

1

# of trailing zeros in 20!, 21!, 22!, 23!, and 24! will be 4 ( $20/5=4$ ). For 21!, 22!, 23! and 24!, instead of 20 you'll have 21, 22, ... but the result will be the same) --> total of  $4*5=20$  trailing zeros for these 5 terms. (Note here that this won't always be correct: for example 20 and 50 have one trailing zero each but  $20*50=1,000$  has three trailing zeros not two. That's because extra 2 in 20 and extra 5 in 50 "produced" one more trailing zero. In our case though, we won't have any extra 5-s in any factorial, as all are already used for existing trailing zeros);

# of trailing zeros in 25!, 26!, 27!, 28!, and 29! will be  $5+1=6$  ( $25/5+25/5^2=6$ ) --> total of  $6*5=30$  trailing zeros for these 5 terms;

# of trailing zeros in 30!, 31!, 32!, and 33! will be  $6+1=7$  ( $30/5+30/5^2=7$ ) --> total of  $7*4=28$  trailing zeros for these 5 terms;

So,

$$(20! \cdot 21! \cdot 22! \cdot \dots \cdot 33!)^3 = (10^{20} \cdot 10^{30} \cdot 10^{28} \cdot \text{something})^3 = (10^{78} \cdot \text{something})^6 = 10^{468} \cdot \text{something}^6$$

Total of 468 trailing zeros.

Answer: A.

Or as we have  $(\text{something})^6$  then the # of trailing zeros must be multiple of 6 only answer choice A satisfies this.

2

The rate of a certain chemical reaction is directly proportional to the square of the concentration of chemical A present and inversely proportional to the concentration of chemical B present. If the concentration of chemical B is increased by 100%, which of the following is closest to the percent change in the concentration of chemical A required to keep the reaction rate unchanged?

- A 100% decrease
- B 50% decrease
- C 40% decrease
- D 40% increase
- E 50% increase

NOTE: Put directly proportional in nominator and inversely proportional in denominator.

$$RATE = \frac{A^2}{B}, \text{ (well as it's not the exact fraction it should be multiplied by some constant but we can ignore this in our case).}$$

We are told that B increased by 100%, hence in denominator we have 2B. We want the rate to be the same. As rate is directly proportional to the SQUARE of A, A should also increase (nominator) by x percent and increase of A in square should be 2. Which means  $x^2 = 2$  --

$$x \approx 1.41, \text{ which is approximately 40\% increase. } R = \frac{A^2}{B} = \frac{(1.4A)^2}{2B} = \frac{2A^2}{2B}$$

Answer: D.

3

Say there are A gallons of fuel A in the tank, then there would be  $200-A$  gallons of fuel B.

The amount of ethanol in A gallons of fuel A is  $0.12A$ ;

The amount of ethanol in  $200-A$  gallons of fuel B is  $0.16(200-A)$ ;

Since the total amount of ethanol is 30 gallons then  $0.12A + 0.16(200-A) = 30$  -->  $A = 50$ .

Answer: E.