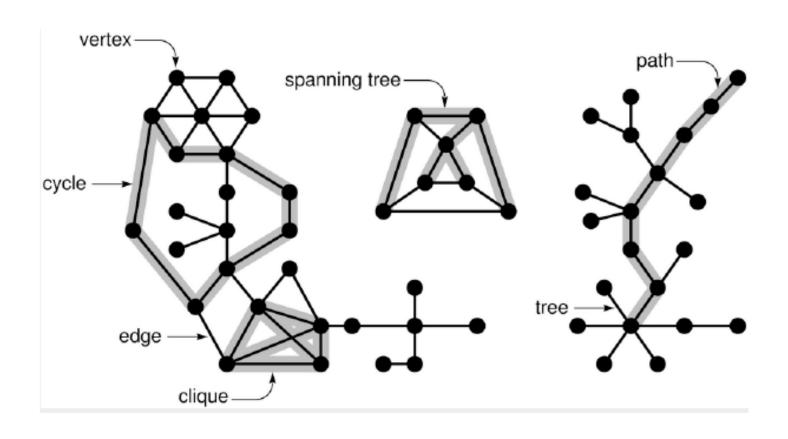
# **Undirected graphs**

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### Undirected graphs

- A graph G=(V, E) where V is a set of vertices connected pairwise by edges E.
- Why study graph algorithms?
  - Interesting and broadly useful abstraction.
  - Challenging branch of computer science and discrete math.
  - Hundreds of graph algorithms known.
  - Thousands of practical applications.
    - Communication, circuits, transportation, scheduling, software systems, internet, games, social network, neural networks, ...

# Graph terminology

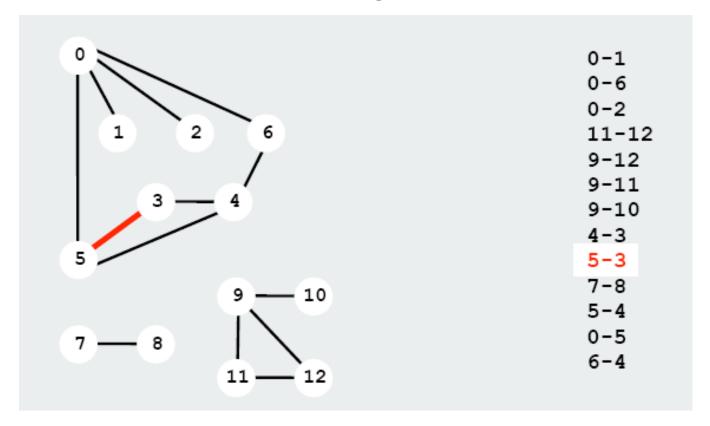


### Some graph-processing problems

- Path: Is there a path between s to t?
- Shortest path: What is the shortest path between s and t?
- Cycle: Is there a cycle in the graph?
- Euler tour: Is there a cycle that uses each edge exactly once?
- Hamilton tour: Is there a cycle that uses each vertex exactly once?
- Connectivity: Is there a way to connect all of the vertices?
- MST: What is the best way to connect all of the vertices?
- Biconnectivity: Is there a vertex whose removal disconnects the graph?

## Graph representation (1)

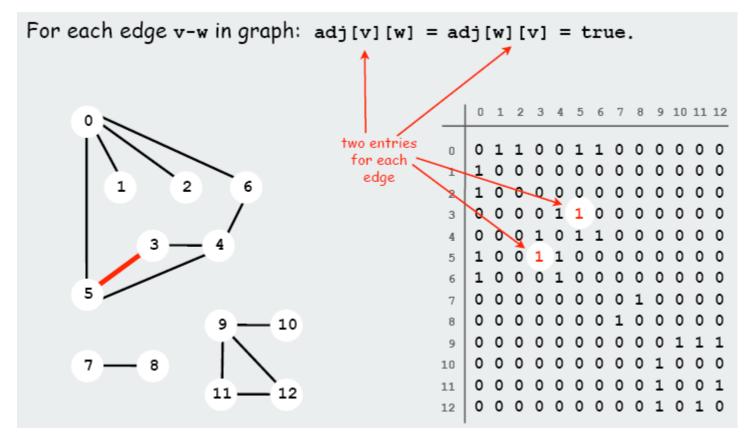
Maintain a list of the edges



Not suitable for searching

## Graph representation (2)

Maintain an adjacency matrix.



Suitable for random accesses to the edges

### A graph data structure

Use a dynamic array to represent a graph as the following

```
typedef struct {
   int * matrix;
   int sizemax;
} Graph;
```

Define the following API

```
Graph createGraph(int sizemax);
void addEdge(Graph graph, int v1, int v2);
int adjacent(Graph graph, int v1, int v2);
int getAdjacentVertices(Graph graph, int vertex, int* output); //
return the number of adjacent vertices.
void dropGraph(Graph graph);
```

#### How to use the API?

```
int i, n, output[100];
Graph g = createGraph(100);
addEdge(g, 0, 1);
addEdge(g, 0, 2);
addEdge(g, 1, 2);
addEdge(g, 1, 3);
n = getAdjacentVertices (g, 1, output);
if (n==0) printf("No adjacent vertices of node 1\n");
else {
  printf("Adjacent vertices of node 1:");
  for (i=0; i<n; i++) printf("%5d", output[i]);
```

#### Quiz 1

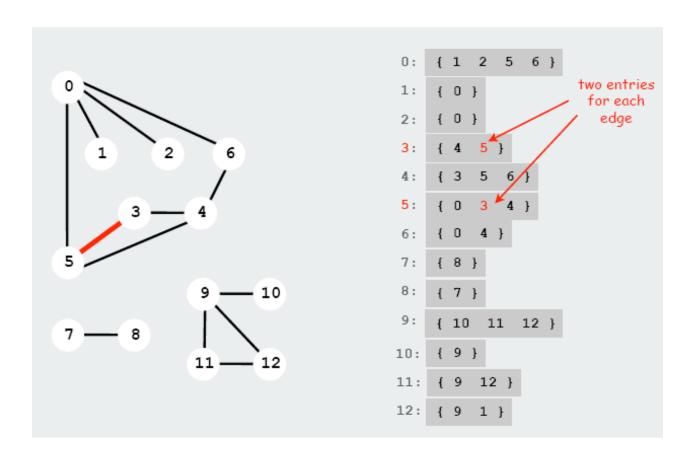
- Write the implementation for the API defined in the previous slide
- Use the example to test your API

# Solution

• graph\_matrix.c

## Graph representation (3)

Maintain an adjacency list.



## Comparison

- Adjacency List is usually preferred, because it provides a compact way to represent sparse graphs – those for which |E| is much less than |V|<sup>2</sup>
- Adjacency Matrix may be preferred when the graph is dense, or when we need to be able to tell quickly if their is an edge connecting two given vertices

### Implementation

- The red black tree can be used to store such a graph where each node in the tree is a vertex and its value is a list of adjacent vertices.
- Such a list of adjacent vertices can be stored in a red black tree as well.

#### Quiz 2

 Rewrite the API defined for graphs using the libfdr library as the following

```
#include "jrb.h"
typedef JRB Graph;
Graph createGraph();
void addEdge(Graph graph, int v1, int v2);
int adjacent(Graph graph, int v1, int v2);
int getAdjacentVertices (Graph graph, int v, int*
  output);
void dropGraph(Graph graph);
```

### Instructions (1)

- To create a graph
   Simply call make\_jrb()
- To add a new edge (v1, v2) to graph g tree = make\_jrb(); jrb\_insert\_int(g, v1, new\_jval\_v(tree)); jrb\_insert\_int(tree, v2, new\_jval\_i(1));

jrb\_insert\_int(tree, v2, new\_jval\_i(1));

 If the node v1 is already allocated in the graph node = jrb\_find\_int(g, v1);
 tree = (JRB) jval\_v(node->val);

### Instructions (2)

To get adjacent vertices of v in graph g

```
node = jrb_find_int(g, v);
tree = (JRB) jval_v(node->val);
total = 0;
jrb_traverse(node, tree)
  output[total++] = jval_i(node->key);
```

To delete/free a graph

```
jrb_traverse(node, graph)
  jrb_free_tree( jval_v(node->val) );
```

# Solution

graph\_jrb.c

#### Homework

 In order to describe the metro lines of a city, we can store the data in a file as the following.

```
[STATIONS]
S1=Name of station 1
S2=Name of station 2
...
[LINES]
M1=S1 S2 S4 S3 S7
M2=S3 S5 S6 S8 S9
```

- Make a program to read such a file and establish the network of metro stations in the memory using the defined API.
- Write a function to find all the stations adjacent to a station given by its name.