## **CAB301 Algorithms and Complexity**

## Assignment 1 – Community library manage application for DVDs

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Section 1. an algorithm that you designed for implementing the function "Display the top 10 most frequently borrowed movie DVDs by the members in the descending order of the frequency"

## **1. ALGORITHM** BSTtoArray(Root)

```
//Convert the Binary Search Tree to Array recursively
//Input: Current BST node which can be a root
//Output: An array which contains the item of each nodes
movieArray <- New Empty Movie Array
index <- 0

IF root is not null

If the left child of root is not null

BSTtoArray(Left child, movieArray)

Array[index] = root.Item
index <- index + 1

If the right child of root is not null
```

BSTtoArray(Right child, movieArray)

**Return** movieArray

## **2. ALGORITHM** sortedMovieToBST(Array, Start, End)

//Input: An array which has sorted items of movie DVDs, start point and end point to operate.

//Output: Return the sorted binary search tree with same order of the input array

If start > end

#### Return null

Tree <- new node of binary search tree with the value of array[start]

Tree.right <- sortedMovieToBST(array, start -1, end)</pre>

Return tree

## **3. ALGORITHM** Top10inOrder(Root)

//Input: the tree of the MovieCollection

//Output: Print out binary search tree

If (root == null) return null

Top10inOrder(root.left) // Go to left child

print detail of item of DVD

Top10inOrder(root.right) // Go to right child

## **4. ALGORITHM** quickSort(Array, Start, End)

//Input: The array of Movie from converting Binary Tree and start point and end point of sorting

//Output: Sorted array by descending order

If start < end

Pivot <- the return value of function for partition(Array, start, end)

quickSort (array, start, pivot -1) // call the method for operating left side of tree quickSort (array, pivot + 1, end) // call the method for operating right side of tree

## **ALGORITHM** partition(Array, start, end)

//Input: An array to store the value after sorting by descending order, start point and end point to sort.

//Output: Inclusive index of array to scan and swap the next value of array pivotVal <- The number of times to get borrowed from the last value of array s <- (start point – 1)

for start to end do

// If the time of rented is smaller than the value in the location of pivot if the number of times to get borrowed from array[i] >= pivotVal

$$s = (s + 1)$$

swap array[s] and array[i]

swap array[s + 1] and array[end]

return s + 1

## Section 2. analysis of the time complexity of the algorithm

Time Complexity 1. BSTtoArray

The number of sub problem is 2 which is a, the size of depth is  $\frac{n}{2}$  and the cost of work on outside of recursive is C which is the size of array and index.

As the Master's Theorem,

$$n^{\log_b a} = n^{\log_2 2} = n$$

$$T(n) = 2T\left(\frac{n}{2}\right) + C = O(n)$$

Hence, the time complexity is O(n).

Time Complexity 2. sortedMovieToBST

Let the size of the given array is n, the number of sub problem is 1 which is a and the size of sub problem is n-1.

So, it is same as worst case of Quick sort,

$$T(n) = T(n-1) + C$$

$$= T(n-2) + T(n-1) + C$$

$$= T(n-3) + T(n-2) + T(n-1) + C$$

•••

$$= T(0) + n * \frac{n+1}{2}$$
$$= O(n^2)$$

Time Complexity 3. Top10inOrder

It is depth first traversal. Let the size of depth is  $\frac{n}{2}$  as it is binary search tree, the number

of sub problem is 2 and the constant times which needs to take when it prints out or move the root to left or right is C.

It is same with above proof for BSTtoArray method. Hence,

$$T(n) = 2T\left(\frac{n}{2}\right) + C = O(n)$$

Time Complexity 4. quicksort and partition

Best Time Complexity:  $\Theta(nlog_2 n)$ 

Average Time Complexity:  $O(nlog_2 n)$  or  $C_{avg}(n) \in \Theta(nlog n)$ 

Let the execution time is T(n) when the given array which contains number of item (Array[n]) and the time of comparison is n before calling a recursion function, so, S(n) = n. The recursive function will be break when the items in array is smaller than 1, it can be represented when  $n^h = 1$ , the recursive function will not be called anymore. Hence,

$$h = \log_2 n, T(n) = O(n\log_2 n)$$

Or it can be represented like below as well.

When the pivot value can split the array with same lengths which can be represented as  $\frac{n}{2}$  and the constant times for storing the sorted values into other array and partitioning which is n. When  $k = log_2 n_i$ 

T(n) = 2T(n/2) + n

$$= 2\left(2T\left(\frac{n}{2}\right) + \frac{n}{2}\right) + n$$

$$= 2^{2}\left(T\left(\frac{n}{2^{2}}\right)\right) + n + n$$
...
$$= 2^{k}T\left(\frac{n}{2^{k}}\right) + n$$

$$= nT\left(\frac{n}{n}\right) + n\log n$$

$$= nT(1) + n\log_{2} n$$

 $= O(nlog_2 n)$ 

Worst time complexity:  $O(n^2)$  or  $C_{worst}(n) \in \Theta(n^2)$ 

The worst cases of time complexity are when the data is already sorted by ascending or descending order when the data is given. So,

$$T(n) = T(n-1) + C$$

$$= T(n-2) + T(n-1) + C$$

$$= T(n-3) + T(n-2) + T(n-1) + C$$
...
$$= T(0) + n * \frac{n+1}{2}$$

$$= O(n^2)$$

# Section 3. your functional testing results - screenshots for each of the functional tests.

#### <Main>

## 1. Staff Login

As the Id of staff is 'staff' and the passwords of staff is 'today123', if staff entered different values, it shows error message on screen.

#### 2. Staff Menu

#### 2.1 Add movie

```
Please make a selection (1-4, or 0 to exit)

1
Enter Title:
A
Enter Starring:
a
Enter Director:
arin
Choose Genre by number:
1. Drama
2. Adventure
3. Family
4. Action
5. Sci-Fi
6. Comedy
7. Animated
8. Thriller
9. Others
e
Sorry, the selection has to be a number
Choose Genre by number:
```

```
Enter Starring:
a
Enter Director:
arin
Choose Genre by number:
1. Drama
2. Adventure
3. Family
4. Action
5. Sci-Fi
6. Comedy
7. Animated
8. Thriller
9. Others
e
Sorry, the selection has to be a number
Choose Genre by number:
1
Choose Classification by number:
1. G
2. PG
3. M15+
4. MA15+
```

```
R C:\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Unitarray\Users\Users\Unitarray\Users\Users\Users\Users\Users\Users\Users\Users\Users\Users\Unitarray\Users\Users\Users\Users\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Users\Unitarray\Unitarray\Users\Unitarray\Unitarray\Unitarray\Unitarray\Unitarray\Unitarray\Unitarray\Unitar
```

If the staff puts empty value for title, it shows error message. However, the other thing for starring and director can be empty spaces or null value.

```
■ C:₩Users₩user₩OneDrive₩바탕 화면₩CAB301_assignment1₩
                                              Drama
                                              Adventure
Family
                                             Action
Sci-Fi
                                          4.
Comedy
Choose Genre by number:
 . Drama
                                              Animated
  Adventure
Family
                                              Thriller
                                           9
                                              Others
  Action
Sci-Fi
                                           Sorry, the selection has to be a number
  Comedy
  Animated
                                           Choose Genre by number:
                                           Choose Classification by number:
Sorry, the selection has to be a number
Choose Genre by number:
                                          2. PG
3. M15+
Choose Classification by number:
                                           4. MA15+
  PG
M15+
                                           Sorry, the selection has to be a number
                                           Choose Classification by number:
Sorry, the selection has to be a number
                                           Enter Duration:
Choose Classification by number
```

If the input is 0 or out of the given index of chooser, it shows error message to confirm the correct input my user.

```
Enter Duration:
d
Sorry, the duration has to be a number
Enter Duration:
2
Enter Released date:
1
Enter the number of copies:
d
Sorry, the number of copies has to be a number
Enter the number of copies:
1
Current DVDs in thie library are...

Title: A
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 4
Copies Available: 3
Times rented: 0

Title: ad
Starring: ad
Director: ad
Genre: 1. Drama
Classification: 1. G
Duration: 2
Released date: 2
Released date: 2
Released date: 2
Released date: 2
```

```
■ C:₩Users₩user₩OneDrive₩바탕 화
                                ■ C:#Osers#user#OneDrive#미당 모[단#CAB301_assic
Duration: 2
Released date: 2
                                  M15+
                               3. M15+
4. MA15+
Copies Available: 2
:Times rented: O
                                Enter Duration:
Title: A
                                Enter Released date:
Starring: a
Director: a
Genre: 1. Drama
                                Enter the number of copies:
Classification: 1. G
                                Current DVDs in thie library are...
Duration: 1
Released date: 1
                                Title: a
Copies Available: 1
                                Starring: a
Times rented: O
                                Director:
                                Genre: 1. Drama
                                Classification: 1. G
Title: B
                                Duration: 2
Starring: b
                                Released date: 2
Director: b
                                Copies Available: 7
Genre: 2. Adventure
                                Times rented: O
Classification: 2. PG
Duration: 2
                                Please press any key to exit
Released date: 2
```

As this application is working with depending on tilte, if the title of movie is same with the movie which has been alreay stored, even the other datas are not matched with new one and previous one, it added under the same title with inputing numbers of copies by user.

#### 2.2 Remove a movie

```
Title: B
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 1
Copies Available: 5
Times rented: 0

Title: D
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 6
Copies Available: 5
Times rented: 0

Title: C
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 6
Copies Available: 5
Times rented: 0

Title: D
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 1
Copies Available: 3
Times rented: 0

Title: E
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 1
Copies Available: 3
Times rented: 0

Seleased date: 4
Copies Available: 3
Times rented: 0

Select movie to remove
Please enter the title of movie to remove
arin
Sorry, the title is incorrect. Please check the title
Please press any key to exit
```

```
Title: E
Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: 4
Copies Available: 3
Times rented: 0
Select movie to remove
Please enter the title of movie to remove
C
Please press any key to exit
```

As every searching is depends on title, if the title input is unmatched with any items of list, it shows error message. If it is successfully deleted, it just shows the message to exit.

## 2.3 Register a new member

The Address and Phone number do not have any requirement to enter. Both are can be digits or any strings.

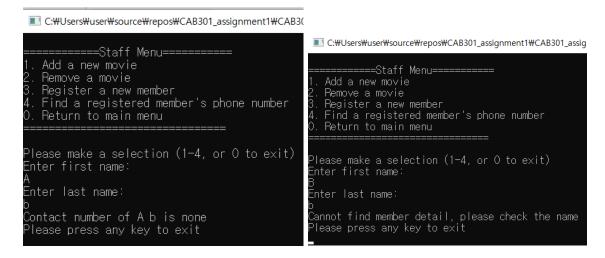
```
C:\(\pi\)Users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\pi\)users\(\p
```

If staff tried to register 11<sup>th</sup> member, it shows error message as this application cannot hold more than 10 members.

```
C:\(\psi \)Users\(\psi \)users
```

If the staff tries to register the member who has same name with registered member, it shows error message at the end of registration.

## 2.4 Find a member's phone number



To get the member's phone number, the staff has to enter the correct first and last name of member. As the phone number does not care it is digits or string when the member was registered, it can be shown with any format such as 'none' like above.

## 3 Member login – This member's Id is Ab and passwords is 0000

If the passwords are not digits or lesser than 4 digits, it show error messages on the screen.

#### 4 Member menu

#### 4.1 Display all movies with alphabetical order

These above pictures are for showing the alphabetical ordering in this application. When you run this, it will show like the picture of left.

#### 4.2 Borrow a DVD

Before borrowing, the number of copies in this library is 1 and the times of borrowed is 0.

When borrowing a DVD, the user must enter the correct title as every searching method in this application is running under the condition with the title and name except display top 10 function.

After the DVD with title 'B' is borrowed by user, we can see the current copy in this library is turning to 0 and times of borrowed is 1.

If the user tries to borrow the same movie, it shows error as the user cannot borrow same two DVDs at a time.

When the user tries to borrow the movie DVDs over 10, it shows error message.

## 4.3 Return a DVD

```
■ C:₩USers₩user₩source₩repos₩CAB3U1_assignment1₩CAB3
                ==Member Menu===
    Display all movies
                                                                                          =Member Menu=
    Borrow a movie DVD
                                                                              Display all movies
    Return a movie DVD
                                                                              Borrow a movie DVD
   List current borrowed movie DVDs
Display top 10 most popular movies
                                                                              Return a movie DVD
                                                                             List current borrowed movie DVDs
Display top 10 most popular movies
    Return to main menu
                                                                              Return to main menu
Please make a selection (1-5, or 0 to exit)
B b arin 2. Adventure 3. M15+ 24/May 0 1
Select movie to return
Please enter the title of movie to return
                                                                           Please make a selection (1-5, or 0 to exit)
T t d 1. Drama 2. PG 24/May 0 2
                                                                          Select movie to return
Please enter the title of movie to return
 has been returned!
                                                                           porry, the title is incorrect. Please check the title Please press any key to exit
```

Returning a DVD is also working under the condition with searching by the movie's title. So, if the user enters different title with the list of borrowed DVD, it shows error message to user.

If user has not borrowed any DVDs yet and user presses return menu, it shows error message.

#### 4.4 List current borrowed movie DVDs

If the borrowed DVDs are over one, it displays by alphabetical order.

```
Please make a selection (1-5, or 0 to exit)

4

Title: B

Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: r
Copies Available: 1

Title: D

Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: r
Copies Available: 1

Title: D

Starring: s
Director: d
Genre: 1. Drama
Classification: 2. PG
Duration: 100
Released date: r
Copies Available: 1
Times rented: 1
Please press any key to exit
```

This is actual running screen.

## 4.4 Display top 10 most popular movies

## Example 1.

```
Borrow a movie DVD
                                                                    =Member Menu========
  Return a movie DVD
                                                           Display all movies
  List current borrowed movie DVDs
Display top 10 most popular movies
                                                           Borrow a movie DVD
                                                           Return a movie DVD
  Return to main menu
                                                          List current borrowed movie DVDs
Display top 10 most popular movies
                                                           Return to main menu
Please make a selection (1-5, or 0 to exit)
Asd1. Drama 2. PG r 1 6
Bsd1. Drama 2. PG r 0 1
                                                        Please make a selection (1-5, or 0 to exit)
                      PG r
                                                         borrowed 6
borrowed 3
borrowed 2
borrowed 1
                                                                      Times
Times
  s d
           Drama
                                                                      Times
  s d
           Drama
                      PG
                                                          borrowed
                                                                      Times
           Drama
                                                         borrowed
                      PG
  s d
           Drama
                                                                      Times
Times
                                                         borrowed
                      PG
                                                         borrowed
                                                          borrowed
                      PG
                                                         borrowed 1 Times
borrowed 0 Times
                      PG
          Drama 2
                      PG r
 ease press any key to exit
```

Left picture is current all movies in the library (It is different format with actual running screen as this picture has to show the alphabetical order berfore sorting). Right picture is when the user choses to display top 10 popular movies frequently borrowed with descending order depends on how may time it has been borrowed.

## Example 2.

```
=Member Menu====
                                                                           Display all movies
Borrow a movie DVD
   Borrow a movie DVD
Return a movie DVD
List current borrowed movie DVDs
Display top 10 most popular movies
Return to main menu
                                                                           Return a movie DVD
List current borrowed movie DVDs
Display top 10 most popular movies
                                                                           Return to main menu
Please make a selection (1-5, or 0 to exit)
                                                                      Please make a selection (1-5, or 0 to exit)
L borrowed 5 Times
C borrowed 3 Times
              Drama 2
Drama 2
Drama 2
Drama 2
                                                                         borrowed
              Drama 2
Drama 2
                                                                                            Times
Times
                                                                         borrowed
                                                                          borrowed
              Drama
Drama
Drama
Drama
Drama
Drama
                                                                         borrowed
                                                                         borrowed
                                                                                            Times
                                                                                            Times
Times
              Drama 2
Drama 2
Drama 2
Drama 2
                                                                          borrowed
                                                                         borrowed
                                                                         borrowed 1
                                                                        lease press any key to exit
  lease press any key
```

It's the second case of display top 10 movies.

#### Referrence

A. Levitin. *Introduction to the Design and Analysis of Algorithms*. Addison-Wesley, *third edition, 2012*. Sections 5.1, 5.2 and 6.4