

$$\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$$

$$\begin{aligned} \frac{d}{dx}(\sqrt{x}) &= \frac{d}{dx}(x^{1/2}) = \frac{1}{2} \cdot x^{\frac{1}{2}-1} = \\ &= \frac{1}{2} x^{-1/2} = \frac{1}{2} \frac{1}{x^{1/2}} = \frac{1}{2} \frac{1}{\sqrt{x}} \end{aligned}$$

$$\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx = 2 \int \frac{1}{2} \frac{\sin \sqrt{x}}{\sqrt{x}} dx = 2 \int \frac{1}{2\sqrt{x}} \sin \sqrt{x} dx =$$

$$= 2(-\cos \sqrt{x}) + C \rightarrow -2 \cos \sqrt{x} + C$$

$$\int f(x) \cdot \sin f(x) dx = -\cos f(x) + C$$