
VL Nichtprozedurale Programmierung

Funktionale Programmierung

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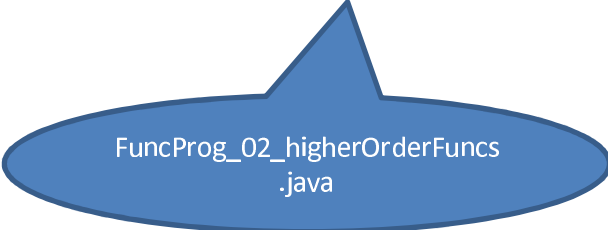
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Some good news...

- We are done with the syntax !
(more or less)
- Now: time for some **big ideas**
 - **Today**
 - **Procedures (cont'd)**
 - **Data**

Procedures (cont'd)

- Last lecture we covered
 - Recursion
 - elegant
 - avoids mutation
 - can be efficiently implemented (tail recursion)
 - Higher-order procedures
 - take a procedure as parameter OR
 - return a procedure (covered today)
 - Lambda
 - anonymous procedures



FuncProg_02_higherOrderFuncs
.java

BUILDING ABSTRACTIONS WITH DATA

Building Abstractions with Data

- Today: excerpt from SICP chapter 2

- Use functions to create and encapsulate data structures.

Encapsulation:

bundling of data with the methods that operate on that data

(also a mechanism to restrict access to some elements within a component
→ *information hiding*)

- Example rational numbers

- $\frac{x}{y}$

- numerator x (integer)
- denominator y (integer)

- We'll write code to do rational arithmetic

Addition (+): A naïve approach (with what we have learned so far)

- $\frac{n1}{d1}$ two integers

$$\frac{n1}{d1} + \frac{n2}{d2} = \frac{n1*d2+n2*d1}{d1*d2}$$

- Addition: Implement two procedures
 - One to get the numerator of the sum

```
(define (addRatNum n1 d1 n2 d2)
  (+ (* n1 d2)
     (* n2 d1)))
```

- One to get the denominator of the sum

```
(define (addRatDenom n1 d1 n2 d2)
  (* d1 d2))
```

- Usage: $\frac{1}{2} + \frac{1}{2}$

```
(addRatNum 1 2 1 2) ; 4
(addRatDenom 1 2 1 2) ; 4
```

$$\rightarrow \frac{4}{4} = 1$$

(Demo3a)

Data Abstraction → Compound Data

- Wishful thinking
 - We assume that we already have a way of **constructing** a rational number from a numerator and a denominator.
 - We further assume that, given a rational number, we have a way of extracting (or **selecting**) its numerator and denominator.

- Constructor

(make-rat <n> <d>)

returns the rational number
whose numerator is the integer <n>
and whose denominator is the integer <d>.

- Selectors

(numer <x>)

returns the numerator
of the rational number <x>.

(denom <x>)

returns the denominator
of the rational number <x>



1/2

1/2

```
(define (add-rat x y)
  (make-rat (+ (* (numer x) (denom y))
                (* (numer y) (denom x)))
            (* (denom x) (denom y))))
```

$$\frac{n1}{d1} + \frac{n2}{d2} = \frac{n1*d2+n2*d1}{d1*d2}$$

```
(define (sub-rat x y)
  (make-rat (- (* (numer x) (denom y))
                (* (numer y) (denom x)))
            (* (denom x) (denom y))))
```

```
(define (mul-rat x y)
  (make-rat (* (numer x) (numer y))
            (* (denom x) (denom y))))
```

```
(define (div-rat x y)
  (make-rat (* (numer x) (denom y))
            (* (denom x) (numer y))))
```

```
(define (equal-rat? x y)
  (= (* (numer x) (denom y))
     (* (numer y) (denom x))))
```

But we haven't yet defined
make-rat, numer, denom.
What do we need for this?

Pairs

- Racket provides a compound structure 'pair'.
- Constructor
 - `cons`
- Selector (names have historical reasons)
 - `car` → 1st element
 - `cdr` → 2nd element (pronounced "could-er")
 - `(define p (cons 1 2))`
 - `(car p)`
 - `(cdr p)`

Pairs (2)

- ```
(define x (cons 1 2))
(define y (cons 3 4))
(define z (cons x y))
```
- **z: ((1,2),(3,4))**
  - ```
(car (car z))
```


1
 - ```
(car (cdr z))
```

  
*3*

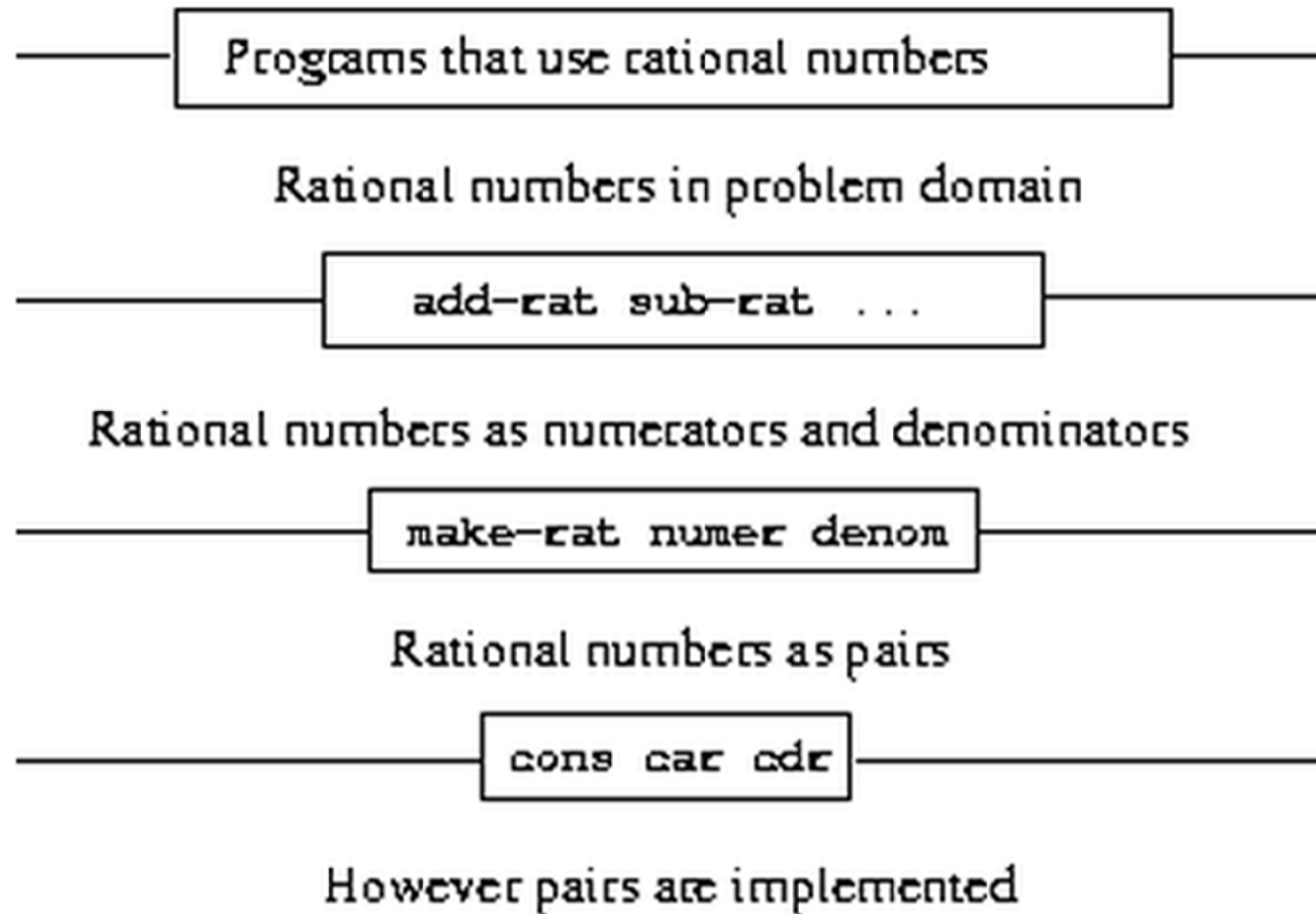
## Example: Rational numbers (cont'd)

- `(define (make-rat n d)` `)`
- `(define (numer x)` `)`
- `(define (denom x)` `)`

## Example: Rational numbers (cont'd)

- `(define (make-rat n d) (cons n d) )`
- `(define (numer x) (car x) )`
- `(define (denom x) (cdr x) )`

# Data-abstraction barriers



## Sample **Benefit**

- Reducing the fraction in constructor

```
(define (make-rat n d)
 (define g (gcd n d))
 (cons (/ n g) (/ d g)))
```

- Reducing the fraction in selectors

```
(define (numer x)
 (define g (gcd (car x) (cdr x)))
 (/ (car x) g))
```

```
(define (denom x)
 (define g (gcd (car x) (cdr x)))
 (/ (cdr x) g))
```

# What is meant by Data ?

- We don't know what pairs are. But we know that Racket provides `cons`, `car`, `cdr` to work with them.
- They are built-in but we can also define them ourselves. (→ really cool. See next slide)
- The only thing we need to know about these three operations is that if we glue two objects together using `cons` we can retrieve the objects using `car` and `cdr`.
- → for any objects `x` and `y`,  
if `z` is `(cons x y)` then  
`(car z)` is `x` and `(cdr z)` is `y`.

---

# How to define **cons/car/cdr** ourselves?



# cons | car | cdr

```
(define (mycons x y)
 (define (dispatch m)
 (cond [(= m 0) x]
 [(= m 1) y]
 [else (error "argument not 0 or 1 -- in mycons" m)]))
 dispatch)
```

Example:

```
(define r (mycons 3 4))
(mycar r) → 3
```

```
(define (mycar z) _____)
```

```
(define (mycdr z) _____)
```

Procedure as Returned Value

# cons | car | cdr

```
(define (mycons x y)
 (define (dispatch m)
 (cond [(= m 0) x]
 [(= m 1) y]
 [else (error "argument not 0 or 1 -- in mycons" m)]))
 dispatch)
```

Example:

```
(define r (mycons 3 4))
(mycar r) → 3
```

```
(define (mycar z) (z 0))
```

```
(define (mycdr z) (z 1))
```

- → no data structures, just procedures
- → the ability to manipulate procedures as objects automatically provides the ability to represent compound data
- Note: Racket implements pairs directly (performance)



Demo3d

# cons | car | cdr with $\lambda$

```
(define (cons2 x y)
 (lambda (m)
 (cond [(= m 0) x]
 [(= m 1) y]
 [else (error "Argument not 0 or 1 -- in cons2" m)])))
```

---

```
(define (cons3 x y)
 (lambda (m) (m x y)))
```

```
(define (car3 z)
 (z (lambda (p q) p)))
```

```
(define (cdr3 z)
 (z (lambda (p q) q)))
```



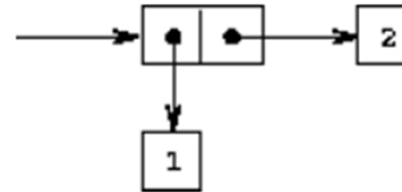
What is going on here?

Demo3e

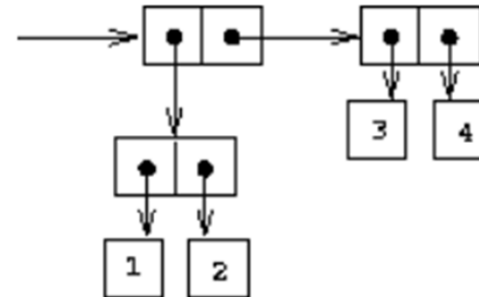
# Hierarchical Data

(box-pointer-representation)

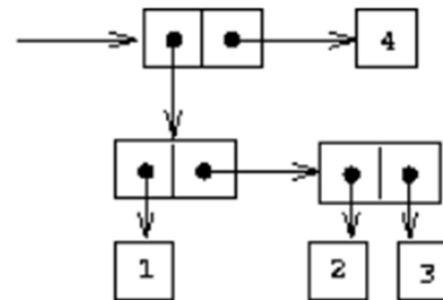
- (cons 1 2)



- (cons (cons 1 2)  
      (cons 3 4))

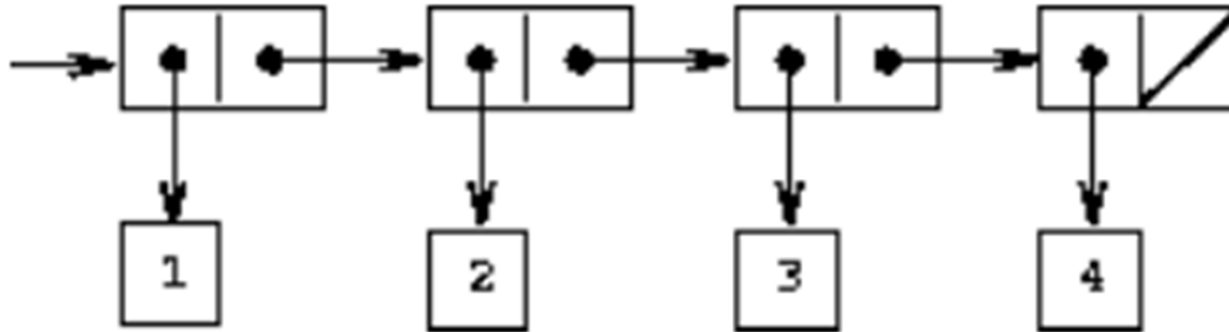


- (cons (cons 1  
              (cons 2 3))  
      4)



# Sequences

(by chaining pairs)



- ```
(cons 1
      (cons 2
            (cons 3
                  (cons 4 null))))
```

`(cons <a1> (cons <a2> (cons ... (cons <an> null) ...)))`

is the same as

`(list <a1> <a2> ... <an>)`

- ```
(list 1 2 3 4)
```

# List operations

- `(define mylist (list 1 2 3 4))`
- `(car mylist)`
- `(cdr mylist)`
- `(car (cdr mylist))`
- `(car (cdr (cdr mylist)))`

# Lists

- To form a list, we always start with the **empty list**:

- ``()`
- `null`
- `empty`
- `(list)`

In Lisp/Scheme the empty list was ***nil*** (from latin *nihil*).

For compatibility:

```
(define nil null)
```

- `(cons 1 null)`
- `(cons 1 (cons 2 (cons 3 null)))`

- Check for emptiness

- `null?`
- `empty?`

## Lists 2: **car|cdr** vs. **first|rest**

- `(define mylist (list 1 2 3 4))`
- `(car mylist)`
- `(cdr mylist)`
- `(car (cdr mylist))`
- `(car (cdr (cdr mylist)))`

vs.

- `(first mylist)`
  - `(rest mylist)`
  - `(first (rest mylist))`
  - `(first (rest (rest mylist)))`
- 
- `(caddr mylist) ← (car (cdr (cdr mylist)))`  
(note: there are only a few shortcuts implemented)



# Lists 3

- Lists may contain different types of data:

**Symbol:** a sequence of characters preceded by a single quotation mark (no blanks)

– (list #t 4 'aSymbol "a String" 5)

true

– (list (list 1 2) (list 3 4))

– (list (list #t 2) (list #f 4) 'S)

false

# Examples [cons | list]

- `(cons 1 2 3)`  
- ;error: cons only takes two arguments
- `(cons 1 2)`  
- ;makes a pair `'(1 . 2)`
- `(cons (list 1) 2)`  
- ;makes a pair `'((1) . 2)`
- `(cons 1 (cons 2 null))`  
- ;makes a list (because of the empty list on the right) `'(1 2)`
- `(cons 1 (list 2))`  
- ;makes a list `'(1 2)` ... so it takes the first argument, ie. 1, and makes it the first entry of the list
- `(cons (list 1) (list 2))`  
- ;makes a list `'((1) 2)` ... again it takes the first argument, ie. a list, and makes it the first entry in the list
- `(list (list 1) (list 2))`  
- ;makes a list of two elements (namely the original lists) `'((1) (2))`
- `(append (list 1 2) (list 3 4))` (just for 'completeness' ... see later)  
- ; `'(1 2 3 4)`

(see Demo3f for  
the code up to this slide)

# List operations

- Get the n-th element of the list
- ```
(define (list-ref items n)
  (if (= n 0)
      (first items)
      (list-ref (rest items) (- n 1))))
```

List operations

- Get the n-th element of the list
- ```
(define (list-ref items n)
```

**conditional** `(if` `(= n 0)`  
    `(first items)` **base case**  
    `(list-ref` `(rest items)` `(- n 1))` **self-referential case**)

## List operations (2)

- Get the n-th element of the list
- (define (list-ref items n)

**conditional** (if (= n 0)  
                  (first items) **base case**  
                  (list-ref (rest items) (- n 1))) **self-referential case**

- Get the length of the list
- (define (length items)  
      (if (null? items)  
          0  
          (+ 1 (length (rest items)))))

---

# That's it for today

## References

- SICP
- HTDP

# Thank you!