

Que 3) A car believes that the percentage of citizens in city ABC that owns a vehicle is 60% or less. A sales manager disagrees with this. He conducted a hypothesis testing surveying 250 residents & found that 170 residents responded yes to owning a vehicle.

- a) State the null & alternate hypothesis    b) At a 10% significance level, is there enough evidence to support the idea that vehicle owner in ABC city is 60% or

less.

Sol.  $H_0 : p_0 \geq 60\%$

$H_1 : p_0 < 60\%$

$x = 170$   
 $n = 250$

$q_0 = 1 - 0.6 = 0.4$   
 $p_0 = 0.6$

$\hat{p} = \frac{x}{n} = \frac{170}{250}$

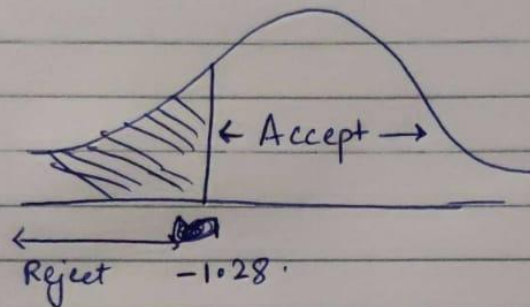
$\hat{p} = 0.68$

$\alpha = 10\%$ ,  $CI = 90\%$

$\alpha = 0.1$

$Z_{\alpha} = -1.28$

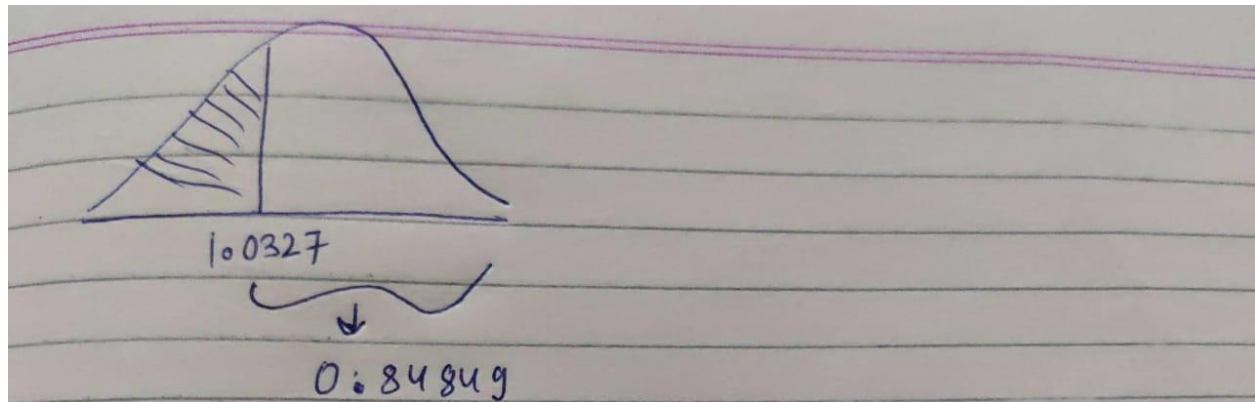
Hence, It is a one-tailed test



So Z proportion test = 
$$\frac{\hat{p} - p_0}{\sqrt{\frac{p_0 \times q_0}{n}}}$$
$$= \frac{0.68 - 0.60}{\sqrt{\frac{0.6 \times 0.4}{250}}}$$

$$= \frac{0.08 \times \sqrt{250}}{\sqrt{0.6 \times 0.4}}$$
$$= \frac{1.2649}{\sqrt{0.6 \times 0.4}}$$
$$= 1.0327$$

$1.0327 > -1.28$  so it ~~reject~~ accept the null hypothesis which means at 90% CI vehicle owner in ABC city is 60% or less.



$$\text{So } p\text{value} = 1 - 0.84849 \\ = 0.15$$

$p\text{value} > \text{significance level}$  so we will accept the null hypothesis,