

GEMPAK Grid Diagnostic Functions

APPENDIX B1

GRID DIAGNOSTIC FUNCTIONS

The following describes the computation of GEMPAK grid diagnostic functions.

Each grid in a grid file is identified by a parameter name, time, level, and vertical coordinate. A scalar grid is a single grid, while a vector grid is composed of two grids containing the u and v components.

The parameter name is used to retrieve a grid from the file, with a few exceptions: Certain special parameters will be computed from other data in the grid file if the parameter name itself is not found in the grid file. These special scalar parameters are

TMPK	DWPK	TVRK	MIXR*	THTA*	DRCT	TMWK*
TMPC	DWPC	TVRC	SMXR	STHA	SPED	TMWC
TMPF	DWPF	TVRF	MIXS	THTE*	RELH	TMWF
		THES*	SMXS	STHE		

where * indicates names which also may be used as operators. Mixing ratio will be computed automatically from dewpoint temperature, specific humidity or vapor pressure, if a pressure grid exists.

The stability indices will be computed automatically from temperature, dewpoint temperature, and wind speed and direction. These special scalar parameters are

CTOT	VTOT	TOTL	KINX	SWET
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Haines Indices for fire weather detection will be computed automatically from temperature and dewpoint at three different levels. These scalar parameters are:

LHAN	Low elevation Haines Index
MHAN	Middle elevation Haines Index
HHAN	High elevation Haines Index

The Heat Index, HEAT, will also be automatically computed from the temperature and relative humidity.

In addition, precipitation will be converted from inches (I) to millimeters (M) and vice versa, if the grids are named P__M or P__I. The middle numeric characters give the time interval over which the precipitation accumulated. For example, P24M is a 24-hour precipitation total.

The units for sea surface temperature (SST_), maximum temperature (TMX_) and minimum temperature (TMN_) will be converted automatically. The underscore may

GEMPAK Grid Diagnostic Functions

be K, C or F.

These special scalar parameter names denote constant value grids:

DTR	Conversion factor for degrees to radians = $\text{PI} / 180$
E	Base of natural logarithms = 2.71828182
GRAVTY	Gravitational constant = 9.80616 (note spelling)
KAPPA	Gas constant/specific heat = 2/7
PI	= 3.14159265
RTD	Conversion factor for radians to degrees = $180 / \text{PI}$
nnn	Any number (i.e., 2, -10.2, ...)

Another class of special parameter names provides information at grid points depending on the navigation of the grid file:

CORL	Coriolis force = $2. * \text{OMEGA} * \text{SIN} (\text{LATR})$
LATR	Latitude in radians
LONR	Longitude in radians
XVAL	Value of the x coordinate in graph coordinates
YVAL	Value of the y coordinate in graph coordinates
MSFX	Map scale factor in the x direction
MSFY	Map scale factor in the y direction
LAND	Land array; land=1, sea=RMISSD
SEA	Sea array; sea=1, land=RMISSD

Finally, scalar grids may be identified by their location within the grid file. The grid number must be prefixed with the symbol #. Note that grids may be renumbered as grids are added to or deleted from the file.

Vector grids are two separate grids containing the u and v components. Special vector parameter names may be used to identify the following vectors:

WND	Total wind
GEO*	Geostrophic wind
AGE*	Ageostrophic wind
ISAL*	Isallobaric wind
THRM*	Thermal wind

where * indicates names that also may be used as operators. Note that all of these wind vectors will have u and v components in meters per second. The total wind must be stored as UWND and VWND in the grid file if the components are north relative and as UREL and VREL if the components are grid relative.

Time, level, and vertical coordinate may be specified in GDATTIM, GLEVEL and GVCORD. However, any of these values may be overridden by in line parameters appended to an operand in the form of ^time@level%ivcord. In-line parameters are only allowed for operands, since they modify parameters for individual grids. The in-

GEMPAK Grid Diagnostic Functions

line parameters may be entered individually or in combinations in any order.

If more than one file is opened, +n may also be used as an in-line parameter, where n is the number corresponding to the position of the file name entered in GDFILE. If +n is omitted, the first file is used.

Grid operators may be nested, allowing a complicated diagnostic function to be computed. One limitation is that layer and time range operators expect to work on operands read directly from the grid file or computed from special names.

In the following list of diagnostic operators, scalar operands are named S_i and vector operands are V_i . Lower case u and v refer to the grid relative components of a vector. All meteorological output grids are in MKS units, except as noted. Operators using PR_ functions are described in the GEMPAK PARAMETER APPENDIX. All scalar and vector differential operators are valid in any map projection for which the map scale factors can be computed. At present, this applies for the stereographic, cylindrical and conic projections available in GEMPAK. In the definitions below, only the cartesian form of the operators is shown. The general curvilinear coordinate forms involving the scale factors are not given.

The operators which are designated for use in polar coordinates are specific to that coordinate system.

SCALAR OUTPUT GRID

Algebraic and trigonometric functions (angles are expressed in radians):

ABS	Absolute value ABS (S)
ACOS	Arc cosine function ACOS (S)
ASIN	Arc sine function ASIN (S)
ATAN	Arc tangent function ATAN (S)
ATN2	Arc tangent function $ATN2 (S1, S2) = ATAN (S1 / S2)$
COS	Cosine function COS (S)
EXP	Exponential to real $EXP (S1, S2) = S1 ** S2$
EXPI	Exponential to integer

GEMPAK Grid Diagnostic Functions

	$\text{EXP}(S1, S2) = S1^{**} \text{NINT}(S2)$
LN	Natural logarithm $\text{LN}(S) = \text{LOG}(S)$
LOG	Base 10 logarithm $\text{LOG}(S) = \text{LOG10}(S)$
NINT	Round to integer $\text{NINT}(S)$
SIN	Sine function $\text{SIN}(S)$
SQRT	Square root $\text{SQRT}(S)$
TAN	Tangent function $\text{TAN}(S)$
ADD	Addition $\text{ADD}(S1, S2) = S1 + S2$
MUL	Multiplication $\text{MUL}(S1, S2) = S1 * S2$
QUO	Division $\text{QUO}(S1, S2) = S1 / S2$
SUB	Subtraction $\text{SUB}(S1, S2) = S1 - S2$
SLT	Less than function $\text{SLT}(S1, S2) = S1 < S2$
SLE	Less than/equal to $\text{SLE}(S1, S2) = S1 \leq S2$
SGT	Greater than function $\text{SGT}(S1, S2) = S1 > S2$
SGE	Greater than/equal to $\text{SGE}(S1, S2) = S1 \geq S2$
SBTW	Between function $\text{SBTW}(S1, S2, S3) = S1 > S2 \text{ AND } S1 < S3$
BOOL	Boolean function $\text{BOOL}(S)$
MASK	Masking function $\text{MASK}(S1, S2) = \text{RMISD}$ IF $S2 = \text{RMISD}$, = $S1$ otherwise
MISS	Missing value replace $\text{MISS}(S1, S2) = S2$ if $S1 = \text{RMISD}$, = $S1$ otherwise
ADV	Advection

GEMPAK Grid Diagnostic Functions

	$ADV (S, V) = - (u * DDX (S) + v * DDY (S))$
AVG	Average $AVG (S1, S2) = (S1 + S2) / 2$
AVOR	Absolute vorticity $AVOR (V) = VOR (V) + CORL$
BVSQ	Brunt-Vaisala frequency squared in a layer $BVSQ (THTA) = [GRAVITY * LDF (THTA)] / [LAV (THTA) * DZ]$ in PRES coordinates $= - (RDGAS / GRAVITY) * LAV (THTA) * (LAV (PRES) / 1000) ** KAPPA * LDF (PRES) / LAV (PRES)$ in THTA coordinates DZ = change in height across the layer
CROS	Vector cross product magnitude $CROS (V1, V2) = u1 * v2 - u2 * v1$
DDEN	Density of dry air (kg / m**3) $DDEN (PRES, TMPC) = PR_DDEN (PRES, TMPC)$
DDR	Partial derivative with respect to R DDR (S) is computed using centered finite differences, with backward or forward differences at the boundary. Polar coordinates are assumed, and (R, THETA) maps into (X, Y).
DDT	Time derivative $DDT (S) = (S (time1) - S (time2)) / (time1 - time2)$ where the time difference is in seconds.
DDX	Partial derivative with respect to X DDX (S) is computed using centered finite differences, with backward or forward differences at the boundary.
DDY	Partial derivative with respect to Y DDY (S) is computed using centered finite differences, with backward or forward differences at the boundary.
DEF	Total deformation $DEF (V) = (STR (V) ** 2 + SHR (V) ** 2) ** .5$
DIRN	North relative direction of a vector $DIRN (V) = PR_DRCT (UN (V), VN (V))$
DIRR	Grid relative direction of a vector $DIRR (V) = PR_DRCT (u, v)$
DIV	Divergence $DIV (V) = DDX (u) + DDY (v)$
DOT	Vector dot product $DOT (V1, V2) = u1 * u2 + v1 * v2$
DTH	Partial derivative with respect to THETA DTH (S) is computed using centered finite differences, with backward or forward differences at the boundary. Polar coordinates are assumed, and (R, THETA) maps into (X, Y).
FCNT	Coriolis force at the center of a polar coordinate grid FCNT (S) can be computed only for lat/lon grids which have been mapped to polar (R,THETA) coordinates and or which the center lat/lon

GEMPAK Grid Diagnostic Functions

have been stored with each grid.

FOSB	<p>Fosberg index, also called Fire Weather Index. FOSB (TMPC, RELH, SPED) is computed with an empirical formula using surface temperature, relative humidity, and wind speed at the 2 meter or 10 meter level, or the mix of the two. High values indicate high flame lengths and rapid drying.</p>
FRNT	<p>Frontogenesis (K / 100 km / 3 h) $FRNT (THTA, V) = 1/2 * CONV * MAG (GRAD (THTA)) * (DEF * COS (2 * BETA) - DIV)$ CONV = unit conversion factor = 1.08E4 * 1.E5 BETA = ASIN ((- COS (DELTA) * DDX (THTA) - SIN (DELTA) * DDY (THTA)) / MAG (GRAD (THTA))) DELTA = 1/2 ATAN (SHR / STR)</p>
GWFS	<p>Horizontal smoothing using normally distributed weights GWFS (S,N) with theoretical response of 1/e for N * delta-x wave. Increasing N increases the smoothing.</p>
HIGH	<p>Relative maxima over a grid HIGH (S, RADIUS) where RADIUS defines a square region of grid points. The region is a moving search area in which all points are compared to derive a relative maximum.</p>
JCBN	<p>Jacobian determinant $JCBN (S1, S2) = DDX (S1) * DDY (S2) - DDY (S1) * DDX (S2)$</p>
KNTS	<p>Convert meters / second to knots $KNTS (S) = PR_MSKN (S) = S * 1.9438$</p>
LAP	<p>Laplacian operator $LAP (S) = DIV (GRAD (S))$</p>
LAV	<p>Layer average (2 levels) $LAV (S) = (S (level1) + S (level2)) / 2.$</p>
LDF	<p>Layer difference (2 levels) $LDF (S) = S (level1) - S (level2)$</p>
LOWS	<p>Relative minima over a grid LOWS (S, RADIUS) where RADIUS defines a square region of grid points. The region is a moving search area in which all points are compared to derive a relative minimum.</p>
MAG	<p>Magnitude of a vector $MAG (V) = PR_SPED (u, v)$</p>
MASS	<p>Mass per unit volume in a layer $MASS = 100 * LDF (PRES) / (GRAVITY * (level1 - level2))$ The 100 converts mb to Pascals. Level1 and level2 are also converted to Pascals when VCOORD = PRES. The volume is expressed in units of m * m * (units of the vertical coordinate). This is an operand.</p>
MDIV	<p>Layer-average mass divergence</p>

GEMPAK Grid Diagnostic Functions

	MDIV (V) = DIV ([MASS * LAV (u), MASS * LAV (v)])
MIXR	Mixing ratio MIXR (DWPC, PRES) = PR_MIXR (DWPC, PRES) The units are kg/kg internally, but g/kg on output.
MRAD	Magnitude of storm relative radial wind MRAD (V, LAT, LON, DIR, SPD) = DOT (Vrel, R) where Vrel is the velocity minus the storm motion vector specified by DIR and SPD, and R is a unit vector tangent to a great circle arc from the storm center specified by LAT, LON to a grid point.
MSDV	Layer-average mass-scalar flux divergence MSDV (S, V) = DIV ([MASS * LAV (S) * LAV (u), MASS * LAV (S) * LAV (v)]) Note: MASS is computed using the in-line parameter values for V rather than those for S.
MSFC	Pseudo angular momentum (for cross sections) MSFC (V) = NORMV (V) + CORL * DIST DIST is the distance along the cross section in meters. The units for the M-surface are expressed in m/s.
MTNG	Magnitude of storm relative tangential wind MTNG (V, LAT, LON, DIR, SPD) = DOT (Vrel, k X R) where Vrel is the velocity minus the storm motion vector specified by DIR and SPD, and R is a unit vector tangent to a great circle arc from the storm center specified by LAT, LON to a grid point. k denotes the local vertical unit vector.
NORM	Scalar vector component normal to a cross section NORM (V) = DOT (V, unit normal vector) If the starting point for the cross section is on the left, the unit normal vector points into the cross section plane.
PLAT	Latitude at each point in polar coordinates PLAT (S) Note: only the header, which contains the center latitude and longitude, is used.
PLCL	Pressure of the lifting condensation level PLCL (PRES, TMPC, DWPC) = PR_PLCL (TMPC, PRES, TLCL) Note: The temperature of the LCL must be calculated as an intermediate quantity.
PLON	Longitude at each point in polar coordinates PLON (S) Note: only the header, which contains the center latitude and longitude, is used.
POIS	Solve Poisson eqn. of a forcing function with the given boundary values POIS (S1, S2) where S1 is the forcing function grid and S2 is the boundary value. The equation LAP (POIS) = S1 is solved for POIS.
POLF	Coriolis force at each point in polar coordinates

GEMPAK Grid Diagnostic Functions

POLF (S)

Note: only the header, which contains the center latitude and longitude, is used.

PVOR

Potential vorticity in a layer

$PVOR (S, V) = - \text{GRAVITY} * AVOR (VLAV (V)) * LDF (THTA) / (100 * LDF (PRES))$

The 100 converts millibars to Pascals.

Units are Kelvins / meters / Pascals / seconds**3 (note that GRAVITY is included).
PVOR works on a layer

in PRES or THTA coordinates. In isobaric coordinates, the scalar operand, S, is THTA, THTE, or THES. In isentropic coordinates, the scalar operand, S, is PRES. Multiplying by 10**6 gives standard PV units.

RELH

Relative humidity

$RELH (TEMP, DWPT) = PR_RELH (TEMP, DWPT)$

RICH

Richardson stability number in a layer

$RICH (V) = \text{GRAVITY} * DZ * LDF (THTA) / (LAV (THTA) * MAG (VLDF (V)) ** 2)$

Note: DZ = change in height across the layer.

RICH can be evaluated in PRES, THTA or HGHT vertical coordinate.

ROSS

Rossby number

$ROSS (V1, V2) = MAG (INAD (V1, V2)) / (CORL * MAG (V1))$

SAVG

Average over whole grid

$SAVG (S) = \text{average of all non-missing grid point values}$

SAVS

Average over subset grid

$SAVS (S) = \text{average of all non-missing grid point values in the subset area}$

SDIV

Flux divergence of a scalar

$SDIV (S, V) = S * DIV (V) + DOT (V, GRAD (S))$

SHR

Shear deformation

$SHR (V) = DDX (v) + DDY (u)$

SM5S

Smooth scalar grid using a 5-point smoother

$SM5S (S) = .5 * S (i,j) + .125 * (S (i+1,j) + S (i,j+1) + S (i-1,j) + S (i,j-1))$

SM9S

Smooth scalar grid using a 9-point smoother

$SM5S (S) = .25 * S (i,j) + .125 * (S (i+1,j) + S (i,j+1) + S (i-1,j) + S (i,j-1)) + .0625 * (S (i+1,j+1) + S (i+1,j-1) + S (i-1,j+1) + S (i-1,j-1))$

STAB

Thermodynamic stability within a layer (lapse rate)

$STAB (TMPC) = LDF (TMPC) / DZ \text{ in PRES coordinates.}$

$= - (RDGAS / \text{GRAVITY}) * LAV (THTA) * (LAV (PRES) / 1000) ** KAPPA *$

$LDF (PRES) / LAV (PRES)$ in THTA coordinates

DZ = change in height across the layer.

Units are degrees / kilometer.

STR

Stretching deformation

$STR (V) = DDX (u) - DDY (v)$

TANG

Scalar vector component tangential to a cross section

GEMPAK Grid Diagnostic Functions

$TANG (V) = DOT (V, \text{unit tangent vector})$

If the starting point for the cross section is on the left, the unit tangent vector points to the right.

TAV	Time average (2 times) $TAV (S) = (S (\text{time1}) + S (\text{time2})) / 2.$
TDF	Time difference (2 times) $TDF (S) = S (\text{time1}) - S (\text{time2})$
THES	Saturated equivalent potential temperature in Kelvin $THES (PRES, TMPC) = PR_THTE (PRES, TMPC, TMPC)$
THTA	Potential temperature in Kelvin $THTA (TMPC, PRES) = PR_THTA (TMPC, PRES)$
THTE	Equivalent potential temperature in Kelvin $THTE (PRES, TMPC, DWPC) = PR_THTE (PRES, TMPC, DWPC)$
THWC	Wet bulb potential temperature in Celsius $THWC (PRES, TMPC, DWPC) = PR_THWC (PRES, TMPC, DWPC)$
TLCL	Temperature of the lifting condensation level $TLCL (TMPC, DWPC) = PR_TLCL (TMPC, DWPC)$
TMST	Parcel temperature in Kelvin along a moist adiabat $TMST (THTE, PRES) = PR_TMST (THTE, PRES, GUESS)$ where THTE is the equivalent potential temperature at the input GLEVEL, PRES is the pressure level at which the parcel temperature is valid, and GUESS is a guess-field calculated automatically.
TMWK	Wet bulb temperature in Kelvin $TMWK (PRES, TMPK, RMIX) = PR_TMWK (PRES, TMPK, RMIX)$
UN	North relative u component $UN (V) = \text{zonal wind component}$
UR	Grid relative u component $UR (V) = u$
VN	North relative v component $VN (V) = \text{meridional wind component}$
VOR	Vorticity $VOR (V) = DDX (v) - DDY (u)$
VR	Grid relative v component $VR (V) = v$
WNDX	WINDEX (index for microburst potential) $WNDX (S1, S2, S3, S4) = 2.5 * \text{SQRT} (\text{HGHTF} * \text{RATIO} * (\text{GAMMA}^{**2} - 30 +$

GEMPAK Grid Diagnostic Functions

$$\text{MIXRS} - 2 * \text{MIXRF}))$$

TMPCS = surface temperature = S1

HGHTF = AGL Height of Freezing level = S2

MIXRS = surface mixing ratio = S3

MIXRF = freezing level mixing ratio = S4

RATIO = MIXRS / 12 if MIXRS < 12, = 1 otherwise

GAMMA = TMPCS / HGHTF

WSHR Magnitude of the vertical wind shear in a layer

WSHR (V) = MAG [VLDF (V)] / DZ in PRES coordinates.

$$= - (\text{RDGAS} / \text{GRAVITY}) * \text{LAV} (\text{THTA}) * (\text{LAV} (\text{PRES}) / 1000) ** \text{KAPPA} *$$

LDF (PRES) / LAV (PRES) in THTA coordinates.

DZ = change in height across the layer

WSHR can be evaluated in PRES, THTA, or HGHT coordinate.

XAV Average along a grid row

$$\text{XAV} (\text{S}) = (\text{S} (\text{X1}) + \text{S} (\text{X2}) + \dots + \text{S} (\text{KXD})) / \text{KNT}$$

KXD = number of points in row

KNT = number of non-missing points in row

XAV for a row is stored at every point in that row.

In polar coord., XAV is the average along a radial.

XSUM Sum along a grid row

$$\text{XSUM} (\text{S}) = (\text{S} (\text{X1}) + \text{S} (\text{X2}) + \dots + \text{S} (\text{KXD}))$$

KXD = number of points in row

XSUM for a row is stored at every point in that row. In polar coord., XSUM is the sum along a radial.

YAV Average value along a grid column

$$\text{YAV} (\text{S}) = (\text{S} (\text{Y1}) + \text{S} (\text{Y2}) + \dots + \text{S} (\text{KYD})) / \text{KNT}$$

KYD = number of points in column

KNT = number of non-missing points in column

YAV for a column is stored at every point in that column. For polar coordinates, YAV is the average around a circle. If the theta coordinate starts at 0 degrees and ends at 360 degrees, the first radial is not used in computing the average.

YSUM Sum along a grid column

$$\text{SUM} (\text{S}) = (\text{S} (\text{Y1}) + \text{S} (\text{Y2}) + \dots + \text{S} (\text{KYD}))$$

KYD = number of points in column

YSUM for a column is stored at every point in that column. For polar coordinates, YSUM is the sum around a circle. If the theta coordinate starts at 0 degrees and ends at 360 degrees, the first radial is not

GEMPAK Grid Diagnostic Functions

used in computing the sum.

VECTOR OUTPUT GRID

AGE Ageostrophic wind

$$\text{AGE} (S) = [u (\text{OBS}) - u (\text{GEO}(S)), v (\text{OBS}) - v (\text{GEO}(S))]$$

CIRC Circulation (for cross sections)

$$\text{CIRC} (V, S) = [\text{TANG} (V), S]$$

DVDX Partial x derivative of a vector

$$\text{DVDX} (V) = [\text{DDX} (u), \text{DDX} (v)]$$

DVDY Partial y derivative of a vector

$$\text{DVDY} (V) = [\text{DDY} (u), \text{DDY} (v)]$$

GEO Geostrophic wind

$$\text{GEO} (S) = [- \text{DDY} (S) * \text{const} / \text{CORL}, \text{DDX} (S) * \text{const} / \text{CORL}]$$

const	S	vert coord
GRAVTY ZMSL	none	
GRAVTY HGHT	PRES	
1	PSYM	THTA
100/RO PRES	HGHT	

$$\text{RO} = \text{PR_DDEN} (\text{PRES}, \text{TMPC})$$

GRAD Gradient of a scalar

$$\text{GRAD} (S) = [\text{DDX} (S), \text{DDY} (S)]$$

GWFV Horizontal smoothing using normally distributed weights

GWFV (V,N) with theoretical response of 1/e for N * delta-x wave. Increasing N increases the smoothing.

INAD Inertial advective wind

$$\text{INAD} (V1, V2) = [\text{DOT} (V1, \text{GRAD} (u2)), \\ \text{DOT} (V1, \text{GRAD} (v2))]$$

ISAL Isallobaric wind

$$\text{ISAL} (S) = [- \text{DDT} (v (\text{GEO}(S))) / \text{CORL}, \\ \text{DDT} (u (\text{GEO}(S))) / \text{CORL}]$$

GEMPAK Grid Diagnostic Functions

KCRS Unit vector k cross a vector

$$\text{KCRS} (V) = [-v, u]$$

KNTV Convert meters / second to knots

$$\text{KNTV} (V) = [\text{PR_MSKN} (u), \text{PR_MSKN} (v)]$$

LTRN Layer-averaged transport of a scalar

$$\text{LTRN} (S, V) = [\text{MASS} * \text{LAV} (S) * \text{LAV} (u), \\ \text{MASS} * \text{LAV} (S) * \text{LAV} (v)]$$

Note: MASS is computed using the in-line parameter values for V rather than those for S.

NORMV Vector component normal to a cross section.

$$\text{NORMV} (V) = \text{NORM} (V) * \text{unit normal vector}$$

QVEC Q-vector at a level (K / m / s)

$$\text{QVEC} (S, V) = [- (\text{DOT} (\text{DVDX} (V), \text{GRAD} (S))), \\ - (\text{DOT} (\text{DVDY} (V), \text{GRAD} (S)))] \text{ where } S \text{ can be any thermal} \\ \text{parameter, usually THTA.}$$

QVCL Q-vector of a layer (mb / m / s)

$$\text{QVCL} (\text{THTA}, V) = (1 / (\text{D} (\text{THTA}) / \text{DP})) * \\ [(\text{DOT} (\text{DVDX} (V), \text{GRAD} (\text{THTA}))), \\ (\text{DOT} (\text{DVDY} (V), \text{GRAD} (\text{THTA})))]$$

RAD Storm relative radial wind

$$\text{RAD} (V, \text{LAT}, \text{LON}, \text{DIR}, \text{SPD}) = \text{SMUL} (\text{DOT} (\text{Vrel}, R), R)$$

where Vrel is the velocity minus the storm motion specified by DIR and SPD, and R is a unit vector tangent to a great circle arc from the storm center specified by LAT, LON to a grid point.

ROT Coordinate rotation

$$\text{ROT} (\text{angle}, V) = [u * \text{COS} (\text{angle}) + v * \text{SIN} (\text{angle}), \\ -u * \text{SIN} (\text{angle}) + v * \text{COS} (\text{angle})]$$

SMUL Multiply a scalar with each component of a vector

$$\text{SMUL} (S, V) = [S * u, S * v]$$

SM5V Smooth vector grid using a 5-point smoother

$$\text{SM5V} (V) = .5 * V (i,j) + .125 * (V (i+1,j) + V (i,j+1) + \\ V (i-1,j) + V (i,j-1))$$

SQUO Vector division by a scalar.

$$\text{SQUO} (S, V) = [u / s, v / s]$$

TANGV Vector component tangential to a cross section.

$$\text{TANGV} (V) = \text{TANG} (V) * \text{unit tangent vector}$$

THRM Thermal wind

$$\text{THRM} (S) = [u (\text{GEO}(S)) (\text{level1}) - u (\text{GEO}(S)) (\text{level2}), \\ v (\text{GEO}(S)) (\text{level1}) - v (\text{GEO}(S)) (\text{level2})]$$

GEMPAK Grid Diagnostic Functions

TNG Storm relative tangential wind

$TNG (V, LAT, LON, DIR, SPD) = SMUL (DOT (Vrel, k \times R), k \times R)$

where Vrel is the velocity minus the storm motion vector specified by DIR and SPD, and R is a unit vector tangent to a great circle arc from the storm center specified by LAT, LON to a grid point. k denotes the local vertical unit vector.

VADD Add the components of two vectors

$VADD (V1, V2) = [u1+u2, v1+v2]$

VASV Vector component of V1 along V2

$VASV (V1, V2) = [DOT (V1, V2) / MAG (V2) ** 2] * V2$

VAVG Average over whole grid

$VAVG (V) =$ average of all non-missing grid point values

VAVS Average over subset grid

$VAVS (V) =$ average of all non-missing grid point values in the subset area

VECN Create a vector grid from two north relative scalar components

$VECN (S1, S2) = [S1, S2]$

VECR Create a vector grid from two grid relative scalar components

$VECR (S1, S2) = [S1, S2]$

VLAV Layer average for a vector

$VLAV (V) = [(u (level1) + u (level2)) / 2.,$
 $(v (level1) + v (level2)) / 2.]$

VLDF Layer difference for a vector

$VLDF (V) = [u (level1) - u (level2),$
 $v (level1) - v (level2)]$

VMUL Multiply the components of two vectors

$VMUL (V1, V2) = [u1*u2, v1*v2]$

VQUO Divide the components of two vectors

$VQUO (V1, V2) = [u1/u2, v1/v2]$

VSUB Subtract the components of two vectors

$VSUB (V1, V2) = [u1-u2, v1-v2]$

VLT Less than function

$VLT (V, S) = V$ IF $|V| < S$

VLE Less than or equal to function

$VLE (V, S) = V$ IF $|V| \leq S$

VGX Greater than function

$VGX (V, S) = V$ IF $|V| > S$

GEMPAK Grid Diagnostic Functions

VGE **Greater than or equal to function**

$VGE(V, S) = V$ IF $|V| \geq S$

VBTW **Between function**

$VBTW(V, S1, S2) = V$ IF $S1 < |V| < S2$

VMSK **Masking function**

$VMSK(V, S) = RMISSD$ IF $S = RMISSD$
= V otherwise