## **Association Rules**

Mining Massive Datasets
Prof. Carlos Castillo
Topic 12



#### Sources

- Data Mining, The Textbook (2015) by Charu Aggarwal (Chapters 4, 5) – slides by Lijun Zhang
- Mining of Massive Datasets  $2^{nd}$  edition (2014) by Leskovec et al. (Chapter 6) slides
- Data Mining Concepts and Techniques, 3<sup>rd</sup> edition (2011) by Han et al. (Chapter 6)
- Introduction to Data Mining 2<sup>nd</sup> edition (2019) by Tan et al. (Chapters 5, 6) slides ch5, slides ch6

## What is a rule

- A rule is of the form X⇒Y
   X and Y are itemsets
- X is the antecedent, Y is the consequent
- The confidence of the rule is:

$$conf(X \Rightarrow Y) = \frac{sup(X \cup Y)}{sup(X)}$$

## Confidence of a rule

• The confidence of the rule  $X \Rightarrow Y$  is:

$$conf(X \Rightarrow Y) = \frac{\sup(X \cup Y)}{\sup(X)}$$

• This is the conditional probability of  $X \cup Y$  occurring in a transaction, given that X occurs in the transaction

# Confidence of a rule (cont.)

```
tid Set of items

1    Bread, Jam, Juice
2    Tofu, Juice, Tomatoes
3    Bread, Strawberries, Tofu, Juice
4    Tofu, Juice, Tomatoes
5    Strawberries, Juice, Tomatoes
```

```
conf(\{tofu, juice\} \Rightarrow \{tomatoes\}) = ?
```

## Lift of a rule

• The **lift** of the rule  $X \Rightarrow Y$  is:

$$\operatorname{lift}(X \Rightarrow Y) = \frac{\sup(X \cup Y)}{\sup(X) \sup(Y)}$$

 This is the ratio between the observed support and the expected support if X and Y were independent

#### **Exercise**

$$\operatorname{conf}(X \Rightarrow Y) = \frac{\sup(X \cup Y)}{\sup(X)}$$

$$\operatorname{lift}(X \Rightarrow Y) = \frac{\sup(X \cup Y)}{\sup(X)\sup(Y)}$$

Answer in Nearpod draw-it Code to be given in class



Rule	$\begin{array}{c} \textbf{Support} \\ \sup(X \cup Y) \end{array}$	Confidence	Lift
$A \Rightarrow D$			
$C \Rightarrow A$			
$A \Rightarrow C$			
$B \& C \Rightarrow D$			

# Association rule (minsup, minconf)

Let X, Y be two itemsets; the rule X⇒Y is an
 association rule of minimum support minsup
 and minimum confidence minconf if:

```
\sup(X\Rightarrow Y) \ge \min\sup
and
\operatorname{conf}(X\Rightarrow Y) \ge \min \operatorname{conf}
```

# Summary

# Things to remember

- Association rule of minsup and minconf
- The concepts of confidence and lift

### Exercises for TT11-TT12

- Data Mining, The Textbook (2015) by Charu Aggarwal
  - Exercises  $4.9 \rightarrow 1-3, 5, 7-8$
  - Exercises  $5.7 \rightarrow 1-5$
- Mining of Massive Datasets 2<sup>nd</sup> edition (2014) by Leskovec et al.
  - Exercises 6.1.5  $\rightarrow$  6.1.1-6.1.7
- Introduction to Data Mining  $2^{nd}$  edition (2019) by Tan et al.
  - Exercises  $5.10 \rightarrow 2-7$