Example of biased estimator better than MVUE

$$MSE(\theta_b) = E[(\theta_b - E[\theta_b])^2] + (E[\theta_b] - \theta_0)^2$$

$$Variance (N+term) + iao^2 (2M term).$$

$$(2nd) = \left[(1+a)\theta_0 - \theta_0 \right]^2 = \tilde{a}\theta_0^2$$

$$(1st) = \left[\left[(1+a)\hat{\theta}_{MVUE} - (1+a)\theta_0 \right] \right] =$$

$$= (1+a)^2 E \left[\left(\hat{\theta}_{MVUE} - \theta_0 \right)^2 \right] =$$

$$= (1+a)^2 MSE \left(\hat{\theta}_{MVUE} \right).$$

$$MSE \left(\hat{\theta}_b \right) = (1+a)^2 MSE \left(\hat{\theta}_{MVUE} \right) + \tilde{a}\theta_0$$

$$\mathcal{Y}$$

We want: y < x i.e y-x<0

$$y-x=(1+a)^2 \times +a\theta_0^2 \times$$

=
$$x + ax + 2ax + a^{2}\theta_{0}^{2} - x = a[a(x+\theta_{0}^{2}) + 2x]$$

Want < 0.

$$a<0$$
 and $a(x+\theta_0^2)+2x>0 \Rightarrow a>-\frac{2x}{x+\theta_0^2}$

$$\frac{2x}{x+\theta_o^2} < \alpha < 0$$

d biased estimator better than the best Unbiosed one.

Optimal value:
$$\frac{dy}{da} = 0 = 2(1ta)x + 2a\theta_0^2$$

$$\Rightarrow \alpha_* = \frac{\times}{\times + \theta_0^2} \Rightarrow Don't Rhow.$$

Ridge regression-toy problem.

$$\left[\sum_{n=1}^{\infty}(x_nx_n)+j_0\right]\theta_1=\sum_{n=1}^{\infty}g_nx_n.$$
where each $x_n=1$.

$$(N+\lambda)\hat{\theta_s} = \sum_{N=1}^{N} y_N \Rightarrow \hat{\theta_s} = \sum_{N+\lambda}^{N+\lambda} = \sum_{N+\lambda}^{N+\lambda} \hat{\theta_s}.$$

$$E[\hat{\theta_s}] = \sum_{N+\lambda}^{N+\lambda} E[\hat{\theta_s}] = \sum_{N+\lambda}^{N+\lambda} \hat{\theta_s}.$$

$$MSE(\theta) = E[(\theta'-\theta)] = E[(MX Q - \theta)]$$

$$MJE = 2^{2}E[(\bar{y})^{2}] - 2$$

$$E\left[(g)^2\right] = \frac{6n}{N} + \theta^2$$

Seek the minimum of MSE:

$$\frac{d \operatorname{MSE}(\hat{\theta_b})}{d z} = 0 \Rightarrow z_* = \frac{\theta_0^2}{\frac{6^2}{N^2 + \theta_0^2}} = \frac{1}{\frac{6^2}{N^2 + 1}}.$$

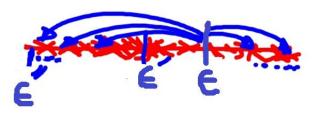
$$\frac{2}{N+\lambda} = \frac{1}{1+\lambda}$$

$$3* = \frac{6n}{\theta^2}$$

MSE
$$(\hat{\theta}_{b}^{*}) = \frac{6^{2}}{N} \frac{1}{1 + \frac{6^{2}}{N6^{2}}}$$
 $(\frac{6^{2}}{N})^{2}$

$$= \int_{y}^{2} f(y) dy - 2 \in \int_{y} y(y) dy$$

$$+ \in^{2} \int_{y} f(y) dy =$$



 $\frac{dQ}{dE} = -2E[y] + 2E = 0.$