Analysing Life Expectancy With Linear Regression

Rinku Bajaj (s3672522), Arion Barzoucas-Evans (s3650046), Deepika Joshi (s3672595) 05/06/2019

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Introduction

The main aim of this project is to identify the most influential factors affecting life expectancy in developed and developing countries from 2000-2015. The project considers factors traditionally studied for life expectancy predictions such as demographic variables, mortality rate and income composition as well as the effects of new factors such as immunization and human development index. The data is sourced from Kaggle Repository and is a combination of life-expectancy and health data from Global Health Observatory (GHO) published by World Health Organisation (WHO) and economic data published by United Nations. It consists of data spanning over 15 years from 2000-2015 for 193 countries and can be broadly divided into Economic Factors, Social Factors, Immunization Factors and Mortality Factors. The dataset has 2938 observations for 20 predictor variables describing the life expectancy of each nation for that year.

Linear regression models will be used to predict the life expectancy based on the variables present in the data. This analysis will help in determining the influential factors different than those traditionally used by implementing different methods involved in a regression analysis.

Data Pre-Processing and Data Exploration

The first step after getting the data was data cleaning. Some basic cleaning steps were necessary like removing the NAs present in the data.

```
# load libraries
library(ggplot2)
library(data.table)
library(knitr)
library(corrplot)
library(TSA)
library(leaps)

# read data
data = setDT(read.csv("Life Expectancy Data.csv"))

# replace/remove NAs
data = data[!is.na(Life.expectancy)]
cols = names(data)[!grep1("Country|Status", names(data))]
data[, (cols) := lapply(.SD, function(x) {ifelse(is.na(x), -1, x)}), .SDcols = cols]
```

Data exploration was implemented by means of various visualisations which gave insights into the data and made next steps clearer.

Figure 1 shows the correlation between the numeric variables in the dataset. According to this, life expectancy has a high negative correlation with adult mortality, HIV, and thinness. Conversely, there is a high positive correlation between life expectancy and BMI, schooling, polio, Diphtheria, and GDP. Additionally, many of the independent variables are correlated to each other and may lead to multi-collinearity issues.

Figure 2 displays the distribution of the life expectancy variable in the dataset. This shows that life expectancy ranges from around 40 to 90 years with 50% of the values being over 72 years. This indicates that the variable is slightly skewed to the left. The bar chart in Figure 3 shows that the majority of countries in the dataset are developing countries with only around 30 countries being developed.

There will be differences in results based on the fact that whether the country is a developed or a developing one. Therefore, different statistics were observed across status of the countries.

Life expectancy is strongly correlated to a country's status (Fig 4). It can be seen that developed countries generally have a life expectancy around 80 with little variation. On the other hand, developing countries have an average life expectancy of just under 70 with much greater variance and several outliers with life expectancy of around 40. Life expectancy for both developed and developing countries has an upward trend having a 5 year improvement from 2000 to 2015 (Fig 5). Figure 6 shows a strong negative correlation between

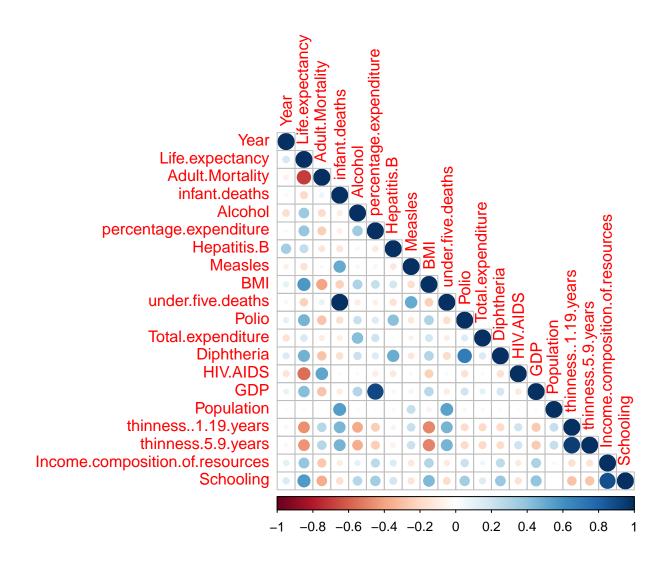


Figure 1: Correlation plot for all numeric variables in the dataset.

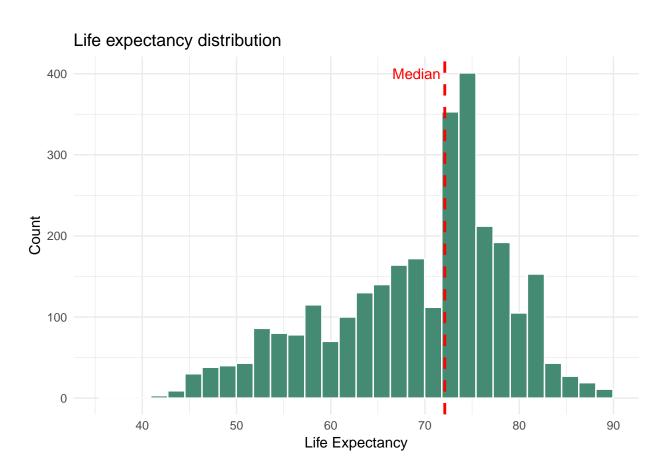


Figure 2: Status distribution in the dataset.

life expectancy and adult mortality for both developed and developing countries. However, there are many cases of countries with a low adult mortality rate that still have low life expectancy. This may indicate that adult mortality alone is not a sufficient indicator of life expectancy.

```
# status
ggplot(data[, length(unique(Country)), Status], aes(x = Status, y = V1)) +
  geom_bar(stat = "identity", fill = "aquamarine4") +
  theme_minimal() +
  labs(y = "Countries", title = "Distribution of countries by status")
```

Distribution of countries by status

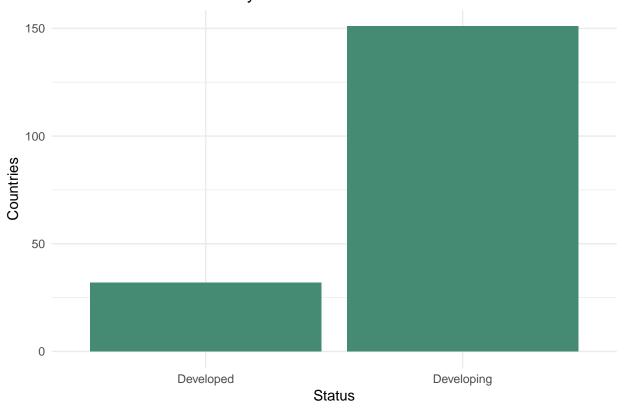


Figure 3: Life expectancy distribution in the dataset.

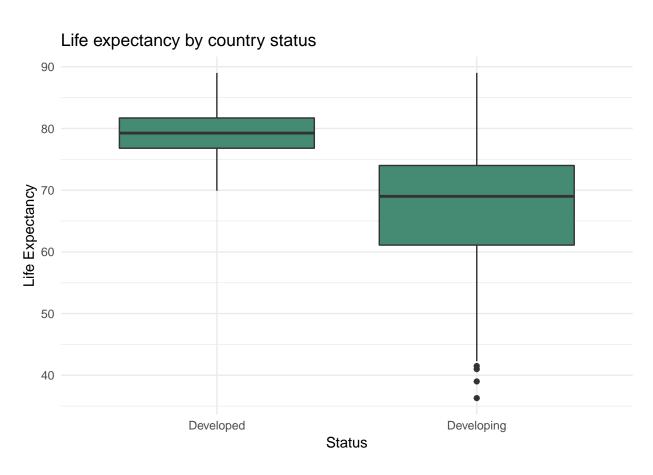


Figure 4: Life expectancy by status.

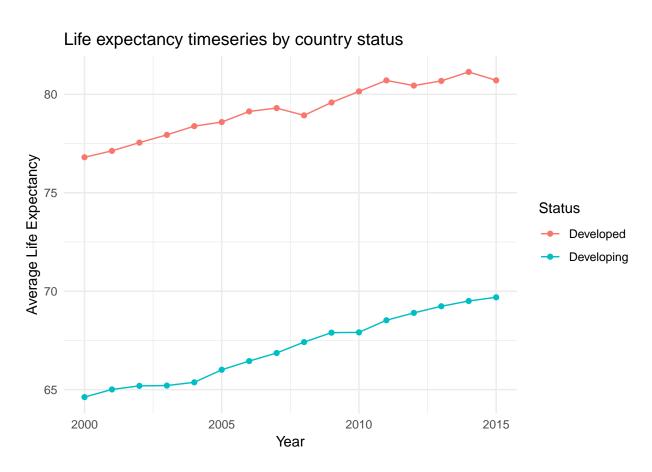


Figure 5: Historical life expectancy by status.

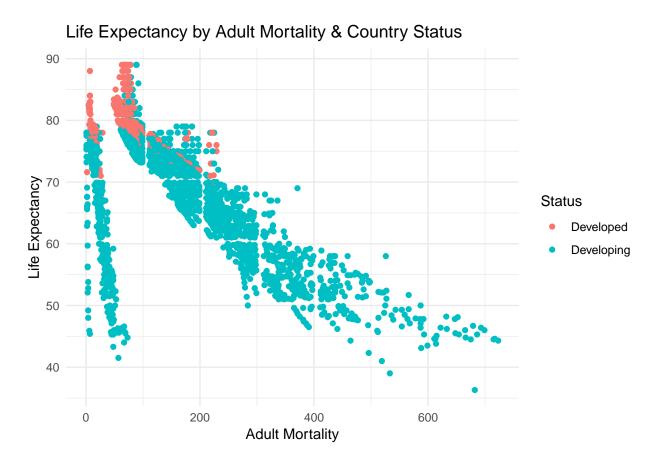


Figure 6: Life expectancy by adult mortality and status.

Methodology

The countries present in the dataset will be categorised into developed and developing. Different linear regression models will be fitted to each group using the traditionally considered factors, the extended factors, and using stepwise regression. The adequacy of the fitted models will be assessed with a combination of residual diagnostics and statistical tests. Using the models with the best fit to the data, the most influential factors will be identified for both developed and developing countries.

Splitting dataset into developed and developing nations

```
#Create Developing and Developed Nations Datasets
data_developing = subset(data,Status=="Developing")
data_developed = subset(data,Status=="Developed")

#Refactor the levels in the Dataset
data_developing$Status <- NULL
data_developed$Status <- NULL
# Discussion</pre>
```

Creating a function for Regression Model Analysis

```
regression.analysis <- function(regression_model){</pre>
\#regression\_model = lm.fit\_1
#Residual check.options
par(mfrow=c(2,2))
plot(regression_model)
# Evaluate homoscedasticity
# non-constant error variance test
cat("\nHomoskedascity Check:\n")
print(ncvTest(regression_model))
# Test for Autocorrelated Errors
cat("\nAutoCorrelation Check:\n")
print(durbinWatsonTest(regression model))
# Test for Normally Distributed Errors
cat("\nNormality Check:\n")
print(shapiro.test(regression_model$residuals))
#Check multicollinearity
cat("\nMulticollinearity Check:\n")
kable(vif(lm.fit_1),col.names = "VIF")
}
```

Linear Regression for Developed Countries

Baseline Model

First a baseline model is created for developed countries. This baseline model includes all features from the data. But on further processing it was observed that the feature for HIV AIDs when included in the model, produces NAs. Therefore, this feature was removed from the model. The variables Country and Year were excluded as well.

From the summary of the model it can be seen that, 51.59% of the variation in life expectancy is explained by the features used in the model. Also, the p-value of the regression is very low and hence it can be concluded that the regression is significant.

```
#Linear Regression Model
lm.fit_1<-lm(Life.expectancy ~. -(Country + Year + HIV.AIDS), data_developed)</pre>
summary(lm.fit_1)
##
## Call:
## lm(formula = Life.expectancy ~ . - (Country + Year + HIV.AIDS),
       data = data_developed)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -5.9487 -1.6294 -0.4584 1.0129
                                    9.7749
##
## Coefficients:
##
                                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    8.295e+01 1.684e+00 49.252 < 2e-16 ***
## Adult.Mortality
                                   -1.646e-02
                                              2.955e-03
                                                         -5.568 4.23e-08 ***
## infant.deaths
                                                          -3.376 0.000794 ***
                                   -1.424e+00 4.218e-01
## Alcohol
                                   -2.602e-01 3.995e-02
                                                         -6.512 1.83e-10 ***
## percentage.expenditure
                                   1.457e-04 8.850e-05
                                                          1.646 0.100374
## Hepatitis.B
                                   -2.927e-03
                                              3.064e-03
                                                          -0.955 0.340026
## Measles
                                    1.702e-05
                                              5.053e-05
                                                           0.337 0.736324
## BMI
                                   -2.010e-02 7.478e-03
                                                          -2.688 0.007422 **
## under.five.deaths
                                    1.141e+00 3.560e-01
                                                           3.206 0.001431 **
## Polio
                                    2.417e-03 1.449e-02
                                                           0.167 0.867590
## Total.expenditure
                                   -2.554e-02 4.392e-02
                                                         -0.582 0.561149
## Diphtheria
                                    2.424e-02 1.246e-02
                                                          1.945 0.052303 .
## GDP
                                    1.010e-05 1.486e-05
                                                           0.680 0.496915
## Population
                                    1.145e-08 9.569e-09
                                                           1.197 0.231996
## thinness..1.19.years
                                   -2.007e+00 1.349e+00
                                                         -1.488 0.137402
## thinness.5.9.years
                                   -2.762e-01 1.240e+00
                                                          -0.223 0.823806
## Income.composition.of.resources -1.930e+00 9.308e-01
                                                          -2.074 0.038618 *
## Schooling
                                    1.811e-01 9.542e-02
                                                           1.898 0.058282 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.735 on 494 degrees of freedom
## Multiple R-squared: 0.5321, Adjusted R-squared: 0.5159
## F-statistic: 33.04 on 17 and 494 DF, p-value: < 2.2e-16
```

Checking significance of regression co-efficients

ANOVA test was performed to get significance of the model parameters. The hypotheses for this test are:

 $H_0: \beta_i = 0$ $H_a: \beta_i \neq 0$ where i runs from 1:17 and i represents each predictor.

For this model it is observed that, at 95% significance level, estimates for adult mortality, infant deaths, alcohol, percentage expenditure, Hepatitis B, under five deaths, population and thinness 1-19 years are statistically significant, when used with all other predictors in the model.

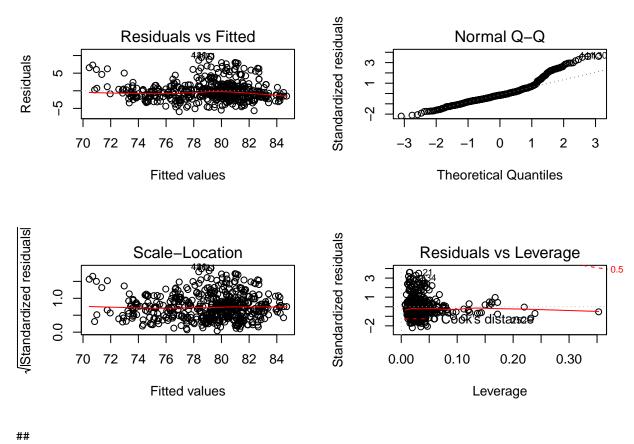
```
#Using ANOVA to check significance of variables
anova(lm.fit_1)
```

```
## Analysis of Variance Table
##
## Response: Life.expectancy
                                     Df Sum Sq Mean Sq F value
##
                                                                     Pr(>F)
## Adult.Mortality
                                      1 1861.1 1861.11 248.8219 < 2.2e-16 ***
## infant.deaths
                                          48.3
                                                  48.30
                                                          6.4574 0.0113536 *
                                         360.4
## Alcohol
                                                360.44
                                                         48.1895 1.222e-11 ***
                                      1
                                         603.6
## percentage.expenditure
                                      1
                                                 603.62
                                                         80.7011 < 2.2e-16 ***
## Hepatitis.B
                                          46.5
                                                          6.2193 0.0129626 *
                                      1
                                                  46.52
## Measles
                                      1
                                            0.0
                                                   0.03
                                                          0.0039 0.9502457
## BMI
                                      1
                                            3.8
                                                   3.77
                                                          0.5034 0.4783421
## under.five.deaths
                                         101.9
                                                 101.88
                                                         13.6211 0.0002485 ***
                                      1
## Polio
                                      1
                                            3.3
                                                   3.34
                                                          0.4464 0.5043390
## Total.expenditure
                                      1
                                            5.6
                                                   5.58
                                                          0.7455 0.3883235
## Diphtheria
                                      1
                                            1.0
                                                   0.97
                                                          0.1300 0.7185952
                                                          0.4000 0.5273981
## GDP
                                      1
                                            3.0
                                                   2.99
## Population
                                      1
                                          44.6
                                                  44.57
                                                          5.9582 0.0149988 *
## thinness..1.19.years
                                      1 1084.2 1084.20 144.9526 < 2.2e-16 ***
## thinness.5.9.years
                                      1
                                            1.5
                                                   1.45
                                                          0.1939 0.6598936
## Income.composition.of.resources
                                                          0.7283 0.3938423
                                      1
                                            5.4
                                                   5.45
                                                          3.6023 0.0582820 .
## Schooling
                                      1
                                          26.9
                                                  26.94
## Residuals
                                    494 3695.0
                                                   7.48
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

Residual analysis for validating Model

Here, the function created for residual analysis is used.

regression.analysis(lm.fit_1)



```
## Homoskedascity Check:
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
  Chisquare = 0.007319894
                              Df = 1
                                          p = 0.9318191
##
##
   AutoCorrelation Check:
    lag Autocorrelation D-W Statistic p-value
##
              0.5877129
                            0.8232728
##
##
    Alternative hypothesis: rho != 0
##
  Normality Check:
##
##
##
    Shapiro-Wilk normality test
##
## data: regression_model$residuals
## W = 0.91705, p-value = 3.76e-16
##
## Multicollinearity Check:
```

	VIF
Adult.Mortality	1.367702
infant.deaths	255.594031
Alcohol	1.450732
percentage.expenditure	7.825414

	VIF
Hepatitis.B	1.318336
Measles	1.115706
BMI	1.129846
under.five.deaths	250.918986
Polio	1.667478
Total.expenditure	1.666328
Diphtheria	1.665702
GDP	7.702266
Population	1.156524
thinness1.19.years	71.143549
thinness.5.9.years	72.205097
Income.composition.of.resources	17.439966
Schooling	16.784452

1) residuals v/s fitted plot

This plot is used for testing the linear approximation assumption. In this case, the residuals seem to be randomly distributed.

2) QQ plot

This plot is used to test the normality assumption. There seems to be deviation of the upper tail from the straight line.

3) scale location plot

This plot is used to check homoskedasticity. There is a horizontal line with randomly spaced points.

4) residual v/s leverage plot

This plot is used to find influential cases. Here, all the points are within cook's distance.

Homoskedasticity test:

 H_0 : Errors have constant variance H_a : Errors have non-constant variance

The nCV test has pvalue > 0.05. Therefore, we fail to reject the null hypothesis. So the constant error variance assumption is not violated.

Test for autocorrelated errors:

 H_0 : Errors are uncorrelated H_1 : Errors are correlated

p-value is > 0.05. So, we don't have enough evidence to reject H_0 . Therefore, uncorrelated error assumption is not violated.

Test for normality of residuals:

 H_0 : errors are normally distributed H_a : errors aren't normally distributed

p-value < 0.05. Therefore, we reject the null hypothesis. This indicates that the normality assumption is violated.

Test for multicollinearity:

Very high values of VIF indicate strong correlation. Hence, it can be said that infant death and under five deaths are highly correlated. Also, 'thinness 1-19 yrs' and 'thinness 5-9 yrs' are correlated.

Some assumptions are violated. Some sort of non-linear transformations can be applied on the data to fix this.

Model Building Comparison using AIC Values

Model building comparison for backward elimination, forward selection and stepwise regression using AIC values

In forward selection, initially there are no variables and then variables are added one at a time. Based on AIC value, the best model is selected. In case of backward elimination, a full model (model with all features included) is created and then variables are examined and removed sequentially. Stepwise is a combination of both forward selection and backward elimination. Here contribution of each feature is checked using partial F test. Akaike Information Criteria (AIC) penalises based on the number of parameters in the model. Smaller value of AIC is desirable.

The coefficients of the parameters for the best model selected using backward elimination are:

```
#Backward Elimination
b1 = step(lm.fit_1, data=data_developed, direction="backward", trace = FALSE)
kable(b1$coefficients, col.names = "Backward Elimination Parameter Estimates")
```

	Backward Elimination Parameter Estimates
(Intercept)	83.0325163
Adult.Mortality	-0.0166258
infant.deaths	-1.4159206
Alcohol	-0.2793219
percentage.expenditure	0.0002058
BMI	-0.0206657
under.five.deaths	1.1266582
Diphtheria	0.0258218
thinness1.19.years	-2.3160206
Income.composition.of.resources	-1.8975011
Schooling	0.1817349

The coefficients of the parameters for the best model selected using forward selection are:

	Forward Selection Parameter Estimates
(Intercept)	84.1376432
thinness.5.9.years	-2.2027031
Alcohol	-0.2564736
GDP	0.0000089
Adult.Mortality	-0.0164504
infant.deaths	-1.3484573
under.five.deaths	1.0778448
BMI	-0.0162380
Diphtheria	0.0199727
percentage.expenditure	0.0001444
Population	0.0000000

The coefficients of the parameters for the best model selected using stepwise regression are:

	Stepwise Regression Parameter Estimates
(Intercept)	84.2388162
thinness.5.9.years	-2.1987648
Alcohol	-0.2630321
Adult.Mortality	-0.0165789
infant.deaths	-1.3362721
under.five.deaths	1.0656474
BMI	-0.0166584
Diphtheria	0.0202817
percentage.expenditure	0.0001927
Population	0.0000000

Model parameters differ a bit based on the chosen method. Features like adult mortality, alcohol, diphtheria, infant deaths, percentage expenditure, BMI, under 5 deaths are significant across all the 3 methods.

Model Building using R Squared Values

thinness.5.9.years

Here, best model is determined by using adjusted r2 as the selection criteria. Model with the highest adjusted R2 value is chosen. Also, adjusted R2 is always a better metric to compare models instead of R2.

Using 'regsubsets' function to determine the best subset model.

```
new_model_developed <- regsubsets(Life.expectancy ~. -(Country + Year + HIV.AIDS),</pre>
                                   data = data_developed)
nm1 = summary(new_model_developed)
nm1
## Subset selection object
## Call: regsubsets.formula(Life.expectancy ~ . - (Country + Year + HIV.AIDS),
       data = data developed)
##
## 17 Variables (and intercept)
                                    Forced in Forced out
## Adult.Mortality
                                        FALSE
                                                   FALSE
## infant.deaths
                                        FALSE
                                                   FALSE
## Alcohol
                                        FALSE
                                                   FALSE
## percentage.expenditure
                                        FALSE
                                                   FALSE
## Hepatitis.B
                                        FALSE
                                                   FALSE
## Measles
                                        FALSE
                                                   FALSE
## BMI
                                        FALSE
                                                   FALSE
## under.five.deaths
                                        FALSE
                                                   FALSE
## Polio
                                        FALSE
                                                   FALSE
## Total.expenditure
                                        FALSE
                                                   FALSE
## Diphtheria
                                        FALSE
                                                   FALSE
## GDP
                                        FALSE
                                                   FALSE
## Population
                                        FALSE
                                                   FALSE
## thinness..1.19.years
                                        FALSE
                                                   FALSE
```

FALSE

FALSE

```
## Income.composition.of.resources
                                      FALSE
                                                 FALSE
## Schooling
                                      FALSE
                                                 FALSE
## 1 subsets of each size up to 8
## Selection Algorithm: exhaustive
           Adult.Mortality infant.deaths Alcohol percentage.expenditure
     (1)""
## 1
                                                 11 11
                           11 11
                                         "*"
## 2
     (1)""
                                         "*"
## 3
     (1)
                           11 11
## 4
     (1)"*"
                                         11 * 11
                                                 11 * 11
     (1)"*"
## 5
                                                 "*"
## 6
     (1)"*"
                                         "*"
     (1)"*"
                            "*"
                                         "*"
                                                 "*"
## 7
                                                 "*"
     (1)"*"
                                         "*"
## 8
##
           Hepatitis.B Measles BMI under.five.deaths Polio Total.expenditure
     (1)""
## 1
                       11 11
                               11 11 11 11
                                                     11 11
     (1)""
                        11 11
## 2
## 3
     (1)""
                        11 11
                                   11 11
     (1)""
## 4
     (1)""
## 5
                        11 11
## 6
     (1)""
     (1)""
                        11 11
## 7
     (1)""
                       11 11
                               "*" "*"
                                                     11 11
## 8
##
           Diphtheria GDP Population thinness..1.19.years thinness.5.9.years
                      11 11 11 11
## 1
     (1)""
                                     11 11
                                                          "*"
## 2 (1)""
                                                          "*"
## 3
     (1)""
                                     11 11
                                                          "*"
     (1)""
## 4
                                                          "*"
## 5
     (1)""
                                     " * "
    (1)""
                                                          "*"
## 6
                        11 11 11
## 7
     (1)""
                                     "*"
                                                          11 11
     (1)"*"
                                     "*"
## 8
##
           Income.composition.of.resources Schooling
     (1)""
## 1
     (1)""
                                           .. ..
## 2
     (1)""
## 3
     (1)""
## 4
## 5
     (1)""
## 6
     (1)""
     (1)""
                                           11 11
## 7
## 8 (1) " "
```

Selecting the best subset model based on highest Adjusted R^2 value

```
adjr2_developed = which.max(nm1$adjr2)
adjr2_developed
```

[1] 8

The model with the highest adjusted R2 value has adult mortality, infant deaths, alcohol, percentage expenditure, BMI, under five deaths, diphtheria, thinness 1-19 in it.

Linear Regression for Developing Countries - Baseline Model

Baseline Model

LM Model and Summary

#Linear Regression Model

The exact same procedure is followed for developing countries as well. First, baseline model with all the features included (except country and year) is built. Summary of the model shows that regression is significant as p-value is very small. Adjusted R2 shows that this baseline model is able to explain 76.8% variability in life expectancy using the predictors in the model.

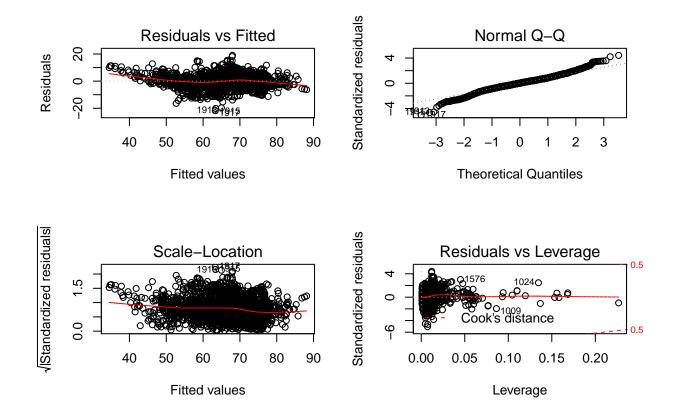
```
lm.fit_2<-lm(Life.expectancy ~. -(Country + Year), data_developing)</pre>
summary(lm.fit_2)
##
## Call:
## lm(formula = Life.expectancy ~ . - (Country + Year), data = data_developing)
##
## Residuals:
##
      Min
                1Q
                   Median
                                3Q
                                       Max
##
  -21.826
           -2.354
                    0.086
                            2.497
                                   19.025
##
## Coefficients:
                                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                   5.872e+01 5.199e-01 112.953 < 2e-16 ***
## Adult.Mortality
                                   -1.908e-02 8.750e-04 -21.807
                                                                 < 2e-16 ***
## infant.deaths
                                   1.235e-01 8.941e-03 13.811 < 2e-16 ***
## Alcohol
                                   1.864e-01 3.046e-02
                                                          6.120 1.09e-09 ***
## percentage.expenditure
                                   1.135e-03
                                              2.057e-04
                                                          5.519 3.78e-08 ***
## Hepatitis.B
                                   1.792e-02 3.087e-03
                                                          5.805 7.30e-09 ***
## Measles
                                   -1.373e-05 8.249e-06
                                                         -1.665
                                                                0.09613 .
## BMI
                                   6.614e-02 5.992e-03 11.038
                                                                 < 2e-16 ***
## under.five.deaths
                                   -9.137e-02 6.559e-03 -13.930 < 2e-16 ***
## Polio
                                   2.455e-02 4.890e-03
                                                          5.020 5.54e-07 ***
## Total.expenditure
                                  -1.123e-01 3.553e-02
                                                         -3.162 0.00159 **
## Diphtheria
                                   2.157e-02 5.280e-03
                                                          4.085 4.55e-05 ***
## HIV.AIDS
                                   -4.929e-01
                                              1.899e-02 -25.952 < 2e-16 ***
## GDP
                                   3.950e-06 2.129e-05
                                                          0.186 0.85281
## Population
                                   -1.046e-09 1.818e-09
                                                         -0.575 0.56518
## thinness..1.19.years
                                   -1.200e-01 5.369e-02
                                                         -2.235
                                                                 0.02552 *
## thinness.5.9.years
                                    2.486e-02 5.314e-02
                                                          0.468 0.63998
## Income.composition.of.resources -2.541e+00 4.554e-01
                                                         -5.579 2.69e-08 ***
## Schooling
                                    6.873e-01 5.102e-02 13.471 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.329 on 2397 degrees of freedom
## Multiple R-squared: 0.7706, Adjusted R-squared: 0.7689
## F-statistic: 447.4 on 18 and 2397 DF, p-value: < 2.2e-16
```

Checking significance of regression co-efficients

ANOVA test is used to check significance of model parameters. It is observed that at 5% significance level, except features like GDP, Population and thinness 5-9 years, rest all the feature parameters are significant when considered with rest of the features.

#Using ANOVA to check significance of variables anova(lm.fit_2)

```
## Analysis of Variance Table
## Response: Life.expectancy
##
                                      Df Sum Sq Mean Sq F value
                                                                      Pr(>F)
                                       1 85542
                                                  85542 4563.9288 < 2.2e-16
## Adult.Mortality
## infant.deaths
                                           3612
                                                   3612 192.7107 < 2.2e-16
                                       1
## Alcohol
                                       1
                                           4593
                                                   4593 245.0676 < 2.2e-16
## percentage.expenditure
                                       1
                                           5877
                                                   5877 313.5666 < 2.2e-16
## Hepatitis.B
                                       1 13459
                                                  13459 718.0636 < 2.2e-16
## Measles
                                       1
                                            668
                                                    668
                                                          35.6362 2.731e-09
## BMI
                                       1
                                         10119
                                                  10119 539.8884 < 2.2e-16
## under.five.deaths
                                       1
                                           6602
                                                   6602 352.2269 < 2.2e-16
## Polio
                                           1799
                                       1
                                                   1799
                                                          95.9591 < 2.2e-16
## Total.expenditure
                                       1
                                            453
                                                    453
                                                          24.1912 9.314e-07
                                                    710
## Diphtheria
                                       1
                                            710
                                                          37.8690 8.841e-10
## HIV.AIDS
                                       1
                                          12122
                                                  12122 646.7694 < 2.2e-16
## GDP
                                       1
                                             32
                                                     32
                                                           1.6825 0.194716
                                                           0.0860 0.769304
## Population
                                       1
                                              2
                                                      2
## thinness..1.19.years
                                                          10.1485 0.001463
                                            190
                                                    190
                                       1
## thinness.5.9.years
                                             49
                                                     49
                                                           2.6272 0.105176
                                       1
## Income.composition.of.resources
                                       1
                                           1724
                                                   1724
                                                          91.9636 < 2.2e-16
## Schooling
                                       1
                                           3401
                                                   3401 181.4672 < 2.2e-16
## Residuals
                                    2397 44927
                                                     19
## Adult.Mortality
                                    ***
## infant.deaths
                                    ***
## Alcohol
                                    ***
## percentage.expenditure
                                    ***
## Hepatitis.B
                                    ***
## Measles
                                    ***
## BMI
## under.five.deaths
                                    ***
## Polio
## Total.expenditure
                                    ***
## Diphtheria
                                    ***
## HIV.AIDS
                                    ***
## GDP
## Population
## thinness..1.19.years
                                    **
## thinness.5.9.years
## Income.composition.of.resources ***
## Schooling
                                    ***
## Residuals
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual analysis for validating Model
regression.analysis(lm.fit_2)
```



```
##
## Homoskedascity Check:
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
   Chisquare = 98.17636
                            Df = 1
                                       p = 3.827325e-23
##
   AutoCorrelation Check:
##
    lag Autocorrelation D-W Statistic p-value
##
               0.669526
                             0.6577663
##
##
    Alternative hypothesis: rho != 0
##
  Normality Check:
##
##
##
    Shapiro-Wilk normality test
##
## data: regression_model$residuals
## W = 0.98232, p-value < 2.2e-16
##
## Multicollinearity Check:
```

	VIF
Adult.Mortality	1.367702
infant.deaths	255.594031
Alcohol	1.450732
percentage.expenditure	7.825414

	VIF
Hepatitis.B	1.318336
Measles	1.115706
BMI	1.129846
under.five.deaths	250.918986
Polio	1.667478
Total.expenditure	1.666328
Diphtheria	1.665702
GDP	7.702266
Population	1.156524
thinness1.19.years	71.143549
thinness.5.9.years	72.205097
Income.composition.of.resources	17.439966
Schooling	16.784452

1) residuals v/s fitted plot

The residuals seem to be randomly distributed.

2) QQ plot

There seems to be slight deviation from the straight line.

3) scale location plot

This plot is used to check homoskedasticity. There is a horizontal line with randomly spaced points.

4) residual v/s leverage plot

All the points are within cook's distance.

Homoskedasticity test:

 H_0 : Errors have constant variance H_a : Errors have non-constant variance

The nCV test has pvalue < 0.05. Therefore, reject the null hypothesis. So the constant error variance assumption is violated.

Test for autocorrelated errors:

 H_0 : Errors are uncorrelated H_1 : Errors are correlated

p-value is > 0.05. So, we don't have enough evidence to reject H_0 . Therefore, uncorrelated error assumption is not violated.

Test for normality of residuals:

 H_0 : errors are normally distributed H_a : errors aren't normally distributed

p-value < 0.05. Therefore, we reject the null hypothesis. This indicates that the normality assumption is violated.

Test for multicollinearity:

Very high values of VIF indicate strong correlation. Hence, it can be said that infant death and under five deaths are highly correlated. Also, 'income composition of resources' and 'schooling' are correlated.

If needed, the models can be improved further using more complex methods to get fix the problem of assumptions being violated.

Model Building Comparison

Best models based on AIC values from backward elimination, forward selection and stepwise regression are compared.

	Backward Elimination Parameter Estimates
(Intercept)	58.7468874
Adult.Mortality	-0.0190778
infant.deaths	0.1227101
Alcohol	0.1853281
percentage.expenditure	0.0011651
Hepatitis.B	0.0179230
Measles	-0.0000137
BMI	0.0658982
under.five.deaths	-0.0909685
Polio	0.0246080
Total.expenditure	-0.1143888
Diphtheria	0.0215884
HIV.AIDS	-0.4925487
thinness1.19.years	-0.0976929
Income.composition.of.resources	-2.5442213
Schooling	0.6879433

	Forward Selection Parameter Estimates
(Intercept)	57.5586999
Adult.Mortality	-0.0198014
Schooling	0.7231942
HIV.AIDS	-0.5070142
BMI	0.0682506
Diphtheria	0.0290133
percentage.expenditure	0.0011390
Income.composition.of.resources	-2.5681629
Hepatitis.B	0.0184523
Polio	0.0281819
thinness1.19.years	-0.0905599
Alcohol	0.1374685

	Forward Selection Parameter Estimates
Total.expenditure Measles	-0.1120023 -0.0000227

	Stepwise Regression Parameter Estimates
(Intercept)	57.5586999
Adult.Mortality	-0.0198014
Schooling	0.7231942
HIV.AIDS	-0.5070142
BMI	0.0682506
Diphtheria	0.0290133
percentage.expenditure	0.0011390
Income.composition.of.resources	-2.5681629
Hepatitis.B	0.0184523
Polio	0.0281819
thinness1.19.years	-0.0905599
Alcohol	0.1374685
Total.expenditure	-0.1120023
Measles	-0.0000227

Across all 3 methods, features like adult mortality, schooling, HIV AIDS, BMI, Diphtheria, percentage expenditure, income composition of resources, hepatitis B', polio, thinness 1-19 years and total expenditure seem to be influential.

Model Building using R Squared Values

Using 'regsubsets' function to determine the best subset model

```
new_model_developing <- regsubsets(Life.expectancy ~. -(Country + Year),</pre>
                                   data = data_developing)
nm2 = summary(new_model_developing)
nm2
## Subset selection object
## Call: regsubsets.formula(Life.expectancy ~ . - (Country + Year), data = data_developing)
## 18 Variables (and intercept)
                                   Forced in Forced out
## Adult.Mortality
                                       FALSE
                                                  FALSE
## infant.deaths
                                       FALSE
                                                  FALSE
## Alcohol
                                       FALSE
                                                  FALSE
                                       FALSE
                                                  FALSE
## percentage.expenditure
## Hepatitis.B
                                       FALSE
                                                  FALSE
## Measles
                                       FALSE
                                                  FALSE.
## BMI
                                       FALSE
                                                  FALSE
## under.five.deaths
                                       FALSE
                                                  FALSE
## Polio
                                       FALSE
                                                  FALSE
                                                  FALSE
## Total.expenditure
                                       FALSE
## Diphtheria
                                       FALSE
                                                  FALSE
## HIV.AIDS
                                       FALSE
                                                  FALSE
## GDP
                                       FALSE
                                                  FALSE
## Population
                                                  FALSE
                                       FALSE
                                                  FALSE
## thinness..1.19.years
                                       FALSE
## thinness.5.9.years
                                       FALSE
                                                  FALSE
## Income.composition.of.resources
                                       FALSE
                                                  FALSE
## Schooling
                                       FALSE
                                                  FALSE
## 1 subsets of each size up to 8
## Selection Algorithm: exhaustive
            Adult.Mortality infant.deaths Alcohol percentage.expenditure
                            11 11
## 1 ( 1 ) "*"
                            11 11
## 2 (1)""
## 3 (1) "*"
## 4 ( 1 ) "*"
                            11 11
     (1)"*"
## 5
                            11 11
## 6 (1) "*"
                                                   11 11
## 7 (1)"*"
## 8 (1) "*"
                            "*"
                                                   "*"
            Hepatitis.B Measles BMI under.five.deaths Polio Total.expenditure
## 1 (1)""
                                11 11 11 11
                        11 11
## 2 (1)""
                        11 11
                                . . . . .
                        11 11
                                ## 3 (1)""
                                "*" " "
                        11 11
## 4 (1)""
## 5 (1)""
                                "*" " "
                        11 11
                                "*" " "
## 6 (1)""
     (1)""
                        11 11
                                "*" "*"
## 7
                        11 11
                                "*" "*"
                                                       11 11
## 8 (1)""
##
            Diphtheria HIV.AIDS GDP Population thinness..1.19.years
## 1 (1)""
                       11 11
                                11 11 11 11
## 2 (1)""
                       "*"
                                11 11 11 11
                                                11 11
                       "*"
                                11 11 11 11
                                                11 11
## 3 (1) " "
```

```
"*"
## 4
    (1)""
## 5
    (1)"*"
                    "*"
                   "*"
## 6
    (1)"*"
     (1)"*"
## 7
                    "*"
                    "*"
                           (1)"*"
## 8
##
          thinness.5.9.years Income.composition.of.resources Schooling
    (1)""
## 1
                                                      "*"
## 2
     (1)""
     (1)""
                           11 11
                                                      "*"
## 3
    (1)""
                                                      "*"
## 4
    (1)""
                                                      "*"
    (1)""
                                                      "*"
## 6
    (1)""
                                                      "*"
## 8 (1)""
                                                      "*"
```

Selecting the best subset model based on highest Adjusted \mathbb{R}^2 value

The model with highest R2 has parameters like schooling, HIV AIDS, Diphtheria, under five deaths, BMI, percentage expenditure, infant deaths, adult mortality.

```
adjr2_developing = which.max(nm2$adjr2)
adjr2_developing
```

[1] 8

Results

For developed nations

Traditionally, features like demographic values like population, mortality rates and income compositions are the only factors considered influential for life expectancy. This analysis shows that along with these 3 factors, there are other factors that are influential as well in determining life expectancy of a country. This result for observed for both developed as well as developing nations.

Model is built with only those factors considered influential traditionally. The summary of the model shows that even though the regression is significant, it is able to explain just 25% variability in life expectancy.

Model with only traditional variables (Developed Country):

F-statistic: 58.81 on 3 and 508 DF, p-value: < 2.2e-16

```
traditional_developed <- lm(Life.expectancy ~ Adult.Mortality + Population</pre>
                            + Income.composition.of.resources,
                            data = data developed)
summary(traditional developed)
##
## Call:
## lm(formula = Life.expectancy ~ Adult.Mortality + Population +
       Income.composition.of.resources, data = data developed)
##
## Residuals:
                       Median
                                    3Q
##
       Min
                  1Q
                                            Max
## -10.7580 -1.9649 -0.0767
                                         9.6595
                                1.5871
##
## Coefficients:
                                     Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                    8.167e+01 3.441e-01 237.304 < 2e-16 ***
## Adult.Mortality
                                   -4.023e-02 3.143e-03 -12.798 < 2e-16 ***
## Population
                                    1.417e-08 1.116e-08
                                                           1.270 0.204723
## Income.composition.of.resources 9.692e-01 2.797e-01
                                                           3.465 0.000575 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.397 on 508 degrees of freedom
## Multiple R-squared: 0.2578, Adjusted R-squared: 0.2534
```

Then, using features found to be significant using all the above methods, model is built and from its summary it can be clearly seen that including variables other than the traditionally chosen ones, the results are far better. The new model is able to explain 51% of the variation in life expectancy. This value is exactly double of the traditional method model. Including features like infant deaths, alcohol, percentage expenditure, BMI, under five deaths, Diphtheria, thinness has improved the model significantly.

Model with highest R^2 analysis:

##

```
## Call:
## lm(formula = Life.expectancy ~ Adult.Mortality + infant.deaths +
      Alcohol + percentage.expenditure + BMI + under.five.deaths +
      Diphtheria + thinness..1.19.years, data = data_developed)
##
##
## Residuals:
      Min
               10 Median
                               30
                                      Max
## -6.0485 -1.6860 -0.3929 1.0440 9.4681
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          8.463e+01 1.031e+00 82.075 < 2e-16 ***
## Adult.Mortality
                         -1.676e-02 2.910e-03 -5.761 1.46e-08 ***
## infant.deaths
                         -1.364e+00 4.000e-01
                                                -3.411 0.000699 ***
                                                -8.090 4.49e-15 ***
## Alcohol
                         -2.731e-01 3.375e-02
## percentage.expenditure 1.967e-04 3.411e-05
                                                 5.766 1.42e-08 ***
## BMI
                         -1.872e-02 7.184e-03
                                                -2.606 0.009443 **
## under.five.deaths
                          1.094e+00 3.408e-01
                                                 3.210 0.001410 **
                          2.267e-02 9.885e-03
## Diphtheria
                                                 2.293 0.022260 *
## thinness..1.19.years
                         -2.423e+00 1.938e-01 -12.503 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.733 on 503 degrees of freedom
## Multiple R-squared: 0.5242, Adjusted R-squared: 0.5166
## F-statistic: 69.27 on 8 and 503 DF, p-value: < 2.2e-16
```

For developing nations

(Intercept)

Population

Adult.Mortality

The model built with just the features from the traditional approach like mortality, population and income composition is able to explain just 50% of the variability in life expectancy.

Model with only traditional variables (Developing Country):

```
traditional_developing <- lm(Life.expectancy ~ Adult.Mortality + Population
                            + Income.composition.of.resources,
                            data = data_developing)
summary(traditional_developing)
##
## Call:
## lm(formula = Life.expectancy ~ Adult.Mortality + Population +
##
       Income.composition.of.resources, data = data_developing)
##
## Residuals:
       Min
                10 Median
                                30
                                       Max
## -29.763 -2.441
                    1.156
                             3.760
                                    24,203
## Coefficients:
                                     Estimate Std. Error t value Pr(>|t|)
##
```

Income.composition.of.resources 5.891e+00 3.513e-01 16.769

7.176e+01 3.264e-01 219.871

-4.150e-02 1.061e-03 -39.118

-5.261e-09 2.198e-09 -2.394

<2e-16 ***

<2e-16 ***

<2e-16 ***

0.0167 *

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.397 on 2412 degrees of freedom
## Multiple R-squared: 0.4962, Adjusted R-squared: 0.4955
## F-statistic: 791.8 on 3 and 2412 DF, p-value: < 2.2e-16
```

When additional predictors like infant.deaths, percentage.expenditure, Schooling, BMI, under.five.deaths, Diphtheria and HIV.AIDS were included in the model, the results improve significantly. This new model is able to explain 75% of the variability. This is huge improvement over the traditional approach. Therefore, this is an indication of a good model.

Model with highest R^2 analysis (Developing Country):

```
final_developing <- lm(Life.expectancy ~ Adult.Mortality + infant.deaths</pre>
                      + percentage.expenditure + Schooling
                      + BMI + under.five.deaths
                      + Diphtheria + HIV.AIDS,
                      data= data_developing)
summary(final_developing)
##
## Call:
## lm(formula = Life.expectancy ~ Adult.Mortality + infant.deaths +
       percentage.expenditure + Schooling + BMI + under.five.deaths +
##
       Diphtheria + HIV.AIDS, data = data_developing)
##
```

```
##
        Min
                  10
                        Median
                                     30
                                              Max
## -23.9740 -2.5569
                        0.0239
                                 2.5986
                                         22.3040
##
## Coefficients:
```

Residuals:

Estimate Std. Error t value Pr(>|t|) ## (Intercept) 58.9523142 0.4504796 130.87 <2e-16 *** ## Adult.Mortality -0.0190058 0.0009022 -21.07 <2e-16 *** ## infant.deaths 0.1168309 0.0089885 13.00 <2e-16 *** ## percentage.expenditure 0.0012202 0.0001151 10.60 <2e-16 *** 16.56 <2e-16 *** ## Schooling 0.4894724 0.0295521 ## BMI 0.0857047 0.0056815 15.09 <2e-16 *** ## under.five.deaths -13.32-0.0884421 0.0066374 <2e-16 *** ## Diphtheria 0.0543058 0.0040040 13.56 <2e-16 *** ## HIV.AIDS -0.5019348 0.0194197 -25.85 <2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1 ## Residual standard error: 4.493 on 2407 degrees of freedom ## Multiple R-squared: 0.752, Adjusted R-squared: 0.7512

F-statistic: 912.3 on 8 and 2407 DF, p-value: < 2.2e-16

Factors affecting Life Expectancy

The influential factors in determining the life expectancy in developed nations are:

- 1. Adult Mortality
- 2. Infant Deaths
- 3. Alcohol
- 4. Percentage expenditure percentage expenditure on health as percent of GDP
- 5. BMI
- 6. Under five deaths
- 7. Diphtheria Percentage of Diphtheria immunization coverage among 1 year-olds
- 8. thinness 1-19 years

The linear regression model used to predict life expectancy for developed nations is:

Life expectancy = 8.463 - 0.0167 Adult.mortality - 1.364 infant.deaths - 0.273 Alcohol + 0.001967 percentage.expenditure - 0.01872 BMI - 1.094 under.five.deaths + 0.02267 Diphtheria - 2.423 thinness.1.19.years

Similarly, influential factors in case of developing nations are:

- 1. Adult Mortality
- 2. Infant Deaths
- 3. Percentage expenditure percentage expenditure on health as percent of GDP
- 4. Schooling
- 5. BMI
- 6. Under five deaths
- 7. Diphtheria Percentage of Diphtheria immunization coverage among 1 year olds
- 8. thinness 1-19 years

The linear regression model used to predict life expectancy for developing nations is:

Life expectancy = 58.95 - 0.019 Adult.mortality - 0.1168 infant.deaths + 0.0012 percentage.expenditure - 0.01872 BMI + 0.4894 Schooling + 0.85 BMI - 0.008 under.five.deaths+ 0.0543 Diphtheria - 0.0501 thinness.1.19.years

Therefore, new predictors that improved model efficiency common across both types of countries are infant deaths, percentage expenditure, BMI, under five deaths, Diphtheria and thinness 1-19 years.

Impact of Healthcare Expenditure on Life Expectancy

Healthcare expenditure has an impact on life expectancy. The positive coefficient implies healthcare expenditure has a positive relationship with life expectancy. Therefore, as expenditure on healthcare increases, life expectancy of that country increases. This is true for both developed and developing nations.

Impact of Alcohol Consumption on Life Expectancy

An interesting observation was made when it comes to alcohol consumption. This is a predictor only for developed nations and not for developing nations. It has a negative relation with life expectancy.

Impact of Immunization Coverage on Life Expectancy

Positive regression coefficient for Diphtheria immunization coverage implies positive relation between immunization coverage and life expectancy. So as immunization increases life expectancy increases as well.

Conclusion

Life expectancy of a country can be determined using various features other than those used traditionally. It was observed that model built using just the traditional predictors was resulting in a weak model which was able to account for just 25% (for developed nations) or 50% (for developing nations) of the variability in life expectancy. But the model improved significantly when other features like healthcare expenditure, alcohol consumption, immunization coverage where included as predictors.

Both healthcare spend and immunization of children have positive relation with life expectancy. Logically, this relationship makes perfect sense as well. If a country has better vaccination rates and higher spend on healthcare, people will be immune against variety of diseases and they also will be privy to good health care facilities thus resulting in increased life expectancy.

In developed nations, alcohol consumption has negative impact on life expectancy. Logically speaking, heavy alcohol consumption leads to various ailments some of which result in pre-mature deaths, can also result in accidents and so on. Therefore, results from the model make sense.

Multiple linear regression model was satisfactorily able to explain influential factors for life expectancy.