agricolae tutorial (Version 1.2-6)

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Preface

The following document was developed to facilitate the use of agricolae package in R, it is understood that the user knows the statistical methodology for the design and analysis of experiments and through the use of the functions programmed in agricolae facilitate the generation of the field book experimental design and their analysis. The first part document describes the use of graph.freq role is complementary to the *hist* function of R functions to facilitate the collection of statistics and frequency table, statistics or grouped data histogram based training grouped data and graphics as frequency polygon or ogive; second part is the development of experimental plans and numbering of the units as used in an agricultural experiment; a third part corresponding to the comparative tests and finally provides agricolae miscellaneous additional functions applied in agricultural research and stability functions, soil consistency, late blight simulation and others.

1 Introduction

The package **agricolae** offers a broad functionality in the design of experiments, especially for experiments in agriculture and improvements of plants, which can also be used for other purposes. It contains the following designs: lattice, alpha, cyclic, balanced incomplete block designs, complete randomized blocks, Latin, Graeco-Latin, augmented block designs, split plot and strip plot. It also has several procedures of experimental data analysis, such as the comparisons of treatments of Waller-Duncan, Bonferroni, Duncan, Student-Newman-Keuls, Scheffe, Ryan, Einot and Gabriel and Welsch multiple range test or the classic LSD and Tukey; and non-parametric comparisons, such as Kruskal-Wallis, Friedman, Durbin, Median and Waerden, stability analysis, and other procedures applied in genetics, as well as procedures in biodiversity and descriptive statistics, De Mendiburu (2009)

1.1 Installation

The main program of **R** should be already installed in the platform of your computer (Windows, Linux or MAC). If it is not installed yet, you can download it from the R project (www.r-project.org) of a repository CRAN, R Core Team (2017).

> install.packages("agricolae") Once the agricolae package is installed, it needs to be made accessible to the current R session by the command:

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> library(agricolae)

For online help facilities or the details of a particular command (such as the function waller.test) you can type:

```
> help(package="agricolae")
> help(waller.test)
```

For a complete functionality, agricolae requires other packages.

MASS: for the generalized inverse used in the function PBIB.test

nlme: for the methods REML and LM in *PBIB.test* **klaR:** for the function *triplot* used in the function *AMMI*

Cluster: for the use of the function consensus

spdep: for the between genotypes spatial relation in biplot of the function AMMI

algDesign: for the balanced incomplete block design design.bib

1.2 Use in R

Since agricolae is a package of functions, these are operational when they are called directly from the console of \mathbf{R} and are integrated to all the base functions of \mathbf{R} . The following orders are frequent:

```
> detach(package:agricolae) # detach package agricole
> library(agricolae) # Load the package to the memory
> designs<-apropos("design")</pre>
```

> print(designs[substr(designs,1,6)=="design"], row.names=FALSE)

```
[1] "design.ab" "design.alpha" "design.bib"
[4] "design.crd" "design.cyclic" "design.dau"
[7] "design.graeco" "design.lattice" "design.lsd"
[10] "design.rcbd" "design.split" "design.strip"
[13] "design.youden"
```

For the use of symbols that do not appear in the keyboard in Spanish, such as:

```
\tilde{}, [, ], &, \hat{}, |. <, >, {, }, \% or others, use the table ASCII code.
```

> library(agricolae) # Load the package to the memory:

In order to continue with the command line, do not forget to close the open windows with any R order. For help:

```
help(graph.freq)
? (graph.freq)
str(normal.freq)
example(join.freq)
```

1.3 Data set in agricolae

```
> A<-as.data.frame(data(package="agricolae")$results[,3:4])</pre>
> A[,2]<-paste(substr(A[,2],1,35),"..",sep=".")</pre>
> head(A)
            Item
                                                     Title
             CIC
1
                     Data for late blight of potatoes...
2
         Chz2006
                          Data amendment Carhuaz 2006...
3
                          Data AUDPC Comas - Oxapampa...
   ComasOxapampa
4
              DC Data for the analysis of carolina g...
5 Glycoalkaloids
                                   Data Glycoalkaloids...
                          Data amendment Huanuco 2006...
6
         Hco2006
```

2 Descriptive statistics

The package **agricolae** provides some complementary functions to the \mathbf{R} program, specifically for the management of the histogram and function hist.

2.1 Histogram

The histogram is constructed with the function *graph.freq* and is associated to other functions: *polygon.freq*, *table.freq*, *stat.freq*. See Figures: 1, 2 and 3 for more details.

Example. Data generated in ${\bf R}$. (students' weight).

2.2 Statistics and Frequency tables

Statistics: mean, median, mode and standard deviation of the grouped data.

```
> stat.freq(h1)

$variance
[1] 51.37655

$mean
[1] 66.6

$median
[1] 68.36
```

```
> par(mfrow=c(1,2),mar=c(4,3,0,1),cex=0.6)
> h1<- graph.freq(weight,col="yellow",frequency=1,las=2,xlab="h1")
> h2<- graph.freq (weight, frequency =2, axes= FALSE,las=2,xlab="h2")
> polygon.freq(h2, col="blue", lwd=2, frequency =2)
> TIC<- h2$breaks[2]- h2$breaks[1]
> axis(1,c(h2$mids[1]-TIC, h2$mids, h2$mids[6]+TIC),cex=0.6)
> axis(2, cex=0.6,las=1)
```

Figure 1: Absolute and relative frequency with polygon.

0.0

50.6 55.4 60.2 65.0 69.8 74.6

79.4

\$mode

[- -] mode [1,] 67.4 72.2 70.45455

Frequency tables: Use table.freq, stat.freq and summary

62.6

The table.freq is equal to summary()

53.0

Limits class: Lower and Upper

Class point: **Main** Frequency: **Frequency**

Percentage frequency: Percentage

Cumulative frequency: CF

Cumulative percentage frequency: CPF

> print(summary(h1),row.names=FALSE)

Lower	Upper	Main	Frequency	Percentage	CF	CPF
53.0	57.8	55.4	5	16.7	5	16.7
57.8	62.6	60.2	5	16.7	10	33.3
62.6	67.4	65.0	3	10.0	13	43.3
67.4	72.2	69.8	10	33.3	23	76.7
72.2	77.0	74.6	6	20.0	29	96.7
77.0	81.8	79.4	1	3.3	30	100.0

2.3 Histogram manipulation functions

You can extract information from a histogram such as class intervals *intervals.freq*, attract new intervals with the *sturges.freq* function or to join classes with *join.freq* function. It is also possible to reproduce the graph with the same creator *graph.freq* or function *plot* and overlay normal function with

normal.freq be it a histogram in absolute scale, relative or density . The following examples illustrates these properties.

```
> sturges.freq(weight)
$maximum
[1] 81.5
$minimum
[1] 53
$amplitude
[1] 29
$classes
[1] 6
$interval
[1] 4.8
$breaks
[1] 53.0 57.8 62.6 67.4 72.2 77.0 81.8
> intervals.freq(h1)
    lower upper
[1,] 53.0 57.8
[2,] 57.8 62.6
[3,] 62.6 67.4
[4,] 67.4 72.2
[5,]
    72.2 77.0
[6,] 77.0 81.8
> join.freq(h1,1:3) -> h3
> print(summary(h3))
 Lower Upper Main Frequency Percentage CF
1 53.0 67.4 60.2
                     13
                                 43.3 13 43.3
  67.4 72.2 69.8
                        10
                                 33.3 23 76.7
                       6
3 72.2 77.0 74.6
                                 20.0 29 96.7
4 77.0 81.8 79.4
                                 3.3 30 100.0
```

2.4 hist() and graph.freq() based on grouped data

The hist and graph.freq have the same characteristics, only f2 allows build histogram from grouped data.

```
0-10 (3)
10-20 (8)
```

```
> par(mfrow=c(1,2), mar=c(4,3,0,1), cex=0.6)
> plot(h3, frequency=2,col="magenta",ylim=c(0,0.6))
> normal.freq(h3,frequency=2,col="green")
> ogive.freq(h3,col="blue")
           RCF
1 53.0 0.0000
2 67.4 0.4333
3 72.2 0.7667
4 77.0 0.9667
5 81.8 1.0000
6 86.6 1.0000
          0.5
          0.4
                                                 0.6
          0.3
          0.2
                                                 0.2
          0.0
                   53.0
                               67.4 72.2 77.0 81.8
                                                    53.0
                                                                         77.0
                                                                             81.8
                                                                     72.2
```

Figure 2: Join frequency and relative frequency with normal and Ogive.

```
20-30 (15)
30-40 (18)
40-50 (6)
```

> print(summary(h5),row.names=FALSE)

Lower	Upper	Main	Frequency	Percentage	CF	CPF
0	10	5	3	6	3	6
10	20	15	8	16	11	22
20	30	25	15	30	26	52
30	40	35	18	36	44	88
40	50	45	6	12	50	100

3 Experiment designs

The package **agricolae** presents special functions for the creation of the field book for experimental designs. Due to the random generation, this package is quite used in agricultural research.

For this generation, certain parameters are required, as for example the name of each treatment, the number of repetitions, and others, according to the design, Cochran and Cox (1957); kueh (2000); Le Clerg and Leonard and Erwin and Warren and Andrew (1992); Montgomery (2002). There are other parameters of random generation, as the seed to reproduce the same random generation or the generation method (See the reference manual of **agricolae**.

http://cran.at.r-project.org/web/packages/agricolae/agricolae.pdf

```
> par(mfrow=c(1,2),mar=c(4,3,2,1),cex=0.6)
> h4<-hist(weight,xlab="Classes (h4)")
> table.freq(h4)
> # this is possible
> # hh<-graph.freq(h4,plot=FALSE)
> # summary(hh)
> # new class
> classes <- c(0, 10, 20, 30, 40, 50)
> freq <- c(3, 8, 15, 18, 6)
> h5 <- graph.freq(classes,counts=freq, xlab="Classes (h5)",main="Histogram grouped data")</pre>
```

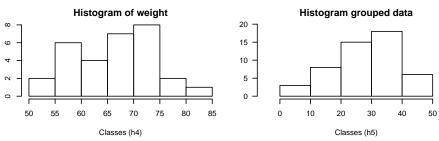


Figure 3: hist() function and histogram defined class

Important parameters in the generation of design:

series: A constant that is used to set numerical tag blocks, eg number = 2, the labels will be: 101, 102, for the first row or block, 201, 202, for the following, in the case of completely randomized design, the numbering is sequencial.

design: Some features of the design requested agricolae be applied specifically to design.ab(factorial) or design.split (split plot) and their possible values are: "rcbd", "crd" and "lsd".

seed: The seed for the random generation and its value is any real value, if the value is zero, it has no reproducible generation, in this case copy of value of the outdesign\$parameters.

kinds: the random generation method, by default "Super-Duper".

first: For some designs is not required random the first repetition, especially in the block design, if you want to switch to random, change to TRUE.

randomization: TRUE or FALSE. If false, randomization is not performed

Output design:

parameters: the input to generation design, include the seed to generation random, if seed=0, the program generate one value and it is possible reproduce the design.

book: field book

statistics: the information statistics the design for example efficiency index, number of treatments.

sketch: distribution of treatments in the field.

The enumeration of the plots

zigzag is a function that allows you to place the numbering of the plots in the direction of serpentine: The zigzag is output generated by one design: blocks, Latin square, graeco, split plot, strip plot, into blocks factorial, balanced incomplete block, cyclic lattice, alpha and augmented blocks.

fieldbook: output zigzag, contain field book.

3.1 Completely randomized design

They only require the names of the treatments and the number of their repetitions and its parameters are:

```
> str(design.crd)
function (trt, r, serie = 2, seed = 0, kinds = "Super-Duper",
    randomization = TRUE)
> trt <- c("A", "B", "C")
> repeticion \leftarrow c(4, 3, 4)
> outdesign <- design.crd(trt,r=repeticion,seed=777,serie=0)</pre>
> book1 <- outdesign$book
> head(book1)
  plots r trt
      1 1
2
      2 1
3
      3 2
            Α
4
      4 1 C
5
      5 2 C
      6 3
```

Excel:write.csv(book1,"book1.csv",row.names=FALSE)

3.2 Randomized complete block design

They require the names of the treatments and the number of blocks and its parameters are:

```
> str(design.rcbd)
function (trt, r, serie = 2, seed = 0, kinds = "Super-Duper",
    first = TRUE, continue = FALSE, randomization = TRUE)
> trt <- c("A", "B", "C", "D", "E")
> repeticion <- 4
> outdesign <- design.rcbd(trt,r=repeticion, seed=-513, serie=2)
> # book2 <- outdesign$book</pre>
> book2<- zigzag(outdesign) # zigzag numeration</pre>
> print(outdesign$sketch)
     [,1] [,2] [,3] [,4] [,5]
[1,] "D"
         "B"
               "C"
                    "E"
                         "A"
                    "B"
                         "C"
[2,] "E" "A"
               "D"
[3,] "E" "D"
               "B" "A"
                         "C"
[4,] "A" "E" "C" "B" "D"
```

```
> print(matrix(book2[,1],byrow = TRUE, ncol = 5))
    [,1] [,2] [,3] [,4] [,5]
              103 104 105
[1,]
    101 102
[2,] 205
          204
              203
                   202
                        201
[3,]
     301
         302
              303
                   304 305
[4,]
     405 404 403
                   402 401
```

Latin square design 3.3

They require the names of the treatments and its parameters are:

```
> str(design.lsd)
function (trt, serie = 2, seed = 0, kinds = "Super-Duper",
    first = TRUE, randomization = TRUE)
> trt <- c("A", "B", "C", "D")
> outdesign <- design.lsd(trt, seed=543, serie=2)
> print(outdesign$sketch)
     [,1] [,2] [,3] [,4]
[1,] "C"
          "A"
               "B"
                    "D"
[2,] "D"
          "B"
               "C"
                    "A"
          "D"
               "A"
                    "C"
[3,] "B"
[4,] "A"
               "D"
Serpentine enumeration:
```

```
> book <- zigzag(outdesign)</pre>
> print(matrix(book[,1],byrow = TRUE, ncol = 4))
     [,1] [,2] [,3] [,4]
[1,] 101 102
               103 104
[2,] 204
          203
               202
                    201
[3,] 301 302
               303
                    304
[4,] 404 403 402 401
```

3.4Graeco-Latin designs

They require the names of the treatments of each factor of study and its parameters are:

```
> str(design.graeco)
function (trt1, trt2, serie = 2, seed = 0, kinds = "Super-Duper",
    randomization = TRUE)
> trt1 <- c("A", "B", "C", "D")
> trt2 <- 1:4
> outdesign <- design.graeco(trt1,trt2, seed=543, serie=2)
> print(outdesign$sketch)
```

```
[,1] [,2] [,3] [,4]
[1,] "A 1" "D 4" "B 3" "C 2"
[2,] "D 3" "A 2" "C 1" "B 4"
[3,] "B 2" "C 3" "A 4" "D 1"
[4,] "C 4" "B 1" "D 2" "A 3"
```

Serpentine enumeration:

```
> book <- zigzag(outdesign)</pre>
> print(matrix(book[,1],byrow = TRUE, ncol = 4))
     [,1] [,2] [,3] [,4]
[1,] 101 102 103 104
     204
          203
               202 201
[2,]
[3,]
     301
          302
               303
                     304
          403
[4,]
     404
               402 401
```

3.5 Youden design

302

They require the names of the treatments of each factor of study and its parameters are:

```
> str(design.youden)
function (trt, r, serie = 2, seed = 0, kinds = "Super-Duper",
    first = TRUE, randomization = TRUE)
> varieties<-c("perricholi","yungay","maria bonita","tomasa")</pre>
> r<-3
> outdesign <-design.youden(varieties,r,serie=2,seed=23)</pre>
> print(outdesign$sketch)
     [,1]
                     [,2]
                                    [,3]
[1,] "maria bonita" "perricholi"
                                    "tomasa"
[2,] "yungay"
                    "tomasa"
                                    "maria bonita"
[3,] "tomasa"
                     "yungay"
                                    "perricholi"
[4,] "perricholi"
                    "maria bonita" "yungay"
> book <- outdesign$book
> print(book) # field book.
   plots row col
                    varieties
1
     101
           1
               1 maria bonita
2
     102
           1
                   perricholi
3
     103
               3
           1
                        tomasa
4
     201
           2
               1
                        yungay
5
     202
           2
               2
                        tomasa
6
     203
           2
              3 maria bonita
     301
7
           3
               1
                       tomasa
```

yungay

```
3 3 perricholi
9
    303
10
    401
          4 1 perricholi
     402
              2 maria bonita
12
     403
          4
              3
                      yungay
> print(matrix(as.numeric(book[,1]),byrow = TRUE, ncol = r))
     [,1] [,2] [,3]
[1,]
     101 102 103
[2,]
     201
          202
               203
[3,]
     301
          302
               303
[4,] 401 402 403
Serpentine enumeration:
> book <- zigzag(outdesign)</pre>
> print(matrix(as.numeric(book[,1]),byrow = TRUE, ncol = r))
     [,1] [,2] [,3]
[1,] 101 102 103
[2,] 203
          202 201
[3,]
     301 302 303
[4,] 403 402 401
     Balanced Incomplete Block Designs
3.6
They require the names of the treatments and the size of the block and its parameters are:
> str(design.bib)
function (trt, k, r = NULL, serie = 2, seed = 0, kinds = "Super-Duper",
   maxRep = 20, randomization = TRUE)
> trt <- c("A", "B", "C", "D", "E")
> outdesign <- design.bib(trt,k, seed=543, serie=2)
Parameters BIB
_____
Lambda
treatmeans : 5
Block size : 4
Blocks : 5
Replication: 4
```

Efficiency factor 0.9375

> book5 <- outdesign\$book
> outdesign\$statistics

<<< Book >>>

```
lambda treatmeans blockSize blocks r Efficiency
values
                        5
                                  4
                                          5 4
                                                  0.9375
> outdesign$parameters
$design
[1] "bib"
$trt
[1] "A" "B" "C" "D" "E"
$k
[1] 4
$serie
[1] 2
$seed
[1] 543
$kinds
[1] "Super-Duper"
```

According to the produced information, they are five blocks of size 4, being the matrix:

> outdesign\$sketch

```
[,1] [,2] [,3] [,4]
[1,] "D"
           "B"
                      "C"
                "E"
[2,] "B"
           "A"
                "C"
                      "D"
                "E"
                      " A "
[3,] "D"
           "B"
[4,] "E"
           "A"
                "C"
                      "D"
                "E"
                      "A"
[5,] "B"
           "C"
```

It can be observed that the treatments have four repetitions. The parameter lambda has three repetitions, which means that a couple of treatments are together on three occasions. For example, B and E are found in the blocks I, II and V.

Serpentine enumeration:

```
> book <- zigzag(outdesign)</pre>
> matrix(book[,1],byrow = TRUE, ncol = 4)
     [,1] [,2] [,3] [,4]
[1,] 101
          102
               103
                    104
[2,]
     204
           203
                202
                     201
     301
           302
                303
                     304
[3,]
           403
[4,]
     404
                402
                     401
[5,] 501 502 503 504
```

3.7 Cyclic designs

> t(X[,,1])

They require the names of the treatments, the size of the block and the number of repetitions. This design is used for 6 to 30 treatments. The repetitions are a multiple of the size of the block; if they are six treatments and the size is 3, then the repetitions can be 6, 9, 12, etc. and its parameters are:

```
> str(design.cyclic)
function (trt, k, r, serie = 2, rowcol = FALSE, seed = 0,
    kinds = "Super-Duper", randomization = TRUE)
> trt <- c("A", "B", "C", "D", "E", "F")
> outdesign <- design.cyclic(trt,k=3, r=6, seed=543, serie=2)
cyclic design
Generator block basic:
1 2 4
1 3 2
Parameters
_____
treatmeans: 6
Block size: 3
Replication: 6
> book6 <- outdesign$book
> outdesign$sketch[[1]]
     [,1] [,2] [,3]
[1,] "A"
          "E"
               "D"
               "C"
[2,] "D"
          "F"
          "D"
               "B"
[3,] "A"
               "F"
[4,] "A"
          "C"
[5,] "C"
          "B"
               "E"
[6,] "B"
          "E"
               "F"
> outdesign$sketch[[2]]
     [,1] [,2] [,3]
          "D"
[1,] "B"
               "C"
[2,] "C"
          "A"
               "B"
          " A "
[3,] "F"
               "B"
[4,] "C"
          "D"
               "E"
               "F"
[5,] "E"
          "A"
[6,] "F"
               "D"
12 blocks of 4 treatments each have been generated. Serpentine enumeration:
> book <- zigzag(outdesign)</pre>
> array(book$plots,c(3,6,2))->X
```

```
[,1] [,2] [,3]
[1,] 101 102 103
[2,] 106
         105
              104
[3,]
    107 108 109
[4,]
    112 111 110
[5,] 113 114 115
[6,] 118 117 116
> t(X[,,2])
    [,1] [,2] [,3]
[1,] 201 202
              203
[2,]
     206
          205
              204
[3,]
     207
         208
             209
[4,]
     212 211 210
[5,] 213 214 215
[6,]
    218 217 216
```

3.8 Lattice designs

> str(design.lattice)

\$type

They require a number of treatments of a perfect square; for example 9, 16, 25, 36, 49, etc. and its parameters are:

function (trt, r = 3, serie = 2, seed = 0, kinds = "Super-Duper",

```
[1] "triple"
$trt
[1] "a" "b" "c" "d" "e" "f" "g" "h" "i"
$r
[1] 3
$serie
[1] 2
$seed
[1] 33
$kinds
[1] "Super-Duper"
> outdesign$sketch
$rep1
    [,1] [,2] [,3]
[1,] "i" "d" "a"
[2,] "b" "c" "e"
[3,] "h" "f" "g"
$rep2
     [,1] [,2] [,3]
[1,] "c" "f" "d"
[2,] "b" "h" "i"
[3,] "e" "g" "a"
$rep3
     [,1] [,2] [,3]
[1,] "e" "h"
[2,] "b" "f" "a"
[3,] "c" "g" "i"
> head(book7)
 plots r block trt
1 101 1
             1
   102 1
             1
3
   103 1
             1
   104 1
   105 1
5
             2
                 С
   106 1
             2
Serpentine enumeration:
```

> book <- zigzag(outdesign)
> array(book\$plots,c(3,3,3)) -> X
> t(X[,,1])

```
[,1] [,2] [,3]
[1,] 101 102
              103
[2,] 106
          105
               104
[3,] 107
          108
              109
> t(X[,,2])
     [,1] [,2] [,3]
[1,] 201 202
              203
[2,] 206
          205
               204
[3,] 207
          208 209
> t(X[,,3])
     [,1] [,2] [,3]
[1,] 301 302
               303
[2,]
     306
          305
               304
[3,]
     307
          308
              309
```

3.9 Alpha designs

These designs are generated by the alpha arrangements, Patterson and Williams (1976). They are similar to the lattice designs, but the tables are rectangular, with s blocks x k treatments. The number of treatments should be equal to s*k and all the experimental units, r*s*k and its parameters are:

```
> str(design.alpha)
function (trt, k, r, serie = 2, seed = 0, kinds = "Super-Duper",
   randomization = TRUE)
> trt <- letters[1:15]
> outdesign <- design.alpha(trt,k=3,r=2,seed=543)
Alpha Design (0,1) - Serie I
Parameters Alpha Design
Treatmeans: 15
Block size : 3
Blocks
       : 5
Replication: 2
Efficiency factor
(E) 0.6363636
<<< Book >>>
> book8 <- outdesign$book
> outdesign$statistics
```

```
treatments blocks Efficiency
values
             15
                 5 0.6363636
> outdesign$sketch
$rep1
     [,1] [,2] [,3]
[1,] "l" "m" "e"
[2,] "g" "c"
             "i"
[3,] "o" "k" "d"
[4,] "h" "f" "j"
[5,] "a" "n" "b"
$rep2
     [,1] [,2] [,3]
[1,] "o" "a"
             "m"
[2,] "l" "k" "g"
[3,] "d" "n" "h"
[4,] "j"
        "b" "c"
[5,] "f"
         "i" "e"
> # codification of the plots
> A<-array(book8[,1], c(3,5,2))
> t(A[,,1])
     [,1] [,2] [,3]
[1,] 101 102 103
[2,] 104 105 106
[3,] 107 108 109
[4,] 110 111 112
[5,] 113 114 115
> t(A[,,2])
     [,1] [,2] [,3]
[1,] 201 202 203
[2,] 204 205 206
[3,] 207 208 209
[4,] 210 211 212
[5,] 213 214 215
```

Serpentine enumeration:

```
> book <- zigzag(outdesign)
> A<-array(book[,1], c(3,5,2))
> t(A[,,1])

       [,1] [,2] [,3]
[1,] 101 102 103
[2,] 106 105 104
```

```
[3,] 107 108 109
[4,] 112 111 110
[5,] 113 114 115

> t(A[,,2])

[,1] [,2] [,3]
[1,] 201 202 203
[2,] 206 205 204
[3,] 207 208 209
[4,] 212 211 210
[5,] 213 214 215
```

3.10 Augmented block designs

These are designs for two types of treatments: the control treatments (common) and the increased treatments. The common treatments are applied in complete randomized blocks, and the increased treatments, at random. Each treatment should be applied in any block once only. It is understood that the common treatments are of a greater interest; the standard error of the difference is much smaller than when between two increased ones in different blocks. The function design.dau() achieves this purpose and its parameters are:

```
> str(design.dau)
function (trt1, trt2, r, serie = 2, seed = 0, kinds = "Super-Duper",
   name = "trt", randomization = TRUE)
> rm(list=ls())
> trt1 <- c("A", "B", "C", "D")
> trt2 <- c("t", "u", "v", "w", "x", "y", "z")
> outdesign <- design.dau(trt1, trt2, r=5, seed=543, serie=2)
> book9 <- outdesign$book
> attach(book9)
> by(trt, block,as.character)
block: 1
[1] "D" "C" "A" "u" "B" "t"
_____
[1] "D" "z" "C" "A" "v" "B"
-----
block: 3
[1] "C" "w" "B" "A" "D"
block: 4
[1] "A" "C" "D" "B" "y"
block: 5
[1] "C" "B" "A" "D" "x"
```

> detach(book9)

Serpentine enumeration:

```
> book <- zigzag(outdesign)
> attach(book)
> by(plots, block, as.character)
[1] "101" "102" "103" "104" "105" "106"
[1] "206" "205" "204" "203" "202" "201"
block: 3
[1] "301" "302" "303" "304" "305"
block: 4
[1] "405" "404" "403" "402" "401"
[1] "501" "502" "503" "504" "505"
> detach(book)
> head(book)
  plots block trt
   101
1
        1 D
           1 C
2
   102
  103
         1 A
4
  104
        1 u
5
   105
        1 B
   106
```

For augmented ompletely randomized design, use the function design.crd().

3.11 Split plot designs

These designs have two factors, one is applied in plots and is defined as $\mathbf{trt1}$ in a randomized complete block design; and a second factor as $\mathbf{trt2}$, which is applied in the subplots of each plot applied at random. The function design.split() permits to find the experimental plan for this design and its parameters are:

Aplication

```
> trt1<-c("A", "B", "C", "D")
> trt2<-c("a","b","c")
> outdesign <-design.split(trt1,trt2,r=3,serie=2,seed=543)</pre>
> book10 <- outdesign$book</pre>
> head(book10)
 plots splots block trt1 trt2
        1
                1 A
          2
2
  101
                1
                      Α
          3
3
  101
                1
                      Α
                          b
  102
           1
4
                1 D
                1 D c
5
  102
          2
6
  102
          3
                1 D
> p<-book10$trt1[seq(1,36,3)]
> q < -NULL
> for(i in 1:12)
+ q <- c(q,paste(book10\$trt2[3*(i-1)+1],book10\$trt2[3*(i-1)+2],book10\$trt2[3*(i-1)+3]))
In plots:
> print(t(matrix(p,c(4,3))))
     [,1] [,2] [,3] [,4]
[1,] "A"
        "D"
             "B"
                  "C"
             "B"
                  "D"
[2,] "A" "C"
[3,] "A" "C"
              "B"
In sub plots (split plot)
> print(t(matrix(q,c(4,3))))
                           [,4]
     [,1]
            [,2]
                   [,3]
[1,] "c a b" "b c a" "b c a" "a b c"
[2,] "b a c" "a b c" "a c b" "b c a"
[3,] "a b c" "a c b" "a c b" "c a b"
Serpentine enumeration:
> book <- zigzag(outdesign)</pre>
> head(book,5)
 plots splots block trt1 trt2
   101
          1
                1
                     Α
          2
  101
                1
                      Α
3
          3 1 A
                         b
  101
  102 1 1 D b
102 2 1 D c
```

3.12 Strip-plot designs

[4,] "A b" "A c" "A a"

These designs are used when there are two types of treatments (factors) and are applied separately in large plots, called bands, in a vertical and horizontal direction of the block, obtaining the divided blocks. Each block constitutes a repetition and its parameters are:

```
> str(design.strip)
function (trt1, trt2, r, serie = 2, seed = 0, kinds = "Super-Duper",
   randomization = TRUE)
Aplication
> trt1<-c("A","B","C","D")
> trt2<-c("a","b","c")
> outdesign <-design.strip(trt1,trt2,r=3,serie=2,seed=543)</pre>
> book11 <- outdesign$book
> head(book11)
 plots block trt1 trt2
1
   101
          1 A
2
   102
           1
                Α
                     b
  102 1 A B
3
  104 1 D a
5
  105
        1
                D
                     b
                D
> t3<-paste(book11$trt1, book11$trt2)</pre>
> B1<-t(matrix(t3[1:12],c(4,3)))
> B2 < -t(matrix(t3[13:24],c(3,4)))
> B3 < -t(matrix(t3[25:36],c(3,4)))
> print(B1)
     [,1] [,2] [,3] [,4]
[1,] "A a" "A b" "A c" "D a"
[2,] "D b" "D c" "B a" "B b"
[3,] "B c" "C a" "C b" "C c"
> print(B2)
     [,1] [,2] [,3]
[1,] "D a" "D b" "D c"
[2,] "A a" "A b" "A c"
[3,] "B a" "B b" "B c"
[4,] "C a" "C b" "C c"
> print(B3)
     [,1] [,2] [,3]
[1,] "B b" "B c" "B a"
[2,] "D b" "D c" "D a"
[3,] "C b" "C c" "C a"
```

Serpentine enumeration:

```
> book <- zigzag(outdesign)</pre>
> head(book)
  plots block trt1 trt2
1
    101
            1
                 Α
2
    102
            1
                 Α
3
   103
            1
                 Α
                      С
   106
            1
                 D
                      a
5
    105
            1
                 D
                      b
    104
> array(book$plots,c(3,4,3))->X
> t(X[,,1])
     [,1] [,2] [,3]
[1,] 101 102 103
[2,] 106 105 104
[3,] 107
           108
               109
[4,] 112 111 110
> t(X[,,2])
     [,1] [,2] [,3]
[1,] 201 202
               203
[2,]
     206
           205
                204
[3,]
     207
           208 209
[4,] 212 211 210
> t(X[,,3])
     [,1] [,2] [,3]
[1,]
     301
          302
                303
[2,]
     306
           305
                304
           308
[3,]
     307
                309
          311
[4,]
     312
               310
```

3.13 Factorial

The full factorial of n factors applied to an experimental design (CRD, RCBD and LSD) is common and this procedure in **agricolae** applies the factorial to one of these three designs and its parameters are:

To generate the factorial, you need to create a vector of levels of each factor, the method automatically generates up to 25 factors and "r" repetitions.

```
> trt <- c (4,2,3) # three factors with 4,2 and 3 levels.
```

to crd and rcbd designs, it is necessary to value "r" as the number of repetitions, this can be a vector if unequal to equal or constant repetition (recommended).

Serpentine enumeration:

1 3 2

1 2 1

- > book <- zigzag(outdesign)</pre>
- > head(book)

105

106

6

```
plots block A B
1
   101
         1 3 1
          1 2 2
2
   102
       1 1 1
3
  103
4 104
       1 1 2
         1 3 2
5
  105
   106
          1 2 1
```

factorial 2 x 2 x 2 with 5 replications in completely randomized design.

```
> trt<-c(2,2,2)
> crd<-design.ab(trt, r=5, serie=2,design="crd")
> names(crd)

[1] "parameters" "book"
> crd$parameters

$design
[1] "factorial"

$trt
[1] "1 1 1" "1 1 2" "1 2 1" "1 2 2" "2 1 1" "2 1 2" "2 2 1"
[8] "2 2 2"
```

```
[1] 5 5 5 5 5 5 5 5
$serie
[1] 2
$seed
[1] 970386955
$kinds
[1] "Super-Duper"
[[7]]
[1] TRUE
$applied
[1] "crd"
> head(crd$book)
 plots r A B C
    101 1 2 2 1
2
    102 1 1 1 2
   103 1 2 1 2
    104 1 2 1 1
5
    105 1 2 2 2
    106 2 2 1 2
```

4 Multiple comparisons

For the analyses, the following functions of **agricolae** are used: LSD.test, HSD.test, duncan.test, scheffe.test, waller.test, SNK.test, REGW.test, Steel and Torry and Dickey (1997); Hsu (1996) and durbin.test, kruskal, friedman, waerden.test and Median.test, Conover (1999).

For every statistical analysis, the data should be organized in columns. For the demonstration, the agricolae database will be used.

The sweetpotato data correspond to a completely random experiment in field with plots of 50 sweet potato plants, subjected to the virus effect and to a control without virus (See the reference manual of the package).

```
> data(sweetpotato)
> model<-aov(yield~virus, data=sweetpotato)
> cv.model(model)

[1] 17.1666
> attach(sweetpotato)
> mean(yield)
```

```
[1] 27.625
```

a

b

СС fc

> detach(sweetpotato)

Model parameters: Degrees of freedom and variance of the error:

```
> df<-df.residual(model)</pre>
> MSerror<-deviance(model)/df
```

4.1 The Least Significant Difference (LSD)

> # comparison <- LSD.test(yield, virus, df, MSerror)

It includes the multiple comparison through the method of the minimum significant difference (Least Significant Difference), Steel and Torry and Dickey (1997).

```
> LSD.test(model, "virus",console=TRUE)
Study: model ~ "virus"
LSD t Test for yield
Mean Square Error: 22.48917
virus, means and individual (95 %) CI
                 std r
                             LCL
                                      UCL Min Max
      yield
cc 24.40000 3.609709 3 18.086268 30.71373 21.7 28.5
fc 12.86667 2.159475 3 6.552935 19.18040 10.6 14.9
ff 36.33333 7.333030 3 30.019601 42.64707 28.0 41.8
oo 36.90000 4.300000 3 30.586268 43.21373 32.1 40.4
Alpha: 0.05; DF Error: 8
Critical Value of t: 2.306004
Least Significant Difference 8.928965
Means with the same letter are not significantly different
Groups, Treatments and means
a
           00
                       36.9
           ff
                       36.33333
```

In the function LSD.test, the multiple comparison was carried out. In order to obtain the probabilities of the comparisons, it should be indicated that groups are not required; thus:

```
> # comparison <- LSD.test(yield, virus, df, MSerror, group=F)
> outLSD <-LSD.test(model, "virus", group=F,console=TRUE)</pre>
```

24.4

12.86667

Study: model ~ "virus"

LSD t Test for yield

Mean Square Error: 22.48917

virus, means and individual (95 %) CI

yield std r LCL UCL Min Max cc 24.40000 3.609709 3 18.086268 30.71373 21.7 28.5 fc 12.86667 2.159475 3 6.552935 19.18040 10.6 14.9 ff 36.33333 7.333030 3 30.019601 42.64707 28.0 41.8 co 36.90000 4.300000 3 30.586268 43.21373 32.1 40.4

Alpha: 0.05; DF Error: 8 Critical Value of t: 2.306004

Minimum difference changes for each comparison

Means with the same letter are not significantly different

Groups, Treatments and means

Comparison between treatments means

Difference pvalue sig. LCL UCL cc - fc 11.5333333 0.0176 * 2.604368 20.462299 cc - ff -11.9333333 0.0151 * -20.862299 -3.004368 cc - oo -12.5000000 0.0121 * -21.428965 -3.571035 fc - ff -23.4666667 0.0003 *** -32.395632 -14.537701 fc - oo -24.0333333 0.0003 *** -32.962299 -15.104368 ff - oo -0.5666667 0.8873 -9.495632 8.362299

Signif. codes:

0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1

> print(outLSD)

\$statistics

Mean CV MSerror 27.625 17.1666 22.48917

\$parameters

Df ntr t.value alpha test name.t 8 4 2.306004 0.05 Fisher-LSD virus

\$means

yield std r LCL UCL Min Max cc 24.40000 3.609709 3 18.086268 30.71373 21.7 28.5

```
fc 12.86667 2.159475 3 6.552935 19.18040 10.6 14.9
ff 36.33333 7.333030 3 30.019601 42.64707 28.0 41.8
oo 36.90000 4.300000 3 30.586268 43.21373 32.1 40.4
$comparison
                                                 UCL
         Difference pvalue sig.
                                      LCL
cc - fc 11.5333333 0.0176 *
                                 2.604368 20.462299
cc - ff -11.9333333 0.0151
                             * -20.862299 -3.004368
cc - oo -12.5000000 0.0121
                          * -21.428965 -3.571035
fc - ff -23.4666667 0.0003 *** -32.395632 -14.537701
fc - oo -24.0333333 0.0003 *** -32.962299 -15.104368
ff - oo -0.5666667 0.8873
                                -9.495632 8.362299
$groups
```

4.2 holm, hommel, hochberg, bonferroni, BH, BY, fdr

With the function LSD.test we can make adjustments to the probabilities found, as for example the adjustment by Bonferroni, holm.

```
> LSD.test(model, "virus", group=F, p.adj= "bon",console=TRUE)
Study: model ~ "virus"
LSD t Test for yield
P value adjustment method: bonferroni
Mean Square Error: 22.48917
virus, means and individual (95 %) CI
      yield
                 std r
                             LCL
                                      UCL Min Max
cc 24.40000 3.609709 3 18.086268 30.71373 21.7 28.5
fc 12.86667 2.159475 3 6.552935 19.18040 10.6 14.9
ff 36.33333 7.333030 3 30.019601 42.64707 28.0 41.8
oo 36.90000 4.300000 3 30.586268 43.21373 32.1 40.4
Alpha: 0.05; DF Error: 8
Critical Value of t: 3.478879
Minimum difference changes for each comparison
Means with the same letter are not significantly different
```

Groups, Treatments and means

NULL

Comparison between treatments means

```
Difference pvalue sig.
                                       LCL
                                                   UCL
cc - fc 11.5333333 0.1058
                                -1.937064 25.0037305
cc - ff -11.9333333 0.0904
                             . -25.403730
                                           1.5370638
                             . -25.970397
cc - oo -12.5000000 0.0725
                                            0.9703971
fc - ff -23.4666667 0.0018
                           ** -36.937064 -9.9962695
fc - oo -24.0333333 0.0015
                            ** -37.503730 -10.5629362
ff - oo -0.5666667 1.0000
                               -14.037064 12.9037305
> out<-LSD.test(model, "virus", group=TRUE, p.adj= "holm")
> print(out$group)
  trt
        means M
1 oo 36.90000 a
2 ff 36.33333 a
  cc 24.40000 b
  fc 12.86667 c
> out<-LSD.test(model, "virus", group=FALSE, p.adj= "holm")
> print(out$comparison)
        Difference pvalue sig.
cc - fc 11.5333333 0.0484
cc - ff -11.9333333 0.0484
cc - oo -12.5000000 0.0484
fc - ff -23.4666667 0.0015
                             **
fc - oo -24.0333333 0.0015
ff - oo -0.5666667 0.8873
```

Other comparison tests can be applied, such as duncan, Student-Newman-Keuls, tukey and waller-duncan

For Duncan, use the function duncan.test; for Student-Newman-Keuls, the function SNK.test; for Tukey, the function HSD.test; for Scheffe, the function scheffe.test and for Waller-Duncan, the function waller.test. The arguments are the same. Waller also requires the value of F-calculated of the ANOVA treatments. If the model is used as a parameter, this is no longer necessary.

4.3 Duncan's New Multiple-Range Test

It corresponds to the Duncan's Test, Steel and Torry and Dickey (1997).

```
> duncan.test(model, "virus",console=TRUE)

Study: model ~ "virus"

Duncan's new multiple range test
for yield

Mean Square Error: 22.48917
```

virus, means

```
yield std r Min Max cc 24.40000 3.609709 3 21.7 28.5 fc 12.86667 2.159475 3 10.6 14.9 ff 36.33333 7.333030 3 28.0 41.8 oo 36.90000 4.300000 3 32.1 40.4
```

Alpha: 0.05; DF Error: 8

Critical Range

2 3 4 8.928965 9.304825 9.514910

Means with the same letter are not significantly different.

Groups, Treatments and means

a	00	36.9
a	ff	36.33
b	cc	24.4
С	fc	12.87

4.4 Student-Newman-Keuls

Student, Newman and Keuls helped to improve the Newman-Keuls test of 1939, which was known as the Keuls method, Steel and Torry and Dickey (1997).

```
> # SNK.test(model, "virus", alpha=0.05,console=TRUE)
> SNK.test(model, "virus", group=FALSE,console=TRUE)
```

Study: model ~ "virus"

Student Newman Keuls Test for yield

Mean Square Error: 22.48917

virus, means

yield std r Min Max cc 24.40000 3.609709 3 21.7 28.5 fc 12.86667 2.159475 3 10.6 14.9 ff 36.33333 7.333030 3 28.0 41.8 oo 36.90000 4.300000 3 32.1 40.4

Alpha: 0.05; DF Error: 8

Critical Range

2 3 4 8.928965 11.064170 12.399670

Comparison between treatments means

```
Difference pvalue sig. LCL UCL cc-fc 11.5333333 0.0176 * 2.604368 20.462299 cc-ff -11.9333333 0.0151 * -20.862299 -3.004368 cc-oo -12.5000000 0.0291 * -23.564170 -1.435830 fc-ff -23.4666667 0.0008 *** -34.530836 -12.402497 fc-oo -24.0333333 0.0012 ** -36.433003 -11.633664 ff-oo -0.5666667 0.8873 -9.495632 8.362299
```

4.5 Ryan, Einot and Gabriel and Welsch

Multiple range tests for all pairwise comparisons, to obtain a confident inequalities multiple range tests, ?Hsu:1996.

```
> # REGW.test(model, "virus", alpha=0.05,console=TRUE)
> REGW.test(model, "virus", group=FALSE,console=TRUE)
Study: model ~ "virus"
Ryan, Einot and Gabriel and Welsch multiple range test
for yield
Mean Square Error: 22.48917
virus, means
      yield
                 std r Min Max
cc 24.40000 3.609709 3 21.7 28.5
fc 12.86667 2.159475 3 10.6 14.9
ff 36.33333 7.333030 3 28.0 41.8
oo 36.90000 4.300000 3 32.1 40.4
Alpha: 0.05; DF Error: 8
Critical Range
       2
                3
10.62212 11.06417 12.39967
```

```
Comparison between treatments means
```

```
Difference pvalue sig. LCL UCL cc - fc 11.5333333 0.0350 * 0.9112173 22.155449 cc - ff -11.9333333 0.0299 * -22.5554494 -1.311217 cc - oo -12.5000000 0.0291 * -23.5641696 -1.435830 fc - ff -23.4666667 0.0008 *** -34.5308363 -12.402497 fc - oo -24.0333333 0.0012 ** -36.4330031 -11.633664 ff - oo -0.5666667 0.9873 -11.1887827 10.055449
```

4.6 Tukey's W Procedure (HSD)

This studentized range test, created by Tukey in 1953, is known as the Tukey's HSD (Honestly Significant Differences), Steel and Torry and Dickey (1997).

```
> outHSD<- HSD.test(model, "virus",console=TRUE)</pre>
Study: model ~ "virus"
HSD Test for yield
Mean Square Error: 22.48917
virus, means
      yield
                 std r Min Max
cc 24.40000 3.609709 3 21.7 28.5
fc 12.86667 2.159475 3 10.6 14.9
ff 36.33333 7.333030 3 28.0 41.8
oo 36.90000 4.300000 3 32.1 40.4
Alpha: 0.05; DF Error: 8
Critical Value of Studentized Range: 4.52881
Honestly Significant Difference: 12.39967
Means with the same letter are not significantly different.
Groups, Treatments and means
           00
           ff
                       36.33
ab
bc
           CC
                       24.4
                     12.87
          fc
> outHSD
$statistics
    Mean
              CV MSerror
                               HSD
  27.625 17.1666 22.48917 12.39967
$parameters
  Df ntr StudentizedRange alpha test name.t
                 4.52881 0.05 Tukey virus
$means
                 std r Min Max
     yield
cc 24.40000 3.609709 3 21.7 28.5
fc 12.86667 2.159475 3 10.6 14.9
ff 36.33333 7.333030 3 28.0 41.8
oo 36.90000 4.300000 3 32.1 40.4
```

\$comparison NULL

\$groups

```
trt means M
1 oo 36.90000 a
2 ff 36.33333 ab
3 cc 24.40000 bc
4 fc 12.86667 c
```

4.7 Waller-Duncan's Bayesian K-Ratio T-Test

Duncan continued the multiple comparison procedures, introducing the criterion of minimizing both experimental errors; for this, he used the Bayes' theorem, obtaining one new test called Waller-Duncan, Waller and Duncan (1969); Steel and Torry and Dickey (1997).

```
> # variance analysis:
> anova(model)
Analysis of Variance Table
Response: yield
          Df Sum Sq Mean Sq F value
                                        Pr(>F)
           3 1170.21 390.07 17.345 0.0007334 ***
virus
Residuals 8 179.91
                       22.49
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> attach(sweetpotato)
> waller.test(yield,virus,df,MSerror,Fc= 17.345, group=F,console=TRUE)
Study: yield ~ virus
Waller-Duncan K-ratio t Test for yield
This test minimizes the Bayes risk under additive loss and certain other assumptions
                            . . . . . .
K ratio
                         100.00000
Error Degrees of Freedom
                          8.00000
Error Mean Square
                          22.48917
F value
                          17.34500
Critical Value of Waller 2.23600
virus, means
      yield
                 std r Min Max
cc 24.40000 3.609709 3 21.7 28.5
fc 12.86667 2.159475 3 10.6 14.9
ff 36.33333 7.333030 3 28.0 41.8
```

```
oo 36.90000 4.300000 3 32.1 40.4
```

Minimum Significant Difference 8.657906 Comparison between treatments means

```
Difference significant
cc - fc 11.5333333 TRUE
cc - ff -11.9333333 TRUE
cc - oo -12.5000000 TRUE
fc - ff -23.4666667 TRUE
fc - oo -24.0333333 TRUE
ff - oo -0.5666667 FALSE
```

> detach(sweetpotato)

In another case with only invoking the model object:

```
> outWaller <- waller.test(model, "virus", group=FALSE,console=FALSE)
```

The found object *outWaller* has information to make other procedures.

```
> names(outWaller)
```

```
[1] "statistics" "parameters" "means" "comparison"
[5] "groups"
```

> print(outWaller\$comparison)

```
Difference significant
cc - fc 11.5333333 TRUE
cc - ff -11.9333333 TRUE
cc - oo -12.5000000 TRUE
fc - ff -23.4666667 TRUE
fc - oo -24.0333333 TRUE
ff - oo -0.5666667 FALSE
```

It is indicated that the virus effect "ff" is not significant to the control "oo".

> outWaller\$statistics

```
Mean CV MSerror F.Value CriticalDifference 27.625 17.1666 22.48917 17.34478 8.657906
```

4.8 Scheffe's Test

This method, created by Scheffe in 1959, is very general for all the possible contrasts and their confidence intervals. The confidence intervals for the averages are very broad, resulting in a very conservative test for the comparison between treatment averages, Steel and Torry and Dickey (1997).

```
> # analysis of variance:
```

- > scheffe.test(model,"virus", group=TRUE,console=TRUE,
- + main="Yield of sweetpotato\nDealt with different virus")

Study: Yield of sweetpotato Dealt with different virus

Scheffe Test for yield

Mean Square Error : 22.48917

virus, means

yield std r Min Max cc 24.40000 3.609709 3 21.7 28.5 fc 12.86667 2.159475 3 10.6 14.9 ff 36.33333 7.333030 3 28.0 41.8 oo 36.90000 4.300000 3 32.1 40.4

Alpha: 0.05; DF Error: 8 Critical Value of F: 4.066181

Minimum Significant Difference: 13.52368

Means with the same letter are not significantly different.

Groups, Treatments and means a oo 36.9 a ff 36.33 ab cc 24.4 b fc 12.87

The minimum significant value is very high. If you require the approximate probabilities of comparison, you can use the option group=FALSE.

> outScheffe <- scheffe.test(model, "virus", group=FALSE, console=TRUE)

Study: model ~ "virus"

Scheffe Test for yield

Mean Square Error : 22.48917

virus, means

yield std r Min Max cc 24.40000 3.609709 3 21.7 28.5 fc 12.86667 2.159475 3 10.6 14.9 ff 36.33333 7.333030 3 28.0 41.8 oo 36.90000 4.300000 3 32.1 40.4

```
Alpha: 0.05; DF Error: 8
Critical Value of F: 4.066181
```

Comparison between treatments means

```
Difference pvalue sig LCL UCL cc - fc 11.5333333 0.0978 . -1.000348 24.0670149 cc - ff -11.9333333 0.0855 . -24.467015 0.6003483 cc - oo -12.5000000 0.0706 . -25.033682 0.0336816 fc - ff -23.4666667 0.0023 ** -36.000348 -10.9329851 fc - oo -24.0333333 0.0020 ** -36.567015 -11.4996517 ff - oo -0.5666667 0.9991 -13.100348 11.9670149
```

4.9 Multiple comparison in factorial treatments

In a factorial combined effects of the treatments. Comparetive tests: LSD, HSD, Waller-Duncan, Duncan, Scheffé, SNK can be applied.

```
> # modelABC <-aov (y \tilde{} A * B * C, data)
> # compare <-LSD.test (modelABC, c ("A", "B", "C"),console=TRUE)
```

The comparison is the combination of A:B:C.

Data RCBD design with a factorial clone x nitrogen. The response variable yield.

```
> yield <-scan (text =
  "6 7 9 13 16 20 8 8 9
   7 8 8 12 17 18 10 9 12
    9 9 9 14 18 21 11 12 11
   8 10 10 15 16 22 9 9 9 "
+ )
> block <-gl (4, 9)
> clone <-rep (gl (3, 3, labels = c ("c1", "c2", "c3")), 4)</pre>
> nitrogen <-rep (gl (3, 1, labels = c ("n1", "n2", "n3")), 12)
> A <-data.frame (block, clone, nitrogen, yield)
> head (A)
  block clone nitrogen yield
           c1
                    n1
                            6
2
                           7
      1
           c1
                    n2
3
      1
          c1
                    n3
                           9
           c2
                          13
      1
                    n1
5
           c2
                    n2
                          16
      1
6
      1
           c2
                    n3
                          20
```

> anova (outAOV)

Analysis of Variance Table

```
Response: yield
```

Df Sum Sq Mean Sq F value Pr(>F)
block 3 20.75 6.917 5.8246 0.0038746 **
clone 2 497.72 248.861 209.5673 6.370e-16 ***
nitrogen 2 54.06 27.028 22.7602 2.865e-06 ***
clone:nitrogen 4 43.28 10.819 9.1111 0.0001265 ***

Residuals 24 28.50 1.188

Signif. codes:

0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

> outFactorial <-LSD.test (outAOV, c("clone", "nitrogen"),
+ main = "Yield ~ block + nitrogen + clone + clone:nitrogen",console=TRUE)</pre>

Study: Yield ~ block + nitrogen + clone + clone:nitrogen

LSD t Test for yield

Mean Square Error: 1.1875

clone:nitrogen, means and individual (95 %) CI

yield std r LCL UCL Min Max c1:n1 7.50 1.2909944 4 6.375459 8.624541 6 9 c1:n2 8.50 1.2909944 4 7.375459 9.624541 7 10 c1:n3 9.00 0.8164966 4 7.875459 10.124541 8 10 c2:n1 13.50 1.2909944 4 12.375459 14.624541 12 15 c2:n2 16.75 0.9574271 4 15.625459 17.874541 16 18 c2:n3 20.25 1.7078251 4 19.125459 21.374541 18 22 c3:n1 9.50 1.2909944 4 8.375459 10.624541 8 11 c3:n2 9.50 1.7320508 4 8.375459 10.624541 8 12 c3:n3 10.25 1.5000000 4 9.125459 11.374541 9 12

Alpha: 0.05; DF Error: 24 Critical Value of t: 2.063899

Least Significant Difference 1.590341

Means with the same letter are not significantly different

Groups, Treatments and means

a	c2:n3	20.25
b	c2:n2	16.75
С	c2:n1	13.5
d	c3:n3	10.25
de	c3:n1	9.5
de	c3:n2	9.5

```
def    c1:n3     9
ef     c1:n2     8.5
f     c1:n1     7.5

> par(mar=c(3,3,2,0))
> pic1<-bar.err(outFactorial$means,variation="range",ylim=c(5,25), bar=FALSE,col=0,las=1)
> points(pic1$index,pic1$means,pch=18,cex=1.5,col="blue")
> axis(1,pic1$index,labels=FALSE)
> title(main="average and range\nclon:nitrogen")
```

4.10 Analysis of Balanced Incomplete Blocks

This analysis can come from balanced or partially balanced designs. The function BIB.test is for balanced designs, and BIB.test, for partially balanced designs. In the following example, the **agricolae** data will be used, Joshi (1987).

```
> # Example linear estimation and design of experiments. (Joshi)
> # Institute of Social Sciences Agra, India
> # 6 varieties of wheat in 10 blocks of 3 plots each.
> block < -gl(10,3)
> variety<-c(1,2,3,1,2,4,1,3,5,1,4,6,1,5,6,2,3,6,2,4,5,2,5,6,3,4,5,3,4,6)</pre>
> Y < -c(69,54,50,77,65,38,72,45,54,63,60,39,70,65,54,65,68,67,57,60,62,
+ 59,65,63,75,62,61,59,55,56)
> head(cbind(block, variety, Y))
     block variety Y
[1,]
         1
                 1 69
[2,]
         1
                 2 54
[3,]
         1
                 3 50
[4,]
         2
                 1 77
[5,]
         2
                 2 65
[6,]
         2
                 4 38
> BIB.test(block, variety, Y,console=TRUE)
```

```
ANALYSIS BIB: Y
```

Class level information

Block: 1 2 3 4 5 6 7 8 9 10

Trt : 1 2 3 4 5 6

Number of observations: 30

Analysis of Variance Table

```
Response: Y
```

```
Df Sum Sq Mean Sq F value Pr(>F)
block.unadj 9 466.97 51.885 0.9019 0.54712
trt.adj 5 1156.44 231.289 4.0206 0.01629 *
Residuals 15 862.89 57.526
```

```
---
```

```
Signif. codes:
0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
coefficient of variation: 12.6 %
Y Means: 60.3
```

variety, statistics

```
Y mean.adj SE r std Min Max

1 70.2 75.13333 3.728552 5 5.069517 63 77

2 60.0 58.71667 3.728552 5 4.898979 54 65

3 59.4 58.55000 3.728552 5 12.381438 45 75

4 55.0 54.96667 3.728552 5 9.848858 38 62

5 61.4 60.05000 3.728552 5 4.505552 54 65

6 55.8 54.38333 3.728552 5 10.756393 39 67
```

LSD test

Std.diff : 5.363111 Alpha : 0.05 LSD : 11.4312

Parameters BIB
Lambda : 2
treatmeans : 6
Block size : 3
Blocks : 10
Replication: 5

Efficiency factor 0.8

<<< Book >>>

Means with the same letter are not significantly different.

Comparison of treatments

Groups,	Treatments	and mean
a	1	75.13
b	5	60.05
b	2	58.72
b	3	58.55
b	4	54.97
b	6	54.38

function (block, trt, Y, test = c("lsd", "tukey", "duncan", "waller", "snk"), alpha = 0.05, group = TRUE) LSD, Tukey Duncan, Waller-Duncan and SNK, can be used. The probabilities of the comparison can also be obtained. It should only be indicated: group=FALSE, thus:

> out <-BIB.test(block, trt=variety, Y, test="tukey", group=FALSE, console=TRUE)

ANALYSIS BIB: Y

Class level information

Block: 1 2 3 4 5 6 7 8 9 10

Trt : 1 2 3 4 5 6

Number of observations: 30

Analysis of Variance Table

Response: Y

Df Sum Sq Mean Sq F value Pr(>F) block.unadj 9 466.97 51.885 0.9019 0.54712

trt.adj 5 1156.44 231.289 4.0206 0.01629 *

Residuals 15 862.89 57.526

Signif. codes:

0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

coefficient of variation: 12.6 %

Y Means: 60.3

variety, statistics

Y mean.adj SE r std Min Max 1 70.2 75.13333 3.728552 5 5.069517 63 77 2 60.0 58.71667 3.728552 5 4.898979 54 65 3 59.4 58.55000 3.728552 5 12.381438 45 75 4 55.0 54.96667 3.728552 5 9.84858 38 62 5 61.4 60.05000 3.728552 5 4.505552 54 65

6 55.8 54.38333 3.728552 5 10.756393 39 67

Tukey

Alpha : 0.05 Std.err : 3.792292 HSD : 17.42458

Parameters BIB
Lambda : 2
treatmeans : 6
Block size : 3
Blocks : 10
Replication: 5

Efficiency factor 0.8

<<< Book >>>

Comparison between treatments means

Difference pvalue sig.

1 - 2 16.4166667 0.0705

1 - 3 16.5833333 0.0666

```
1 - 4 20.1666667 0.0191
1 - 5 15.0833333 0.1096
1 - 6 20.7500000 0.0155
2 - 3 0.1666667 1.0000
2 - 4 3.7500000 0.9792
2 - 5 -1.3333333 0.9998
2 - 6 4.3333333 0.9616
3 - 4 3.5833333 0.9829
3 - 5 -1.5000000 0.9997
3 - 6 4.1666667 0.9674
4 - 5 -5.0833333 0.9273
4 - 6 0.5833333 1.0000
5 - 6 5.6666667 0.8908
> names(out)
[1] "parameters" "statistics" "comparison" "means"
[5] "groups"
> rm(block, variety)
bar.group: out$groups
bar.err: out$means
```

4.11 Partially Balanced Incomplete Blocks

The function *PBIB.test* Joshi (1987), can be used for the lattice and alpha designs.

Consider the following case: Construct the alpha design with 30 treatments, 2 repetitions, and a block size equal to 3.

The generated plan is plan\$book.

Suppose that the corresponding observation to each experimental unit is:

```
> yield <-c(5,2,7,6,4,9,7,6,7,9,6,2,1,1,3,2,4,6,7,9,8,7,6,4,3,2,2,1,1,
            2,1,1,2,4,5,6,7,8,6,5,4,3,1,1,2,5,4,2,7,6,6,5,6,4,5,7,6,5,5,4)
```

The data table is constructed for the analysis. In theory, it is presumed that a design is applied and the experiment is carried out; subsequently, the study variables are observed from each experimental unit.

- > data<-data.frame(plan\$book, yield)</pre>
- > rm(yield, Genotype)
- > # The analysis:
- > attach(data)
- > modelPBIB <- PBIB.test(block, Genotype, replication, yield, k=3, group=TRUE,
- + console=TRUE)

ANALYSIS PBIB: yield

Class level information

block: 20 Genotype: 30

Number of observations:

Estimation Method: Residual (restricted) maximum likelihood

Parameter Estimates

Variance block:replication 2.834033e+00 replication 8.045902e-09

Residual 2.003098e+00 Fit Statistics

213.65937 BIC 259.89888 -2 Res Log Likelihood -73.82968

Analysis of Variance Table

Response: yield

AIC

Df Sum Sq Mean Sq F value Pr(>F)

Genotype 29 72.006 2.4830 1.2396 0.3668

Residuals 11 22.034 2.0031

Coefficient of variation: 31.2 %

yield Means: 4.533333

Parameters PBIB

Genotype 30

```
block size 3
block/replication 10
replication 2
Efficiency factor 0.6170213
```

Comparison test 1sd

```
<<< to see the objects: means, comparison and groups. >>>
```

> detach(data)

The adjusted averages can be extracted from the modelPBIB.

head(modelPBIB\$means)

The comparisons:

head(modelPBIB\$comparison)

The data on the adjusted averages and their variation can be illustrated see Figure ??. since the created object is very similar to the objects generated by the multiple comparisons.

Analysis of balanced lattice 3x3, 9 treatments, 4 repetitions.

Create the data in a text file: latice3x3.txt and read with R:

sqr block trt yield						
1 1 1 48.76	1 1 4 14.46	1 1 3 19.68				
1 2 8 10.83	1 2 6 30.69	1 2 7 31.00				
1 3 5 12.54	1 3 9 42.01	1 3 2 23.00				
2 4 5 11.07	2 4 8 22.00	2 4 1 41.00				
2 5 2 22.00	2 5 7 42.80	2 5 3 12.90				
2 6 9 47.43	2 6 6 28.28	2 6 4 49.95				
3 7 2 27.67	3 7 1 50.00	3 7 6 25.00				
3 8 7 30.00	3 8 5 24.00	3 8 4 45.57				
3 9 3 13.78	3 9 8 24.00	3 9 9 30.00				
4 10 6 37.00	4 10 3 15.42	4 10 5 20.00				
4 11 4 42.37	4 11 2 30.00	4 11 8 18.00				
4 12 9 39.00	4 12 7 23.80	4 12 1 43.81				

```
> trt < -c(1,8,5,5,2,9,2,7,3,6,4,9,4,6,9,8,7,6,1,5,8,3,2,7,3,7,2,1,3,4,6,4,9,5,8,1)
```

ANALYSIS PBIB: yield

 ${\tt Class\ level\ information}$

block: 12 trt: 9

> yield<-c(48.76,10.83,12.54,11.07,22,47.43,27.67,30,13.78,37,42.37,39,14.46,30.69,42.01,

^{+ 22,42.8,28.28,50,24,24,15.42,30,23.8,19.68,31,23,41,12.9,49.95,25,45.57,30,20,18,43.81)}

> sqr < -rep(gl(4,3),3)

> block<-rep(1:12,3)

> modelLattice<-PBIB.test(block,trt,sqr,yield,k=3,console=TRUE)

Number of observations: 36

Estimation Method: Residual (restricted) maximum likelihood

Parameter Estimates

Variance

block:sqr 1.735327e-08 sqr 1.783279e-07 Residual 5.693724e+01

Fit Statistics

AIC 222.23197 BIC 237.78201 -2 Res Log Likelihood -99.11599

Analysis of Variance Table

Response: yield

Df Sum Sq Mean Sq F value Pr(>F)
trt 8 3749.4 468.68 8.2315 0.0001987 ***

Residuals 16 911.0 56.94

Signif. codes:

0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Coefficient of variation: 25.9 %

yield Means: 29.16167

Parameters PBIB

trt

block size 3

block/sqr 3

sqr 4

Efficiency factor 0.75

Comparison test 1sd

<<< to see the objects: means, comparison and groups. >>>

The adjusted averages can be extracted from the modelLattice.

print(modelLattice\$means)

The comparisons:

head(modelLattice\$comparison)

4.12 Augmented Blocks

The function *DAU.test* can be used for the analysis of the augmented block design. The data should be organized in a table, containing the blocks, treatments, and the response.

The treatments are in each block:

With their respective responses:

> by(yield,block,as.character)

```
block: I
[1] "83" "77" "78" "78" "70" "75" "74"

------
block: II
[1] "79" "81" "81" "91" "79" "78"

------
block: III
[1] "92" "79" "87" "81" "89" "96" "82"
```

Analysis:

> modelDAU<- DAU.test(block,trt,yield,method="lsd",console=TRUE)

ANALYSIS DAU: yield Class level information

Block: I II III

Trt: ABCDefghijkl

Number of observations: 20

ANOVA, Treatment Adjusted Analysis of Variance Table

Response: yield

Df Sum Sq Mean Sq F value Pr(>F)
block.unadj 2 360.07 180.036
trt.adj 11 285.10 25.918 0.9609 0.5499
Control 3 52.92 17.639 0.6540 0.6092
Control + control.VS.aug. 8 232.18 29.022 1.0760 0.4779
Residuals 6 161.83 26.972

ANOVA, Block Adjusted Analysis of Variance Table

Response: yield

Df Sum Sq Mean Sq F value Pr(>F)
trt.unadj 11 575.67 52.333
block.adj 2 69.50 34.750 1.2884 0.3424
Control 3 52.92 17.639 0.6540 0.6092
Augmented 7 505.87 72.268 2.6793 0.1253
Control vs augmented 1 16.88 16.875 0.6256 0.4591
Residuals 6 161.83 26.972

coefficient of variation: 6.4 %

yield Means: 81.5

Critical Differences (Between)

Std Error Diff.
Two Control Treatments 4.240458
Two Augmented Treatments (Same Block) 7.344688
Two Augmented Treatments(Different Blocks) 8.211611
A Augmented Treatment and A Control Treatment 6.360687

Means with the same letter are not significantly different.

Groups, Treatments and means

h	93.5
f	86.5
Α	84.67
D	83.33
C	82
j	79.5
В	79
	f A D C j

```
      ab
      e
      78.25

      ab
      k
      78.25

      ab
      i
      77.25

      ab
      l
      77.25

      b
      g
      73.25
```

Comparison between treatments means

```
<<< to see the objects: comparison and means >>>
```

> modelDAU\$means

```
std r Min Max mean.adj
     yield
                                             SE block
A 84.66667 6.658328 3 79
                           92 84.66667 2.998456
B 79.00000 2.000000 3
                       77
                           81 79.00000 2.998456
C 82.00000 4.582576 3
                       78
                           87 82.00000 2.998456
D 83.33333 6.806859 3 78
                           91 83.33333 2.998456
e 79.00000
                 NA 1 79
                           79 78.25000 5.193479
                                                   II
f 89.00000
                 NA 1
                       89
                           89 86.50000 5.193479
                                                  III
g 70.00000
                 NA 1
                      70
                           70 73.25000 5.193479
                                                    Ι
h 96.00000
                 NA 1
                       96
                           96 93.50000 5.193479
                                                  III
i 78.00000
                 NA 1
                       78
                           78 77.25000 5.193479
                                                   II
j 82.00000
                 NA 1
                       82
                           82 79.50000 5.193479
                                                   III
k 75.00000
                 NA 1
                       75
                           75 78.25000 5.193479
                                                    Ι
1 74.00000
                 NA 1 74 74 77.25000 5.193479
                                                     Ι
```

- > modelDAU<- DAU.test(block,trt,yield,method="lsd",group=F,console=FALSE)
- > head(modelDAU\$comparison,8)

```
Difference pvalue sig.
```

```
A - B 5.666667 0.2298
```

A - C 2.666667 0.5526

A - D 1.333333 0.7638

A - e 6.416667 0.3520

A - f -1.833333 0.7828

A - g 11.416667 0.1228

A - h -8.833333 0.2142

A - i 7.416667 0.2878

5 Non-parametric comparisons

The functions for non-parametric multiple comparisons included in **agricolae** are: kruskal, waerden.test, friedman and durbin.test, Conover (1999).

The post hoc nonparametrics tests (kruskal, friedman, durbin and waerden) are using the criterium Fisher's least significant difference (LSD).

The function kruskal is used for N samples (N>2), populations or data coming from a completely random experiment (populations = treatments).

The function waerden.test, similar to kruskal-wallis, uses a normal score instead of ranges as kruskal does.

The function *friedman* is used for organoleptic evaluations of different products, made by judges (every judge evaluates all the products). It can also be used for the analysis of treatments of the randomized complete block design, where the response cannot be treated through the analysis of variance.

The function *durbin.test* for the analysis of balanced incomplete block designs is very used for sampling tests, where the judges only evaluate a part of the treatments.

Montgomery book data, Montgomery (2002). Included in the agricolae package

For the examples, the agricolae package data will be used

5.1 Kruskal-Wallis

Post Hoc Analysis

It makes the multiple comparison with Kruskal-Wallis. The parameters by default are alpha = 0.05.

```
> str(kruskal)
function (y, trt, alpha = 0.05, p.adj = c("none", "holm",
    "hommel", "hochberg", "bonferroni", "BH", "BY",
    "fdr"), group = TRUE, main = NULL, console = FALSE)
Analysis
> outKruskal<-with(corn,kruskal(observation,method,group=TRUE, main="corn", console=TRUE))
Study: corn
Kruskal-Wallis test's
Ties or no Ties
Critical Value: 25.62884
Degrees of freedom: 3
Pvalue Chisq : 1.140573e-05
method, means of the ranks
  observation r
1
     21.83333 9
2
     15.30000 10
3
     29.57143 7
      4.81250 8
```

```
t-Student: 2.042272
Alpha : 0.05
```

Minimum difference changes for each comparison

Means with the same letter are not significantly different

```
Groups, Treatments and mean of the ranks a 3 29.57143 b 1 21.83333 c 2 15.3 d 4.8125
```

The object output has the same structure of the comparisons see Figure 8.

5.2 Kruskal-Wallis: adjust P-values

To see p.adjust.methods()

means M

```
> out<-with(corn,kruskal(observation,method,group=TRUE, main="corn", p.adj="holm"))
> print(out$group)
```

```
1 3 29.57143 a
2 1 21.83333 b
3 2 15.30000 c
4 4 .81250 d
```

trt

> out<-with(corn,kruskal(observation,method,group=FALSE, main="corn", p.adj="holm"))
> print(out\$comparison)

```
Difference pvalue sig.
1 - 2 6.533333 0.0079 **
1 - 3 -7.738095 0.0079 **
1 - 4 17.020833 0.0000 ***
2 - 3 -14.271429 0.0000 ***
```

2 - 4 10.487500 0.0003 ***

3 - 4 24.758929 0.0000 ***

5.3 Friedman

```
> str(friedman)
function (judge, trt, evaluation, alpha = 0.05, group = TRUE,
    main = NULL, console = FALSE)
```

Analysis

```
> rm(trt)
> data(grass)
```

```
> attach(grass)
> out<-friedman(judge,tr</pre>
```

> out<-friedman(judge,trt, evaluation,alpha=0.05, group=FALSE,

+ main="Data of the book of Conover", console=TRUE)

Study: Data of the book of Conover

trt, Sum of the ranks

	${\tt evaluation}$	r	
t1	38.0	12	
t2	23.5	12	
t3	24.5	12	
t4	34.0	12	

Friedman's Test

Adjusted for ties

Critical Value: 8.097345 P.Value Chisq: 0.04404214

F Value: 3.192198 P.Value F: 0.03621547

Post Hoc Analysis

Alpha: 0.05

t-Student: 2.034515

Comparison between treatments

Sum of the ranks

```
Difference pvalue sig.
                              LCL
                                     UCL
t1 - t2
        14.5 0.0149 * 3.02 25.98
t1 - t3
            13.5 0.0226
                          * 2.02 24.98
t1 - t4
             4.0 0.4834
                             -7.48 15.48
t2 - t3
            -1.0 0.8604
                            -12.48 10.48
t2 - t4
           -10.5 0.0717
                           . -21.98 0.98
t3 - t4
            -9.5 0.1017
                            -20.98 1.98
```

> detach(grass)

5.4 Waerden

A nonparametric test for several independent samples. Example applied with the sweet potato data in the **agricolae** basis.

Analysis

```
> rm(yield)
> data(sweetpotato)
> attach(sweetpotato)
> outWaerden<-waerden.test(yield,virus,alpha=0.01,group=TRUE,console=TRUE)
Study: yield ~ virus
Van der Waerden (Normal Scores) test's
Value: 8.409979
Pvalue: 0.03825667
Degrees of Freedom: 3
virus, means of the normal score
        yield
                   std r
cc -0.2328353 0.3028832 3
fc -1.0601764 0.3467934 3
ff 0.6885684 0.7615582 3
oo 0.6044433 0.3742929 3
Post Hoc Analysis
t-Student: 3.355387
Alpha : 0.01
LSD
       : 1.322487
Means with the same letter are not significantly different
Groups, Treatments and means of the normal score
               0.6886
                     0.6044
          00
a
                      -0.2328
ab
           СС
                      -1.06
           fc
The comparison probabilities are obtained with the parameter group = FALSE
> names(outWaerden)
[1] "statistics" "parameters" "means"
                                          "comparison"
[5] "groups"
To see outWaerden$comparison
> out<-waerden.test(yield,virus,group=F,console=TRUE)
Study: yield ~ virus
Van der Waerden (Normal Scores) test's
```

```
Value: 8.409979
Pvalue: 0.03825667
Degrees of Freedom: 3
virus, means of the normal score
        yield
                    std r
cc -0.2328353 0.3028832 3
fc -1.0601764 0.3467934 3
ff 0.6885684 0.7615582 3
oo 0.6044433 0.3742929 3
Comparison between treatments means
mean of the normal score
        Difference pvalue sig.
                                       LCL
                                                    UCL
cc - fc 0.8273411 0.0690 . -0.08154345 1.73622564
cc - ff -0.9214037 0.0476
                           * -1.83028827 -0.01251917
cc - oo -0.8372786 0.0664 . -1.74616316 0.07160593
fc - ff -1.7487448 0.0022 ** -2.65762936 -0.83986026
fc - oo -1.6646197 0.0029
                            ** -2.57350426 -0.75573516
ff - oo 0.0841251 0.8363
                               -0.82475944 0.99300965
> detach(sweetpotato)
5.5
     Median test
A nonparametric test for several independent samples. The median test is designed to examine whether
several samples came from populations having the same median, Conover (1999).
> str(Median.test)
function (y, trt, correct = TRUE, simulate.p.value = FALSE,
    console = TRUE)
Analysis
> data(sweetpotato)
> attach(sweetpotato)
> outMedian<-Median.test(yield,virus,console=TRUE)
The Median Test for yield ~ virus
```

DF = 3 P.Value 0.08331631

Chisq pvalue sig

Chi Square = 6.666667

Median

cc and fc 18.30 6.0000000 0.0143 cc and ff 28.25 0.6666667 0.4142 cc and oo 30.30 6.0000000 0.0143

Median = 28.25

```
fc and ff 21.45 6.0000000 0.0143
fc and oo
           23.50 6.0000000 0.0143
ff and oo
          38.70 0.6666667 0.4142
> detach(sweetpotato)
> names(outMedian)
[1] "statistics" "parameters" "Medians"
                                            "comparison"
[5] "data"
> outMedian$statistics
     Chisq
              p.chisq Median
  6.666667 0.08331631 28.25
> outMedian$Medians
  trt Median grather lessEqual
        23.0
                             2
  СС
                   1
1
                   0
                             3
  fc
        13.1
3
  ff
        39.2
                   2
                             1
        38.2
                   3
                             0
```

5.6 Durbin

E 0.634

durbin.test; example: Myles Hollander (p. 311) Source: W. Moore and C.I. Bliss. (1942) A multiple comparison of the Durbin test for the balanced incomplete blocks for sensorial or categorical evaluation. It forms groups according to the demanded ones for level of significance (alpha); by default, 0.05.

```
> str(durbin.test)
function (judge, trt, evaluation, alpha = 0.05, group = TRUE,
    main = NULL, console = FALSE)
Analysis
> days <-gl(7,3)
> chemical<-c("A", "B", "D", "A", "C", "E", "C", "D", "G", "A", "F", "G", "B", "C", "F",
+ "B", "E", "G", "D", "E", "F")
> toxic<-c(0.465,0.343,0.396,0.602,0.873,0.634,0.875,0.325,0.330, 0.423,0.987,0.426,
+ 0.652,1.142,0.989,0.536,0.409,0.309, 0.609,0.417,0.931)
> head(data.frame(days,chemical,toxic))
  days chemical toxic
     1
              A 0.465
1
2
     1
              B 0.343
3
              D 0.396
     1
4
     2
              A 0.602
5
     2
              C 0.873
```

- > out<-durbin.test(days,chemical,toxic,group=F,console=TRUE,
- + main="Logarithm of the toxic dose")

Study: Logarithm of the toxic dose chemical, Sum of ranks

sum

- 5 Α
- В 5
- С 9
- D 5
- Ε 5
- F 8
- G 5

Durbin Test

Value : 7.714286

DF 1 : 6

P-value : 0.2597916 : 0.05 Alpha

DF 2 : 8

t-Student : 2.306004

Least Significant Difference

between the sum of ranks: 5.00689

Parameters BIB

Lambda : 1 Treatmeans: 7 Block size : 3

Blocks : 7 Replication: 3

Comparison between treatments sum of the ranks

Difference pvalue sig.

A - B 0 1.0000

A - C -4 0.1026

A - D 0 1.0000

A - E 0 1.0000

A - F -3 0.2044

A - G 0 1.0000 B - C

-4 0.1026 B - D

0 1.0000 B - E 0 1.0000

B - F -3 0.2044

B - G 0 1.0000

C - D4 0.1026

C - E 4 0.1026

C - F 1 0.6574

```
C - G
               4 0.1026
D - E
               0 1.0000
D - F
              -30.2044
D - G
               0 1.0000
E - F
              -30.2044
E - G
               0 1.0000
F - G
               3 0.2044
> names(out)
[1] "statistics" "parameters" "means"
                                            "rank"
[5] "comparison" "groups"
> out$statistics
  chisq.value
                p.value t.value
                                      LSD
     7.714286 0.2597916 2.306004 5.00689
```

6 Graphics of the multiple comparison

The results of a comparison can be graphically seen with the functions bar.group, bar.err and diffograph.

6.1 bar.group

A function to plot horizontal or vertical bar, where the letters of groups of treatments is expressed. The function applies to all functions comparison treatments. Each object must use the group object previously generated by comparative function in indicating that group = TRUE. example:

```
> # model <-aov (yield ~ fertilizer, data = field)
> # out <-LSD.test (model, "fertilizer", group = TRUE)
> # bar.group (out $ group)
> str(bar.group)

function (x, horiz = FALSE, ...)
```

The found object of one comparison is the entry for these functions, see Figure 4. The objects outHSD and outWaller are used in the following exercise: outHSD, for the functions bar.group and bar.err outWaller, for the function bar.err

6.2 bar.err

A function to plot horizontal or vertical bar, where the variation of the error is expressed in every treatments. The function applies to all functions comparison treatments. Each object must use the means object previously generated by the comparison function, see Figure 4

```
> # model <-aov (yield ~ fertilizer, data = field)
> # out <-LSD.test (model, "fertilizer", group = TRUE)
> # bar.err(out$means)
> str(bar.err)
function (x, variation = c("SE", "SD", "range"), horiz = FALSE,
    bar = TRUE, ...)
variation SE: Standard error
SD: standard deviation
range: max-min)
> par(mfrow=c(1,2), mar=c(3,3,2,0), cex=0.7)
> c1<-colors()[480]; c2=colors()[65]; c3=colors()[15]; c4=colors()[140]</pre>
> G1 < -bar.group(outHSD\$groups, ylim=c(0,45), main="Tukey\nG1",col=c1,las=1)
> # G2<-bar.group(outHSD$groups, horiz=T, xlim=c(0,45), main="Tukey\nG2",col=c2,las=1)
> # G3<-bar.err(outWaller$means, variation="range",ylim=c(0,45), col=c3,main="Range\nG3",las=1)
> G4<-bar.err(outWaller$means, horiz=T, xlim=c(0,45), col=c4, variation="SE",
+ main="Standard error \nG4",las=1)
```

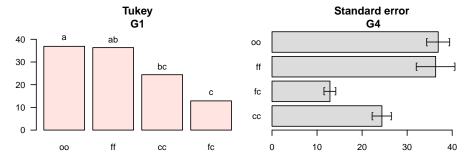


Figure 4: Comparison between treatments

```
> par(mfrow=c(2,2),cex=0.7,mar=c(3.5,1.5,3,0))
> C1<-bar.err(modelPBIB$means[1:7, ], ylim=c(0,9), col=0, main="C1",
+ variation="range",border=3,las=2)
> C2<-bar.err(modelPBIB$means[8:15,], ylim=c(0,9), col=0, main="C2",
+ variation="range", border =4,las=2)
> # Others graphic
> C3<-bar.err(modelPBIB$means[16:22,], ylim=c(0,9), col=0, main="C3",
+ variation="range",border =2,las=2)
> C4<-bar.err(modelPBIB$means[23:30,], ylim=c(0,9), col=0, main="C4",
+ variation="range", border =6,las=2)
> # Lattice graphics
> par(mar=c(2.5,2.5,1,0),cex=0.6)
> bar.group(modelLattice$group,ylim=c(0,55),density=10,las=1)
```

6.3 diffograph

It plots bars of the averages of treatments to compare. It uses the objects generated by a procedure of comparison like LSD (Fisher), duncan, Tukey (HSD), Student Newman Keul (SNK), Scheffe, Ryan, Einot and Gabriel and Welsch (REGW), Kruskal Wallis, Friedman and Waerden, Hsu (1996), see Figure 6.

```
> # function (x, main = NULL, color1 = "red", color2 = "blue",
> # color3 = "black", cex.axis = 0.8, las = 1, pch = 20,
> # bty = "l", cex = 0.8, lwd = 1, xlab = "", ylab = "",
> # ...)
> # model : yield ~ virus
> # Important group=FALSE
> x<-HSD.test(model, "virus", group=FALSE)
> diffograph(x,cex.axis=0.9,xlab="Yield",ylab="Yield",cex=0.9)
```

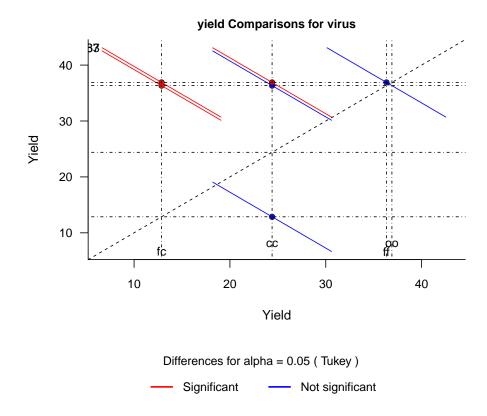


Figure 5: Mean-Mean scatter plot representation of the Tukey method

7 Stability Analysis

In agricolae there are two methods for the study of stability and the AMMI model. These are: a parametric model for a simultaneous selection in yield and stability "SHUKLA'S STABILITY VARIANCE AND KANG'S", Kang (1993) and a non-parametric method of Haynes, based on the data range.

7.1 Parametric Stability

Use the parametric model, function stability.par.

Prepare a data table where the rows and the columns are the genotypes and the environments, respectively. The data should correspond to yield averages or to another measured variable. Determine the variance of the common error for all the environments and the number of repetitions that was evaluated for every genotype. If the repetitions are different, find a harmonious average that will represent the set. Finally, assign a name to each row that will represent the genotype, Kang (1993). We will consider five environments in the following example:

```
> options(digit=2)
> v1 <- c(10.2,8.8,8.8,9.3,9.6,7.2,8.4,9.6,7.9,10,9.3,8.0,10.1,9.4,10.8,6.3,7.4)
> v2 <- c(7,7.8,7.0,6.9,7,8.3,7.4,6.5,6.8,7.9,7.3,6.8,8.1,7.1,7.1,6.4,4.1)
> v3 <- c(5.3,4.4,5.3,4.4,5.5,4.6,6.2,6.0,6.5,5.3,5.7,4.4,4.2,5.6,5.8,3.9,3.8)
> v4 <- c(7.8,5.9,7.3,5.9,7.8,6.3,7.9,7.5,7.6,5.4,5.6,7.8,6.5,8.1,7.5,5.0,5.4)
> v5 <- c(9,9.2,8.8,10.6,8.3,9.3,9.6,8.8,7.9, 9.1,7.7,9.5,9.4,9.4,10.3,8.8,8.7)
```

For 17 genotypes, the identification is made by letters.

```
> study <- data.frame(v1, v2, v3, v4, v5)
> rownames(study) <- LETTERS[1:17]</pre>
```

An error variance of 2 and 4 repetitions is assumed.

Analysis

```
> output <- stability.par(study, rep=4, MSerror=2)
> names(output)

[1] "analysis" "statistics" "stability"
```

> print(output\$stability)

```
Yield Rank Adj.rank Adjusted Stab.var Stab.rating YSi ...
                             15 1.671833
  7.86
                    1
                                                       15
В
  7.22
           5
                    -1
                              4 1.822233
                                                    0
                                                        4
С
   7.44
           9
                     1
                             10 0.233967
                                                    0
                                                        10
D
  7.42
                                                        7
           8
                              9 4.079567
                                                    -2
                     1
Ε
  7.64
          11
                    1
                             12 2.037967
                                                    0
                                                       12
F
   7.14
                                                    -4
           4
                    -1
                              3 5.161967
                                                        -1
G
   7.90
          15
                     1
                             16 1.759300
                                                    0
                                                        16
  7.68
                                                    0
                                                        14
Η
          13
                    1
                             14 1.757167
Ι
  7.34
           7
                              6 5.495300
                                                    -4
                                                         2
                    -1
   7.54
          10
                                                         9
J
                    1
                             11 4.129967
                                                    -2
K
   7.12
           3
                    -1
                              2 3.848900
                                                    0
                                                         2
  7.30
           6
                    -1
                              5 2.675300
                                                    0
                                                        5
Τ.
М
  7.66
          12
                    1
                             13 3.473167
                                                    0
                                                       13
   7.92
                                                    0
                                                       17
N
          16
                    1
                             17 0.806233
0
   8.30
          17
                    2
                             19 1.951300
                                                    0
                                                       19
Ρ
   6.08
                    -2
                              0 3.647833
                                                    0
                                                         0
   5.88
          1
                    -3
                             -2 3.598500
```

The selected genotypes are: A, C, E, G, H, J, M, N and O. These genotypes have a higher yield and a lower variation. to see output\$analysis, the interaction is significant.

If for example there is an environmental index, it can be added as a covariate. For this case, the altitude of the localities is included.

```
> altitude<-c(1200, 1300, 800, 1600, 2400)
> stability <- stability.par(study,rep=4,MSerror=2, cova=TRUE, name.cov= "altitude",
+ file.cov=altitude)</pre>
```

7.2 Non-parametric Stability

For non-parametric stability, the function in 'agricolae' is stability.nonpar(). The names of the genotypes should be included in the first column, and in the other columns, the response by environments, Haynes and Lambert and Christ and Weingartner and Douches and Backlund and Secor and Fry and Stevenson (1998).

Analysis

```
> data <- data.frame(name=row.names(study), study)
> output<-stability.nonpar(data, "YIELD", ranking=TRUE)
> names(output)

[1] "ranking" "statistics"

> output$statistics

MEAN es1 es2 vs1 vs2 chi.ind chi.sum
1 7.378824 5.647059 24 2.566667 148.8 8.843605 27.58711
```

7.3 AMMI

The model AMMI uses the biplot constructed through the principal components generated by the interaction environment-genotype. If there is such interaction, the percentage of the two principal components would explain more than the 50% of the total variation; in such case, the biplot would be a good alternative to study the interaction environment-genotype, Crossa (1990).

The data for AMMI should come from similar experiments conducted in different environments. Homogeneity of variance of the experimental error, produced in the different environments, is required. The analysis is done by combining the experiments.

The data can be organized in columns, thus: environment, genotype, repetition, and variable.

The data can also be the averages of the genotypes in each environment, but it is necessary to consider a harmonious average for the repetitions and a common variance of the error. The data should be organized in columns: environment, genotype, and variable.

When performing AMMI, this generates the Biplot, Triplot and Influence graphics, see Figures?? For the application, we consider the data used in the example of parametric stability (study):

AMMI structure

> str(AMMI)

```
function (ENV, GEN, REP, Y, MSE = 0, console = FALSE,
    PC = FALSE
plot.AMMI structure, plot()
    str(plot.AMMI)
function (x, first = 1, second = 2, third = 3, type = 1,
    number = FALSE, gcol = NULL, ecol = NULL, icol = NULL,
    angle = 25, lwd = 1.8, length = 0.1, xlab = NULL,
    ylab = NULL, xlim = NULL, ylim = NULL, ...)
type: 1=biplot, 2= triplot 3=influence genotype
    rdto <- c(study[,1], study[,2], study[,3], study[,4], study[,5])</pre>
> environment <- gl(5,17)
> genotype <- rep(rownames(study),5)</pre>
> model<-AMMI(ENV=environment, GEN=genotype, REP=4, Y=rdto, MSE=2, console=TRUE)
ANALYSIS AMMI: rdto
Class level information
ENV: 1 2 3 4 5
GEN: A B C D E F G H I J K L M N O P Q
REP: 4
Number of means: 85
Dependent Variable: rdto
Analysis of variance
          Df
                Sum Sq
                          Mean Sq F value
                                                 Pr(>F)
ENV
           4 734.2475 183.561882
REP(ENV)
          15
GEN
          16 120.0875
                        7.505471 3.752735 3.406054e-06
ENV:GEN
         64 181.2725
                         2.832382 1.416191 3.279630e-02
Residuals 240 480.0000
                         2.000000
Coeff var
                  Mean rdto
19.16584
                  7.378824
Analysis
   percent acum Df
                       Sum.Sq Mean.Sq F.value
       38.0 38.0 19 68.96258 3.629609 1.81 0.0225
PC1
PC2
       29.8 67.8 17 54.02864 3.178155
                                       1.59 0.0675
PC3
       22.5 90.4 15 40.84756 2.723170 1.36 0.1680
PC4
       9.6 100.0 13 17.43370 1.341054 0.67 0.7915
> pc <- model$analysis[, 1]</pre>
> pc12<-sum(pc[1:2])
> pc123<-sum(pc[1:3])
> rm(rdto,environment,genotype)
```

```
> par(cex=0.8,mar=c(4,4,1,0))
> plot(model,type=1,las=1)
```

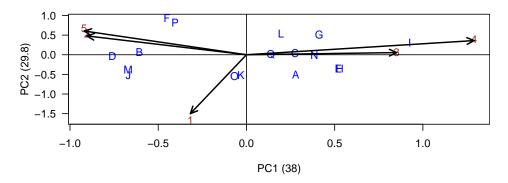


Figure 6: Biplot

In this case, the interaction is significant. The first two components explain 67.8 %; then the biplot can provide information about the interaction genotype-environment. With the triplot, 90.3% would be explained.

To triplot require klaR package. in R execute:

plot(model,type=2,las=1)

To Influence graphics genotype require spdep package, in R execute:

plot(model,type=3,las=1)

7.4 AMMI index and yield stability

Calculate AMMI stability value (ASV) and Yield stability index (YSI), ?; Purchase (1997).

```
> data(plrv)
> attach(plrv)
> model<- AMMI(Locality, Genotype, Rep, Yield, console=FALSE)
> detach(plrv)
> index<-index.AMMI(model)
> # Crops with improved stability according AMMI.
```

> # Crops with improved stability according A

> print(index[order(index[,3]),])

	ASV	YSI	rASV	rYSI	means
402.7	0.2026430	20	1	19	27.47748
506.2	0.5646275	13	2	11	33.26623
364.21	0.5966506	13	3	10	34.05974
427.7	0.9507170	11	4	7	36.19020
233.11	1.0521529	22	5	17	28.66655
241.2	1.1739456	28	6	22	26.34039
221.19	1.2740344	33	7	26	22.98480
104.22	1.3792025	21	8	13	31.28887
317.6	1.5167528	18	9	9	35.32583
121.31	1.7912464	25	10	15	30.10174

```
314.12 2.0368354 29 11 18 28.17335
342.15 2.0954103 36 12 24 26.01336
Canchan 2.1652861 33 13 20 27.00126
406.12 2.1722949 26 14 12 32.68323
351.26 2.3436592 23 15 8 36.11581
320.16 2.3623790 37 16 21 26.34808
450.3 2.3663500 23 17 6 36.19602
255.7 2.4615460 32 18 14 30.58975
102.18 2.5131813 42 19 23 26.31947
405.2 2.7709324 36 20 16 28.98663
157.26 2.8907699 26 21 5 36.95181
163.9 3.0764673 49 22 27 21.41747
141.28 3.1531170 24 23 1 39.75624
235.6 3.3065468 28 24 4 38.63477
Unica 3.3470545 27 25 2 39.10400
346.2 3.6050812 51 26 25 23.84175
319.20 4.8741897 30 27 3 38.75767
Desiree 5.5374138 56 28 28 16.15569
```

> # Crops with better response and improved stability according AMMI.
> print(index[order(index[,4]),])

	ASV	YSI	rASV	rYSI	means
141.28	3.1531170	24	23	1	39.75624
Unica	3.3470545	27	25	2	39.10400
319.20	4.8741897	30	27	3	38.75767
235.6	3.3065468	28	24	4	38.63477
157.26	2.8907699	26	21	5	36.95181
450.3	2.3663500	23	17	6	36.19602
427.7	0.9507170	11	4	7	36.19020
351.26	2.3436592	23	15	8	36.11581
317.6	1.5167528	18	9	9	35.32583
364.21	0.5966506	13	3	10	34.05974
506.2	0.5646275	13	2	11	33.26623
406.12	2.1722949	26	14	12	32.68323
104.22	1.3792025	21	8	13	31.28887
255.7	2.4615460	32	18	14	30.58975
121.31	1.7912464	25	10	15	30.10174
405.2	2.7709324	36	20	16	28.98663
233.11	1.0521529	22	5	17	28.66655
314.12	2.0368354	29	11	18	28.17335
402.7	0.2026430	20	1	19	27.47748
Canchan	2.1652861	33	13	20	27.00126
320.16	2.3623790	37	16	21	26.34808
241.2	1.1739456	28	6	22	26.34039
102.18	2.5131813	42	19	23	26.31947
342.15	2.0954103	36	12	24	26.01336
346.2	3.6050812	51	26	25	23.84175
221.19	1.2740344	33	7	26	22.98480
163.9	3.0764673	49	22	27	21.41747
Desiree	5.5374138	56	28	28	16.15569

8 Special functions

8.1 Consensus of dendrogram

Consensus is the degree or similarity of the vertexes of a tree regarding its branches of the constructed dendrogram. The function to apply is consensus().

The data correspond to a table, with the name of the individuals and the variables in the rows and columns respectively. For the demonstration, we will use the "pamCIP" data of 'agricolae', which correspond to molecular markers of 43 entries of a germplasm bank (rows) and 107 markers (columns).

The program identifies duplicates in the rows and can operate in both cases. The result is a dendrogram, in which the consensus percentage is included, see Figure 7.

```
> par(cex=0.6,mar=c(3,3,2,0))
> data(pamCIP)
> rownames(pamCIP)<-substr(rownames(pamCIP),1,6)
> output<-consensus(pamCIP,distance="binary", method="complete", nboot=5)</pre>
```

Duplicates: 18

New data : 25 Records

Consensus hclust

Method distance: binary Method cluster : complete rows and cols : 25 107

n-bootstrap : 5

Run time : 1.903203 secs

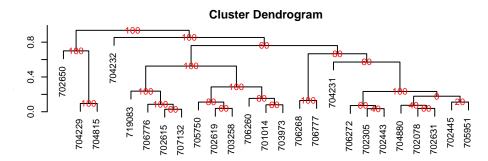


Figure 7: Dendrogram, production by consensus

When the dendrogram is complex, it is convenient to extract part of it with the function hcut(), see Figure 8.

The obtained object "output" contains information about the process:

> names(output)

[1] "table.dend" "dendrogram" "duplicates"

```
> par(cex=0.6,mar=c(3,3,1.5,0))
> out1<- hcut(output,h=0.4,group=8,type="t",edgePar = list(lty=1:2, col=colors()[c(42,84)]),
+ main="group 8" ,col.text="blue",cex.text=1,las=1)</pre>
```

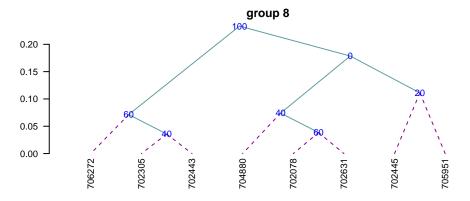


Figure 8: Dendrogram, production by hcut()

Construct a classic dendrogram, execute procedure in R

use the previous result 'output'

```
> dend <- as.dendrogram(output$dendrogram)</pre>
```

> data <- output\$table.dend

> head(output\$table.dend)

```
X2 xaxis
                     height percentage groups
   -6 -24 7.50 0.02857143
                                          6-24
1
                                     60
       -4 19.50 0.03571429
                                     40
                                           3 - 4
       -8 22.50 0.03846154
                                     60
                                           2-8
  -7 -10 10.50 0.03846154
                                     60
                                          7-10
 -21
        2 18.75 0.07142857
                                     60 3-4-21
        3 21.75 0.07407407
6 -16
                                    40 2-8-16
```

```
> par(mar=c(3,3,1,1),cex=0.6)
```

- > plot(dend, type="r", edgePar = list(lty=1:2, col=colors()[c(42,84)]) ,las=1)
- > text(data[,3],data[,4],data[,5],col="blue",cex=1)

8.2 Montecarlo

It is a method for generating random numbers of an unknown distribution. It uses a data set and, through the cumulative behavior of its relative frequency, generates the possible random values that follow the data distribution. These new numbers are used in some simulation process.

The probability density of the original and simulated data can be compared, see Figure 9.

```
> data(soil)
```

- > # set.seed(9473)
- > simulated <- montecarlo(soil\$pH,1000)
- > h<-graph.freq(simulated,nclass=7,plot=FALSE)</pre>

- > par(mar=c(2,0,2,1),cex=0.6)
- > plot(density(soil\$pH),axes=F,main="pH density of the soil\ncon Ralstonia",xlab="",lwd=4)
- > lines(density(simulated), col="blue", lty=4,lwd=4)
- > axis(1,0:12)
- > legend("topright",c("Original","Simulated"),lty=c(1,4),col=c("black", "blue"), lwd=4)

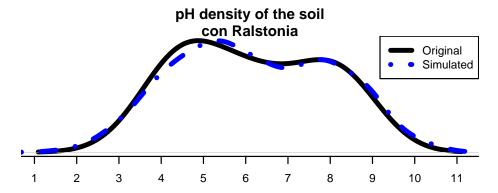


Figure 9: Distribution of the simulated and the original data

1000 data was simulated, being the frequency table:

> round(table.freq(h),2)

	Lower	Upper	Main	Frequency	Percentage	CF	CPF
1	1.50	2.81	2.16	20	2.0	20	2.0
2	2.81	4.12	3.47	120	12.0	140	14.0
3	4.12	5.43	4.78	238	23.8	378	37.8
4	5.43	6.74	6.09	225	22.5	603	60.3
5	6.74	8.05	7.40	198	19.8	801	80.1
6	8.05	9.36	8.70	168	16.8	969	96.9
7	9.36	10.67	10.02	31	3.1	1000	100.0

Some statistics, original data:

> summary(soil\$pH)

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 3.800 4.700 6.100 6.154 7.600 8.400
```

Some statistics, montecarlo simulate data:

> summary(simulated)

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 1.600 4.776 6.090 6.218 7.737 10.659
```

8.3 Re-Sampling in linear model

It uses the permutation method for the calculation of the probabilities of the sources of variation of ANOVA according to the linear regression model or the design used. The principle is that the Y

response does not depend on the averages proposed in the model; hence, the Y values can be permutated and many model estimates can be constructed. On the basis of the patterns of the random variables of the elements under study, the probability is calculated in order to measure the significance.

For a variance analysis, the data should be prepared similarly. The function to use is: resampling.model()

```
> data(potato)
> potato[,1]<-as.factor(potato[,1])</pre>
> potato[,2]<-as.factor(potato[,2])</pre>
> model<-"cutting~variety + date + variety:date"</pre>
> analysis<-resampling.model(model, potato, k=100)</pre>
> Xsol<-as.matrix(round(analysis$solution,2))</pre>
> print(Xsol,na.print = "")
             Df Sum Sq Mean Sq F value Pr(>F) Resampling
              1 25.09
                          25.09
                                   7.26 0.02
                                                      0.01
variety
                                                      0.16
              2 13.89
                                   2.01
                                           0.18
date
                           6.95
variety:date 2 4.85
                           2.43
                                   0.70 0.51
                                                      0.61
Residuals
             12 41.48
                           3.46
```

The function resampling.model() can be used when the errors have a different distribution from normal

8.4 Simulation in linear model

Under the assumption of normality, the function generates pseudo experimental errors under the proposed model, and determines the proportion of valid results according to the analysis of variance found.

The function is: simulation.model(). The data are prepared in a table, similarly to an analysis of variance.

Considering the example proposed in the previous procedure:

```
> simModel <- simulation.model(model, potato, k=100,console=TRUE)
Simulation of experiments
Under the normality assumption
_ _ _ _ _ _ _ _ _ _ _ _ _ _ _ _ _ _
Proposed model: cutting variety + date + variety:date
Analysis of Variance Table
Response: cutting
             Df Sum Sq Mean Sq F value Pr(>F)
              1 25.087 25.0868 7.2580 0.01952 *
variety
date
              2 13.892 6.9459 2.0096 0.17671
variety:date 2 4.853 2.4265 0.7020 0.51484
Residuals
            12 41.477 3.4564
Signif. codes:
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Validation of the analysis of variancia for the proposed model Simulations: 100

	Df F value %	Acceptance %	Rejection
variety	1 7.2580377	49	51
date	2 2.0095604	60	40
variety:date	2 0.7020312	61	39
	Criterion		
variety	nonacceptable		
date	acceptable		
variety:date	acceptable		

The validation is referred to the percentage of decision results equal to the result of the ANOVA decision. Thus, 61% of the results simulated on the interaction variety*date gave the same result of acceptance or rejection obtained in the ANOVA.

8.5 Path Analysis

[1] 0.4266667

It corresponds to the "path analysis" method. The data correspond to correlation matrices of the independent ones with the dependent matrix (XY) and between the independent ones (XX).

It is necessary to assign names to the rows and columns in order to identify the direct and indirect effects.

```
> corr.x <- matrix(c(1,0.5,0.5,1),c(2,2))
> corr.y<- rbind(0.6,0.7)
> names<-c("X1","X2")
> dimnames(corr.x)<-list(names,names)</pre>
> dimnames(corr.y)<-list(names,"Y")</pre>
> output<-path.analysis(corr.x,corr.y)</pre>
Direct(Diagonal) and indirect effect path coefficients
X1 0.3333333 0.2666667
X2 0.1666667 0.5333333
Residual Effect<sup>2</sup> = 0.4266667
> output
$Coeff
         X1
                   X2
X1 0.3333333 0.2666667
X2 0.1666667 0.5333333
$Residual
```

8.6 Line X Tester

It corresponds to a crossbreeding analysis of a genetic design. The data should be organized in a table. Only four columns are required: repetition, females, males, and response. In case it corresponds to progenitors, the females or males field will only be filled with the corresponding one. See the heterosis data, Singh and Chaudhary (1979).

Example with the heterosis data, locality 2.

```
Replication
                   Female
                            Male
109
               1
                     LT-8 TS-15 2.65
110
               1
                     LT-8 TPS-13 2.26
               1 Achirana TPS-13 3.55
131
               1 Achirana TPS-67 3.05
132
140
               1 Achirana
                             <NA> 3.35
. . .
               3
                     <NA> TPS-67 2.91
215
```

where $\langle NA \rangle$ is empty.

If it is a progeny, it comes from a "Female" and a "Male." If it is a progenitor, it will only be "Female" or "Male."

The following example corresponds to data of the locality 2:

24 progenies 8 females 3 males 3 repetitions

ANALYSIS LINE x TESTER: v2

They are 35 treatments (24, 8, 3) applied to three blocks.

```
> rm(list=ls())
> options(digits = 2)
> data(heterosis)
> str(heterosis)
'data.frame':
                     324 obs. of 11 variables:
 $ Place
              : num
                     1 1 1 1 1 1 1 1 1 1 ...
 $ Replication: num
                     1 1 1 1 1 1 1 1 1 1 . . .
 $ Treatment : num 1 2 3 4 5 6 7 8 9 10 ...
              : Factor w/ 3 levels "Control", "progenie", ...: 2 2 2 2 2 2 2 2 2 2 ...
 $ Factor
              : Factor w/ 8 levels "Achirana", "LT-8",...: 2 2 2 6 6 6 7 7 7 8 ...
 $ Female
              : Factor w/ 3 levels "TPS-13", "TPS-67", \ldots 3 1 2 3 1 2 3 1 2 3 \ldots
 $ Male
 $ v1
              : num 0.948 1.052 1.05 1.058 1.123 ...
              : num 1.65 2.2 1.88 2 2.45 2.63 2.75 3 2.51 1.93 ...
 $ v2
 $ v3
              : num 17.2 17.8 15.6 16 16.5 ...
 $ v4
              : num
                     9.93 12.45 9.3 12.77 14.13 ...
              : num 102.6 107.4 120.5 83.8 90.4 ...
 $ v5
> site2<-subset(heterosis,heterosis[,1]==2)</pre>
> site2<-subset(site2[,c(2,5,6,8)],site2[,4]!="Control")</pre>
> output1<-with(site2,lineXtester(Replication, Female, Male, v2))
```

ANOVA with parents and crosses

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Replications	2	0.5192	0.2596	9.80	0.0002
Treatments	34	16.1016	0.4736	17.88	0.0000
Parents	10	7.7315	0.7731	29.19	0.0000
Parents vs. Crosses	1	0.0051	0.0051	0.19	0.6626
Crosses	23	8.3650	0.3637	13.73	0.0000
Error	68	1.8011	0.0265		
T-+-1	101	10 /010			

Total 104 18.4219

ANOVA for line X tester analysis

	Df	Sum Sq	Mean Sq F	value	Pr(>F)
Lines	7	4.98	0.711	3.6	0.019
Testers	2	0.65	0.325	1.7	0.226
Lines X Testers	14	2.74	0.196	7.4	0.000
Error	68	1.80	0.026		

ANOVA for line X tester analysis including parents

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Replications	2	0.5192	0.2596	9.80	0.0002
Treatments	34	16.1016	0.4736	17.88	0.0000
Parents	10	7.7315	0.7731	29.19	0.0000
Parents vs. Crosses	1	0.0051	0.0051	0.19	0.6626
Crosses	23	8.3650	0.3637	13.73	0.0000
Lines	7	4.9755	0.7108	3.63	0.0191
Testers	2	0.6494	0.3247	1.66	0.2256
Lines X Testers	14	2.7401	0.1957	7.39	0.0000
Error	68	1.8011	0.0265		
Total	104	18.4219			

GCA Effects:

=========

Lines Effects:

Achirana	LT-8	MF-I	MF-II	Serrana	TPS-2
0.022	-0.338	0.199	-0.449	0.058	-0.047
TPS-25	TPS-7				
0.414	0.141				

Testers Effects:

TPS-13 TPS-67 TS-15 0.087 0.046 -0.132

SCA Effects:

========

Testers

Lines TPS-13 TPS-67 TS-15 Achirana 0.061 0.059 -0.120 LT-8 -0.435 0.519 -0.083

```
MF-I -0.122 -0.065 0.187
MF-II -0.194 0.047 0.148
Serrana 0.032 -0.113 0.081
TPS-2 0.197 -0.072 -0.124
TPS-25 0.126 -0.200 0.074
TPS-7 0.336 -0.173 -0.162
```

Standard Errors for Combining Ability Effects:

```
S.E. (gca for line) : 0.054

S.E. (gca for tester) : 0.033

S.E. (sca effect) : 0.094

S.E. (gi - gj)line : 0.077

S.E. (gi - gj)tester : 0.047

S.E. (sij - skl)tester: 0.13
```

Genetic Components:

```
Cov H.S. (line) : 0.057
Cov H.S. (tester) : 0.0054
Cov H.S. (average): 0.0039
Cov F.S. (average): 0.13
```

F = 0, Adittive genetic variance: 0.015 F = 1, Adittive genetic variance: 0.0077 F = 0, Variance due to Dominance: 0.11 F = 1, Variance due to Dominance: 0.056

Proportional contribution of lines, testers and their interactions to total variance

Contributions of lines : 59 Contributions of testers: 7.8 Contributions of lxt : 33

> options(digits = 7)

8.7 Soil Uniformity

The Smith index is an indicator of the uniformity, used to determine the parcel size for research purposes. The data correspond to a matrix or table that contains the response per basic unit, a number of n rows x m columns, and a total of n*m basic units.

For the test, we will use the rice file. The graphic is a result with the adjustment of a model for the plot size and the coefficient of variation, see Figure 10.

```
> par(mar=c(3,3,4,0),cex=0.7)
```

- > data(rice)
- > table<-index.smith(rice, col="blue",
- + main="Interaction between the CV and the plot size",type="1",xlab="Size")

Interaction between the CV and the plot size

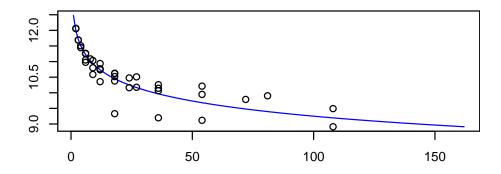


Figure 10: Adjustment curve for the optimal size of plot

3	2	2	1	324 7831.232 12.1
4	3	1	3	216 7347.975 11.7
5	3	3	1	216 7355.216 11.7
6	4	1	4	162 7047.717 11.4

8.8 Confidence Limits In Biodiversity Indices

The biodiversity indices are widely used for measuring the presence of living things in an ecological area. Many programs indicate their value. The function of 'agricolae' is also to show the confidence intervals, which can be used for a statistical comparison. Use the bootstrap procedure. The data are organized in a table; the species are placed in a column; and in another one, the number of individuals. The indices that can be calculated with the function index.bio() of 'agricolae' are: "Margalef", "Simpson.Dom", "Simpson.Div", "Berger.Parker", "McIntosh", and "Shannon."

In the example below, we will use the data obtained in the locality of Paracsho, district of Huasahuasi, province of Tarma in the department of Junin.

The evaluation was carried out in the parcels on 17 November 2005, without insecticide application. The counted specimens were the following:

```
> data(paracsho)
> species <- paracsho[79:87,4:6]
> species
```

	Orden	Family	Number.of.specimens
79	DIPTERA	TIPULIDAE	3
80	LEPIDOPTERA	NOCTUIDAE	1
81	NOCTUIDAE	PYRALIDAE	3

82	HEMIPTERA	ANTHOCORIDAE	1
83	DIPTERA	TACHINIDAE	16
84	DIPTERA	ANTHOCORIDAE	3
85	DIPTERA	SCATOPHAGIDAE	5
86	DIPTERA	SYRPHIDAE	1
87	DIPTERA	MUSCIDAE	3

The Shannon index is:

```
> output <- index.bio(species[,3],method="Shannon",level=95,nboot=200)
Method: Shannon
The index: 3.52304
95 percent confidence interval:
3.180131; 4.260501</pre>
```

8.9 Correlation

The function correlation() of 'agricolae' makes the correlations through the methods of Pearson, Spearman and Kendall for vectors and/or matrices. If they are two vectors, the test is carried out for one or two lines; if it is a matrix one, it determines the probabilities for a difference, whether it is greater or smaller.

For its application, consider the soil data: data(soil)

```
> data(soil)
> correlation(soil[,2:4],method="pearson")
$correlation
       pH EC CaCO3
      1.00 0.55 0.73
рΗ
EC
      0.55 1.00 0.32
CaCO3 0.73 0.32 1.00
$pvalue
                         EC
                                  CaCO3
               рΗ
      1.000000000 0.0525330 0.004797027
рΗ
      0.052532997 1.0000000 0.294159813
CaCO3 0.004797027 0.2941598 1.000000000
$n.obs
[1] 13
> attach(soil)
> correlation(pH,soil[,3:4],method="pearson")
$correlation
     EC CaCO3
```

```
pH 0.55 0.73
$pvalue
       EC CaCO3
pH 0.0525 0.0048
$n.obs
[1] 13
> correlation(pH,CaCO3,method="pearson")
Pearson's product-moment correlation
data: pH and CaCO3
t = 3.520169 , df = 11 , p-value = 0.004797027
alternative hypothesis: true rho is not equal to 0
sample estimates:
cor
 0.7278362
> detach(soil)
8.10
       tapply.stat()
Gets a functional calculation of variables grouped by study factors.
Application with 'agricolae' data:
max(yield)-min(yield) by farmer
> data(RioChillon)
> attach(RioChillon$babies)
> tapply.stat(yield,farmer,function(x) max(x)-min(x))
            farmer yield
1
  AugustoZambrano
                    7.5
2
         Caballero 13.4
3
        ChocasAlto 14.1
4
        FelixAndia 19.4
5
       Huarangal-1
                    9.8
6
       Huarangal-2
7
       Huarangal-3
                     9.4
          Huatocay 19.4
9 IgnacioPolinario 13.1
> detach(RioChillon$babies)
```

It corresponds to the range of variation in the farmers' yield.

The function "tapply" can be used directly or with function.

If A is a table with columns 1,2 and 3 as category, and 5,6 and 7 as variables, then the following procedures are valid:

```
tapply.stat(A[,5:7], A[,1:3],mean)
tapply.stat(A[,5:7], A[,1:3],function(x) mean(x,na.rm=TRUE))
tapply.stat(A[,c(7,6)], A[,1:2],function(x) sd(x)*100/mean(x))
```

8.11 Coefficient of variation of an experiment

If "model" is the object resulting from an analysis of variance of the function aov() or lm() of R, then the function cv.model() calculates the coefficient of variation.

```
> data(sweetpotato)
> model <- model<-aov(yield ~ virus, data=sweetpotato)
> cv.model(model)

[1] 17.1666
```

8.12 Skewness and kurtosis

The skewness and kurtosis results, obtained by 'agricolae', are equal to the ones obtained by SAS, MiniTab, SPSS, InfoStat, and Excel.

If x represents a data set:

```
> x<-c(3,4,5,2,3,4,5,6,4,NA,7)
skewness is calculated with:
> skewness(x)
```

and kurtosis with:

> kurtosis(x)
[1] -0.1517996

[1] 0.3595431

8.13 Tabular value of Waller-Duncan

The function Waller determines the tabular value of Waller-Duncan. For the calculation, value F is necessary, calculated from the analysis of variance of the study factor, with its freedom degrees and the estimate of the variance of the experimental error. Value K, parameter of the function is the ratio between the two types of errors (I and II). To use it, a value associated with the alpha level is assigned. When the alpha level is 0.10, 50 is assigned to K; for 0.05, K=100; and for 0.01, K=500. K can take any value.

```
> q<-5
> f<-15
> K<-seq(10,1000,100)</pre>
```

```
> n<-length(K)
> y<-rep(0,3*n)
> dim(y)<-c(n,3)
> for(i in 1:n) y[i,1]<-waller(K[i],q,f,Fc=2)
> for(i in 1:n) y[i,2]<-waller(K[i],q,f,Fc=4)
> for(i in 1:n) y[i,3]<-waller(K[i],q,f,Fc=8)</pre>
```

Function of Waller to different value of parameters K and Fc The next procedure illustrates the function for different values of K with freedom degrees of 5 for the numerator and 15 for the denominator, and values of calculated F, equal to 2, 4, and 8.

```
> par(mar=c(3,3,4,0),cex=0.7)
> plot(K,y[,1],type="l",col="blue",ylab="waller",bty="l")
> lines(K,y[,2],type="l",col="brown",lty=2,lwd=2)
> lines(K,y[,3],type="l",col="green",lty=4,lwd=2)
> legend("topleft",c("2","4","8"),col=c("blue","brown","green"),lty=c(1,8,20),
+ lwd=2,title="Fc")
> title(main="Waller in function of K")
```

Generating table Waller-Duncan

> K<-100 > Fc<-1.2

```
> q<-c(seq(6,20,1),30,40,100)
> f < -c(seq(4,20,2),24,30)
> n<-length(q)
> m<-length(f)
> W.D < -rep(0,n*m)
> dim(W.D) < -c(n,m)
> for (i in 1:n) {
+ for (j in 1:m) {
+ W.D[i,j] <- waller(K, q[i], f[j], Fc)
+ }}
> W.D<-round(W.D,2)
> dimnames(W.D)<-list(q,f)</pre>
> cat("table: Waller Duncan k=100, F=1.2")
table: Waller Duncan k=100, F=1.2
> print(W.D)
                8
                    10
                         12
                                            20
                             14
                                  16
                                       18
   2.85 2.89 2.92 2.93 2.94 2.94 2.94 2.94 2.94 2.94 2.94
   2.85 2.91 2.94 2.96 2.97 2.98 2.99 2.99 2.99 3.00 3.00
   2.85 2.92 2.96 2.99 3.01 3.02 3.03 3.03 3.04 3.04 3.05
10 2.85 2.93 2.98 3.01 3.04 3.05 3.06 3.07 3.08 3.09 3.10
11 2.85 2.94 3.00 3.04 3.06 3.08 3.09 3.10 3.11 3.12 3.14
12 2.85 2.95 3.01 3.05 3.08 3.10 3.12 3.13 3.14 3.16 3.17
13 2.85 2.96 3.02 3.07 3.10 3.12 3.14 3.16 3.17 3.19 3.20
14 2.85 2.96 3.03 3.08 3.12 3.14 3.16 3.18 3.19 3.21 3.23
```

8.14 AUDPC

The area under the disease progress curve (AUDPC), see Figure 10 calculates the absolute and relative progress of the disease. It is required to measure the disease in percentage terms during several dates, preferably equidistantly.

```
> days<-c(7,14,21,28,35,42)
> evaluation<-data.frame(E1=10,E2=40,E3=50,E4=70,E5=80,E6=90)
> print(evaluation)

E1 E2 E3 E4 E5 E6
1 10 40 50 70 80 90
> absolute1 <-audpc(evaluation,days)
> relative1 <-round(audpc(evaluation,days,"relative"),2)</pre>
```

8.15 **AUDPS**

The Area Under the Disease Progress Stairs (AUDPS), see Figure 11. A better estimate of disease progress is the area under the disease progress stairs (AUDPS). The AUDPS approach improves the estimation of disease progress by giving a weight closer to optimal to the first and last observations...

```
> absolute2 <-audps(evaluation,days)
> relative2 <-round(audps(evaluation,days,"relative"),2)</pre>
```

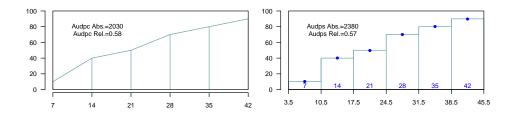


Figure 11: Area under the curve (AUDPC) and Area under the Stairs (AUDPS)

8.16 Non-Additivity

Tukey's test for non-additivity is used when there are doubts about the additivity veracity of a model. This test confirms such assumption and it is expected to accept the null hypothesis of the non-additive effect of the model.

For this test, all the experimental data used in the estimation of the linear additive model are required.

Use the function nonadditivity() of 'agricolae'. For its demonstration, the experimental data "potato", of the package 'agricolae', will be used. In this case, the model corresponds to the randomized complete block design, where the treatments are the varieties.

```
> data(potato)
> potato[,1]<-as.factor(potato[,1])</pre>
> model <-lm(cutting ~ date + variety, potato)
> df<-df.residual(model)</pre>
> MSerror<-deviance(model)/df
> attach(potato)
> analysis<-nonadditivity(cutting, date, variety, df, MSerror)
Tukey's test of nonadditivity
cutting
P: 15.37166
0:77.44441
Analysis of Variance Table
Response: residual
              Df Sum Sq Mean Sq F value Pr(>F)
Nonadditivity 1 3.051 3.0511
                                   0.922 0.3532
Residuals
              14 46.330 3.3093
> detach(potato)
```

According to the results, the model is additive because the p.value 0.35 is greater than 0.05.

8.17 LATEBLIGHT

LATEBLIGHT is a mathematical model that simulates the effect of weather, host growth and resistance, and fungicide use on asexual development and growth of Phytophthora infestans on potato foliage, see Figure 12

LATEBLIGHT Version LB2004 was created in October 2004 (Andrade-Piedra et al., 2005a, b and c), based on the C-version written by B.E. Ticknor ('BET 21191 modification of cbm8d29.c'), reported by Doster et al. (1990) and described in detail by Fry et al. (1991) (This version is referred as LB1990 by Andrade-Piedra et al. [2005a]). The first version of LATEBLIGHT was developed by Bruhn and Fry (1981) and described in detail by Bruhn et al. (1980).

```
> f <- system.file("external/weather.csv", package="agricolae")
> weather <- read.csv(f,header=FALSE)
> f <- system.file("external/severity.csv", package="agricolae")</pre>
```

```
> severity <- read.csv(f)
> weather[,1]<-as.Date(weather[,1],format = \frac{m}{d}\frac{y}{d}
> # Parameters dates
> dates<-c("2000-03-25","2000-04-09","2000-04-12","2000-04-16","2000-04-22")
> dates<-as.Date(dates)</pre>
> EmergDate <- as.Date("2000/01/19")</pre>
> EndEpidDate <- as.Date("2000-04-22")</pre>
> dates<-as.Date(dates)</pre>
> NoReadingsH<- 1
> RHthreshold <- 90
> WS<-weatherSeverity(weather, severity, dates, EmergDate, EndEpidDate,
+ NoReadingsH, RHthreshold)
> # Parameters to Lateblight function
> InocDate<-"2000-03-18"
> LGR <- 0.00410
> IniSpor <- 0
> SR <- 292000000
> IE <- 1.0
> LP <- 2.82
> InMicCol <- 9
> Cultivar <- "NICOLA"
> ApplSys <- "NOFUNGICIDE"
> main<-"Cultivar: NICOLA"
> par(mar=c(3,3,4,0),cex=0.7)
> model<-lateblight(WS, Cultivar, ApplSys, InocDate, LGR, IniSpor, SR, IE,
+ LP, MatTime='LATESEASON', InMicCol, main=main, type="1", xlim=c(65,95), lwd=1.5,
+ xlab="Time (days after emergence)", ylab="Severity (Percentage)")
```

Cultivar: NICOLA

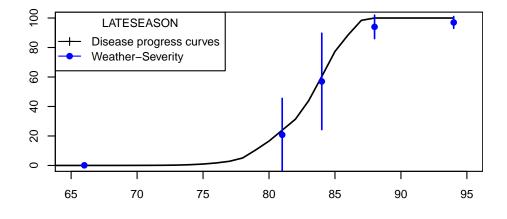


Figure 12: lateblight: LATESEASON

> head(model\$Gfile)

```
dates nday MeanSeverity StDevSeverity MinObs
Eval1 2000-03-25 66
                         0.1
                                 0.000000 0.100000
Eval2 2000-04-09 81
                          20.8
                                  24.722459 -3.922459
Eval3 2000-04-12 84
                         57.0
                                  32.710854 24.289146
Eval4 2000-04-16 88
                         94.0
                                 7.968689 86.031311
                                  4.000000 93.000000
Eval5 2000-04-22 94
                         97.0
       MaxObs
     0.10000
Eval1
Eval2 45.52246
Eval3 89.71085
Eval4 101.96869
Eval5 101.00000
```

> str(model\$Ofile)

```
94 obs. of 13 variables:
'data.frame':
$ Date
          : Date, format: "2000-01-20" ...
$ nday
          : num 1 2 3 4 5 6 7 8 9 10 ...
          : num 0000000000...
$ MicCol
$ SimSeverity: num 0 0 0 0 0 0 0 0 0 ...
       : num 0.01 0.0276 0.0384 0.0492 0.06 0.086 0.112 0.138 0.164 0.19 ...
$ LAI
$ LatPer
          : num 0 2 2 2 2 2 2 2 2 2 ...
$ LesExInc : num
                 0 0 0 0 0 0 0 0 0 0 ...
$ AttchSp : num 0 0 0 0 0 0 0 0 0 ...
$ AUDPC
           : num 0000000000...
$ rLP
           : num 0000000000...
           : num 0000000000...
$ InvrLP
$ BlPr
          : num 0000000000...
           : num 0000000000...
$ Defol
```

> head(model\$Ofile[,1:7])

	Date	ndav	MicCol	SimSeverity	LAI	LatPer	LesExInc
1	2000-01-20	1	0	3	0.0100	0	0
	2000-01-21	2	0		0.0276	2	0
	2000-01-22	3	0		0.0384	2	0
	2000-01-23	4	0		0.0492	2	0
	2000-01-24	5	0		0.0600	2	0
	2000-01-25	6	0		0.0860	2	0

Repeating graphic

```
> x<- model$Ofile$nday
```

> y<- model\$Ofile\$SimSeverity</pre>

> w<- model\$Gfile\$nday

> z<- model\$Gfile\$MeanSeverity

> Min<-model\$Gfile\$MinObs

> Max<-model\$Gfile\$MaxObs

```
> par(mar=c(3,2.5,1,0),cex=0.7)
> plot(x,y,type="l",xlim=c(65,95),lwd=1.5,xlab="Time (days after emergence)",
+ ylab="Severity (Percentage)")
> points(w,z,col="red",cex=1,pch=19); npoints <- length(w)
> for ( i in 1:npoints)segments(w[i],Min[i],w[i],Max[i],lwd=1.5,col="red")
> legend("topleft",c("Disease progress curves","Weather-Severity"),
+ title="Description",lty=1,pch=c(3,19),col=c("black","red"))
```

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