

1

If  $x$  is positive, which of the following could be correct ordering of  $\frac{1}{x}$ ,  $2x$ , and  $x^2$ ?

(I)  $x^2 < 2x < \frac{1}{x}$

(II)  $x^2 < \frac{1}{x} < 2x$

(III)  $2x < x^2 < \frac{1}{x}$

- (a) none
- (b) I only
- (c) III only
- (d) I and II
- (e) I, II and III

2

In a room filled with 7 people, 4 people have exactly 1 sibling in the room and 3 people have exactly 2 siblings in the room. If two individuals are selected from the room at random, what is the probability that those two individuals are NOT siblings?

- A.  $\frac{5}{21}$
- B.  $\frac{3}{7}$
- C.  $\frac{4}{7}$
- D.  $\frac{5}{7}$
- E.  $\frac{16}{21}$

3

At a certain hospital, 75% of the interns receive fewer than 6 hours of sleep and report feeling tired during their shifts. At the same time, 70% of the interns who receive 6 or more hours of sleep report no feelings of tiredness. If 80% of the interns receive fewer than 6 hours of sleep, what percent of the interns report no feelings of tiredness during their shifts?

- A. 6
- B. 14
- C. 19
- D. 20
- E. 81

4

It takes 6 days for 3 women and 2 men working together to complete a work. 3 men would do the same work 5 days sooner than 9 women. How many times does the output of a man exceed that of a woman?

- A. 3 times
- B. 4 times
- C. 5 times
- D. 6 times
- E. 7 times

5

How many positive integers less than 10,000 are there in which the sum of the digits equals 5?

- (A) 31
- (B) 51
- (C) 56
- (D) 62
- (E) 93