

Graficas

1.1 Kruskal

```

1 //Incluye Union Find bajo Estructuras.
2 struct edge {
3     int u, v, w;
4     bool operator< (const edge &o) const{ return w < o.w; }
5 };
6 vector<edge> edges;
7 int kruskal() {
8     int res = 0;
9     sort(edges.begin(), edges.end());
10    for(auto e : edges) if(join(e.u, e.v))
11        res += e.w; // uv es arista del MST
12    return res;
13 }

```

1.2 LCA

```

1 const int MAXN = 1e6, LOG = 20;
2 vector<int> adj[MAXN];
3 int up[LOG][MAXN], dep[MAXN];
4 void dfs(int s, int p = 0) {
5     up[0][s] = (p != s);
6     dep[s] = (p ? dep[p] + 1 : s);
7     for(auto v : adj[s]) if(v != s) dfs(v, s);
8 }
9 void build() {
10    dfs(1);
11    for(int l = 1; l < LOG; l++) for(int v = 1; v < MAXN; v++)
12        up[l][v] = up[l - 1][up[l - 1][v]];
13 }
14 void jmp(int &u, int v, int d) {
15     for(int l = LOG - 1; l >= 0; l--) if(d & (1 << l))
16         u = up[l][u];
17 }
18 int LCA(int u, int v) {
19     if(dep[u] < dep[v]) swap(u, v);
20     jmp(u, v, dep[u] - dep[v]);
21     if(u == v) return u;
22     for(int l = LOG - 1; l >= 0; l--)
23         if(up[l][u] != up[l][v])
24             u = up[l][u], v = up[l][v];
25     return up[0][u];
26 }

```

1.3 Vertices y Aristas de Corte

```

1 const int MAXN = 1e5;
2 int low[MAXN], ord[MAXN], tin;
3 vector<int> adj[MAXN];
4 int dfs(int s) {
5     low[s] = ord[s] = ++tin;
6     for(auto v : adj[s]) {
7         if(!low[v]) {

```

```

8             dfs(v);
9             if(low[v] > ord[s]) { /* uv es puente */ }
10            if(low[v] >= ord[s]) { /* u es punto de articulacin (o ra z) */}
11            low[s] = min(low[s], low[v]);
12        }
13        else if(ord[v] < ord[s])
14            low[s] = min(low[s], ord[v]);
15    }
16    return low[s];
17 }

```

1.4 SCC

```

1 vi val, comp, sta;
2 int Time, ncomps;
3 template<class G> int dfs(int s, G &g) {
4     int low = val[s] = ++Time, x; sta.push_back(s);
5     for(auto v : g[s]) if(comp[v] < 0)
6         low = min(low, val[v] ? dfs(v, g));
7     if(low == val[s]) {
8         do {
9             x = sta.back(); sta.pop_back();
10            comp[x] = ncomps;
11        } while(x != s);
12        ncomps++;
13    }
14 }
15 template<class G> int scc(G &g) {
16     int n = g.size();
17     comp.assign(n, -1), val.assign(0, -1);
18     Time = ncomps = 0;
19     for(int i = 0; i < n; i++) if(comp[i] < 0) dfs(i, g);
20 }

```

2 Strings

2.1 Z Function

```

1 vi z_func(string &s) {
2     int n = s.length(), l = -1, r = -1;
3     vi z(n);
4     for(int i = 1; i < n; i++) {
5         if(i <= r) z[i] = min(z[i - l], r - i + 1);
6         while(i + z[i] < n && s[z[i]] == s[i + z[i]]) z[i]++;
7         if(i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
8     }
9     return z;
10 }

```

2.2 Manacher

```

1 vi manacher(string &s) {
2     // Encuentra palindromos de longitud impar.
3     int n = s.length(), l = -1, r = -1;
4     vi p(n);

```

```

5  for(int i = 0; i < n; i++) {
6      if(i <= r) p[i] = min(p[l + r - i], r - i + 1);
7      while(i+p[i]+1 < n && i-p[i]-1 >= 0 && s[i+p[i]+1] == s[i-p[i]-1]) p[i]++;
8      if(i + p[i] > r) l = i - p[i], r = i + p[i];
9  }
10 return p;
11 }

```

2.3 Suffix Array

```

1  const int MAXN = 4e5;
2  string s;
3  int SA[MAXN], LCP[MAXN], val[MAXN], cnt[MAXN], n;
4
5  void csort(int l) {
6      int mx = max(300, n), sum = 0, tSA[MAXN];
7      fill(cnt, cnt + mx, 0);
8      for(int i = 0; i < n; i++)
9          cnt[(SA[i] + l < n) ? val[SA[i] + l] : 0]++;
10     for(int i = 0; i < mx; i++)
11         {int t = cnt[i]; cnt[i] = sum; sum += t;}
12     for(int i = 0; i < n; i++)
13         tSA[cnt[SA[i] + l < n ? val[SA[i] + l] : 0]++] = SA[i];
14     for(int i = 0; i < n; i++)
15         SA[i] = tSA[i];
16 }
17 void buildSA() {
18     int nval[MAXN], rk, l = 1;
19     iota(SA, SA + n, 0);
20     for(int i = 0; i < n; i++)
21         val[SA[i]] = s[i];
22     do {
23         csort(l);
24         csort(0);
25         nval[SA[0]] = rk = 0;
26         for(int i = 1; i < n; i++) nval[SA[i]] =
27             ii{val[SA[i]], val[SA[i]+l]} == ii{val[SA[i-1]], val[SA[i-1]+l]} ? rk++ : rk;
28         for(int i = 0; i < n; i++)
29             val[i] = nval[i];
30         l <= 1;
31     } while(val[SA[n-1]] != n-1 && l < n);
32 }
33 void buildLCP() {
34     int pre[MAXN], PLCP[MAXN], L = 0;
35     pre[SA[0]] = -1;
36     for(int i = 1; i < n; i++)
37         pre[SA[i]] = SA[i-1];
38     for(int i = 0; i < n; i++) {
39         if(pre[i] == -1) {
40             PLCP[i] = -1;
41             continue;
42         }
43         while(s[i + L] == s[pre[i] + L]) L++;
44         PLCP[i] = L;
45         L = max(0, L-1);
46     }
47     for(int i = 0; i < n; i++)

```

```

48     LCP[i] = PLCP[SA[i]];
49 }

```

2.4 Hashing

```

1  struct rhash {
2      ll P, Q; // P ~ cantidad de caracteres del alfabeto, Q ~ 10^9
3      vl H, po; // Se pueden usar varios hashes si las colisiones son problema
4      rhash(string &s, ll P, ll Q) : P(P), Q(Q) {
5          int n = s.length(); H.resize(n); po.resize(n);
6          po[0] = 1; H[0] = s[0];
7          for(int i = 1; i < n; i++) {
8              H[i] = (P*H[i-1] + s[i])%Q;
9              po[i] = (po[i-1] * P)%Q;
10         }
11     }
12     ll get(ll l, ll r) { // Hash de s[l, r]
13         if(l == 0) return H[r];
14         ll res = (H[r] - po[r-l+1]*H[l-1])%Q;
15         return res >= 0 ? res : res + Q;
16     }
17 };

```

3 Geometria

3.1 Punto

```

1  template<class T>
2  struct pt {
3      T x, y;
4      pt(T x = 0, T y = 0) : x(x), y(y) {}
5      bool operator< (pt o) const {return (x < o.x || (x == o.x && y < o.y)); }
6      bool operator== (pt o) const {return (x == o.x && y == o.y); }
7      pt operator+ (pt o) const {return pt(x + o.x, y + o.y); }
8      pt operator- (pt o) const {return pt(x - o.x, y - o.y); }
9      pt operator* (T l) const {return pt(l*x, l*y); }
10     pt operator/ (T l) const {return pt(x/l, y/l); }
11     T dot(pt o) { return x*o.x + y*o.y; }
12     T cross(pt o) { return x*o.y - y*o.x; }
13     T cross(pt a, pt b) { return (a - *this).cross(b - *this); }
14     T normsq(pt o) { return x*x + y*y; }
15     double norm(pt o) { return hypot(x, y); }
16 };

```

3.2 Envolverte

```

1  vector<pt<ll>> convex_hull(vector<pt<ll>> P) {
2      int n = P.size();
3      if(n <= 2) return P;
4      vector<pt<ll>> L, U;
5      sort(P.begin(), P.end());
6      for(int i = 0; i < n; i++) {
7          while(U.size() >= 2 && U[U.size()-2].cross(U[U.size()-1], P[i]) >= 0)
8              U.pop_back();
9          while(L.size() >= 2 && L[L.size()-2].cross(L[L.size()-1], P[n-i-1]) >= 0)

```

```

10     L.pop_back();
11     U.push_back(P[i]), L.push_back(P[n - i - 1]);
12 }
13 U.insert(U.end(), L.begin() + 1, L.end() - 1);
14 return U;
15 }

```

4 Flujo

4.1 Dinic

```

1  const int MAXN = 5000, INF = 1e9;
2  int dist[MAXN], ptr[MAXN], src, dst;
3  struct Edge {
4      int to, rev, f, cap;
5      Edge(int to, int rev, int f, int cap) : to(to), rev(rev), f(f), cap(cap);
6  };
7  vector<Edge> G[MAXN];
8  void addEdge(int u, int v, int cap) {
9      G[u].push_back(Edge(v, G[v].size(), 0, cap));
10     G[v].push_back(Edge(u, G[u].size() - 1, 0, 0));
11 }
12 bool bfs() {
13     queue<int> q({src});
14     memset(dist, -1, sizeof dist);
15     dist[src] = 0;
16     while(!q.empty() && dist[dst] == -1) {
17         int u = q.front();
18         q.pop();
19         for(auto e : G[u]) {
20             int v = e.to;
21             if(dist[v] == -1 && e.f < e.cap) {
22                 dist[v] = dist[u] + 1;
23                 q.push(v);
24             }
25         }
26     }
27     return dist[dst] != -1;
28 }
29 int dfs(int u, int f) {
30     if(u == dst || !f) return f;
31     for(int &i = ptr[u]; i < G[u].size(); i++) {
32         Edge &e = G[u][i];
33         int v = e.to;
34         if(dist[v] != dist[u] + 1) continue;
35         if(int df = dfs(v, min(f, e.cap - e.f))) {
36             e.f += df;
37             G[v][e.rev].f -= df;
38             return df;
39         }
40     }
41     return 0;
42 }
43 long long dinic() {
44     long long mf = 0;
45     while(bfs()) {

```

```

46     memset(ptr, 0, sizeof ptr);
47     while(long long pushed = dfs(src, INF))
48         mf += pushed;
49 }
50 return mf;
51 }

```

5 Estructuras

5.1 CHT

```

1  // Tomado de KACTL.  $O(n \log n)$ . Para  $O(n)$  se hace un deque de lineas y se saca del
2  // lado correspondiente cuando salen de la envolvente o no son relevantes.
3  bool Q;
4  struct Line {
5      mutable ll m, b, p;
6      bool operator<(const Line& o) const {
7          return Q ? p < o.p : m < o.m;
8      }
9  };
10 struct LineContainer : multiset<Line> {
11     const ll inf = LLONG_MAX;
12     ll div(ll a, ll b) {
13         return a / b - ((a ^ b) < 0 && a % b);
14     }
15     bool isect(iterator x, iterator y) {
16         if (y == end()) { x->p = inf; return false; }
17         if (x->m == y->m) x->p = x->b > y->b ? inf : -inf;
18         else x->p = div(y->b - x->b, x->m - y->m);
19         return x->p >= y->p;
20     }
21     void add(ll m, ll b) {
22         auto z = insert({m, b, 0}), y = z++, x = y;
23         while (isect(y, z)) z = erase(z);
24         if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
25         while ((y = x) != begin() && (--x)->p >= y->p)
26             isect(x, erase(y));
27     }
28     ll query(ll x) {
29         assert(!empty());
30         Q = 1; auto l = *lower_bound({0, 0, x}); Q = 0;
31         return l.m * x + l.b;
32     }
33 };

```

5.2 Union Find

```

1  const int MAXN = 1e6;
2  int rep[MAXN], sz[MAXN];
3  void init() {
4      fill(rep, rep + MAXN, -1), fill(sz, sz + MAXN, 1);
5  }
6  int find(int u) {
7      return (rep[u] == -1) ? u : rep[u] = find(rep[u]);
8  }
9  bool join(int u, int v) {
10     u = find(u), v = find(v);

```

```

11 if(u == v) return false;
12 if(sz[u] < sz[v]) swap(u, v);
13 return sz[u] += sz[v], rep[v] = u, true;
14 }

```

5.3 Wavelet Tree

```

1 struct wnode {
2     wnode *left, *right;
3     int lo, hi;
4     vector<int> c;
5     wnode(int lo, int hi, int* st, int* en) : lo(lo), hi(hi) {
6         if(hi == lo || st == en)
7             return;
8         int mi = (lo + hi)/2;
9         auto f = [mi](int x) { return x <= mi; };
10        c.push_back(0);
11        for(auto it = st; it != en; ++it)
12            c.push_back(c.back() + f(*it));
13        auto it = stable_partition(st, en, f);
14        left = new wnode(lo, mi, st, it);
15        right = new wnode(mi + 1, hi, it, en);
16    }
17    int kth(int L, int R, int k) {
18        if(lo == hi)
19            return lo;
20        int der = c[R], izq = c[L - 1], tol = der - izq;
21        if(tol >= k)
22            return left->kth(izq + 1, der, k);
23        return right->kth(L - izq, R - der, k - tol);
24    }
25 };

```

5.4 Segment Tree

```

1 const int NE = 1e9;
2 struct node {
3     int mn, l, r;
4     node *left, *right;
5     node(int l, int r, int* A) : l(l), r(r) {
6         if(l == r)
7             mn = A[l];
8         else {
9             int mi = (l + r)/2;
10            left = new node(l, mi, A);
11            right = new node(r + 1, mi, A);
12            mn = min(left->mn, right->mn);
13        }
14    }
15    void upd(int p, int v) {
16        if(r < p || p < l)
17            return;
18        if(l == r) {
19            mn = v;
20            return;
21        }
22        left->upd(p, v), right->upd(p, v);

```

```

23        mn = min(left->mn, right->mn);
24    }
25    int qry(int rl, int rr) {
26        if(rr < l || r < rl)
27            return NE;
28        if(rl <= l && r <= rr)
29            return mn;
30        return min(left->qry(rl, rr), right->qry(rl, rr));
31    }
32 };

```

6 Mate

6.1 Miller-Rabin

```

1 bool isprime(ll p) {
2     if(p == 1) return false;
3     if(p % 2 == 0) return p == 2 ? true : false;
4     ll d = p - 1;
5     while(d % 2 == 0) d >>= 1ll;
6     for(int its = 0; its < 15; its++) {
7         ll a = (rand() % (p - 1)) + 1, x = d;
8         a = mpow(a, d, p);
9         while(x != p - 1 && a != p - 1 && a != 1) {
10            a = mmul(a, a, p);
11            x *= 2ll;
12        }
13        if(a != p - 1 && x % 2 == 0) return false;
14    }
15    return true;
16 }

```

6.2 CRT

```

1 template<typename T> void euclid(T a, T b, T &x, T &y) {
2     if(!b) {x = 1, y = 0; return;}
3     euclid(b, a % b, y, x);
4     y -= a/b * x;
5 }
6 template<typename T> T crt(T x1, T m1, T x2, T m2) {
7     T d = __gcd(m1, m2), r, s;
8     if(x1 % d != x2 % d)
9         return -1;
10    euclid(m1, m2, r, s);
11    m1 /= d, m2 /= d;
12    T mod = d*m1*m2, a1 = ((m1*r)%mod*x2)%mod, a2 = ((m2*s)%mod*x1)%mod, y = (a1 +
13        a2)%mod;
14    return (y >= 0 ? y : y + mod);

```

7 Varios

7.1 LIS

```
1 vl lis(vl a) {
2   int n = a.size(), sz = 0; map<pl, pl> pre;
3   vl dp(n + 1, LLONG_MAX); dp[0] = LLONG_MIN;
4   for(int i = 0; i < n; i++) {
5     auto it = upper_bound(dp.begin(), dp.end(), a[i]); //a[i]-1 para estricta.
6     if(*it == LLONG_MAX) sz++; *it = min(*it, a[i]);
7     int pos = distance(dp.begin(), it); pre[{pos, a[i]}] = {pos - 1, dp[pos - 1]};
8   }
9   vl ans; pl cu = {sz, dp[sz]};
10  do {
11    ans.push_back(cu.second);
12    cu = pre[cu];
13  } while(cu.first);
14  return reverse(ans.begin(), ans.end()), ans;
15 }
```