Military Institute of Science & Technology - MIST_CodeCrafters

1 Important Notes;

1.1 STL Common Libraries

```
 Common libraries
/*** Functions ***/
#include<algorithm>
#include<functional> // for hash
#include<climits> // all useful
constants
#include<cmath>
#include<cstdio>

#include<cstdlib> // random
#include<ctime>
#include<iostream>
#include<sstream>
#include<iomanip>//right justifying
std::right and std::setw(width)
```
/* Data Structure ***/**
```
#include<deque>//double ended queue
#include<list>
#include<queue>
#include<stack>
#include<string>
#include<vector>
```

1.2 Useful constant

```
INT_MIN
INT_MAX
LONG_MIN
LONG_MAX
LLONG_MIN
LLONG_MAX
```

1 Some Useful Code

```
Max priority_queue<ll>
Min
priority_queue<ll,vector<ll>,greater<ll
>>
```

2 Number Theory

2.1 Prime number under 100

```
// there are 25 numbers
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,
37,41, 43, 47, 53, 59, 61, 67, 71, 73,
79, 83, 89, 97
```

2.2 If prime number

```
bool prime(ll n)
{
    if (n<2) return false;
    if (n<=3) return true;
    if (!(n%2) || !(n%3)) return false;
    for (ll i=5; i*i<=n; i+=6)
        if (!(n%i) || !(n%(i+2)))
return false;
    return true;
}
```

2.3 Prime factorization

```
// smallest prime factor of a number.
ll factor(ll n)
{
    ll a;
    if (n%2==0)
        return 2;
    for (a=3; a<=sqrt(n); a++)
    {
        if (n%a==0)
            return a;
    }
    return n;
}
// complete factorization
ll r;
while (n>1)
{
r = factor(n);
    printf("%d", r);
    n /= r;
}
```

2.4 Leap year

```
bool isLeap(ll n)
{
    if (n%100==0)
      {
        if (n%400==0) return true;
        else return false;
      }
    if (n%4==0) return true;
    else return false;
}
```

2.5 Binary Exponentiation: (a^b)

```
ll power(ll a, ll b) {

        ll res = 1;

        while (b > 0) {

            if (b & 1)

                res = res * a;

            a = a * a;

            b >>= 1;

        }

        return res;

    }
```

2.6 Binary Exponentiation: (a^b^c)

```
ll binexp(ll base, ll power, ll modulo)
{
    ll ans = 1;
    while (power)
    {
        if (power % 2 == 1)
            ans = (ans * base) %
modulo;
        base = (base * base) % modulo;
        power /= 2;
    }
    return ans;
}
//function call
binexp(a, binexp (b, c, mod - 1), mod);
```

2.7 a^b mod p

```
ll powmod(ll base, ll exp, ll modulus)
{
    base %= modulus;
    ll result = 1;
    while (exp > 0)
    {
        if (exp & 1) result = (result *
base) % modulus;
        base = (base * base) % modulus;
        exp >>= 1;
    }
    return result;
}
```

2.8 Factorial mod

//n! mod p

```
ll factmod (ll n, ll p)
{
    ll res = 1;
    while (n > 1)
    {
        res = (res * powmod (p-1, n/p,
p)) % p;
        for (ll i=2; i<=n%p; ++i)
            res=(res*i) %p;
        n /= p;
    }
    return ll (res % p);
}
```

2.9 Next Greater Element :

```
//monotonic stack
ll output[1000005];
void nextGreaterElement(ll x[], ll n) {
    stack<ll> s;
    s.push(0);
    for (ll i = 0; i < n; i++) {
        while (!s.empty() && x[s.top()]
<= x[i]) {
            output[s.top()] = i;
            s.pop();
        }
        s.push(i);
    }
    while (!s.empty()) {
        output[s.top()] = -1;
        s.pop();
    }
}
```

2.10 Sieve:

```
ll prime[20000005];
void sieve(ll n){
    for (ll i=2;i<=n;i++){
        prime[i]=1;
    }
    for(ll i=4;i<=n;i+=2){
        prime[i]=0;
    }
    for(ll i=3;i*i<=n;i++){
        if(prime[i]){
            for(ll j=i*i;j<=n;j+=i*2){
                prime[j]=0;
            }
        }
    }
}
```

2.11 Optimized Sieve:finds (n+1)th prime

```
vector<ll> nth_prime;
bitset<MX> visited;
void optimized_prime(){
    nth_prime.push_back(2);
    for(ll i=3; i<MX; i+=2){
            if(visited[i])
                continue;
            nth_prime.push_back(i);
            if(1ll*i*i > MX)
                continue;
            for(ll j = i*i; j< MX; j+=
i+i)
                visited[j] = true;
    }
}
```

2.12 Segment Sieve

```
void SegmentSieve(ll L, ll R){
    if (L == 1)
        L++;
    ll maxN = R - L + 1;
    ll a[maxN] = {0};
    for (auto p : prime){
        if (p * p <= R)
        {
            ll x = (L / p) * p;
            if (x < L)
                x += p;
            for (ll i = x; i <= R; i +=
p)
            {
                if (i != p)
                    a[i - L] = 1;
            }
        }
        else
            break;}
    for (ll i = 0; i < maxN; i++)
        if (a[i] == 0)
            cout << i + L << endl;
}
```

2.13 Greatest common divisor – GCD

```
int gcd(int a, int b)
{
if (b==0) return a;
else return gcd(b, a%b);
}
```

2.14 Least common multiple – LCM

```
int lcm(int a, int b)
{
return a*b/gcd(a,b);
}
```

2.15 Num of trailing Zeros in factorial

```
int res=0;
for(int i=5;i<=n;i=i*5){
      res=res+n/i;
}
cout<<res<<endl;
```

2.16 Common Divisors:

You are given an array of *n* positive integers. Your task is to find two integers such that their greatest common divisor is as large as possible.

```
int main()
{
    int n;
    cin>>n;
    vector<int> range(1e6+1,0);
    for(int i=0; i<n; i++)
    {
        int x;
        cin>>x;
        range[x]++;
    }
    for(int gcd=1e6; gcd >=1; gcd--)
    {
        int multiples=0;
        for(int
pointer=gcd,pointer<=1e6; pointer+=gcd)
        {
            multiples+=range[pointer];
        }
        if(multiples>1)
        {
            cout<<gcd<<endl;
            return 0;
        }
    }
}
```

2.17 nCr:

```
const ll MOD = 1e9 + 7;
const ll MAX = 2e5 + 5;
vector<ll> fact(MAX), inv(MAX);
void factorial() {
    fact[0] = 1;
    for (ll i = 1; i < MAX; i++)
        fact[i] = (i * fact[i - 1]) %
MOD;
}
ll bigmod(ll a, ll n, ll M = MOD) {
    ll res = 1;
    while (n) {
        if (n & 1)
            res = (res * a) % M;
        a = (a * a) % M, n /= 2;
    }
    return res;
}
void inverse() {
    for (ll i = 0; i < MAX; ++i)
        inv[i] = bigmod(fact[i], MOD -
2);
}
ll C(ll a, ll b) {
    if (a < b or a < 0 or b < 0)
        return 0;
    ll de = (inv[b] * inv[a - b]) %
MOD;
    return (fact[a] * de) % MOD;
}
// call factorial() and inverse() from
main function
//  end nCR

ll ModInv(ll a, ll M) {  // M is prime
    return bigmod(a, M - 2, M);
}
```

2.18 Set Balancing:

```
// return middle element of the set
void balance(multiset<ll> right,
multiset<ll> &left){
    while (true){
        ll st = right.size();
        ll sl = left.size();
        if (st == sl || st == sl + 1)
            break;
        if (st < sl)
            right.insert(left.begin()),
left.erase(left.begin());
        else

left.insert(right.rbegin()),
right.erase(right.rbegin());
    }
}
void insert_in_set(multiset<ll> &right,
multiset<ll> &left, ll value)
{
    if (right.emptleft())
        right.insert(value);
    else
    {
        auto it = right.end();
        it--;
        if (value < *it)
            right.insert(value);
        else
            left.insert(value);
    }
}
```

3 String Algorithm

3.1 KMP ALGORITHM: O(n + m)

```
vector<ll> createLPS(string pattern)
{
    vector<ll> lps(pattern.length());
    ll index = 0;
    for (ll i = 1; i <
pattern.length();)
    {
        if (pattern[index] ==
pattern[i])
        {
            lps[i] = index + 1;
            index++, i++;
        }
        else
        {
            if (index != 0)
                index = lps[index - 1];
            else
                lps[i] = index, i++;
        }
    }
    return lps;
}
ll kmp(string text, string pattern)
{
    ll cnt_of_match = 0;
    vector<ll> lps =
createLPS(pattern);
    debug(lps);
    ll i = 0, j = 0;
    // i -> text, j -> pattern
    while (i < text.length())
    {
        if (text[i] == pattern[j])
            i++, j++;
        else
        {
            if (j != 0)
                j = lps[j - 1];
            else
                i++;
        }
        if (j == pattern.length())
        {
            cnt_of_match++;
            // the index where match
found -> (i - pattern.length());
            j = lps[j - 1];
        }
    }
    return cnt_of_match;
}
```

4 Dynamic Programming

4.1 0/1 Knapsack problems-O(n*w)

```
//Top Down
ll ks(ll W, ll i){
    if(i==0 || W<=0) return 0;
    if(weight[i]>W) return ks(W,i-1);
    if(mem[W][i]==0)
mem[W][i]=max(ks(W,i-1),value[i]+ks(W-
weight[i],i-1));
    return mem[W][i];
}
//Bottom Up
ll knapsack(ll capacity, ll ind){
    for(ll i=1;i<=ind;i++){
        for(ll c=1;c<=capacity;c++){
            if(weight[i]>c){
                mem[i][c]=mem[i-1][c];
            }
            else{
                ll k1=mem[i-1][c];
                ll k2=value[i]+mem[i-
1][c-weight[i]];
                mem[i][c]=max(k1,k2);
            }
        }
    }
    ll max_profit=mem[ind][capacity];
    return max_profit;
}
```

4.2 Complete Knapsack problems

```
#include <iostream>
using namespace std;
ll f[1000] = {0};
ll n = 0, m = 0;
ll main(void)
{
    cin >> n >> m;
    for (ll i = 1; i <= n; i++)
    {
        ll price = 0, value = 0;
        cin >> price >> value;
        for (ll j = price; j <= m; j++)
            if (f[j - price] + value >
f[j])
                f[j] = f[j - price] +
value;
```

```
    }
    cout << f[m] << endl;
    return 0;
}
```

4.3 Longest common subsequence (LCS)-O(n*m)

```
ll dp[1001][1001];
ll lcs(const string &s, const string
&t)
{
    ll m = s.size(), n = t.size();
    if (m == 0 || n == 0)
        return 0;
    for (ll i = 0; i <= m; ++i)
        dp[i][0] = 0;
    for (ll j = 1; j <= n; ++j)
        dp[0][j] = 0;
    for (ll i = 0; i < m; ++i)
        for (ll j = 0; j < n; ++j)
            if (s[i] == t[j])
                dp[i + 1][j + 1] =
dp[i][j] + 1;
            else
                dp[i + 1][j + 1] =
max(dp[i + 1][j], dp[i][j + 1]);
    return dp[m][n];
}
```

4.4 Longest increasing common sequence (LICS)

```
#include <iostream>
using namespace std;
ll a[100] = {0};
ll b[100] = {0};
ll f[100] = {0};
ll n = 0, m = 0;
ll main(void)
{
    cin >> n;
    for (ll i = 1; i <= n; i++)
        cin >> a[i];
    cin >> m;
    for (ll i = 1; i <= m; i++)
        cin >> b[i];
    for (ll i = 1; i <= n; i++)
    {
        ll k = 0;
        for (ll j = 1; j <= m; j++)
        {
            if (a[i] > b[j] && f[j] >
k)
                k = f[j];
            else if (a[i] == b[j] && k
+ 1 > f[j])
                f[j] = k + 1;
        }
    }
    ll ans = 0;
    for (ll i = 1; i <= m; i++)
        if (f[i] > ans)
            ans = f[i];
    cout << ans << endl;
    return 0;
}
```

4.5 Longest Increasing Subsequence (LIS)-O(n^2)

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
ll n = 0;
ll a[100] = {0}, f[100] = {0}, x[100] =
{0};
ll main(void)
{
    cin >> n;
    for (ll i = 1; i <= n; i++)
    {
        cin >> a[i];
        x[i] = LONG_LONG_MAX;
    }
    f[0] = 0;
    ll ans = 0;
    for (ll i = 1; i <= n; i++)
    {
        ll l = 0, r = i;
        while (l + 1 < r)
        {
            ll m = (l + r) / 2;
            if (x[m] < a[i])
                l = m;
            else
                r = m;
            // change to x[m]<=a[i] for
non-decreasing case
        }
        f[i] = l + 1;
        x[l + 1] = a[i];
        if (f[i] > ans)
            ans = f[i];
    }
    cout << ans << endl;
    return 0;
}
```

4.6 MCM

```
const ll N = 1005;
ll d[N];
ll dp[N][N], mark[N][N];

ll MCM(ll i, ll j)
```

```
{
    if (i == j)
        return dp[i][j] = 0;
    if (dp[i][j] != -1)
        return dp[i][j];
    ll mn = inf;
    for (ll k = i; k < j; k++)
    {
        ll x = mn;
        mn = min(mn, MCM(i, k) + MCM(k
+ 1, j) + d[i - 1] * d[k] * d[j]);
        if (x != mn)
            mark[i][j] = k;
    }
    return dp[i][j] = mn;
}
```

5. Graph Theory

5.1 Knight Moves

```
ll X[8]={2,1,-1,-2,-2,-1,1,2};
ll Y[8]={1,2,2,1,-1,-2,-2,-1};
```

5.2 SPFA (Shortest Path) O(VxE)

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
ll q[3001] = {0}; // queue for node
ll d[1001] = {0}; // record shortest
path from start to ith node
bool f[1001] = {0};
ll a[1001][1001] = {0}; // adjacency
list
ll w[1001][1001] = {0}; // adjacency
matrix
void SPFA(ll v0);
ll main(void)
{
    ll n = 0, m = 0;
    cin >> n >> m;
    for (ll i = 1; i <= m; i++)
    {
        ll x = 0, y = 0, z = 0;
        cin >> x >> y >> z; // node x
to node y has weight z
        a[x][0]++;
        a[x][a[x][0]] = y;
        w[x][y] = z;
        // for undirected graph
        a[x][0]++;
        a[y][a[y][0]] = x;
        w[y][x] = z;
    }
    ll s = 0, e = 0;
    cin >> s >> e; // s: start, e: end
    SPFA(s);
    cout << d[e] << endl;
    return 0;
}
void SPFA(ll v0)
{
    ll t, h, u, v;
    for (ll i = 0; i < 1001; i++)
        d[i] = INT_MAX;
    for (ll i = 0; i < 1001; i++)
        f[i] = false;
    d[v0] = 0;
    h = 0;
    t = 1;
    q[1] = v0;
    f[v0] = true;
    while (h != t)
    {
        h++;
        if (h > 3000)
            h = 1;
        u = q[h];
        for (ll j = 1; j <= a[u][0];
j++)
        {
            v = a[u][j];
            if (d[u] + w[u][v] < d[v])
// change to > if calculating longest
path
            {
                d[v] = d[u] + w[u][v];
                if (!f[v])
                {
                    t++;
                    if (t > 3000)
                        t = 1;
                    q[t] = v;
                    f[v] = true;
                }
            }
        }
        f[u] = false;
    }
}
```

5.3 Floyd-Warshall algorithm – shortest path of all pairs O(n^3)

```
// map[i][j]=infinity at start
void floyd()
{
    for (ll k=1; k<=n; k++)
        for (ll i=1; i<=n; i++)
            for (ll j=1; j<=n; j++)
                if (i!=j && j!=k &&
i!=k)
```

```
                    if
(map[i][k]+map[k][j]<map[i][j])
      map[i][j]=map[i][k]+map[k][j];;}
```

5.4 Prims- Hasnat

```
typedef pair<ll,pair<ll,ll>> pairUV;
map<ll, bool> visited;
map<ll, vector<pair<ll, ll>>> adj;
void Prims() {
    ll sum = 0, c = 0;
    vector<pairUV> ans;
    priority_queue<pairUV,
vector<pairUV>, greater<pairUV>> pq;
    pq.push({0, {1, -1}});
    while (!pq.empty()) {
        pairUV k = pq.top();
        pq.pop();
        ll u = k.second.first;
        ll v = k.second.second;
        ll wt = k.first;
        if (visited[u])
            continue;
        sum += wt;
        visited[u] = 1;
        if (v != -1)
            ans.pb({wt, {u, v}});
        for (auto it : adj[u]) {
            ll adjNode = it.first;
            ll adjwt = it.second;
            if (!visited[adjNode])
                pq.push({adjwt,
{adjNode, u}});
        }
    }
}
```

5.5 Prims – minimum spanning tree o(ElogV)-Rizu Bhai

```
ll d[1001] = {0};
bool v[1001] = {0};
ll a[1001][1001] = {0};
ll main(void){
    ll n = 0;
    cin >> n;
    for (ll i = 1; i <= n; i++)
    {
        ll x = 0, y = 0, z = 0;
        cin >> x >> y >> z;
        a[x][y] = z;
    }
    for (ll i = 1; i <= n; i++)
        for (ll j = 1; j <= n; j++)
            if (a[i][j] == 0)
                a[i][j] =INT_MAX;
    cout << prim(1, n) << endl;}
ll prim(ll u, ll n){
    ll mst = 0, k;
    for (ll i = 0; i < d.length; i++)
        d[i] =INT_MAX;
    for (ll i = 0; i < v.length; i++)
        v[i] = false;
    d[u] = 0;
    ll i = u;
    while (i != 0){
        v[i] = true;
        k = 0;
        mst += d[i];
        for (ll j = 1; j <= n; j++)
            if (!v[j])
            {
                if (a[i][j] < d[j])
                    d[j] = a[i][j];
                if (d[j] < d[k])
                    k = j;
            }
        i = k;}
    return mst;}
```

5.6 Kruskal

```
#include<bits/stdc++.h>
#define ll long long int
using namespace std;
ll n,e;
class DSU{
    ll* parent;
    ll* _size;
public:
    DSU(ll n){
        parent = new ll[n+1];
        _size = new ll[n+1];
        for(ll i=1;i<=n;i++){
            parent[i]=i;
            _size[i]=1;
        }
    }
ll find_set(ll x){
        if(x==parent[x]) return x;
        ll y=find_set(parent[x]);
        parent[x]=y;
        return y;
    }

    void Union(ll x, ll y){
        ll rx=find_set(x);
        ll ry=find_set(y);
        if(rx==ry) return;
        if(_size[rx]<=_size[ry]){
            parent[rx]=parent[ry];
            _size[ry]+=_size[rx];
        }
        else{
            parent[ry]=parent[rx];
            _size[rx]+=_size[ry];
        }
    }

    ~DSU(){
        delete parent;
        delete _size;
    }
};
ll
Kruskal(pair<ll,pair<ll,ll>>edges[]){
    DSU d(n);
    sort(edges,edges+n+1);
    ll weight=0;
    for(ll i=0;i<e;i++){
        ll w=edges[i].first;
        ll u=edges[i].second.first;
        ll v=edges[i].second.second;

if(d.find_set(u)!=d.find_set(v)){
            weight+=w;
            d.Union(u,v);
        }
    }
    return weight;
}
int main(){
    cin>>n>>e;
    pair<ll,pair<ll,ll>>edges[e];
    for(ll i=0;i<e;i++){
        ll u,v,w; cin>>u>>v>>w;
        edges[i].first=w;
        edges[i].second.first=u;
        edges[i].second.second=v;
    }
    ll ans=Kruskal(edges);
    cout<<ans<<"\n";
}
```

5.7 DSU:

```
#For every i, set parent[i]=I ans
size[i]=1
ll find_set(ll x){
    if(parent[x]==x) return x;
    ll y=find_set(parent[x]);
    parent[x]=y;
    return y;
}
void Union(ll x, ll y){
    x=find_set(x); y=find_set(y);
    if(x==y) return;
    if(Size[x]>Size[y]) swap(x,y);
    parent[x]=y;
    Size[y]+=Size[x];
}
```

5.8 Topological sort:

```
// Find any solution of topological
sort.
#include <iostream>
using namespace std;
ll f[100] = {0}, ans[100] = {0};
bool g[100][100] = {0}, v[100] = {0};
ll n = 0, m = 0;
void dfs(ll k){
    ll i = 0;
    v[k] = true;
    for (ll i = 1; i <= n; i++)
        if (g[k][i] && !v[i])
            dfs(i);
    m++;
    ans[m] = k;}
ll main(void){
    cin >> n >> m;
    for (ll i = 1; i <= m; i++)
    {
        ll x = 0, y = 0;
        cin >> x >> y;
        g[y][x] = true;
    }
    m = 0;
    for (ll i = 1; i <= n; i++)
        if (!v[i])
            dfs(i);
    for (ll i = 1; i <= n; i++)
        cout << ans[i] << endl;
    return 0;}
```

5.9 Dijkstra

```
map<ll, vector<pair<ll, ll>>> m;
map<ll, ll> dist;
#define pairi pair<ll, ll>
void dijkstra(ll src, ll n) {
    priority_queue<pairi,
vector<pairi>, greater<pairi>> pq;
    pq.push({0, src});
    dist[src] = 0;
    vector<ll> dis(n, inf);
    dis[src] = 0;
    while (!pq.empty()) {
        ll u = pq.top().second;
        pq.pop();
        for (ll i = 0; i < m[u].size();
i++) {
            ll wt = m[u][i].second;
            ll v = m[u][i].first;
            if (dis[v] > dis[u] + wt) {
                dis[v] = dis[u] + wt;
                pq.push({dis[v], v});
                dist[v] = dis[u] + wt;
            }
        }
    }
}
```

5.10 Rerooting:

```
map<ll, vector<ll>> m;
ll dp[1000001], dp1[1000001],
sub[1000001], n;
void dfs(ll x, ll parent) {
    dp[x] = 0;
    sub[x] = 1;
    for (ll i = 0; i < m[x].size();
i++) {
        if (m[x][i] != parent) {
            dfs(m[x][i], x);
            sub[x] += sub[m[x][i]];
            dp[x] += dp[m[x][i]] +
sub[m[x][i]];
        }
    }
}
void dfs1(ll x, ll parent, ll carry) {
    dp1[x] = dp[x] + carry;
    sub[x] = 1;
    for (ll i = 0; i < m[x].size();
i++) {
        if (m[x][i] != parent) {
            ll parent_dp = dp1[x];
            parent_dp = dp[m[x][i]] +
sub[m[x][i]];
            ll parent_sub = (n -
sub[m[x][i]]);
            ll new_carry = parent_dp +
parent_sub;
            dfs1(m[x][i], x,
new_carry);
        }
    }
}
ll main() {
    ll x, y, n;
    cin >> n;
    for (ll i = 0; i < n - 1; i++) {
        cin >> x >> y;
        m[x].pb(y);
        m[y].pb(x);
    }
    dfs(1, -1);
    dfs1(1, -1, 0);
    for (ll i = 0; i < n; i++) {
        cout << i + 1 << " " << dp[i +
1] << "\n";
    }
    m.clear();
    return 0;
}
```

5.11 Bipartite Graph Test:

```
bool dfs(int v, int c)
{
      vis[v]=1;
      col[v]=c;
      for(int child : ar[v]){
            if(vis[child]==0){
            if(dfs(child,c^1)==false)
                  return false;
            }
            else

      if(col[v]==col[child])
                              return false;
      }
  return true;
}
```

5.12 Euler Tour:

```
map<ll, vector<ll>> m;
map<ll, ll> vis, dis, discover, finish;
map<ll, ll> par;
ll hascycle = 0, pos = 0;
vector<ll> eulertour;
void dfs(ll st, ll parent = -1)
{
    vis[st] = 1;
    eulertour.pb(st);
    discover[pos] = st;
    pos++;
    for (ll i = 0; i < m[st].size();
i++)
    {
        ll cur = m[st][i];
        if (!vis[cur])
        {
            dfs(cur, st);
            par[cur] = st;
            dis[cur] = dis[par[cur]] +
1;
        }
        else if (vis[st] && cur !=
parent)
            hascycle = 1;
        ;
    }
    eulertour.pb(st);
    finish[pos] = st;
    pos++;
}
int main()
```

```
{
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);
    cout.tie(NULL);
    ll i, j, k, n, s, f, t, x, y, e, w,
c;
    s = 0, f = 0, c = 0;
    cin >> n >> e;
    for (i = 0; i < e; i++)
    {
        cin >> x >> y;
        m[x].pb(y);
        m[y].pb(x);
    }
    for (auto it = m.begin(); it !=
m.end(); it++)
    {
        if (!vis[it->first])
        {
            dfs(it->first);
        }
    }
    if (hascycle)
        cout << "Cyclic\n";
    else
        cout << "Not Cyclic\n";
    for (i = 0; i < pos; i++)
    {
        cout << eulertour[i] << " ";
    }
    return 0;
}
```

6. Range Quarey:

6.1 Segment Tree:

```
vector<ll> v(2*1e5 +5),seg(4*1e5 + 5);
void build(ll ti, ll low, ll high){
    if (high == low){
        seg[ti] = v[low];
        return;
    }
    ll mid = (low + high) / 2;
    build(2 * ti + 1, low, mid);
    build(2 * ti + 2, mid + 1, high);
    seg[ti] = seg[2*ti+1]+seg[ti*2+2];
}
//tree left, tree right, query left,
query right, index
ll findValue(ll tl, ll tr, ll ql, ll
qr, ll ti){
    if (tl > qr or tr < ql)
        return 0;(sum, xor)
      // return INT_MAX;(min)
      // return INT_MIN;(max)
    if (tl >= ql and tr <= qr)
        return seg[ti];
    ll mid = (tl + tr) / 2;
    ll l = findValue(tl, mid, ql, qr, 2
* ti + 1);
    ll r = findValue(mid + 1, tr, ql,
qr, 2 * ti + 2);
    return l + r;(sum)
    // return min(l,r);
    // return max(l,r);
}
void update(ll ti, ll low, ll high, ll
id, ll val){
    if (id > high or id < low)
        return;
    if (id == high and high == low){
        seg[ti] = val;
        return;
    }
    ll mid = (low + high) / 2;
    update(2 * ti + 1, low, mid, id,
val);
    update(2 * ti + 2, mid + 1, high,
id, val);
    seg[ti] = (seg[2 * ti + 1] + seg[ti
* 2 + 2]);
}
```

6.2 Fenwick Tree:

```
struct FenwickTree{
    vector<ll> bit; // binary indexed
tree
    ll n;
    FenwickTree(ll n){
        this->n = n;
        bit.assign(n, 0);}
    FenwickTree(vector<ll> const &a) :
FenwickTree(a.size()){
        for (size_t i = 0; i <
a.size(); i++)
            add(i, a[i]);}
    ll sum(ll r){
        ll ret = 0;
        for (; r >= 0; r = (r & (r +
1)) - 1)
            ret += bit[r];
        return ret;}
    ll sum(ll l, ll r){
        return sum(r) - sum(l - 1);}
    void add(ll idx, ll delta){
        for (; idx < n; idx = idx |
(idx + 1))
            bit[idx] += delta;}};
```

//in main func

```
ll n,q;
    cin>>n>>q;
    vector<ll>arr(n+1),dif(n+1);
    for(ll i=1; i<=n; ++i) cin>>arr[i];
    dif[1]=arr[1];
    for(ll i=2; i<=n; ++i){
        dif[i]=arr[i]-arr[i-1];}
    FenwickTree st(dif);
    while(q--){
        ll x; cin>>x;
        if(x==1){
            ll a,b,c;
            cin>>a>>b>>c;
            st.add(a,c);
            st.add(b+1,-c);}
        else{
            ll a;
            cin>>a;
            cout<<st.sum(a)<<nl;}}
```

6.3 Lazy Segment Tree:

```
template <class T>
class LazySegmentTree {
private:
    T n;
    vector<T> tree;
    vector<T> lazy;
    void build(vector<T>& arr, T v, T
tl, T tr) {
        if (tl == tr) {
            tree[v] = arr[tl];
        } else {
            T tm = (tl + tr) / 2;
            build(arr, v * 2, tl, tm);
            build(arr, v * 2 + 1, tm +
1, tr);
            tree[v] = tree[v * 2] +
tree[v * 2 + 1];
        }
    }
    void push(T v, T tl, T tr) {
        if (lazy[v] != 0) {
            tree[v] += (tr - tl + 1) *
lazy[v];
            if (tl != tr) {
                lazy[v * 2] += lazy[v];
                lazy[v * 2 + 1] +=
lazy[v];
            }
            lazy[v] = 0;
        }
    }
    void update(T v, T tl, T tr, T l, T
r, T val) {
        if (l > r) return;
        if (l == tl && r == tr) {
            lazy[v] += val;
            push(v, tl, tr);
        } else {
            push(v, tl, tr);
            T tm = (tl + tr) / 2;
            update(v * 2, tl, tm, l,
min(r, tm), val);
            update(v * 2 + 1, tm + 1,
tr, max(l, tm + 1), r, val);
            tree[v] = tree[v * 2] +
tree[v * 2 + 1];
        }
    }
    T query(T v, T tl, T tr, T l, T r)
{
        if (l > r) return 0; // Return
0 for invalid queries
        if (l <= tl && tr <= r) {
            return tree[v];
        } else {
            push(v, tl, tr);
            T tm = (tl + tr) / 2;
            T left_sum = query(v * 2,
tl, tm, l, min(r, tm));
            T right_sum = query(v * 2 +
1, tm + 1, tr, max(l, tm + 1), r);
            return left_sum +
right_sum;
        }
    }
public:
    LazySegmentTree(vector<T>& arr) {
        n = arr.size();
        tree.resize(4 * n);
        lazy.resize(4 * n);
        build(arr, 1, 0, n - 1);
    }
    void updateRange(T l, T r, T val) {
        update(1, 0, n - 1, l, r, val);
    }
    T queryRange(T l, T r) {
        return query(1, 0, n - 1, l,
r);
    }
};
```

7 Game Theory:

7.1 Nim Game:

The current player has a winning strategy if and only if the xor-sum of the pile sizes is non-zero.

7.2 Miser Nim:

-Last player to remove stones loses.
-Winning state if xor-sum of pile sizes is non-zero.
-Exception: Each pile has one stone only.
-Winning strategy: If there is only one pile of size greater than one,take all or all but one from that pile leaving an odd number one-size piles.
Otherwise, same as normal nim.

7.3 Grundy's Game:

The starting configuration is a single heap of objects. The two players take turn splitting a single heap into two heaps of different sizes. The player who can't make a move loses./ **In each turn, a player can pick any pile and divide it into two unequal piles.**
If a player cannot do so, he/she loses the game.

```
int mex(vector<int> v) {
	sort(v.begin(), v.end());
	int ret = 0;
	for(int i=0; i<(int) v.size(); ++i) {
		if(v[i] == ret) ++ret;
		else if(v[i] > ret) break;
	}
	return ret;
}
const int N = 1e3 + 7;
int dp[N];
int g(int n) {
	if(n == 0) return 0;
	if(dp[n] != -1) return dp[n];

	vector<int> gsub;
	for(int i=1; i<n-i; ++i) {
		int cur = g(i) xor g(n-i);
		gsub.push_back(cur);
	}
	dp[n] = mex(gsub);
	return dp[n];
}
int main() {
	memset(dp, -1, sizeof dp);
	int n;
	while(cin >> n) {
		if(g(n) > 0) cout << "First\n";
		else cout << "Second\n";
	}
}
```

7.4 Again Stone Game:

Alice and Bob are playing a stone game. Initially there are n piles of stones and each pile contains some stone. Alice stars the game and they alternate moves. In each move, a player has to select any pile and should remove at least one and no more than half stones from that pile. So, for example if a pile contains 10 stones, then a player can take at least 1 and at most 5 stones from that pile. If a pile contains 7 stones; at most 3 stones from that pile can be removed.

```
bool t[N];
ll mex(const vector<ll> &grd)
{
	for(auto it : grd)
	{
		t[it]=true;
	}
	ll res=0;
	while(t[res]) res++;
	for(auto it : grd)
	{
		t[it]=false;
	}
	return res;

}
ll dp[N];
ll g(ll n)
{
	if(n<=1) return 0;
	ll &ret=dp[n];
       if(ret!=-1) return ret;
	vector<ll> grd;

	for(int i=1;i<=n/2;i++)
	{
		ll x=g(n-i);
	       // dbg3(i,n-i,x);
		grd.push_back(x);

	}
	ll ans=mex(grd);
	return ret=ans;
}
ll get_g(ll n)
{
	if(n<2) return 0;
	if(n%2==0) return n/2;
	return get_g(n/2);
}
void solve()
```

```
{
 ll n;

 cin>>n;
 ll ans=0;
 loop(i,0,n)
 {
         ll x;
         cin>>x;
        ll p=get_g(x);
        ans^=p;
       // dbg1(p)
 }
 if(ans)
 {
         cout<<"Alice"<<endl;
 }
 else
 cout<<"Bob"<<endl;
}
```

8 Extra

8.1 Ordered Set:

```
#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>

using namespace std;
using namespace __gnu_pbds;

typedef tree<int, null_type, less<int>,
rb_tree_tag,
tree_order_statistics_node_update>
pbds; // find_by_order, order_of_key
// finding kth element - 4th query
*A.find_by_order(0)--- index 0 er value
// finding number of elements smaller
than X
A.order_of_key(6) --- 6 er smaller
kotogulo elements
```

8.2 Multiply Large Numbers represented as Strings

```
#include <bits/stdc++.h>
using namespace std;
// Multiplies str1 and str2, and prints
result.
string multiply(string num1, string
num2){
    int len1 = num1.size();
    int len2 = num2.size();
    if (len1 == 0 || len2 == 0)
        return "0";
    // will keep the result number in
vector
    // in reverse order
    vector<int> result(len1 + len2, 0);
    // Below two indexes are used to
find positions
    // in result.
    int i_n1 = 0;
    int i_n2 = 0;
    // Go from right to left in num1
    for (int i = len1 - 1; i >= 0; i--
){
        int carry = 0;
        int n1 = num1[i] - '0';
        // To shift position to left
after every
        // multiplication of a digit in
num2
        i_n2 = 0;
        // Go from right to left in
num2
        for (int j = len2 - 1; j >= 0;
j--){
            // Take current digit of
second number
            int n2 = num2[j] - '0';
            // Multiply with current
digit of first number
            // and add result to
previously stored result
            // at current position.
            int sum = n1 * n2 +
result[i_n1 + i_n2] + carry;
            // Carry for next iteration
            carry = sum / 10;
            // Store result
            result[i_n1 + i_n2] = sum %
10;
            i_n2++;
        }
        // store carry in next cell
        if (carry > 0)
            result[i_n1 + i_n2] +=
carry;
        // To shift position to left
after every
        // multiplication of a digit in
num1.
        i_n1++;
    }
    // ignore '0's from the right
    int i = result.size() - 1;
    while (i >= 0 && result[i] == 0)
        i--;
    // If all were '0's - means either
both or
    // one of num1 or num2 were '0'
    if (i == -1)
        return "0";
    // generate the result string
    string s = "";
    while (i >= 0)
        s += std::to_string(result[i--
]);
    return s;
}
// Driver code
int main(){
    string str1 =
"1235421415454545454545454544";
    string str2 =
"1714546546546545454544548544544545";
    cin >> str1 >> str2;
    if ((str1.at(0) == '-' ||
str2.at(0) == '-') &&
        (str1.at(0) != '-' ||
str2.at(0) != '-'))
        cout << "-";
    if (str1.at(0) == '-')
        str1 = str1.substr(1);
    if (str2.at(0) == '-')
        str2 = str2.substr(1);
    cout << multiply(str1, str2);
    return 0;
}
```

8.3 Sum of two large numbers:

```
#include <bits/stdc++.h>
using namespace std;
// Function for finding sum of larger
numbers
string findSum(string str1, string
str2){
    // Before proceeding further, make
sure length
    // of str2 is larger.
    if (str1.length() > str2.length())
        swap(str1, str2);
    // Take an empty string for storing
result
    string str = "";
    // Calculate length of both string
    int n1 = str1.length(), n2 =
str2.length();
    int diff = n2 - n1;
    // Initially take carry zero
    int carry = 0;
    // Traverse from end of both
strings
    for (int i = n1 - 1; i >= 0; i--){
        // Do school mathematics,
compute sum of
        // current digits and carry
        int sum = ((str1[i] - '0') +
(str2[i + diff] - '0') + carry);
        str.push_back(sum % 10 + '0');
        carry = sum / 10;}
    // Add remaining digits of str2[]
    for (int i = n2 - n1 - 1; i >= 0;
i--){
        int sum = ((str2[i] - '0') +
carry);
        str.push_back(sum % 10 + '0');
        carry = sum / 10;}
    // Add remaining carry
    if (carry)
        str.push_back(carry + '0');
    // reverse resultant string
    reverse(str.begin(), str.end());
    return str;}
// Driver code
int main(){
    string str1 = "12";
    string str2 = "198111";
    cin >> str1 >> str2;
    cout << findSum(str1, str2);
    return 0;}
```

8.4 Divide large number represented as string:

```
#include <bits/stdc++.h>
using namespace std;
// A function to perform division of
large numbers
string longDivision(string number, int
divisor){
    // As result can be very large
store it in string
    string ans;
    // Find prefix of number that is
larger
    // than divisor.
    int idx = 0;
    int temp = number[idx] - '0';
    while (temp < divisor)
        temp = temp * 10 +
(number[++idx] - '0');

    // Repeatedly divide divisor with
temp. After
    // every division, update temp to
include one
    // more digit.
    while (number.size() > idx) {
        // Store result in answer i.e.
temp / divisor
        ans += (temp / divisor) + '0';

        // Take next digit of number
        temp = (temp % divisor) * 10 +
number[++idx] - '0';}

    // If divisor is greater than
number
    if (ans.length() == 0)
        return "0";
    // else return ans
    return ans;}
// Driver program to test
longDivision()
int main(){
    string number =
"1248163264128256512";
    int divisor = 125;
    cout << longDivision(number,
divisor);
    return 0;}
```

8.5 Subtraction of two large numbers:

```
#include <bits/stdc++.h>
using namespace std;
// Returns true if str1 is smaller than
str2,
// else false.
bool isSmaller(string str1, string
str2){
    // Calculate lengths of both string
    int n1 = str1.length(), n2 =
str2.length();
    if (n1 < n2)
        return true;
    if (n2 < n1)
        return false;
    for (int i = 0; i < n1; i++) {
        if (str1[i] < str2[i])
            return true;
        else if (str1[i] > str2[i])
            return false;}
    return false;}
// Function for finding difference of
larger numbers
string findDiff(string str1, string
str2){
    // Before proceeding further, make
sure str1
    // is not smaller
    if (isSmaller(str1, str2))
        swap(str1, str2);
    // Take an empty string for storing
result
    string str = "";
    // Calculate lengths of both string
    int n1 = str1.length(), n2 =
str2.length();
    int diff = n1 - n2;
    // Initially take carry zero
    int carry = 0;
    // Traverse from end of both
strings
    for (int i = n2 - 1; i >= 0; i--) {
        // Do school mathematics,
compute difference of
        // current digits and carry
        int sub = ((str1[i + diff] -
'0') - (str2[i] - '0')
                     - carry);
        if (sub < 0) {
            sub = sub + 10;
            carry = 1;}
        else
            carry = 0;
        str.push_back(sub + '0');}
    // subtract remaining digits of
str1[]
    for (int i = n1 - n2 - 1; i >= 0;
i--) {
        if (str1[i] == '0' && carry) {
            str.push_back('9');
            continue;}
        int sub = ((str1[i] - '0') -
carry);
        if (i > 0 || sub > 0) // remove
preceding 0's
            str.push_back(sub + '0');
        carry = 0;}
    // reverse resultant string
    reverse(str.begin(), str.end());
    return str;}
// Driver code
int main(){
    string str1 = "88";
    string str2 = "1079";
    // Function call
    cout << findDiff(str1, str2);
    return 0;}
```

8.6 2D Prefix sum:

```
#include <bits/stdc++.h>
using namespace std;
const int N = 2005;
int a[N][N], pref[N][N];
int main(){
    int n, m;
    cin >> n >> m;
    for (int i = 1; i <= n; i++){
        for (int j = 1; j <= m; j++){
            cin >> a[i][j];
        }
    }
    // precal
    for (int x = 1; x <= n; x++){
        for (int y = 1; y <= m; y++){
            pref[x][y] = a[x][y] +
pref[x][y - 1] + pref[x - 1][y] -
pref[x - 1][y - 1];
        }
    }
    int q;
    cin >> q;
    while (q--){
        int x1, y1, x2, y2;
        cin >> x1 >> y1 >> x2 >> y2;
        int sum = pref[x2][y2] -
pref[x1 - 1][y2] - pref[x2][y1 - 1] +
pref[x1 - 1][y1 - 1];
        cout << sum << "\n";
    }
    return 0;}
```