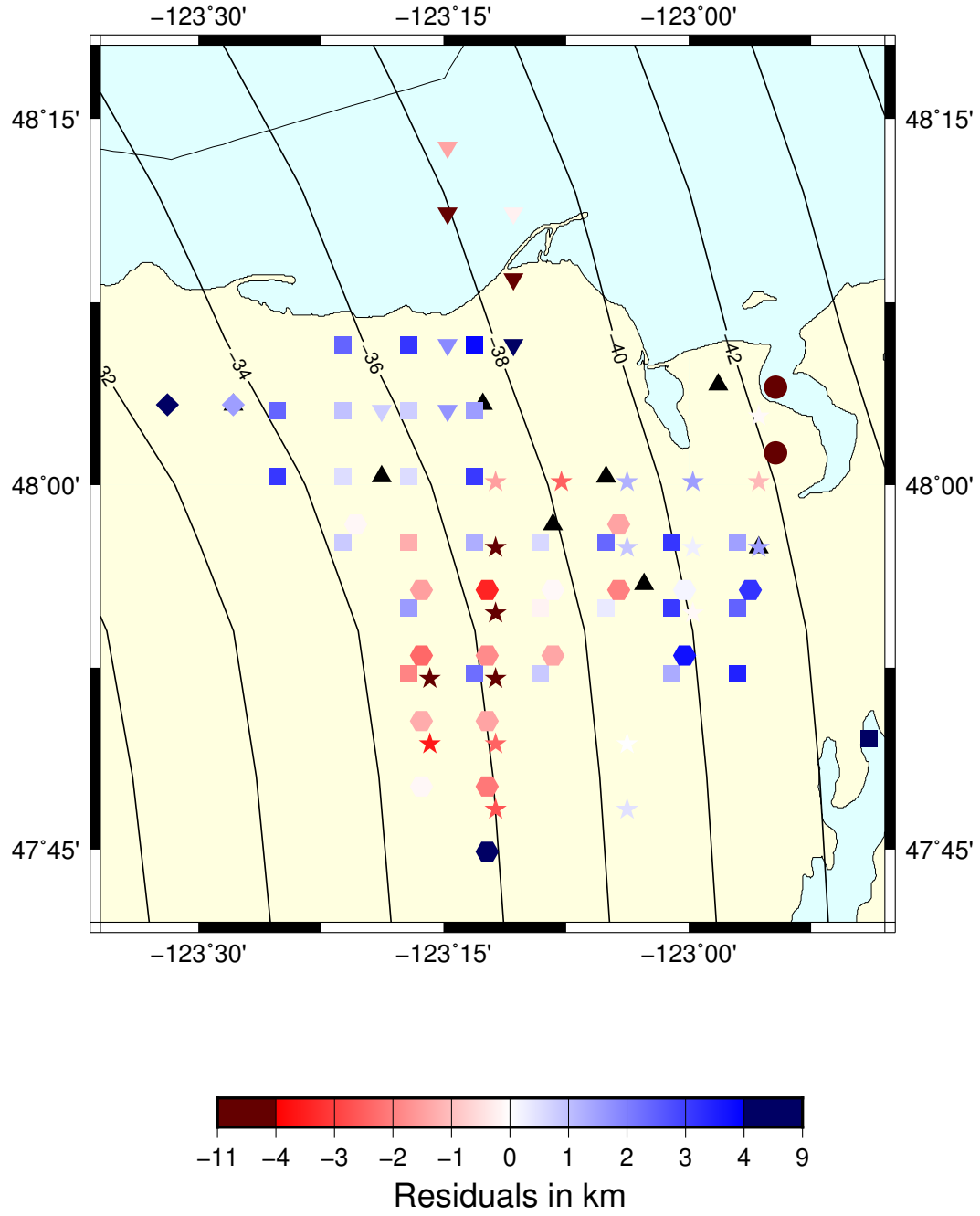
In Table 1, we report the values of the median, the median absolute deviation (MAD), and the Qn estimator of scale for the difference between the depth of the tremor and the low-frequency earthquakes and the depth of the plate boundary, for the McCrory model and for the Preston model. Small negative values of the median correspond to tremor and low-frequency earthquakes located a little bit above the plate boundary. The depth range of the tremor (Qn = 1.3 km) is larger than the depth range of the low-frequency earthquake families from Chestler and Creager (2017a, 2017b) (Qn = 0.9 km). It is also larger than the thickness of the flow channel where Sammis and Bostock (2021) suggest that the LFEs are generated (0.5 to 1.5 km). However, this may be due to the uncertainty on the determination of the tremor depth. The tremor and low-frequency earthquakes are slightly closer to the plate boundary for the Preston model than for the McCrory model. This may be because the P-wave velocity model of Preston et al. (2003) was used as the initial velocity model by Merrill et al. (2020) to compute the full P- and S-wave velocity model that we use to get tremor depth from S minus P times. The Preston P-wave velocity model was also used by Chestler and Creager (2017a, 2017b) to locate the low-frequency earthquake families.

## 6 Conclusion

We developed a method to estimate the depth of the source of the tectonic tremor, and the depth extent of the region from which the tremor originates, using S minus P times determined from lag times of stacked cross-correlations of horizontal and vertical components of seismic recordings from small aperture arrays in the Olympic Peninsula, Washington. We found that the source of the tremor is located close to the plate boundary in a region no more than 2-3 kilometers thick. The source of the tremor is thus distributed over a slightly wider depth range than the low-frequency earthquakes. However, due to the depth uncertainty, it is difficult to conclude whether the tremor is located near the top of the subducting oceanic crust, in the lower continental crust just above the plate boundary, in a layer distributed above and below the plate boundary, or confined to a very narrow plate boundary. The location of the tremor relative to the low-velocity layer also observed near the plate boundary also remains uncertain. Tremor and LFE depths are consistent with filling a volume in the upper subducted crust that is characterized by high fluid pressure and very low S-wave velocities described as the preferred model by Bostock (2013).

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**Figure 12.** Map of the residuals from the linear regression fitting all the depths to a plane. Residuals are from arrays Burnt Hill (squares), Big Skidder (stars), Danz Ranch (inverted triangles), Gold Creek (large circles), Port Angeles (diamonds), and Three Bumps (hexagons).

done using GMT (Wessel & Smith, 1991). The Python scripts used to analyze the data and make the figures can be found on the first author’s Github account, accessible through Zenodo (Ducellier, 2021).

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