

Applied Statistics HW1 #4 solution.

Arinjay Jain, A20447307, ajain80@hawk.iit.edu

Create a sample of 40 numbers which are normally distributed.

```
norm <- rnorm(40,0,0.1)
```

```
x <- seq(-1,1,length.out = 40)
```

```
y <- 2*x+norm
```

#SLR pass from origin point (0,0) then $y = b_1 \cdot x$;

```
b1 <- sum(x*y)/sum(x*x)
```

Y origin (Yhat)

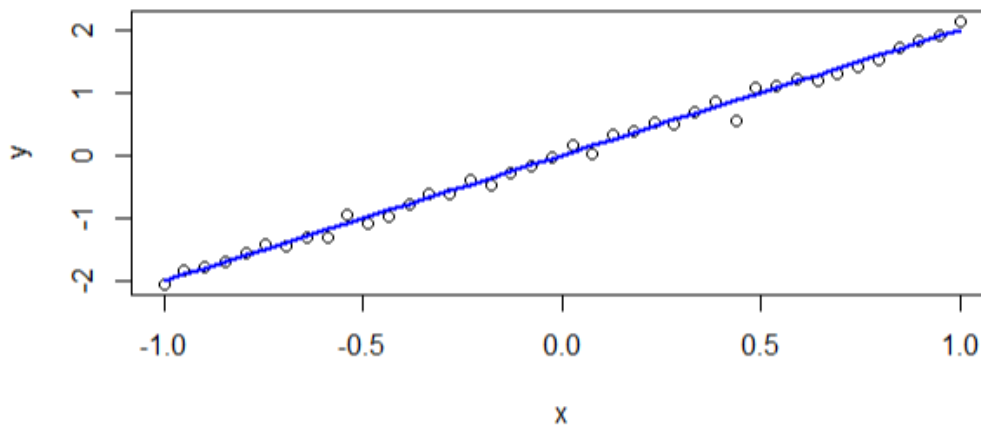
```
y0 <- c(b1*x)
```

```
c(y0)
```

```
[1] -2.01151897 -1.90836415 -1.80520933 -1.70205451 -1.59889969 -1.49574488  
[7] -1.39259006 -1.28943524 -1.18628042 -1.08312560 -0.97997078 -0.87681596  
[13] -0.77366114 -0.67050632 -0.56735150 -0.46419669 -0.36104187 -0.25788705  
[19] -0.15473223 -0.05157741  0.05157741  0.15473223  0.25788705  0.36104187  
[25]  0.46419669  0.56735150  0.67050632  0.77366114  0.87681596  0.97997078  
[31]  1.08312560  1.18628042  1.28943524  1.39259006  1.49574488  1.59889969  
[37]  1.70205451  1.80520933  1.90836415  2.01151897
```

```
plot(x,y)
```

```
lines(x,y0,col="blue", lwd="2")
```



#Error in origin line

```
e = abs(sum(y-y0))
```

```
c(e) = 0.3039365
```

Mean of Y_i is \bar{Y}

```
ybar0 = sum(y)/40
```

```
c(ybar0) = -0.007598413
```

r^2 is SSR/SST

```
SSR = sum((y0-ybar0)*(y0-ybar0))
```

```
c(SSR) = 56.7184
```

```
SST = sum((y-ybar0)*(y-ybar0))
```

```
c(SST) = 57.02526
```

```
rsquare <- SSR/SST
```

```
c(rsquare) = 0.9946188
```

Applied Statistics HW1 #4 solution.

Arinjay Jain, A20447307, ajain80@hawk.iit.edu

PART-2 ordinary linear regression $\hat{y}_i = b_0 + b_1x_i$

#ordinary linear regression $\hat{y}_i = b_0 + b_1x_i$

```
b1<- sum((x-mean(x))*(y-mean(y)))/sum((x-mean(x))*(x-mean(x)))
```

```
c(b1) = 2.011519
```

```
bo <- mean(y)-b1*mean(x)
```

```
c(bo)= -0.007598413
```

#bo is very small near to zero '0', so it looks like RTO

```
yhat = bo+b1*x
```

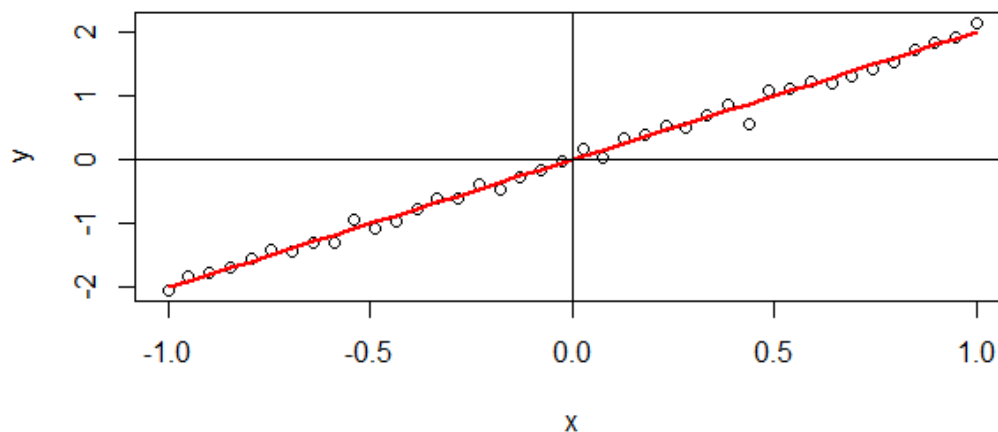
```
c(yhat)
```

```
[1] -2.01911738 -1.91596256 -1.81280775 -1.70965293 -1.60649811 -1.50334329  
[7] -1.40018847 -1.29703365 -1.19387883 -1.09072401 -0.98756919 -0.88441437  
[13] -0.78125956 -0.67810474 -0.57494992 -0.47179510 -0.36864028 -0.26548546  
[19] -0.16233064 -0.05917582 0.04397900 0.14713382 0.25028863 0.35344345  
[25] 0.45659827 0.55975309 0.66290791 0.76606273 0.86921755 0.97237237  
[31] 1.07552719 1.17868201 1.28183682 1.38499164 1.48814646 1.59130128  
[37] 1.69445610 1.79761092 1.90076574 2.00392056
```

```
plot(x,y)
```

```
lines(x,yhat,col="red",lwd="2")
```

```
abline(h=0,v=0)
```



#calculate error e1

error almost zero.

```
e1<-abs(sum(y-yhat))
```

```
c(e1) = 1.491862e-15
```

#calculate $r^2 = SSR/SST$

SSR

```
SSR1 <- sum((yhat -mean(y))*(yhat -mean(y)))
```

```
c(SSR1) = 56.71609
```

SST

```
SST1 <- sum ((y-mean(y))*(y -mean(y)))
```

```
c(SST1) = 57.02526
```

#rsquare shows the prefect correlation.

```
rsquare1 <-SSR1/SST1 c(rsquare1) = 0.9945783
```