Factor Trinomials

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Definition: A trinomial is a polynomial that has three terms. For example, $x^2 + 5x + 4$ is a trinomial. The factored form of $x^2 + 5x + 4$ is (x + 4)(x + 1).

To factor a trinomial:

Step 1: Set up a product of two () where each will hold two terms. It will look like ()().

Step 2: Find the factors that go in the first positions of each set of ().

Step 3: Decide on the signs that will go in each set of ().

Step 4: Find that factors that go in the last positions of each set of ().

Example: Factor: $x^2 + 4x - 12$.

Step 1: () (

) The only possible factors of x^2 are x and x. Step 2: (x) (x

Step 3: (x +)(x -) The last term is negative, use opposite signs.

Step 4: (x + 6)(x - 2) The factors of -12 are $\pm 1 \cdot \pm 12$ or $\pm 3 \cdot \pm 4$ or $\pm 6 \cdot \pm 2$ and the only pair of these that can have a sum of 4 (the coefficient of the middle term) is 6 and -2.

Practice on Your Own

Factor each polynomial completely.

1.
$$x^2 + 5x + 4$$

2.
$$x^2 + 3x - 10$$

3.
$$x^2 - 4x + 3$$

4.
$$x^2 - x - 20$$

5.
$$x^2 + 2x - 24$$

6.
$$x^2 + 10x + 21$$

7.
$$x^2 - 10x + 16$$

8.
$$x^2 - 8x - 9$$

9.
$$x^2 - 18x + 45$$

Check

Factor each polynomial completely.

10.
$$x^2 + 7x + 10$$

11.
$$x^2 - 11x + 28$$

12.
$$x^2 + 7x - 30$$

13.
$$x^2 - 3x + 2$$

14.
$$x^2 + 49x + 48$$

15.
$$x^2 - 7x - 60$$