

Let the length of Array =  $n$

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④  $i = 1 \quad j = 1, 2, 3, \dots, n$

$i = 2 \quad j = 1, 2, 3, \dots, n$

$i = N \quad (j = 1, \dots, n)$

Since the loop are nested we multiply their complexities:

$$O(N) \times O(N) = O(N^2)$$

Space complexity  $O(1)$ .

⑤ As  ~~$i = 1$~~   
~~loop will execute on~~  
 ~~$i = 2$~~   
~~loop will~~

⑤ The loop runs from  $i = 1$  to  $n$  times. So, the time complexity will be  $O(n)$ .  
Space complexity  $O(1)$ .

⑥ This is also runs from  $i = 1$  to  $n$ , So, the time complexity will be  $O(n)$  and space complexity  $O(1)$  because it only using a single loop variable ( $i$ ) which use constant space.

③ Give time complexity  $O(n^2)$

i) 10  $O(100) \Rightarrow O(10^2)$

So, the algorithm will perform almost 100 operation.

ii) 50  $O(n^2) = O(50^2)$   
it will perform 2500 oper.

iii) 100  $O(n^2) = O(10^4)$   
it will perform 10000 oper -

~~iv) 500~~  $O(n^2) = O(500^2)$   
it will perform 250000 oper so it will take long time

②  $O(\log n) \rightarrow$  i have not study yet  
 but i know because I saw  
 KK video and from there I get  
 to know but still don't know  
 how.

①

⑧

$i = 1$

while ( $i < n$ )

$i = i * 2$

$\therefore$  i is initialize from 1 and the cond<sup>n</sup>  
 is i should be less than n and  
 $i = i * 2$

So,  $i = 1, 2, 4, 8, 16, \dots$

$i = 2^0 \mid i = 2^1 \mid i = 2^2 \mid i = 2^3 \mid \dots$

Power =  $2^k$

$2^k < n$

$k < \log_2 n$

⑨ As the loop runs from 1 to  $n$

Since the loop iterates  $n$  times so,

$$T(n) = O(n).$$

⑩ This loop is also runs from 1 to  $n$

So, the loop iterates  $n$  times so,

$$T(n) = O(n).$$

⑪ As the outer loop is running from 1 to  $k$   
and the inner loop is running from 1 to  $\text{array.length}$   
and inner loop is independent of outer loop.

So, Time Complexity will be

as ~~they~~ the loops are ~~not~~ nested so,

$$TC = O(k \cdot \text{length}(\text{array}))$$

⑫ As outer loop runs from 1 to  $\text{length}(\text{array})$   
Let say  $\text{length}(\text{array})$  be  $n$ .

So, outer loop runs from 1 to  $n$ .

$$\text{if } i=0 \quad j = 1, 2, 3, \dots, n$$

$$i=1 \quad j = 1, 2, 3, \dots, n$$

$$i=n \quad j = \frac{n(n+1)}{2} = \frac{n^2}{2}$$





Ques

23. As the  $\wedge$  loop runs from 1 to  $n$  times,  
and inner loop runs from 1 to  $n$  times;  
and they are nested loop;

$$S_0, TC = O(n \times n) \\ = O(n^2)$$

Ex

24. As this loop runs from 1 to  $\text{length}(\text{matrix})/2$

Let  $\text{length}(\text{matrix}) \rightarrow n$

So,

$$TC = O(n/2)$$

$$\# SC = O(1)$$

the only additional  
space used is  
for temporary  
variables.

$$S_0, TC = O(n)$$

26. As this loop runs from 1 to  $\text{length}(\text{array})$  then

variable do  
not depend on the  
input size and  
memory

$$\text{Let say } \text{length}(\text{array}) = n$$

constant.

$$S_0, TC = O(n), SC = O(1)$$

result

27.  $TC = O(n)$  One input variable ~~is~~ and ~~others~~ they  
will take space, the space of  $i$  will be constant

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$\therefore$  i runs from 1 to  $n$   
and  $i = i * 2$

so, we have already solved.

$$S_0, TC = O(\log n)$$

to n.

$$S_0, SC = O(n)$$

$$SC = O(1)$$

and check if  $1 > 0$

so,  $j = 1-1$   
 $j = 0$

if  $j = 2$  // Space complexity =  $O(1)$

$j = 2$

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$j = 1$

As outer loop runs from 1 to  $\text{length}(\text{array}) - 1$   
 let  $\text{length}(\text{array}) = n$

and 1 to  $(n-1)$

inner loop