

1

(1) $vw = v^2 \rightarrow vw - v^2 = 0 \rightarrow v(w - v) = 0$: either $v = 0$ or $v = w$, but as we are told that v and w are different integers then this case is out, so $v = 0$. Sufficient.

(2) $w = 2$. Clearly not sufficient.

Answer: A.

2

$x(x-5)(x+2) = 0 \rightarrow x = 0$ or $x = 5$ or $x = -2$. Question is $x < 0$ or is $x = -2$?

(1) $x^2 - 7x \neq 0 \rightarrow x(x-7) \neq 0 \rightarrow x \neq 0$ and $x \neq 7$, so x can be 5 or -2 (from the stem as $x = 0$ is out). Not sufficient.

(2) $x^2 - 2x - 15 \neq 0 \rightarrow (x+3)(x-5) \neq 0 \rightarrow x \neq -3$ and $x \neq 5$, so x can be 0 or -2 (from the stem as $x = 5$ is out). Not sufficient.

(1)+(2) As $x = 0$ and $x = 5$ are out, only value left is $x = -2$, so x is negative. Sufficient.

Answer: C.

3

If $xy > 0$, does $xy - y = 3$?

(1) $xy = 3 \rightarrow$ question becomes: is $3 - y = 3$? or is $y = 0$? Since given that $xy > 0$ (or the same $xy = 3$) then it's clear that $y \neq 0$ so we have the answer NO. Sufficient.

(2) $y - 1 = 0 \rightarrow$ question becomes: is $x = 4$? We don't know that. Not sufficient.

Answer: A.

4

Given: a and b are integers, also $\sqrt{a^3 - a^2 - b} = 7 \rightarrow a^3 - a^2 - b = 49$

(1) $a^2 - a = 12 \rightarrow a = -3$ or $a = 4$. Now, both values of a give an integer solution for b ($b = 85$ or $b = -1$), so both values are valid. Not sufficient.

(2) $b^2 - b = 2 \rightarrow b = -1$ or $b = 2 \rightarrow$ if $b = -1$ then $a^3 - a^2 = 48 \rightarrow a^2(a-1) = 48 \dots a = 4 = \text{integer}$ BUT if $b = 2$ then $a^3 - a^2 = 51 \rightarrow a^2(a-1) = 51 = 3 \cdot 17 \rightarrow$ this equation has no integer solution for a , hence only the first case is valid: $b = -1$ and $a = 4 = \text{integer}$. Sufficient.

Answer: B.

5

Given: x and y are positive integers and $y = \sqrt{9-x} \rightarrow y^2 = 9-x \rightarrow y^2$ is a positive perfect square less than 9: so $y^2 = 4 = 2^2$ if $x = 5$ or $y^2 = 1 = 1^2$ if $x = 8$.

(1) $x < 8 \rightarrow x = 5$ and $y = 2$. Sufficient.

(2) $y > 1 \rightarrow y = 2$. Sufficient.

Answer: D.

