SYSC 4906 Introduction to Machine Learning Fall 2020

Assignment 1

Submission instructions: Please prepare a single Jupyter Notebook with all of your answers. Some answers will only require text while others require text+code+results. Please use the template solution available from the course GitHub repo under "Assignments/Assignment1".

Q1) Calculate the gradient of the $f(x, y, z) = x^3z - 2xy^2 + 5z$ at (-3, -2, 1). What does this vector represent?

Q2) You are working at a COVID-19 testing center as a data scientist and are asked to determine how severe the symptoms of patients who come to get tested are. For a day, you record each person's symptom severity using a subjective rating on a 1-5 scale for. These are the results from that day:

1	4	4	3	4	3	1	3	2	3

1. What is the <u>expected value</u> from this sample? Using an <u>unbiased estimator</u>, what is the sample <u>variance</u> and <u>standard deviation</u>?

After a long time of collecting this data, your statistician friend has determined the probability mass function, Pr(x), where x is severity rating. They also found the probability that a patient tested positive for COVID, given their symptom severity, Pr(+|x). They provide the table below, but you spilled coffee on Pr(2) and can't make out the value. You need to present these results to your boss!

x	1	2	3	4	5
Pr(x)	0.20	??	0.30	0.30	0.05
Pr(+ x)	0.10	0.15	0.20	0.40	0.70

- 2. What is Pr(2)?
- 3. Find the expected value and the variance for Pr(x).
- 4. Find the probability that a patient has a symptom severity of x=5, given that they tested **negative** for COVID-19. That is, find Pr(5|-). *Hint: Pr(+) can be found by summing over Pr(+|x)Pr(x), for all x. Pr(-|x) can be derived from Pr(+|x).*

- Q3) Create a python notebook which loads the Kaggle Heart attack possibility dataset (https://www.kaggle.com/nareshbhat/health-care-data-set-on-heart-attack-possibility). This dataset has 13 features each and 2 classes of heart attack possibility: target: 0= less chance of heart attack; 1= more chance of heart attack. *Hint: look at the notebooks from Tutorials 2 & 3 for example code for achieving the steps below.*
 - a) Split the data, using 75% for training and 25% for test. Make sure you use stratified sampling.
 - b) Train and test a logistic regression classifier. How accurate is your classifier?
 - c) Repeat part b), but using only the age and resting blood pressure features from the dataset. Was the classifier accuracy impacted?
 - d) Using the 2-feature classifier from part c), create two subplots using the <u>age and</u> <u>resting blood pressure</u> features from the data set. See Tutorial 3 Part 2 for similar plots.
 - i) On the first, plot the decision boundary and the training data. Use green for less chance (target==0) and blue for more chance (target==1).
 - ii) On the second, plot the decision boundary and the test data. Use the same colours (blue/green), but highlight all misclassified test points (from either class) in red.
- Q4) Linear regression. Download the file "Assig1Q3.csv" from the course GitHub repo under "Assignments/Assignment1". The first column represents the X values, while the second column represents the Y values.
 - 1. Plot the data
 - We are going to use linear regression to fit a linear and a quadratic model to these data. <u>Without using sklearn.linear_model</u> (or other linear regression libraries), write your own python code to implement the least squares solution for linear regression. That is:

$$\beta = (X^T X)^{-1} X^T y$$

- 3. Assuming the model y=mx+b, use your code to best-fit the parameters m and b to the data. Report your optimal parameter values. *Hints:*
 - a. recall that you must create the 'augmented' feature vector X from the given x data (add a column of 1's).
 - b. look at numpy.T(), numpy.matmul(), numpy.dot(), and numpy.linalg.inv()
- 4. Plot your line of best fit on top of the data
- 5. Calculate the sum of square residuals, or mean squared error, as in:

$$MSE(\beta) = \sum_{i=1}^{N} (y - X\beta)^{2}$$

- 6. Assuming the model $y = ax^2 + bx + c$, repeat steps 2-4 using this new model (i.e. estimate the optimal values for a,b,c; report those estimates; plot the line of best fit; report the MSE).
- 7. Briefly discuss which model would you prefer for these data?
- 8. Why is best-fitting the second (quadratic) model still considered linear regression?

- Q5) Create a Jupyter Notebook based on <code>Tutorial-3_ComparingMultipleClassifiers.ipynb</code> to use <code>make_classification</code> to create a linearly separable dataset, with 2 classes, 2 informative features, the number of clusters per class to 1, 1500 samples per class, using a class_sep=1.7, and a random_state of 5. Generate some random noise of the same shape as your feature data, drawn from a standard normal distribution (see <code>numpy.random</code>) and a random state of 5.
 - 1. Create four datasets: 1) no noise, 2) data + 0.5 * noise, 3) data + 1.0 * noise, and 4) data + 2.0 * noise. For all four datasets, plot the data, labelling each (sub)plot by the degree of noise added (i.e. 0, 0.5, 1.0, and 2.0)
 - 2. For each dataset, create training and test data using a 70/30 train/test split
 - 3. For each dataset, train and test an SVM classifier with a polynomial kernel with degree=2, and C=1.0. Report the test score for each. How does prediction accuracy change with noise level?
 - 4. For a noise level of 0.5, train and test SVM classifiers using the following values for C: {0.001, 0.01, 0.1, 1, 10, 100}. Report the test accuracy for each. How does performance vary with C? Briefly describe what the C controls for sklearn.svc. *Hint: look at the documentation for sklearn.svc rather than the class notes here...*