

Task 3

The best case of my the Dijkstra's algorithm would give $O(1)$ time complexity as it checks in the first line if the adjacency list is empty.

If there are N nodes, initializing $\text{dist}[]$, $\text{parent}[]$ and $\text{explored}[]$ take $O(N)$ time.

We are using a min heap to give the least weighted path. which takes $N \log N$ time. And traversing through the M edges takes $\log(N+M)$ time.

The while loop depends on the number of edges which is N so its time complexity is $O(N)$. Using a min-heap to extract the minimum edge takes $\log(N)$ time in the while loop and the second for-loop runs to traverse the edges so its time is $O(M)$.

Overall time complexity is:

$$O(N) + N \log N + O(N+M)$$

$O(N \log N)$ is the dominant figure so the time complexity of this algorithm is $O(N \log N)$

The same algorithm is used in Task 2 with a minor change. I used a path string and use a while loop to create a string from parent[] and return the reverse string. The time complexity would be

$O(N)$. which adds to $O(N) + N \log N + O(N+M)$

However, the final time complexity is still $O(N \log N)$

BFS algorithm is used if number of

Titan is 1. Its time complexity is $O(N+M)$.

The inputs will be N and M where

N is the number of place and M numbers of path and followed by M lines of pair values to create the graph.