

Logarithms

The definition of a log:

$$p^q = r \leftrightarrow \log_p r = q$$

some basic examples:

$$\log_3 9 = 2$$

$$\log_5 1/5 = -1$$

$$\log_x (\sqrt[3]{x}) = 1/3$$

$$\log_4 (1/8) = -3/2$$

Natural Logarithms

- Generally, if the logarithm is base e , it is called the natural log (\ln)

Older Notation

In some older questions, the $\log_{10}(x)$ may be expressed as $\text{lug}(x)$

The Log Laws

- $\log_p(xy) = \log_p(x) + \log_p(y)$
- $\log_p\left(\frac{x}{y}\right) = \log_p(x) - \log_p(y)$
- $\log_p(x^y) = y\log_p(x)$
- $\log_p(x) = \frac{\log_q(x)}{\log_q(p)}$
(This one is known as the base change rule. It rarely comes up in A-level)
- $\log_p(p) = 1$
- $\log_p(1) = 0$