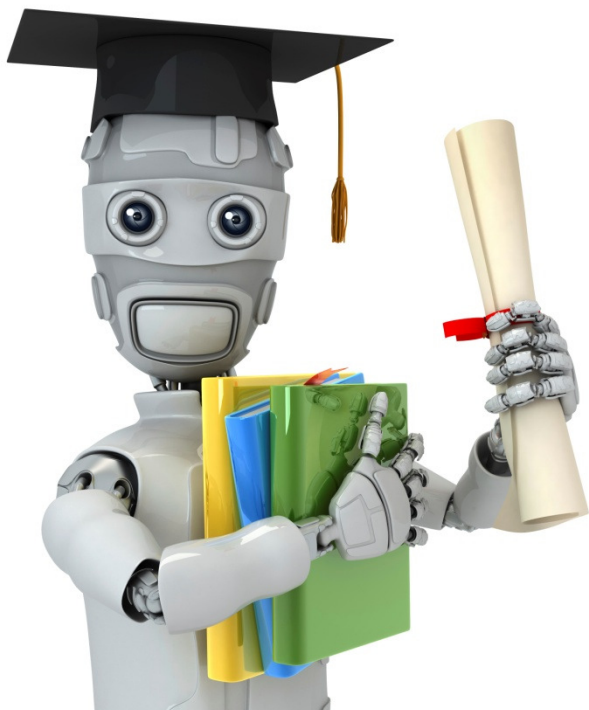




Machine Learning

# Octave Tutorial

## Basic operations



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## Moving data around



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## Computing on data



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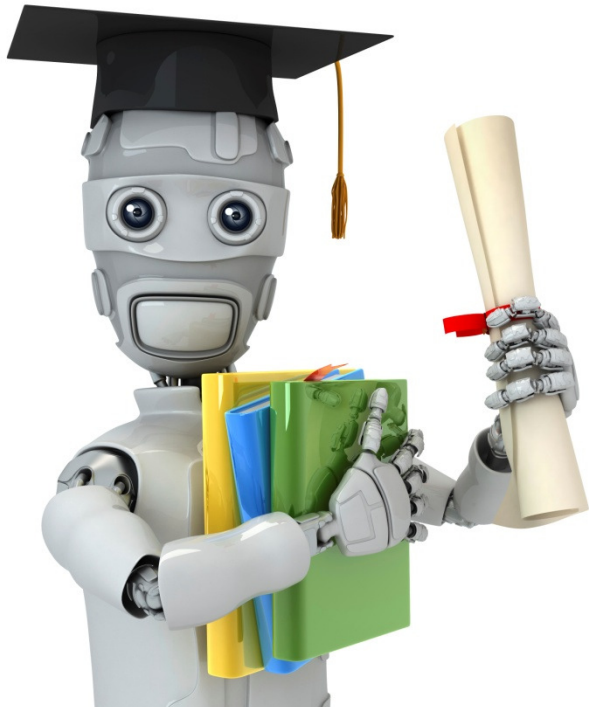
## Plotting data



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Control statements: for,  
while, if statements



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Vectorial implementation

矢量化实现线性回归

在特征个数很多时运行更快

## Vectorization example.

线性回归假设函数

$$h_{\theta}(x) = \sum_{j=0}^n \theta_j x_j$$

即进行计算  $\sum_{j=0}^n \theta_j x_j = 0 \cdot \theta_0 + \dots + \theta_n x_n$

$$= \theta^T x \quad \text{即 } \theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \end{bmatrix} \quad x = \begin{bmatrix} x_0 \\ x_1 \\ x_2 \end{bmatrix}$$

### Unvectorized implementation

```
prediction = 0.0;
for j = 1:n+1,
    prediction = prediction +
        theta(j) * x(j)
end;
```

即从 1 开始

### Vectorized implementation

```
prediction = theta' * x;
```

$\theta^T * x$

即求解  $\begin{bmatrix} \theta(1) \\ \theta(2) \\ \theta(3) \end{bmatrix}$

## Vectorization example.

$$h_{\theta}(x) = \sum_{j=0}^n \theta_j x_j$$
$$= \theta^T x$$

C++

### Unvectorized implementation

```
double prediction = 0.0;
for (int j = 0; j < n; j++)
    prediction += theta[j] * x[j];
```

### Vectorized implementation

```
double prediction
    = theta.transpose() * x;
```

转置  $\Rightarrow \theta^T$



## Gradient descent

线性回归参数更新规则

$$\theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

(for all  $\underline{j}$ )

$\underline{j} = 0, 1, 2$

eg:

$$\underline{\theta_0} := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \underline{x_0^{(i)}}$$

$$\underline{\theta_1} := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \underline{x_1^{(i)}}$$

$$\underline{\theta_2} := \theta_2 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \underline{x_2^{(i)}}$$

} 同步更新

$$\begin{aligned}\theta_0 &:= \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)} \\ \theta_1 &:= \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_1^{(i)} \\ \theta_2 &:= \theta_2 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_2^{(i)} \\ (n=2)\end{aligned}$$

$$u(j) = 2v(j) + 5w(j) \quad (\text{for all } j)$$

$$u = 2v + 5w$$

Vectorized Implementation:

$$\theta := \theta - \alpha \delta$$

$\mathbb{R}^{n+1}$     $\mathbb{R}^{n+1}$     $\mathbb{R}$     $\mathbb{R}^{n+1}$   
 $\uparrow$  向量减法

where  $\delta = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x^{(i)}$     $x^{(i)} = \begin{bmatrix} x_0^{(i)} \\ x_1^{(i)} \\ x_2^{(i)} \end{bmatrix}$

$\mathbb{R}^{n+1}$     $\mathbb{R}$  标量    $\mathbb{R}^{n+1}$  向量

$$\frac{(h_{\theta}(x^{(1)}) - y^{(1)}) \cdot x^{(1)}}{+} \frac{(h_{\theta}(x^{(2)}) - y^{(2)}) \cdot x^{(2)}}{+} \dots + \frac{(h_{\theta}(x^{(m)}) - y^{(m)}) \cdot x^{(m)}}{+}$$

$\rightarrow$   $m$  个标量的向量加法  
 标量 \* 向量 = 向量

$$\delta = \begin{bmatrix} \delta_0 \\ \delta_1 \\ \delta_2 \end{bmatrix} \quad \delta_0 = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

$\downarrow$   
 $\sum_{i=1}^m$  标量和,  $\delta$  是一个标量, 可分解为标量