

Logistic Regression

$$H(x) = 1/(1 + \exp^{(-\theta_0 + \theta_1(x))})$$

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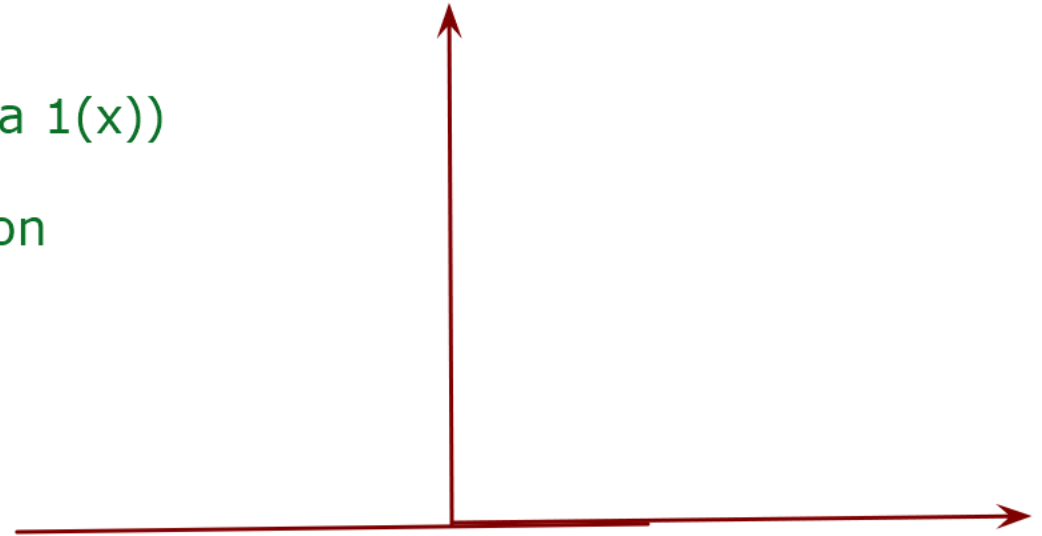
Sigmoid function or logistic function

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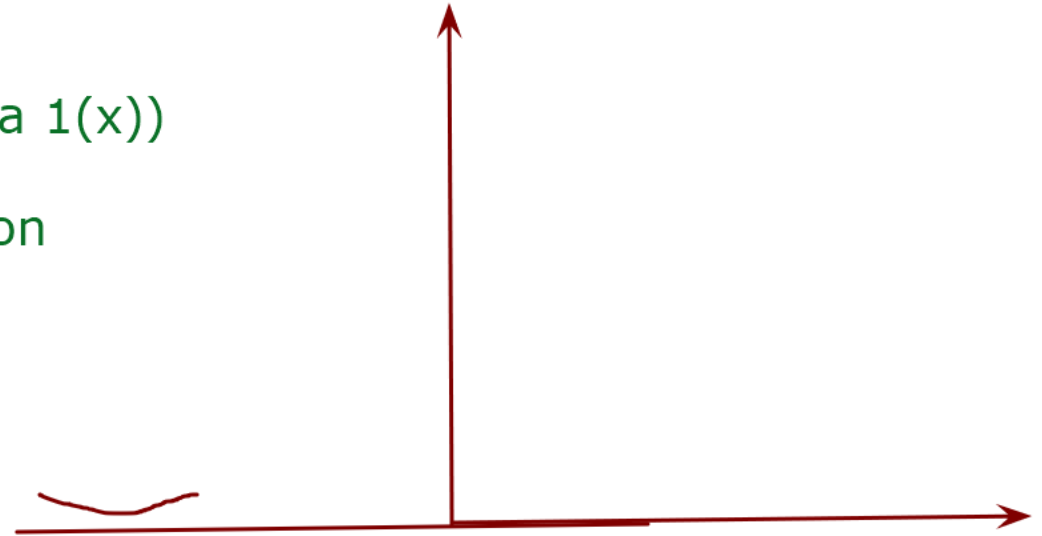
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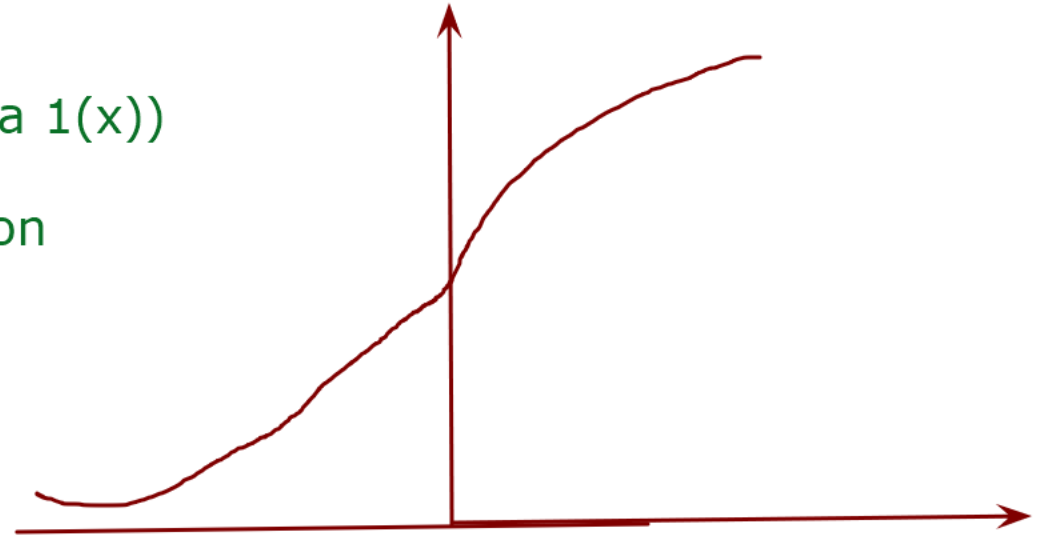
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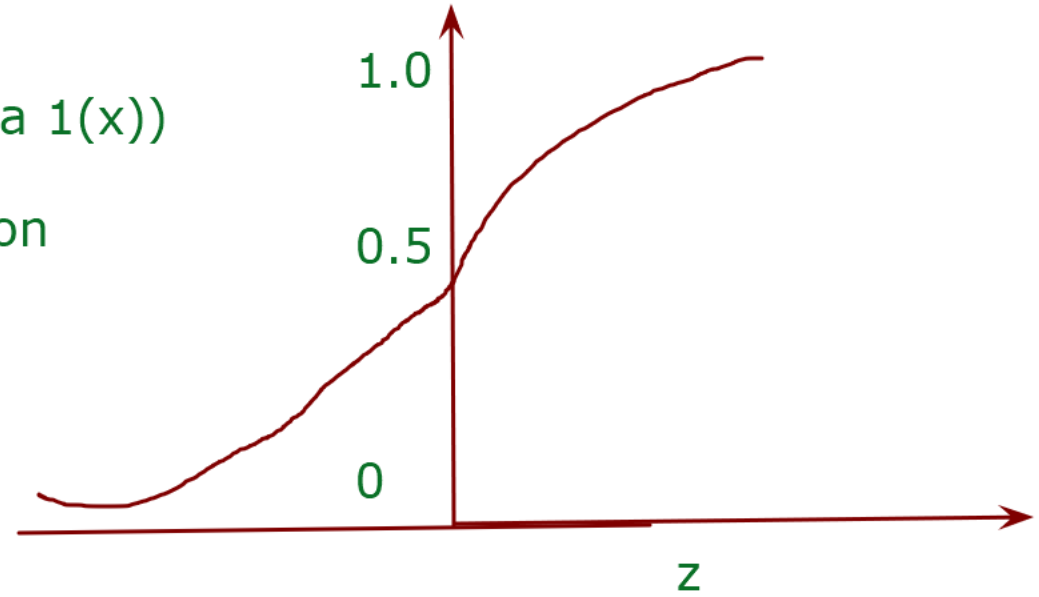
$$H(x) = 1/(1 + \exp^{-(\theta_0 + \theta_1 x)})$$

Sigmoid function or logistic function



$$H(x) = 1 / (1 + \exp^{-\theta_0 - \theta_1(x)})$$

Sigmoid function or logistic function

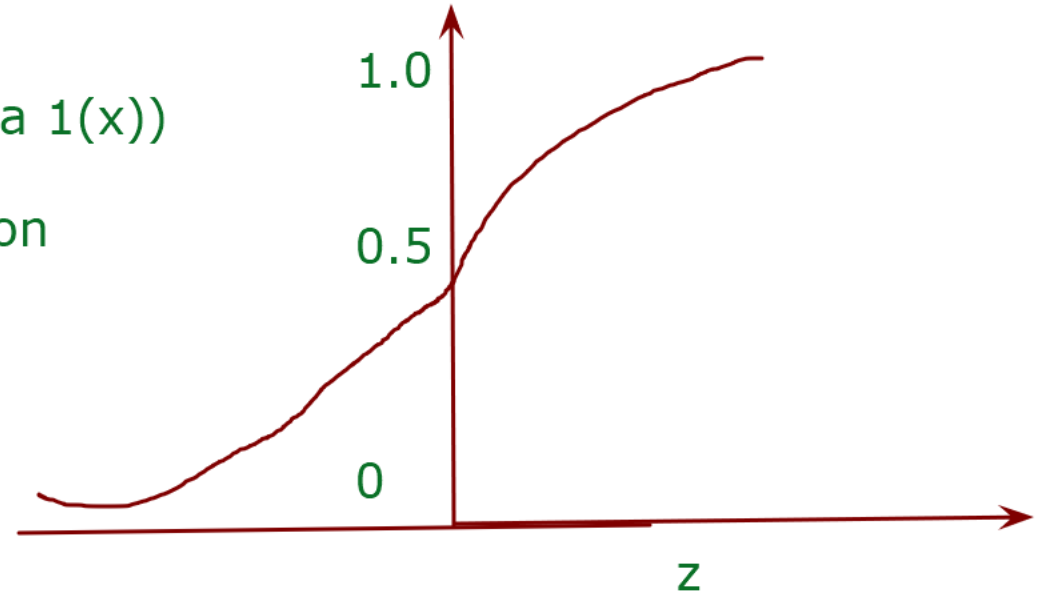


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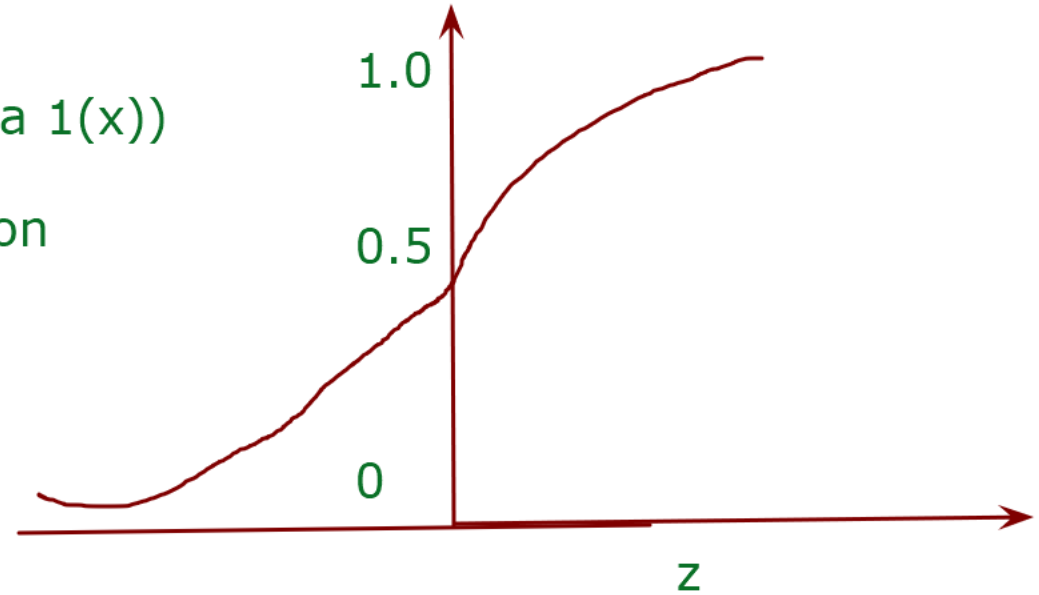


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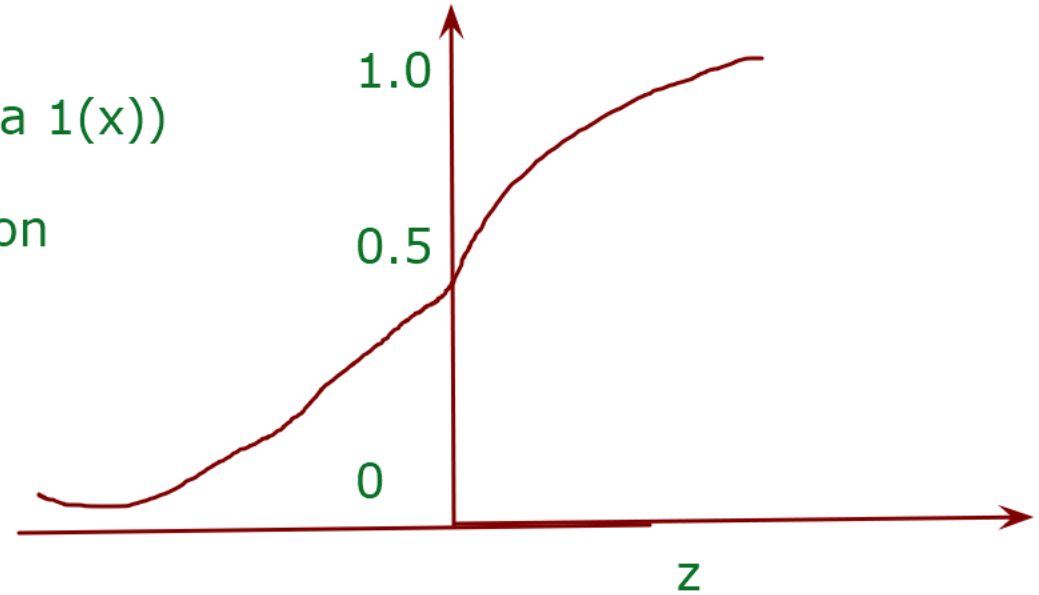
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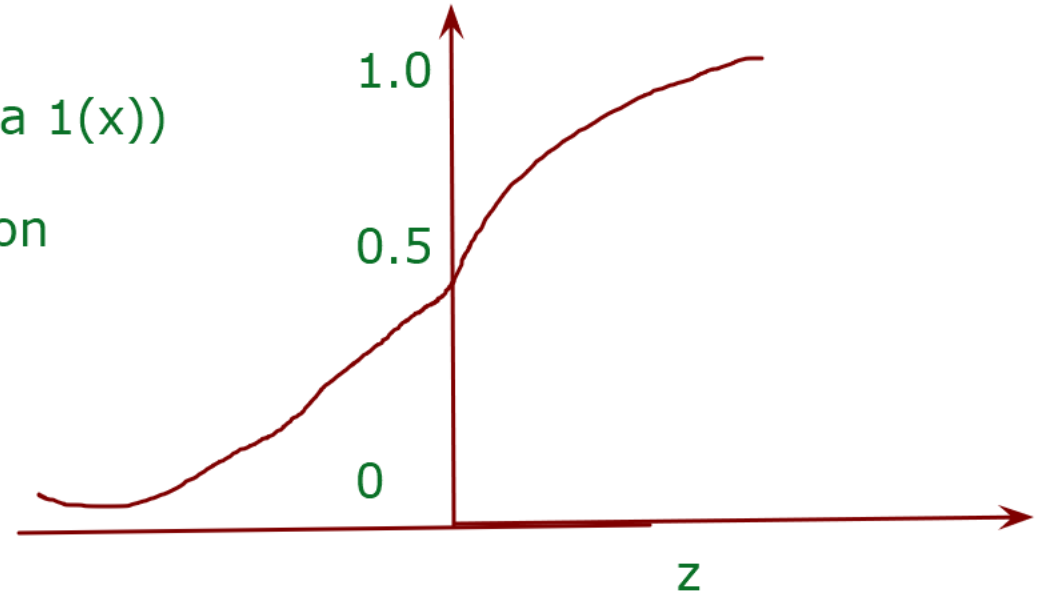
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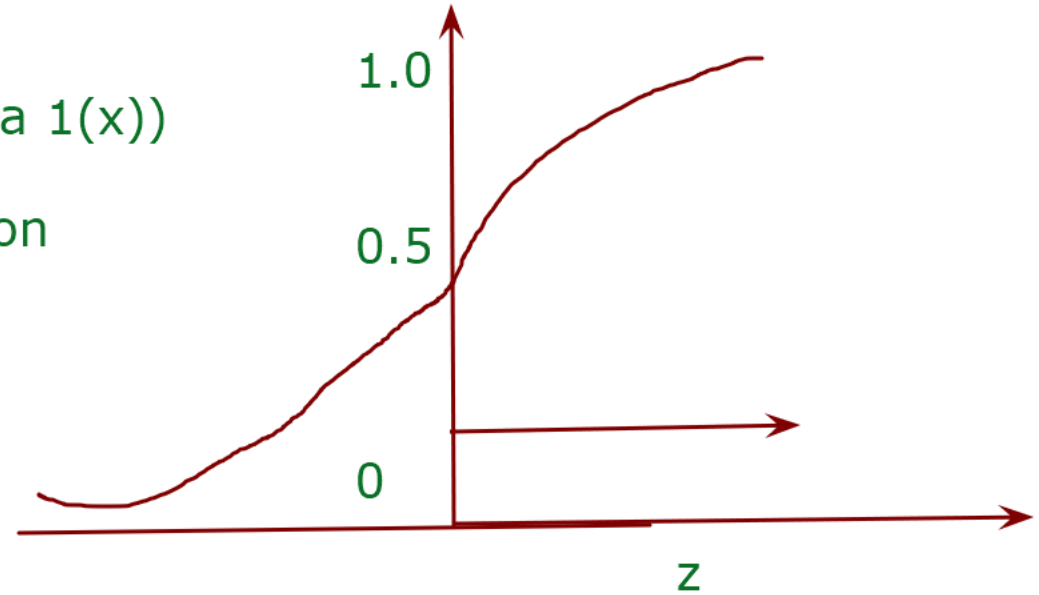
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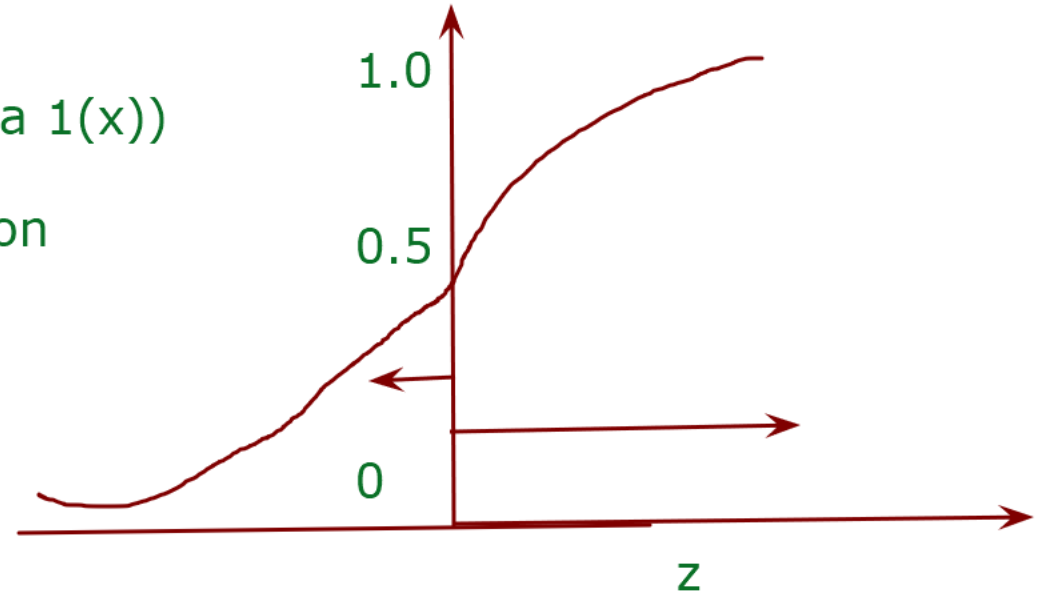
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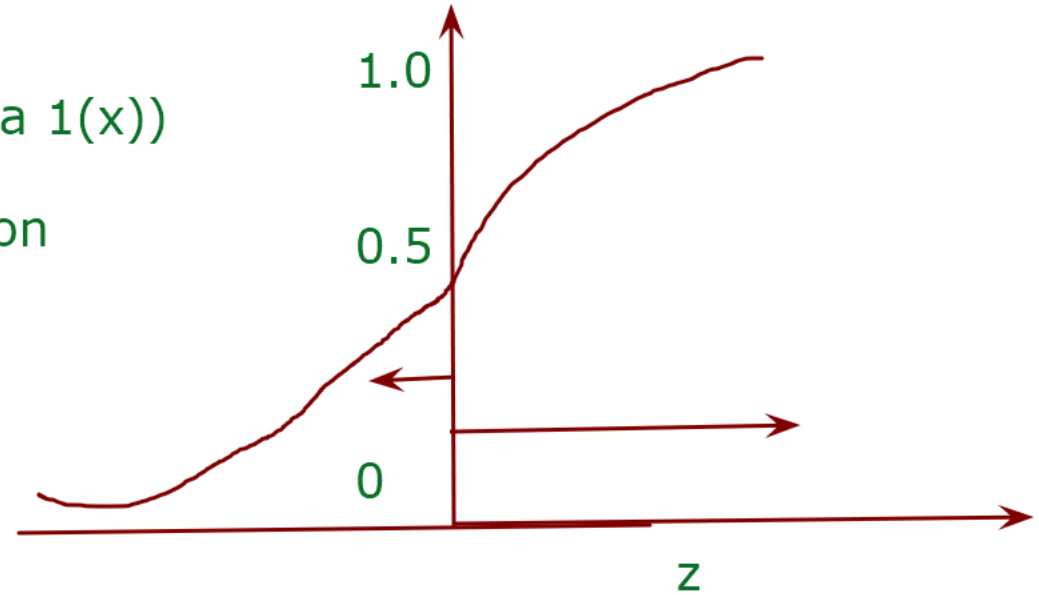
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Decision Boundary



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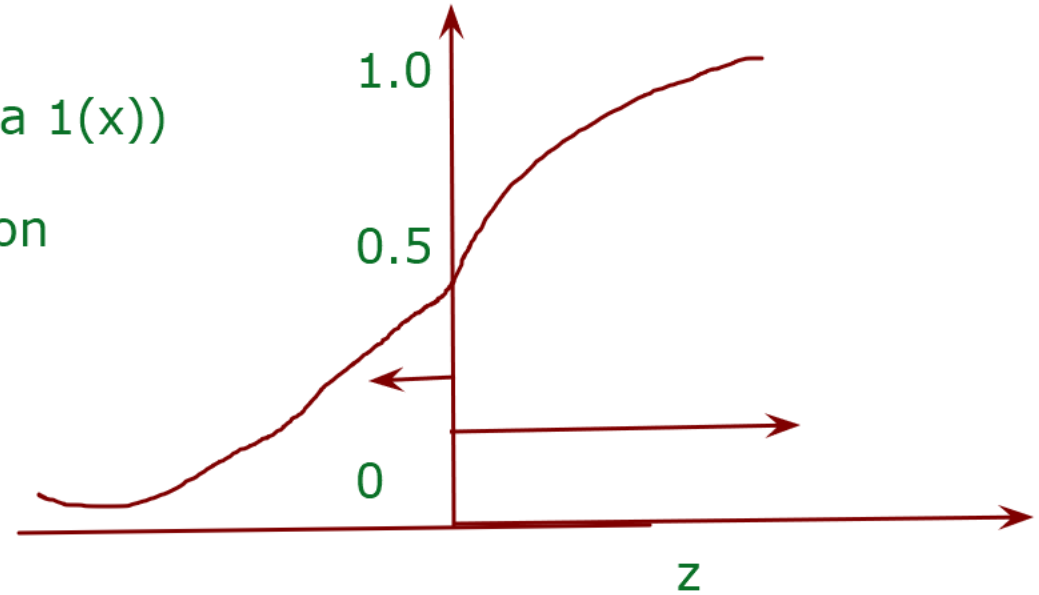
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cost function = summation from $i = 1$ to m $(h(x_i) - y_i)^2$



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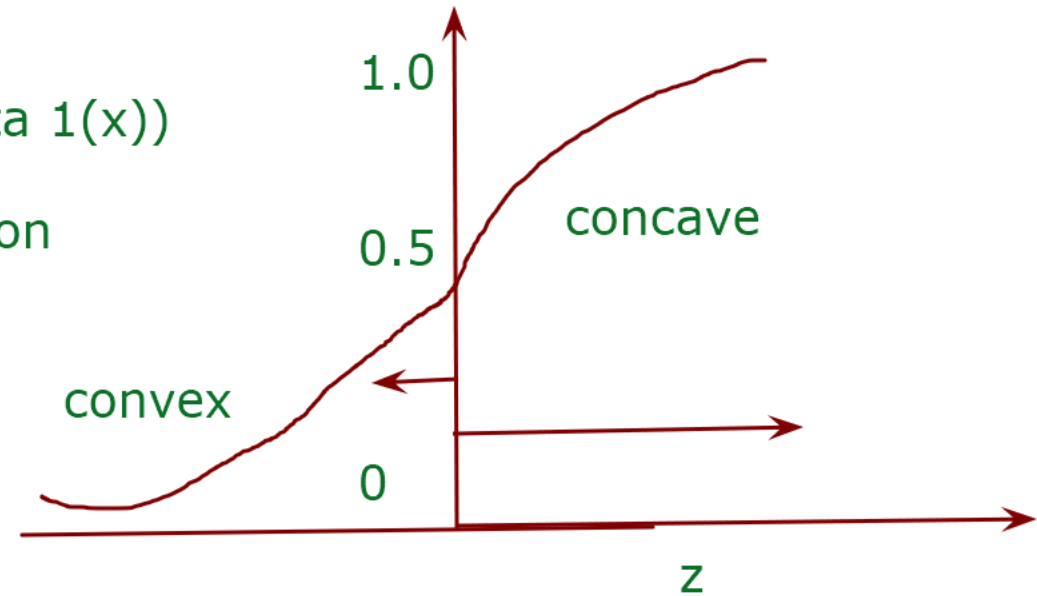
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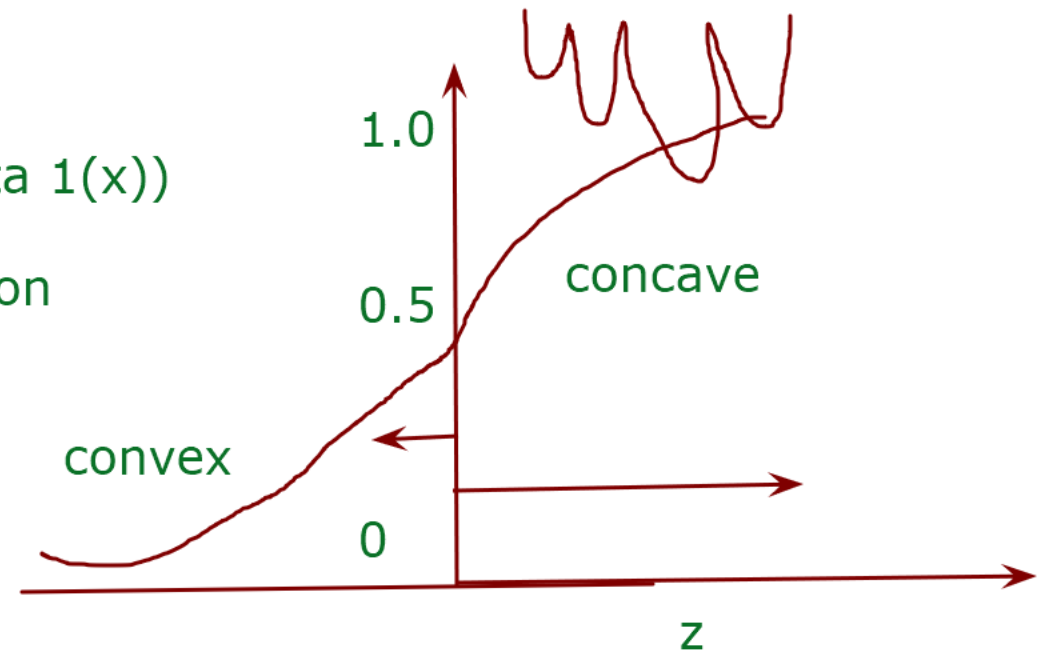
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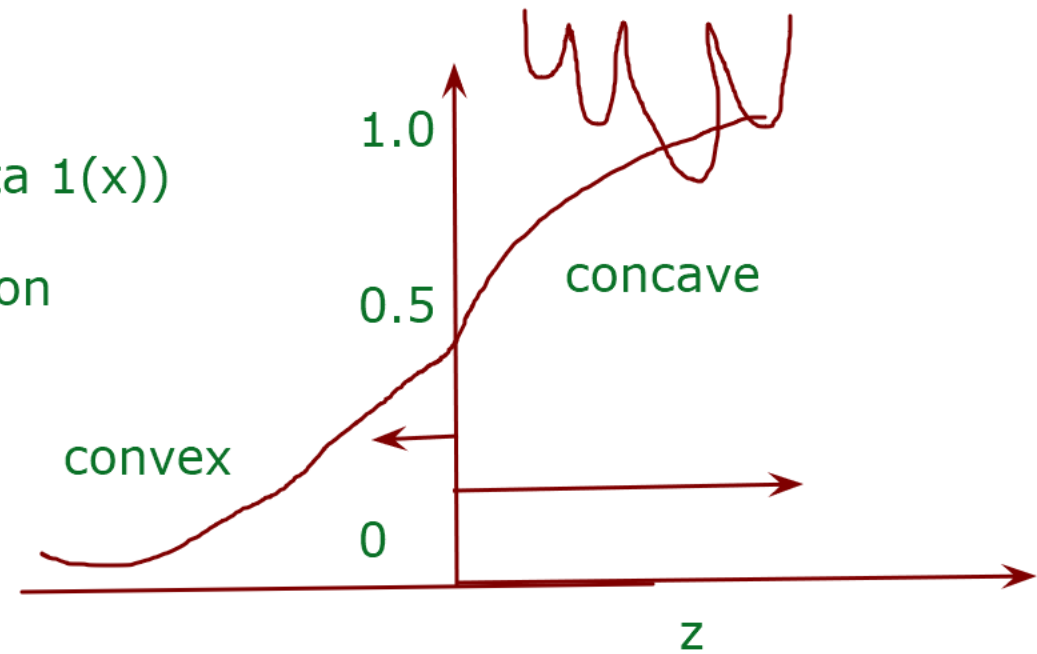
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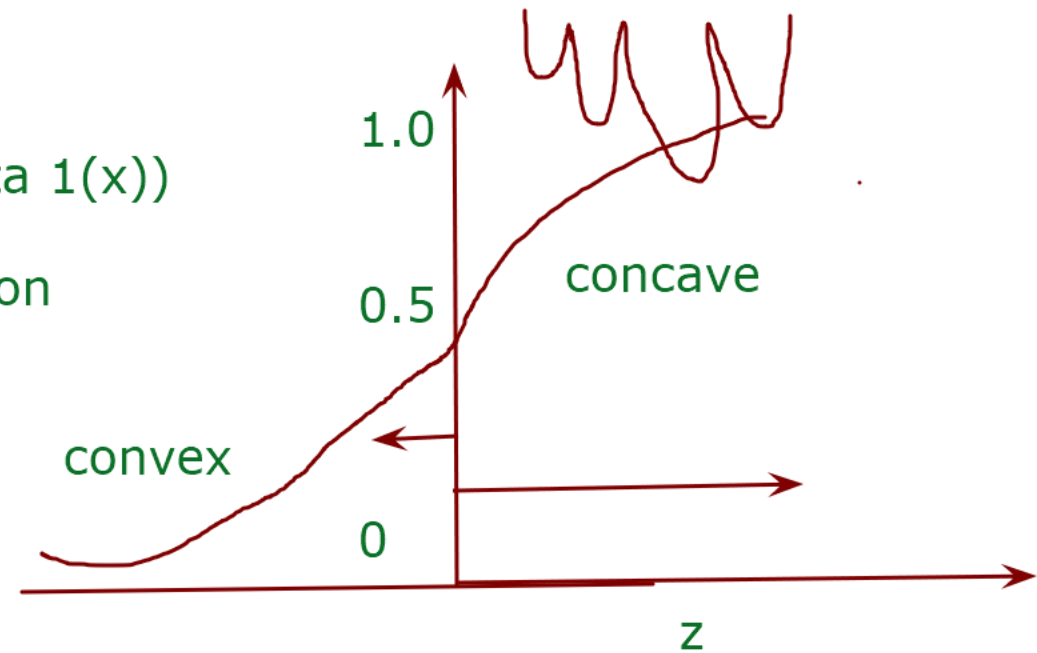
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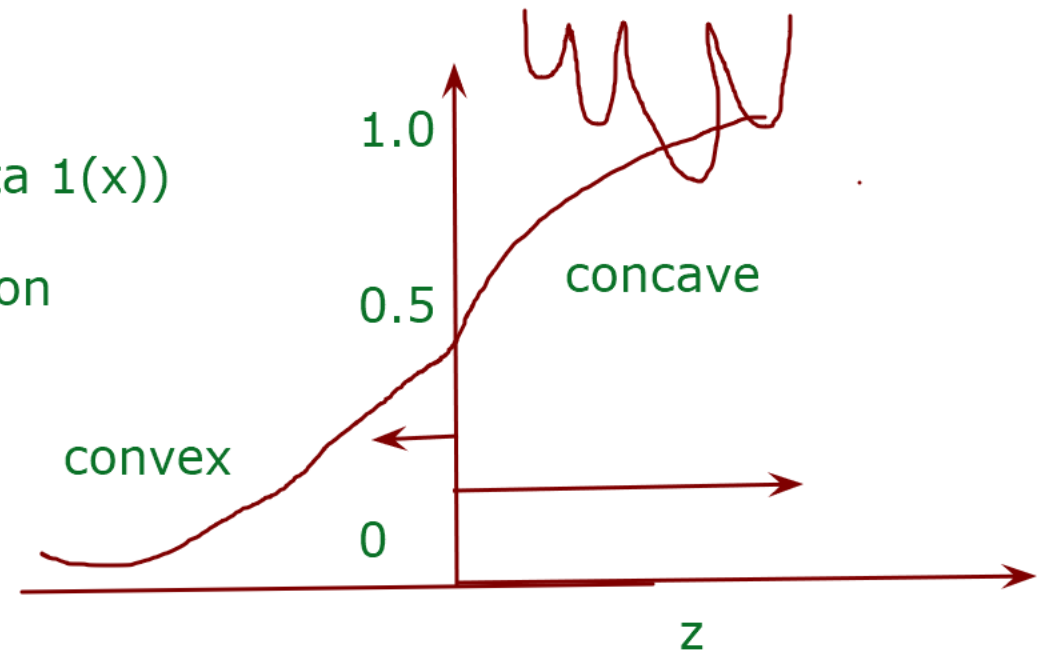
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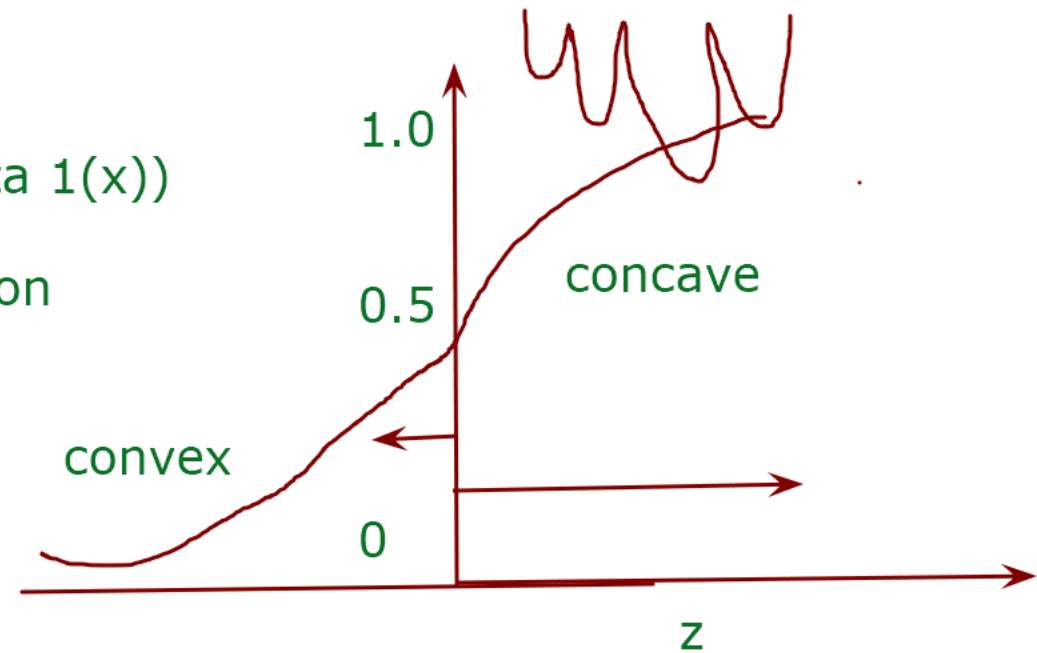
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$$x_1 + x_2 \geq 3; y = 1$$

$$H(x) = g(\theta_0 + \theta_1(x_1) + \theta_2(x_2)) \quad ; \quad H(x) = g(z)$$

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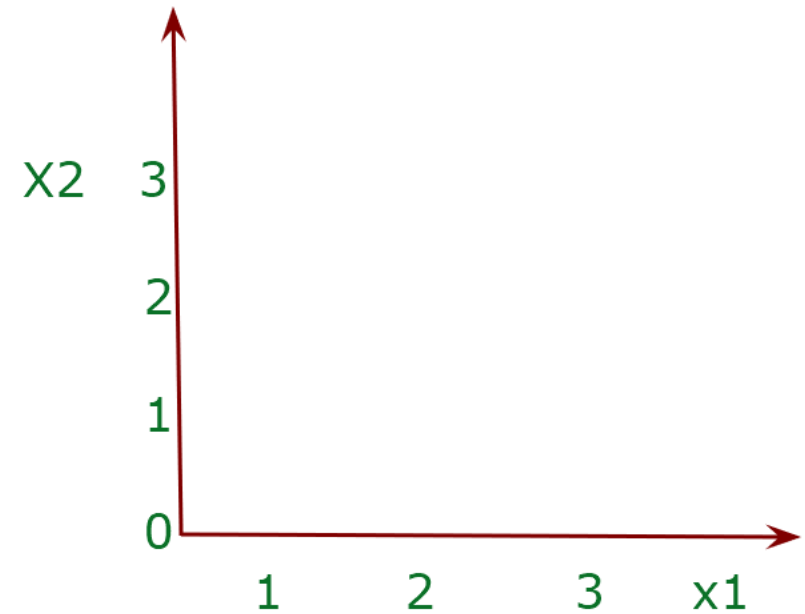


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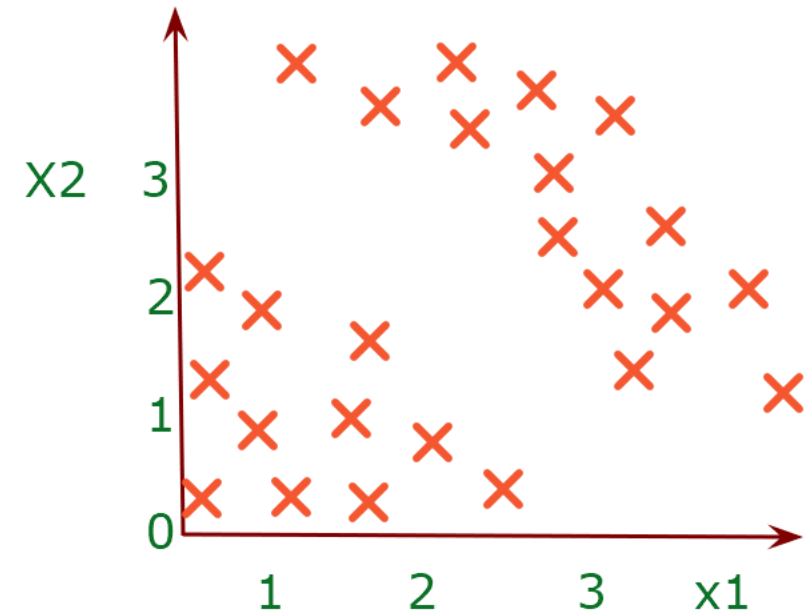


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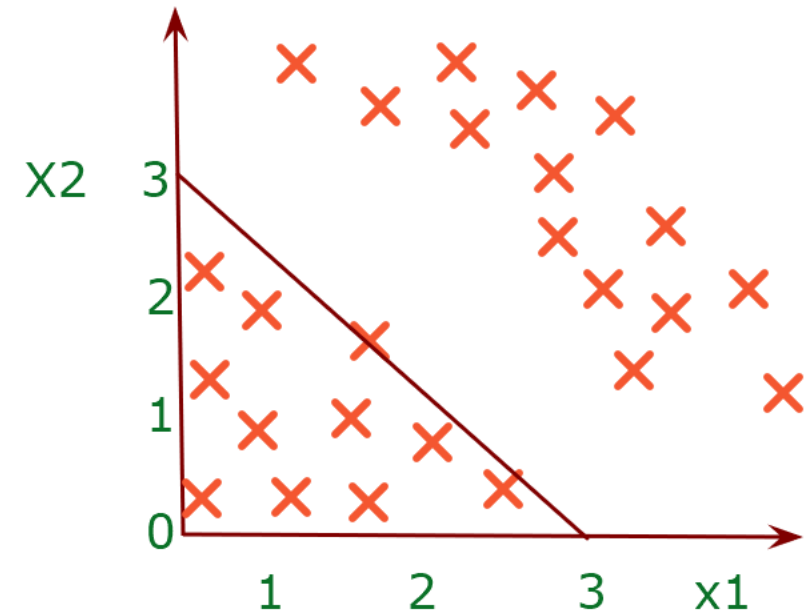
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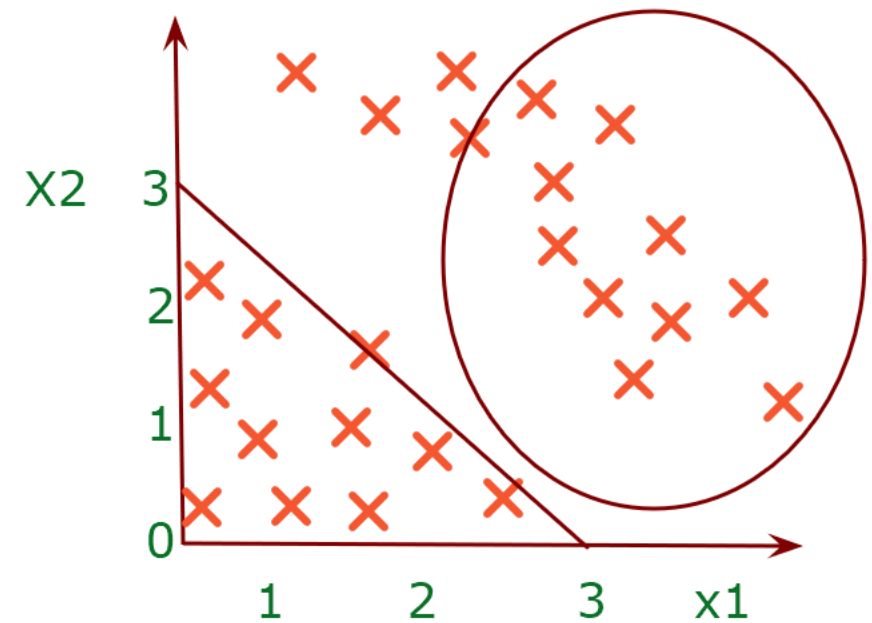
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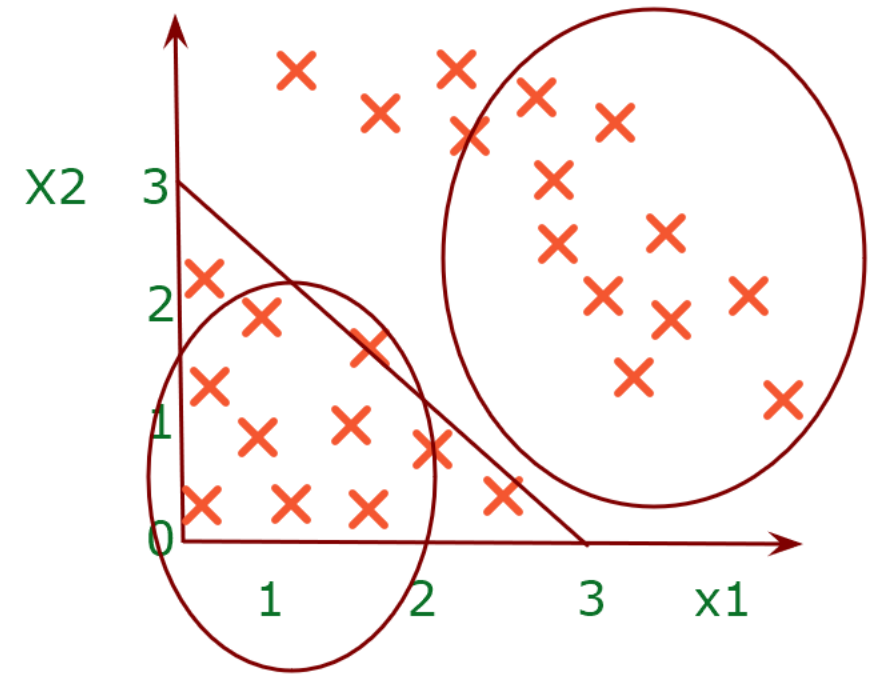
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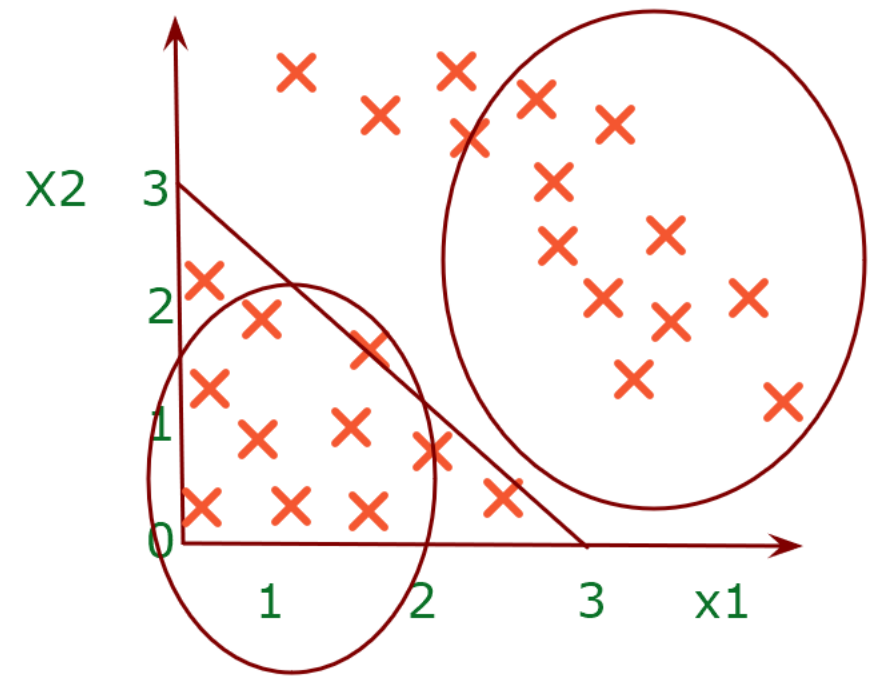
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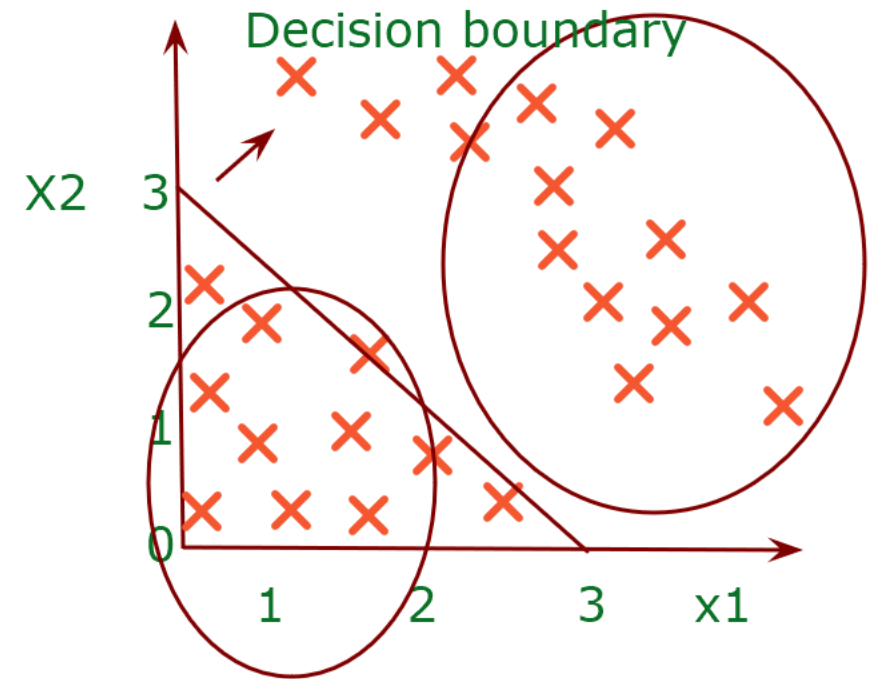


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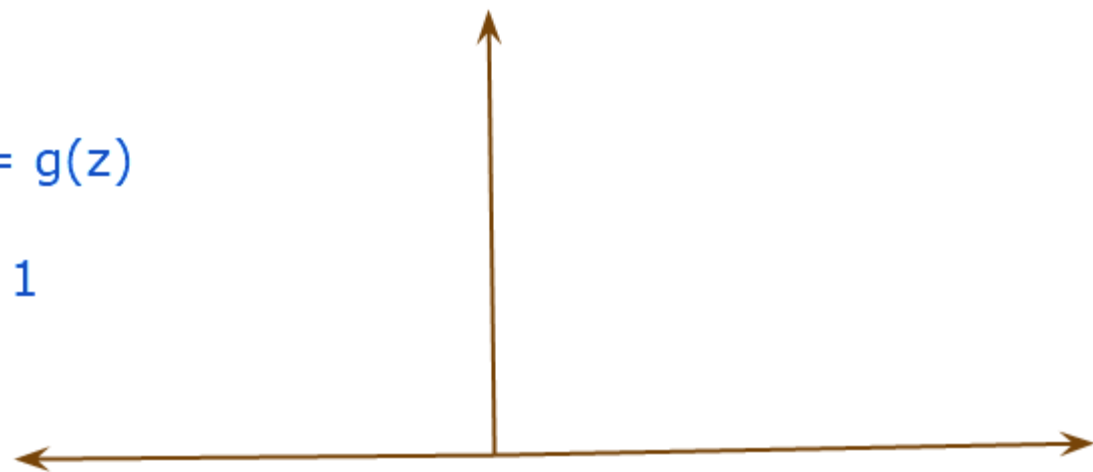
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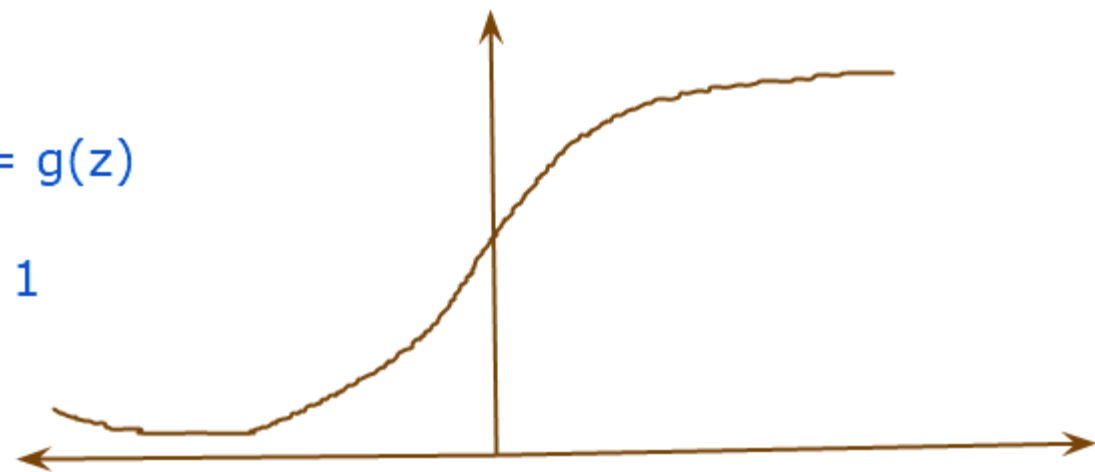
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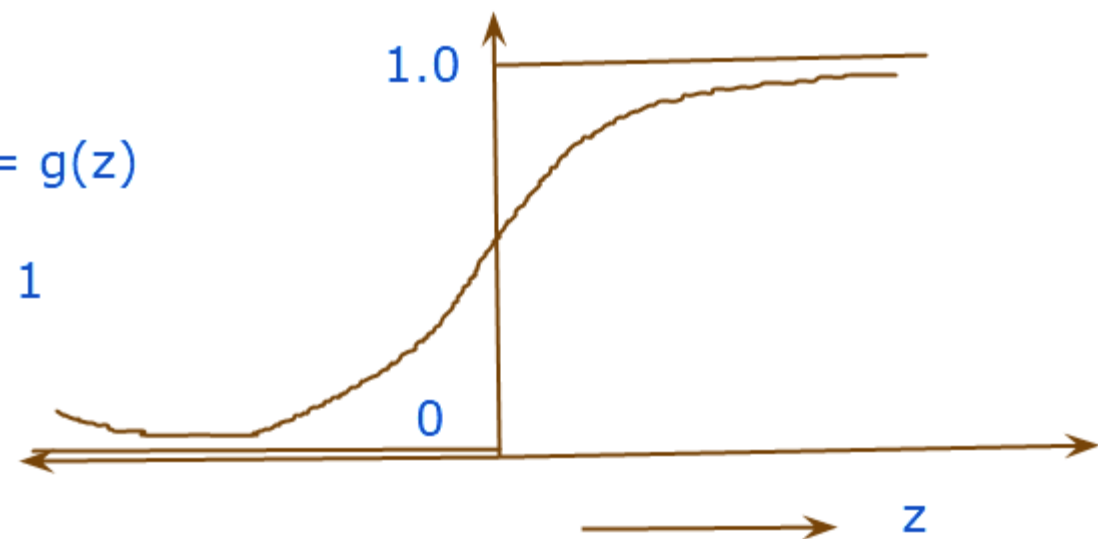
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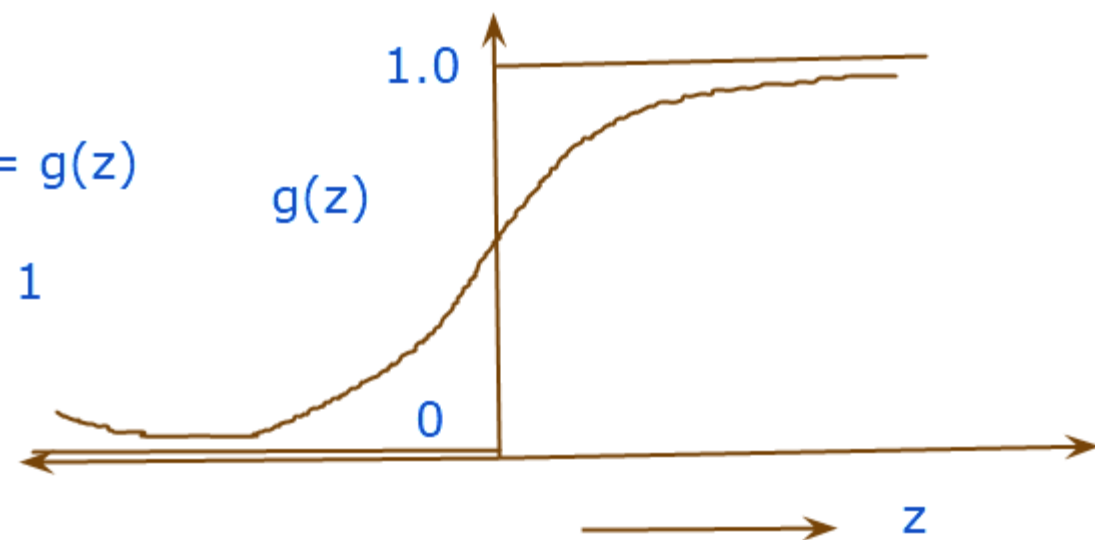
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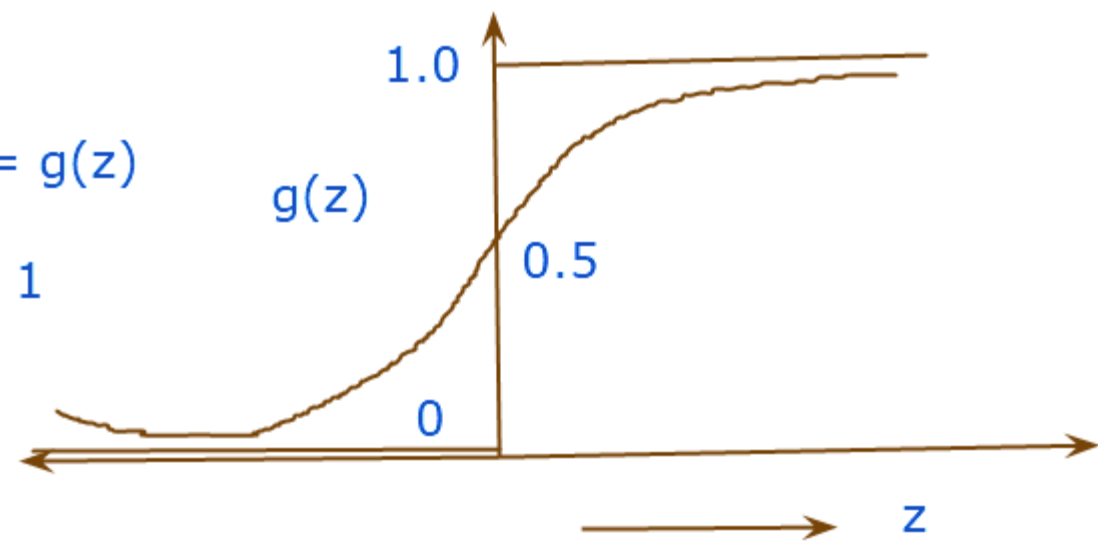
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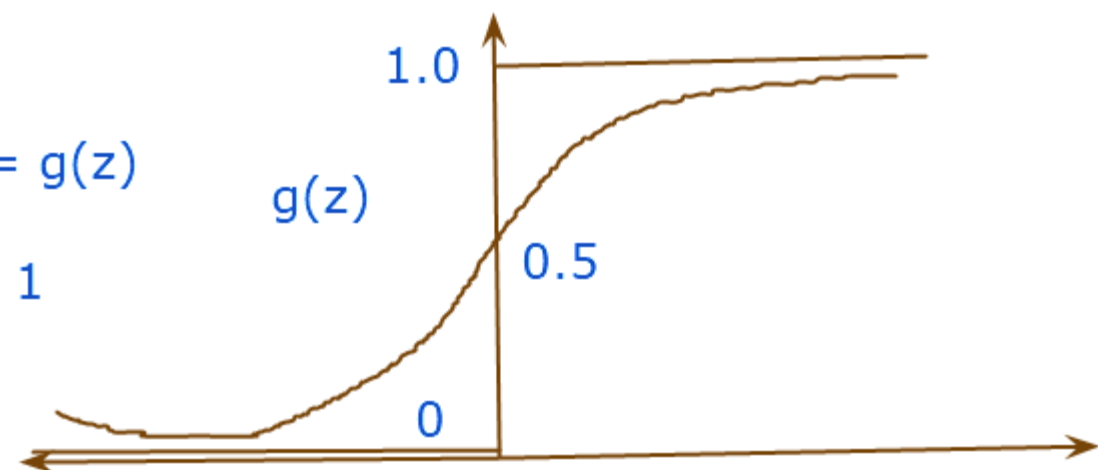
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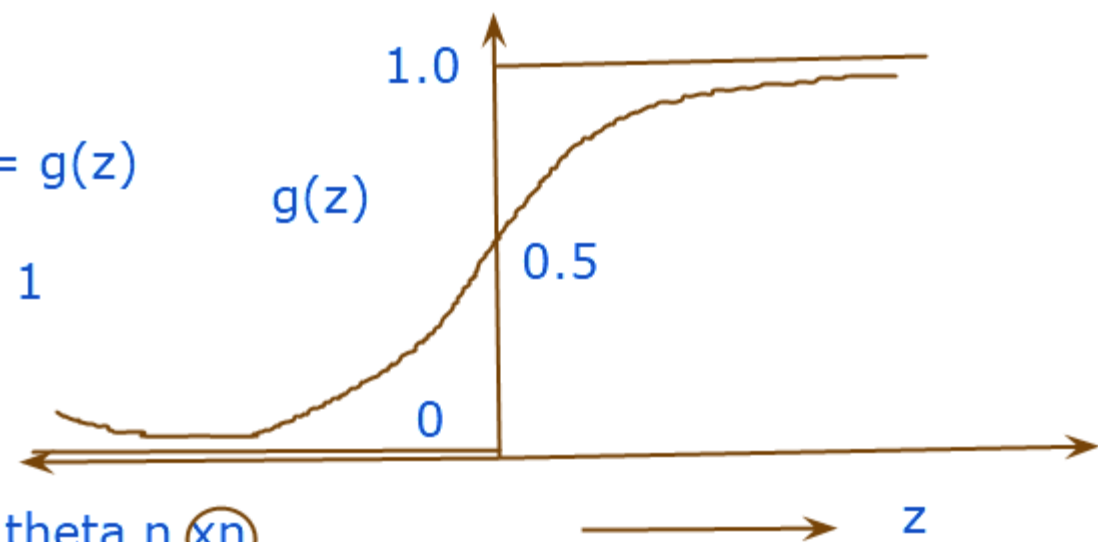
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$$z = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

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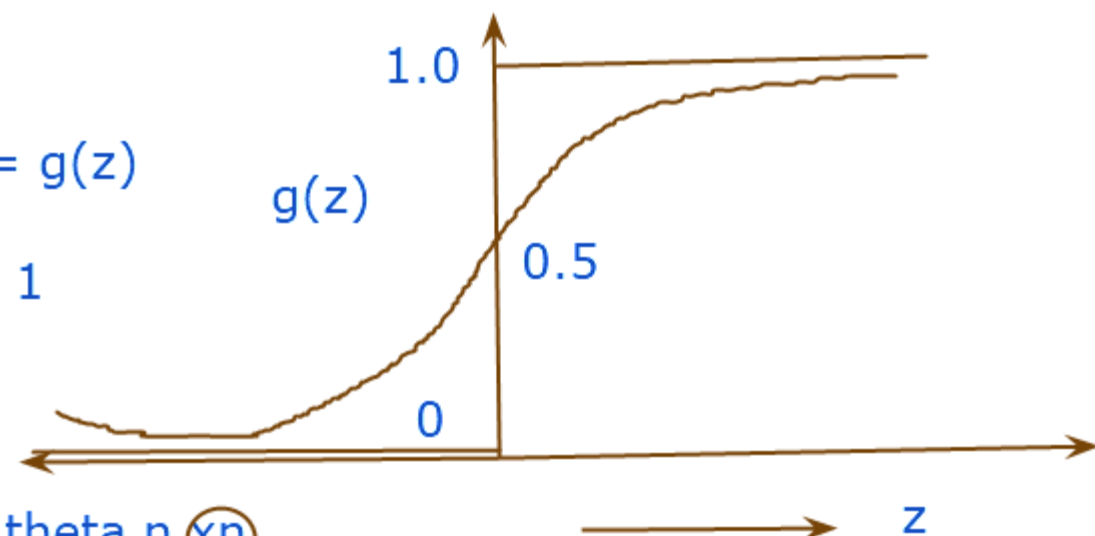
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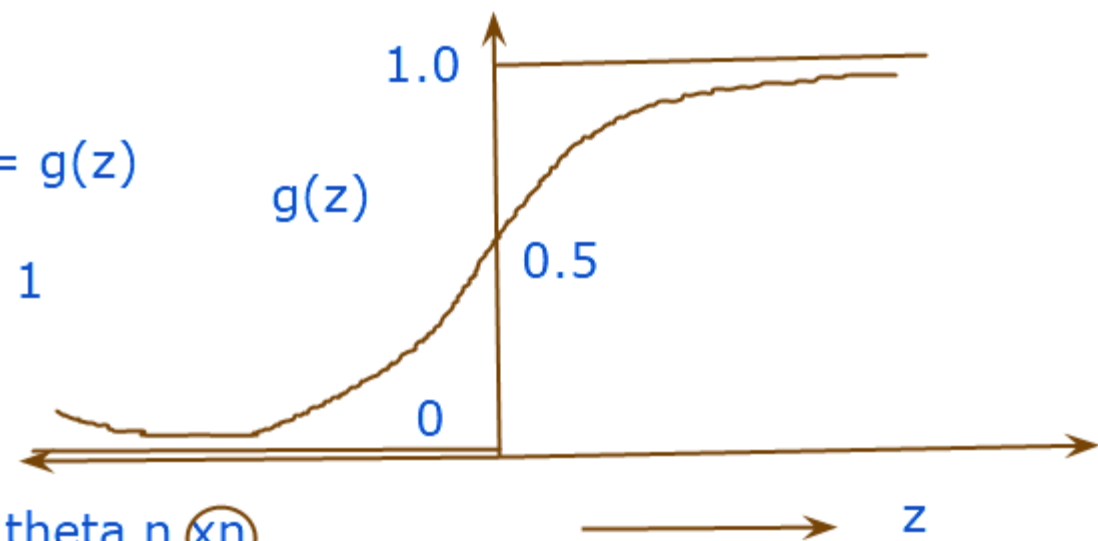


$$z = \text{theta } 0 + \text{theta } 1 \textcircled{x1} + \text{theta } 2 \textcircled{x2} + \dots + \text{theta } n \textcircled{xn}$$

Lets assume: $H(x) = g(\text{theta } 0 + \text{theta } 1 x1 + \text{theta } 2 x2)$

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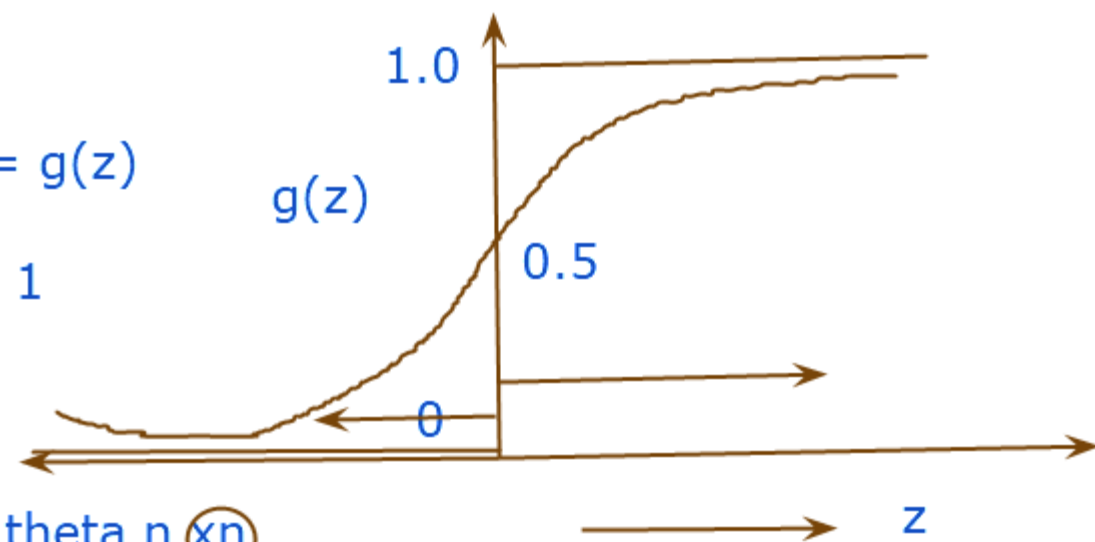
-3

1

1

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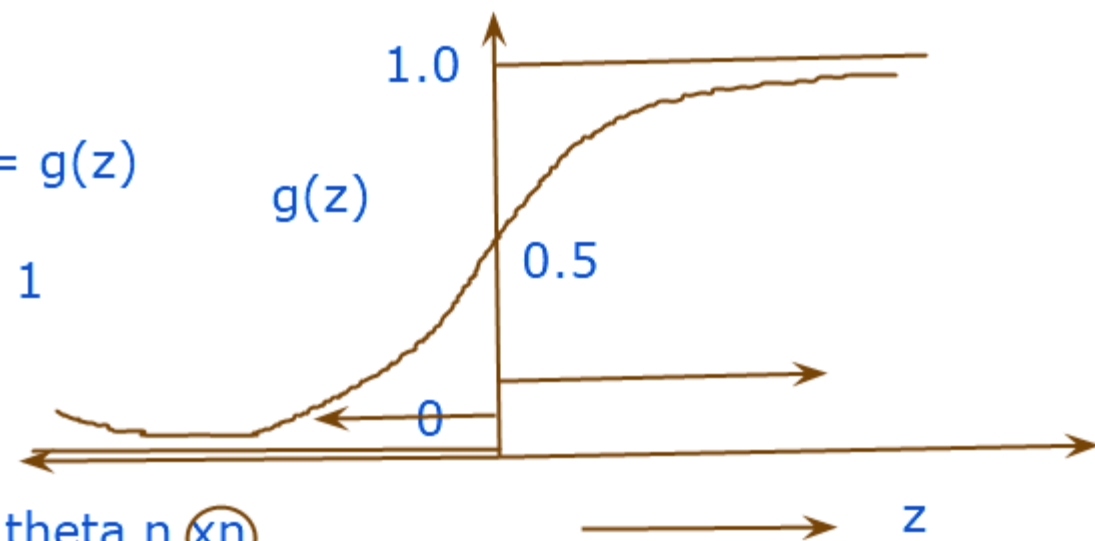
$$\begin{matrix} -3 & 1 & 1 \end{matrix}$$

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$$H(x) = g(z) \geq 0.5; y = 1$$

$$= g(z) < 0.5; y = 0$$



$$z = \text{theta } 0 + \text{theta } 1 \textcircled{x1} + \text{theta } 2 \textcircled{x2} + \dots + \text{theta } n \textcircled{xn}$$

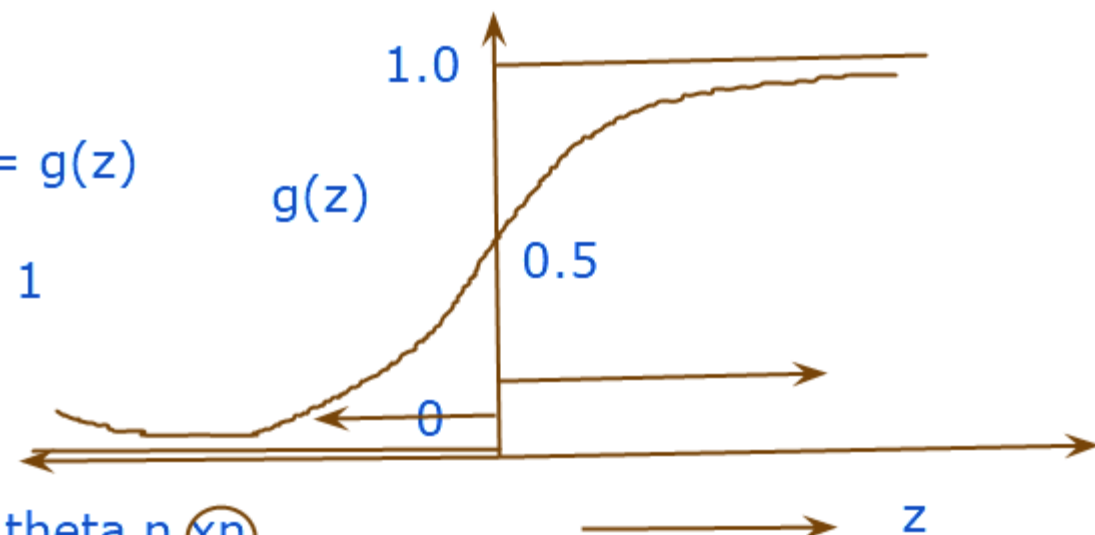
$$\text{Lets assume: } H(x) = g(\text{theta } 0 + \text{theta } 1 x1 + \text{theta } 2 x2)$$

$$\begin{matrix} & -3 & 1 & 1 \end{matrix}$$

$$H(x) = -3 + x1 + x2 \quad \text{If } H(x) \geq 0.5 ; z \geq 0; Y = 1$$

$$H(x) = p = 1/(1+e^{(-z)}) = g(z)$$

$$\begin{aligned} H(x) &= g(z) \geq 0.5; y = 1 \\ &= g(z) < 0.5; y = 0 \end{aligned}$$



$$z = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

$$\text{Let's assume: } H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$$

$$\begin{matrix} -3 & 1 & 1 \end{matrix}$$

$$H(x) = -3 + x_1 + x_2 \quad \text{If } H(x) \geq 0.5; z \geq 0; Y = 1$$

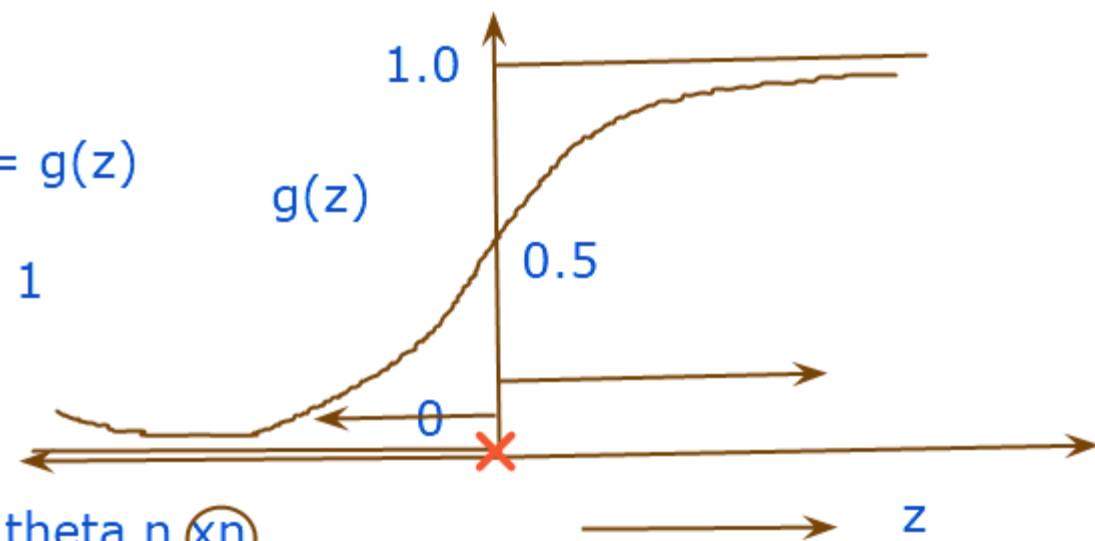
$$-3 + x_1 + x_2 \geq 0; y = 1$$

$$-3 + x_1 + x_2 < 0; y = 0$$

$$H(x) = p = 1/(1+e^{(-z)}) = g(z)$$

$$H(x) = g(z) \geq 0.5; y = 1$$

$$= g(z) < 0.5; y = 0$$



$$z = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

Lets assume: $H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$

$$\begin{matrix} -3 & 1 & 1 \end{matrix}$$

$$H(x) = -3 + x_1 + x_2 \quad \text{If } H(x) \geq 0.5; z \geq 0; Y = 1$$

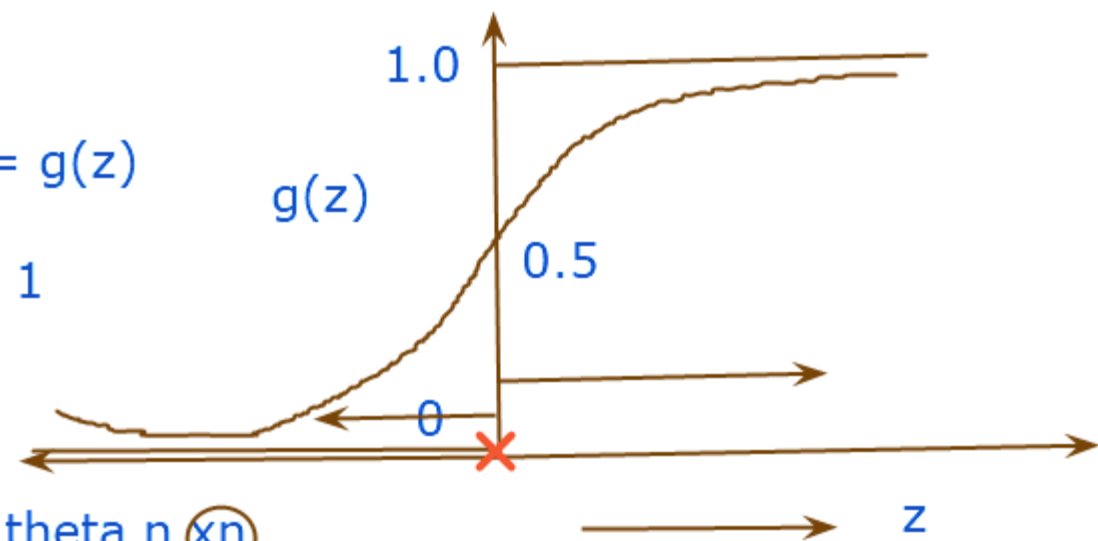
$$-3 + x_1 + x_2 \geq 0; y = 1$$

$$-3 + x_1 + x_2 < 0; y = 0 \quad -3 + x_1 + x_2 = 0; \text{decision boundary}$$

$$H(x) = p = 1/(1+e^{(-z)}) = g(z)$$

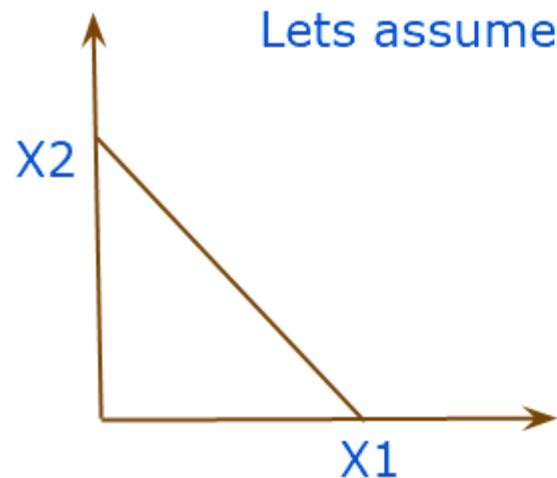
$$H(x) = g(z) \geq 0.5; y = 1$$

$$= g(z) < 0.5; y = 0$$



$$z = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \dots + \theta_n x_n$$

Lets assume: $H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$

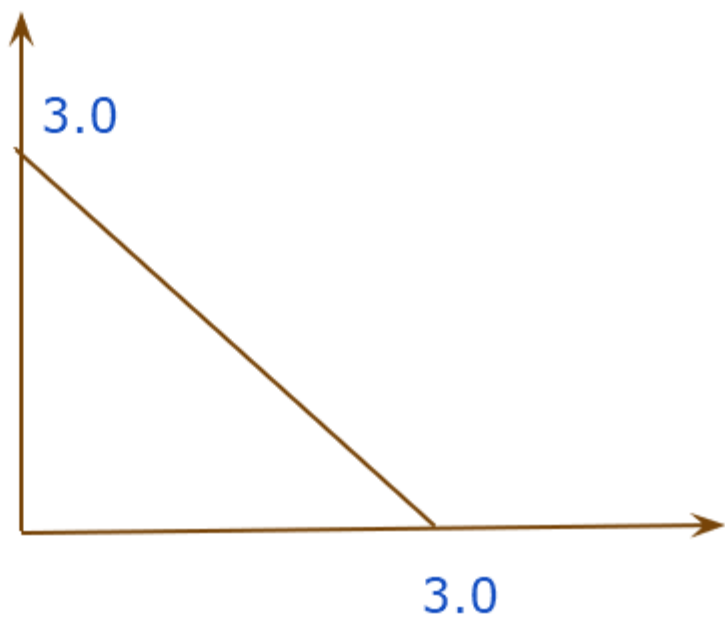


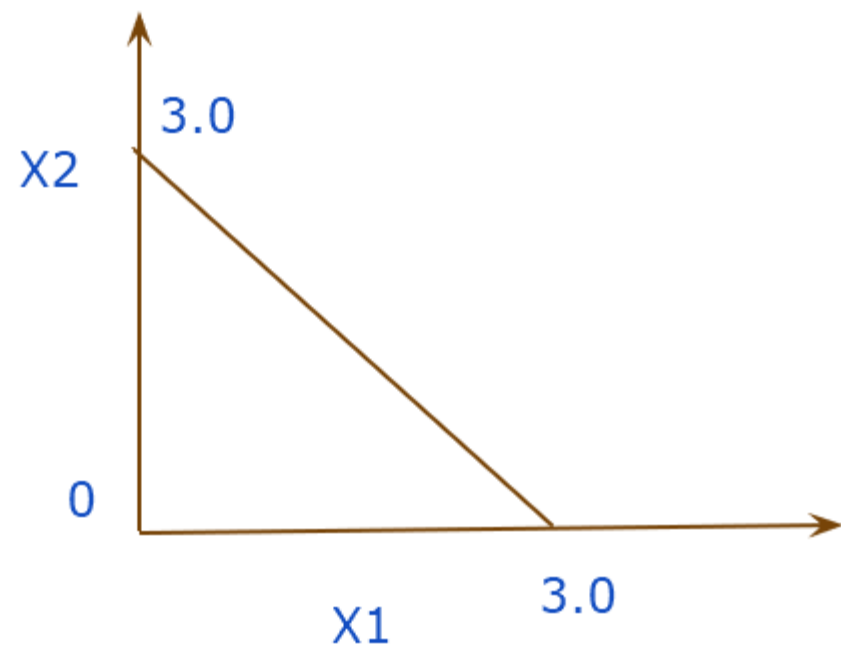
$$-3 \quad 1 \quad 1$$

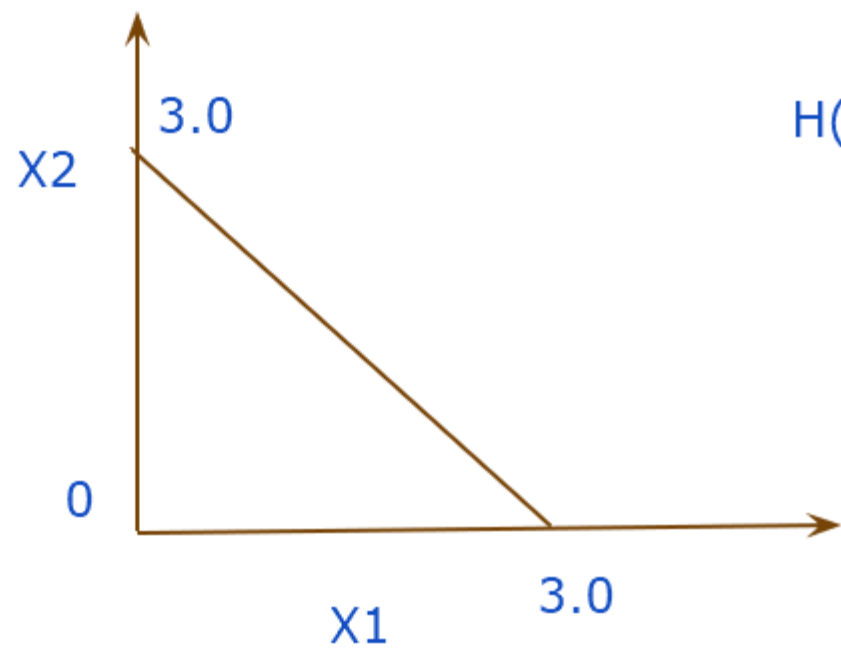
$$H(x) = -3 + x_1 + x_2 \quad \text{If } H(x) \geq 0.5; z \geq 0; Y = 1$$

$$-3 + x_1 + x_2 \geq 0; y = 1$$

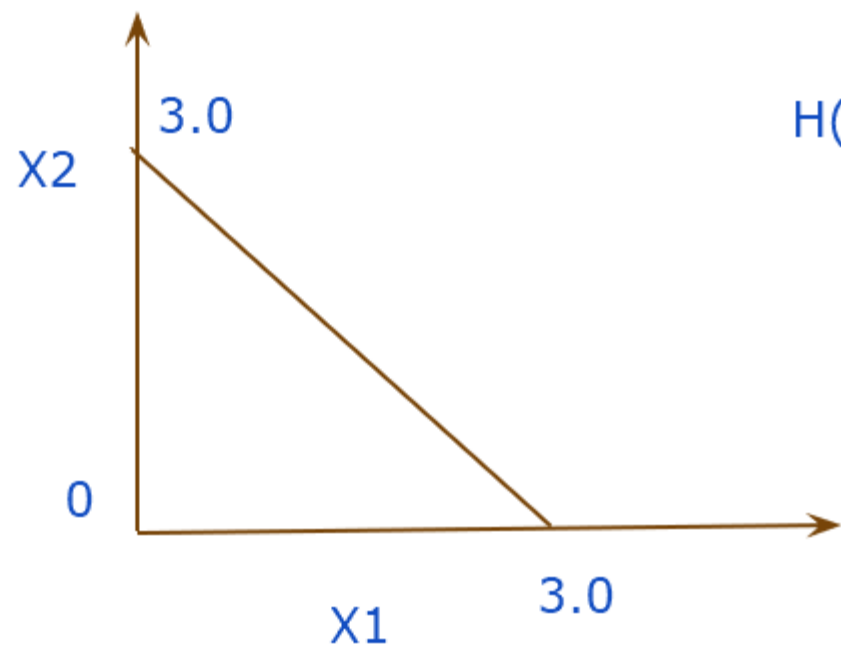
$$-3 + x_1 + x_2 < 0; y = 0 \quad -3 + x_1 + x_2 = 0; \text{decision boundary}$$





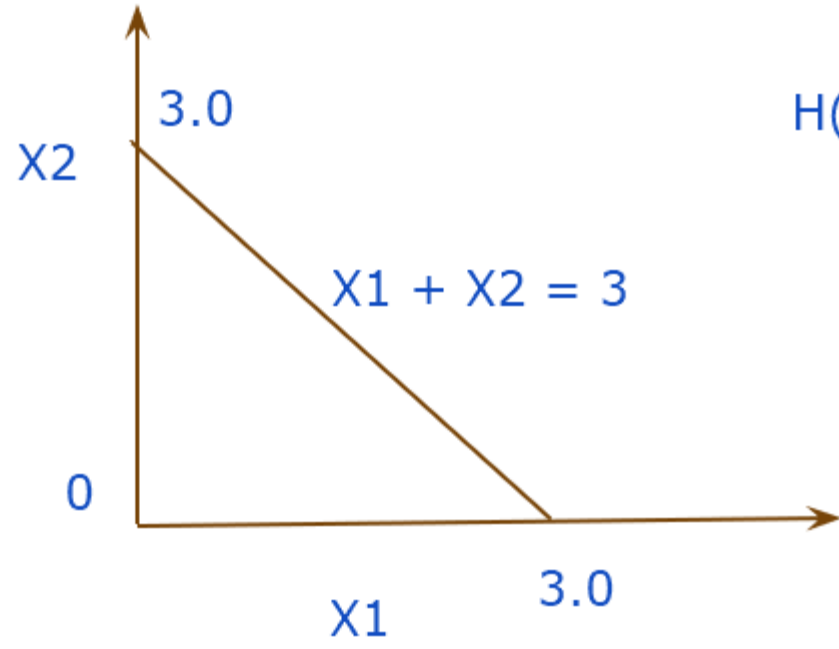


$$H(x) = -3 + X_1 + X_2$$



$$H(x) = -3 + x_1 + x_2$$

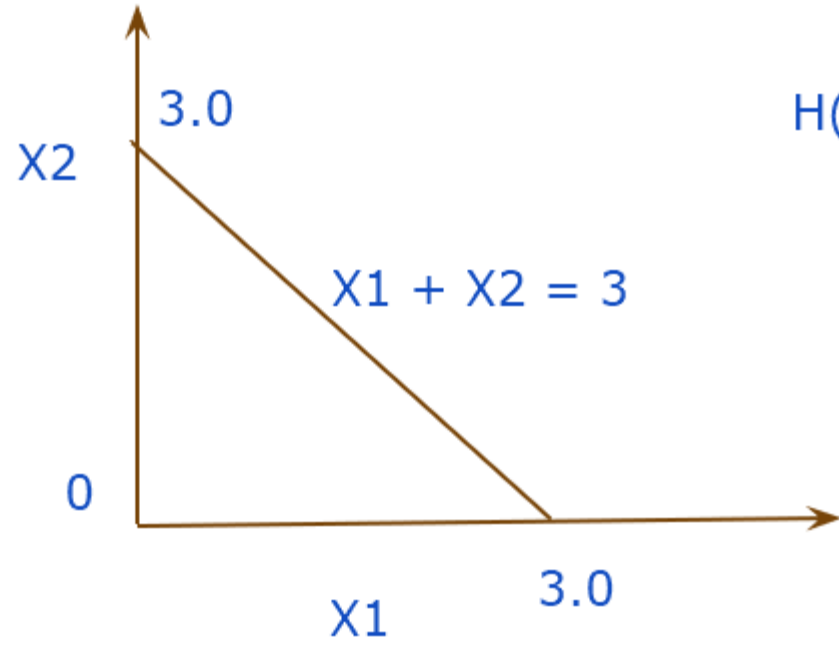
$$x_1 + x_2 = 3$$



$$H(x) = -3 + X_1 + X_2$$

$$X_1 + X_2 = 3$$

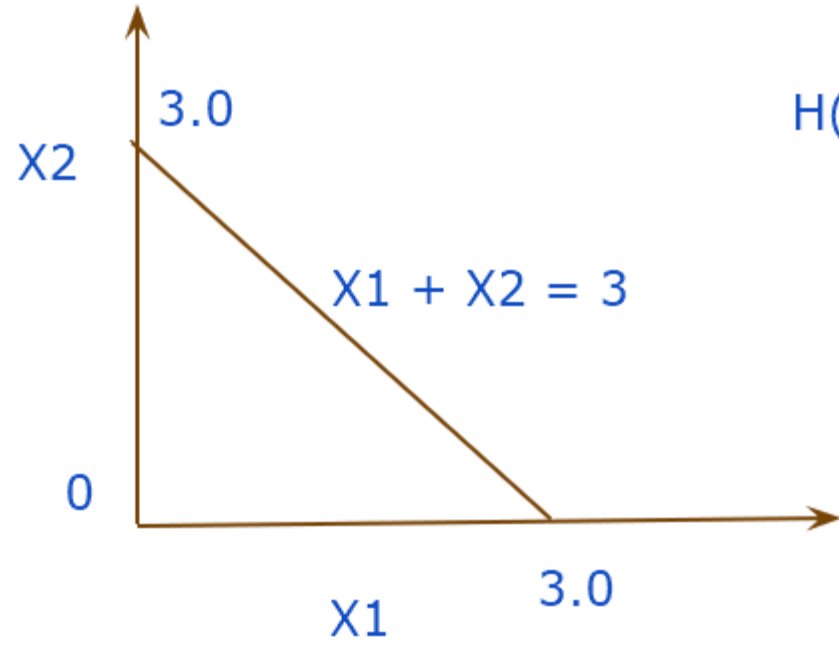
$$H(X) = 0.5; z = 0$$



$$H(x) = g(3 + X_1 + X_2)$$

$$X_1 + X_2 = 3$$

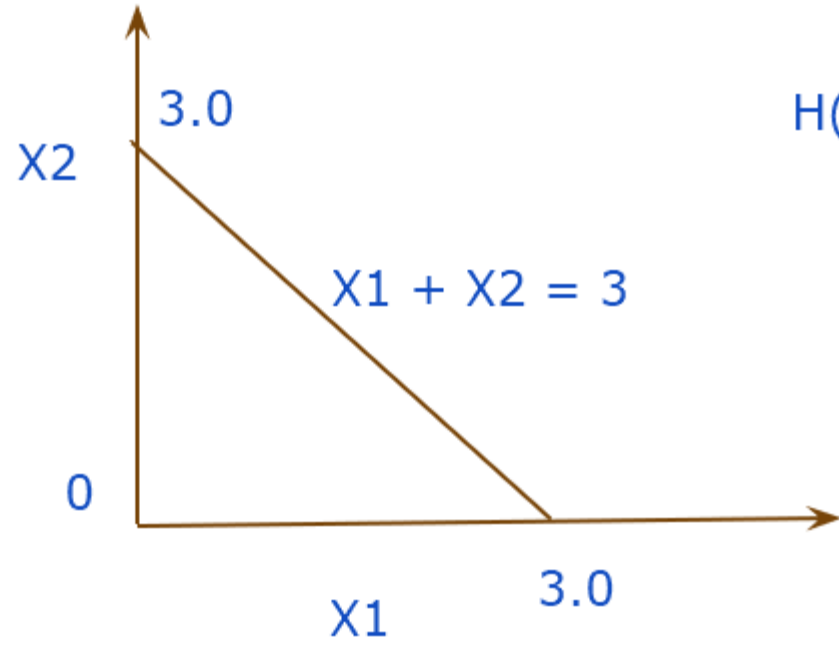
$$H(X) = 0.5; z = 0$$



$$H(x) = g(3 + X_1 + X_2)$$

$$X_1 + X_2 = 3$$

$$H(X) = 0.5; z = 0$$

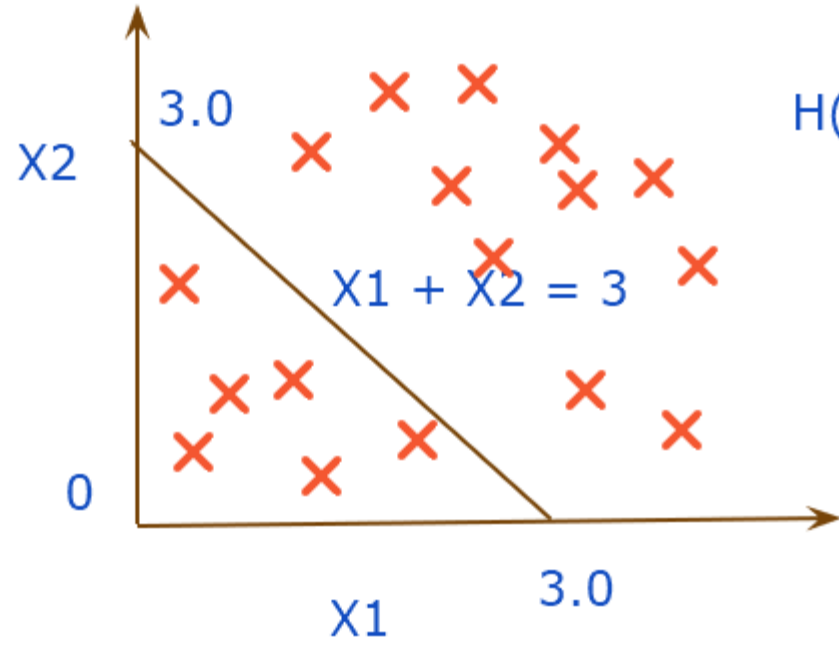


$$H(x) = g(3 + X_1 + X_2)$$

$$H(X) = 0.5; z = 0$$

$$X_1 + X_2 = 3$$

Decision boundary

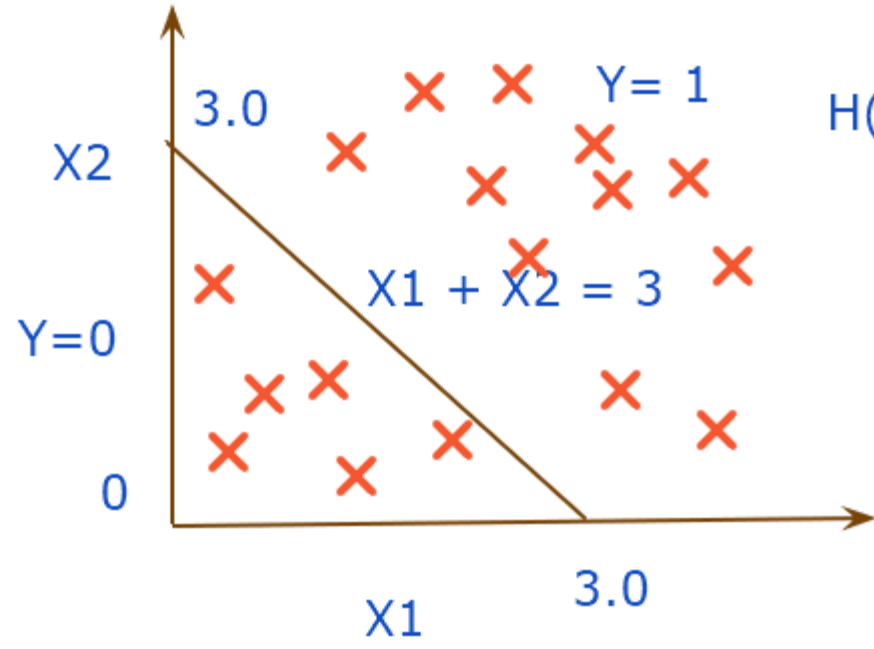


$$H(x) = g(3 + X_1 + X_2)$$

$$H(X) = 0.5; z = 0$$

$$X_1 + X_2 = 3$$

Decision boundary

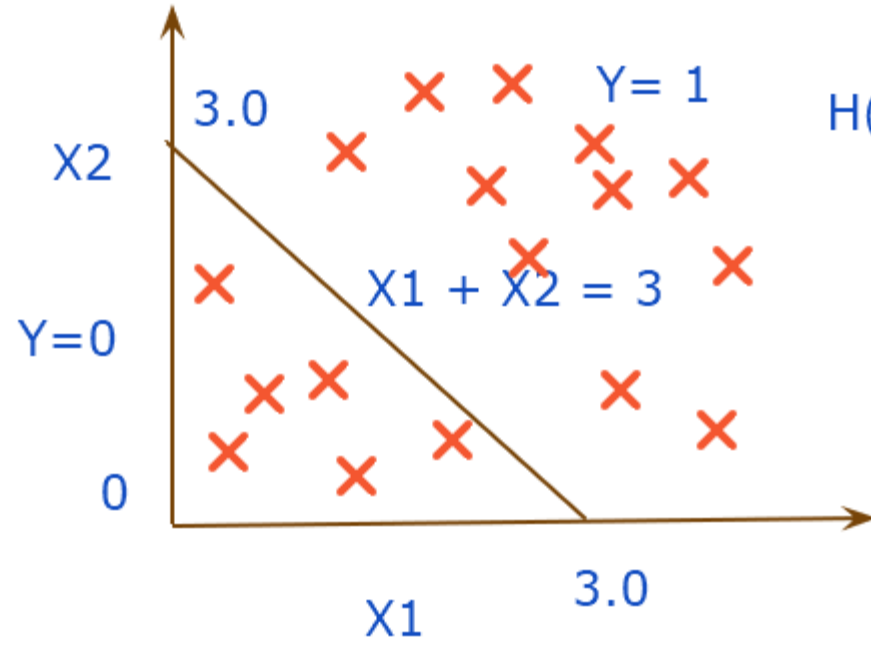


$$H(x) = g(3 + X_1 + X_2)$$

$$H(X) = 0.5; z = 0$$

$$X_1 + X_2 = 3$$

Decision boundary



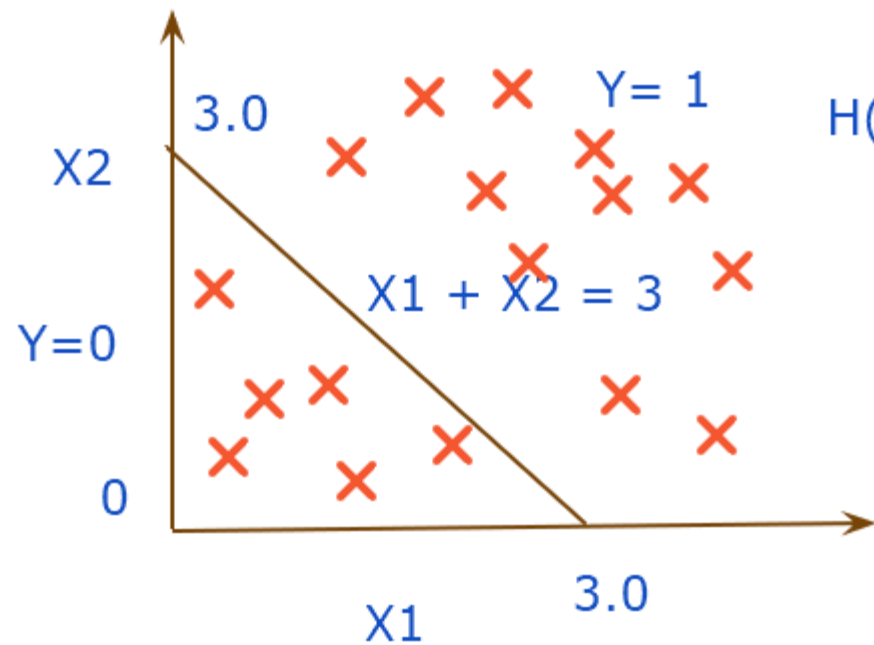
$$H(x) = g(3 + X_1 + X_2)$$

$$H(X) = 0.5; z = 0$$

$$X_1 + X_2 = 3$$

Decision boundary

Linear decision boundary



$$H(x) = g(3 + X_1 + X_2)$$

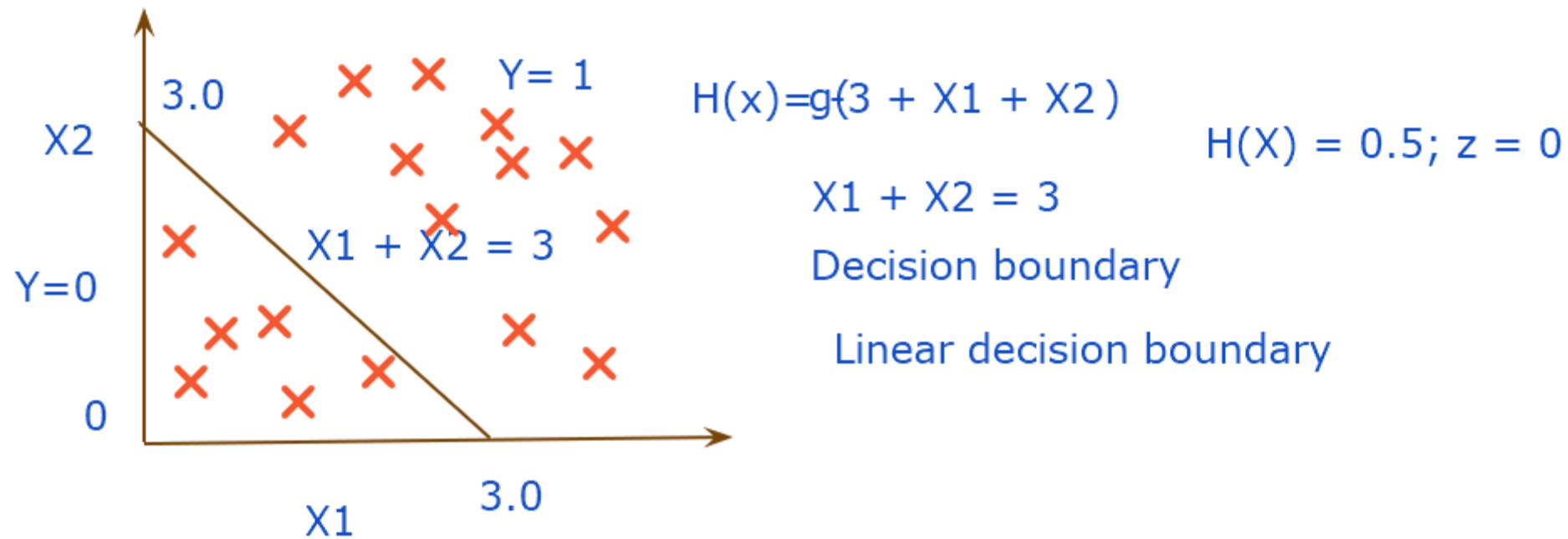
$$H(X) = 0.5; z = 0$$

$$X_1 + X_2 = 3$$

Decision boundary

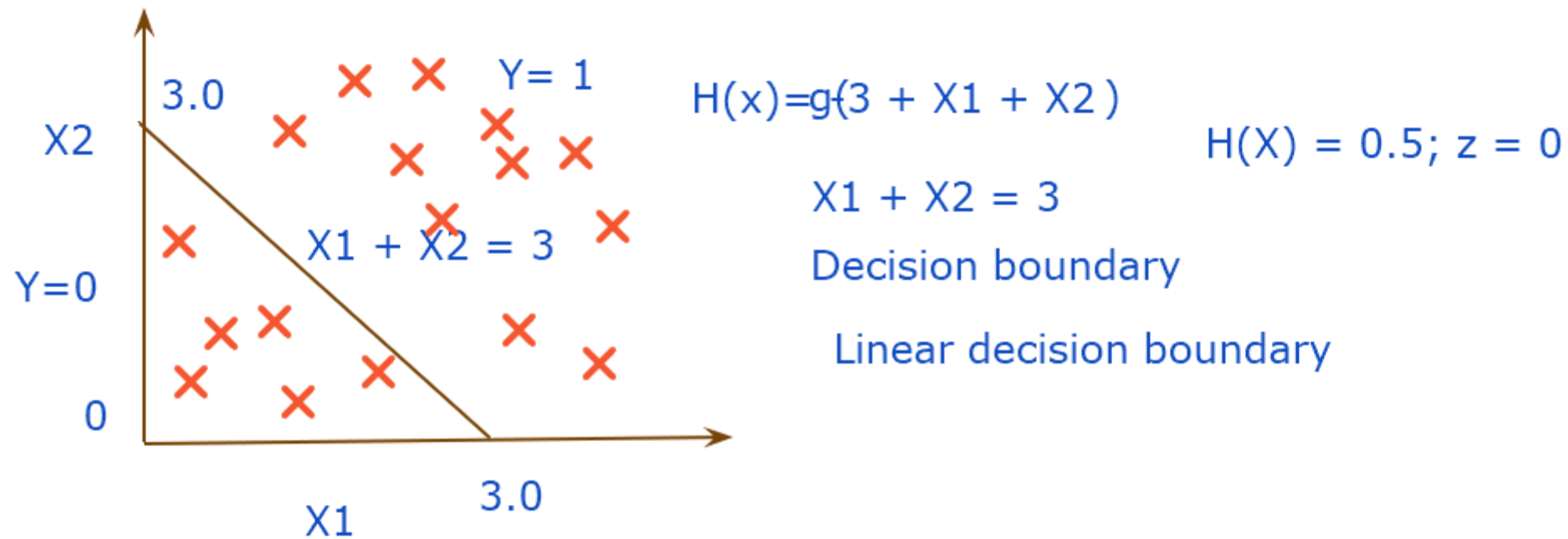
Linear decision boundary

$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$



$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

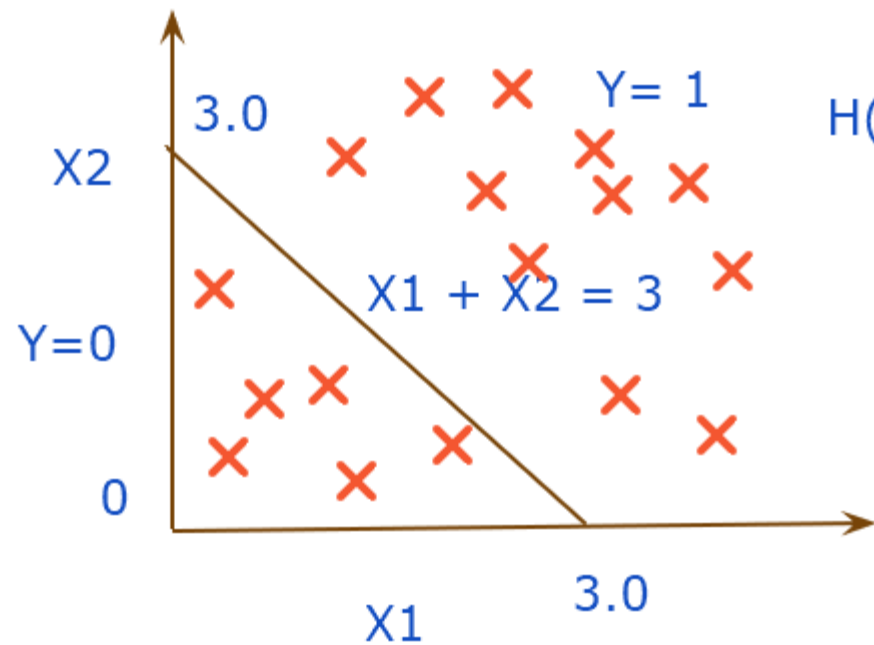
$$\theta_0 = -1; \theta_1 = \theta_2 = 0; \theta_3 = 1 \text{ \& } \theta_4 = 1$$



$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

$$\theta_0 = -1; \theta_1 = \theta_2 = 0; \theta_3 = 1 \text{ \& } \theta_4 = 1$$

$$H(X) = g(-1 + 0 + 0 + X1^2 + X2^2)$$



$$H(x) = g(3 + X_1 + X_2)$$

$$H(X) = 0.5; z = 0$$

$$X_1 + X_2 = 3$$

Decision boundary

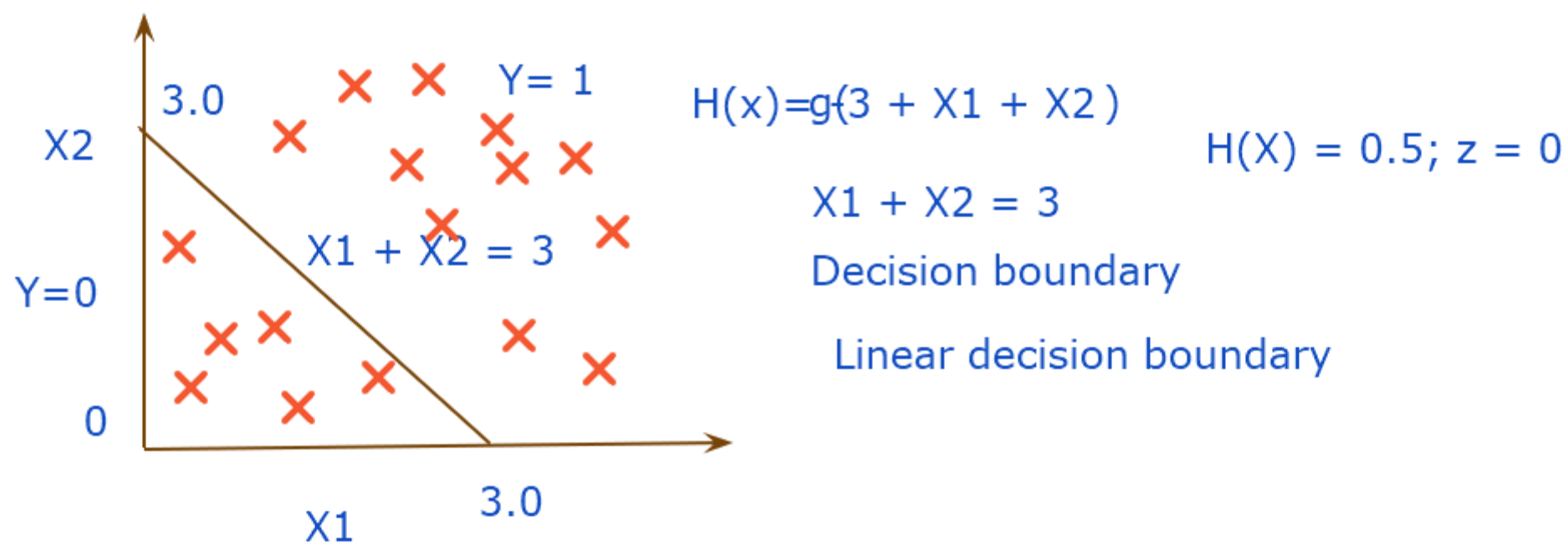
Linear decision boundary

$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

$$\theta_0 = -1; \theta_1 = \theta_2 = 0; \theta_3 = 1 \text{ \& } \theta_4 = 1$$

$$H(X) = g(-1 + 0 + 0 + X_1^2 + X_2^2)$$

$$X_1^2 + X_2^2 = 1$$

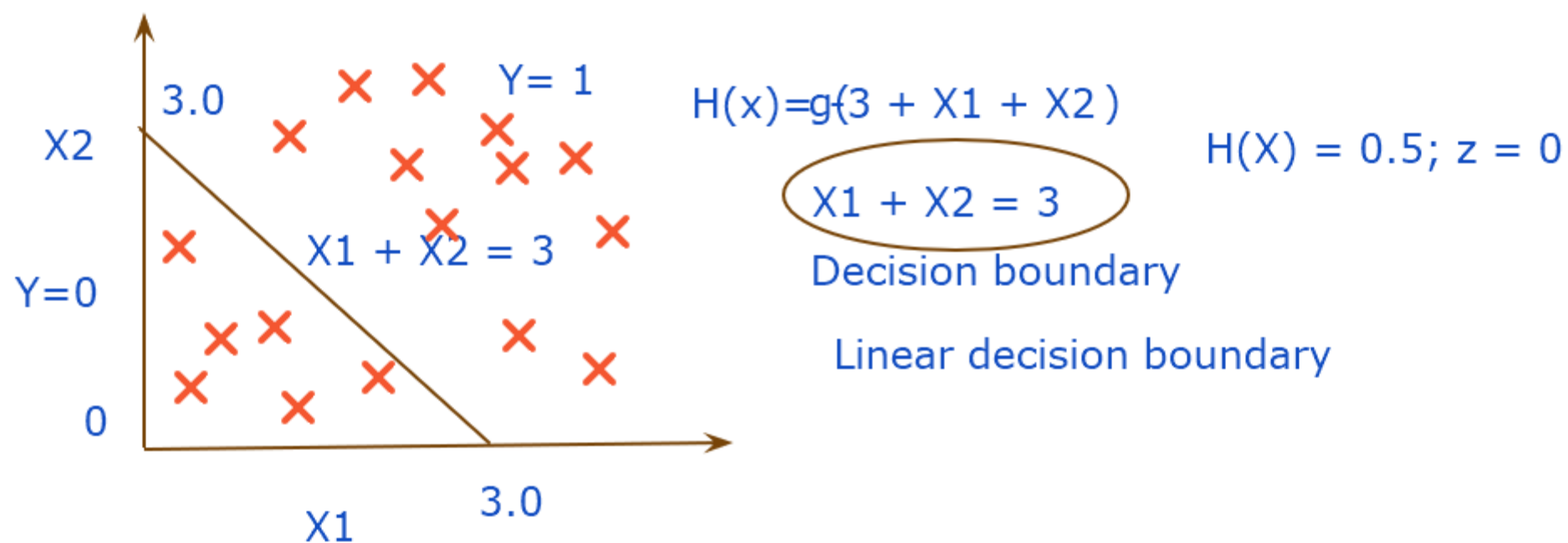


$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

$$\theta_0 = -1; \theta_1 = \theta_2 = 0; \theta_3 = 1 \text{ \& } \theta_4 = 1$$

$$H(X) = g(-1 + 0 + 0 + X_1^2 + X_2^2)$$

$$X_1^2 + X_2^2 = 1 \quad \text{Decision boundary; non-linear}$$

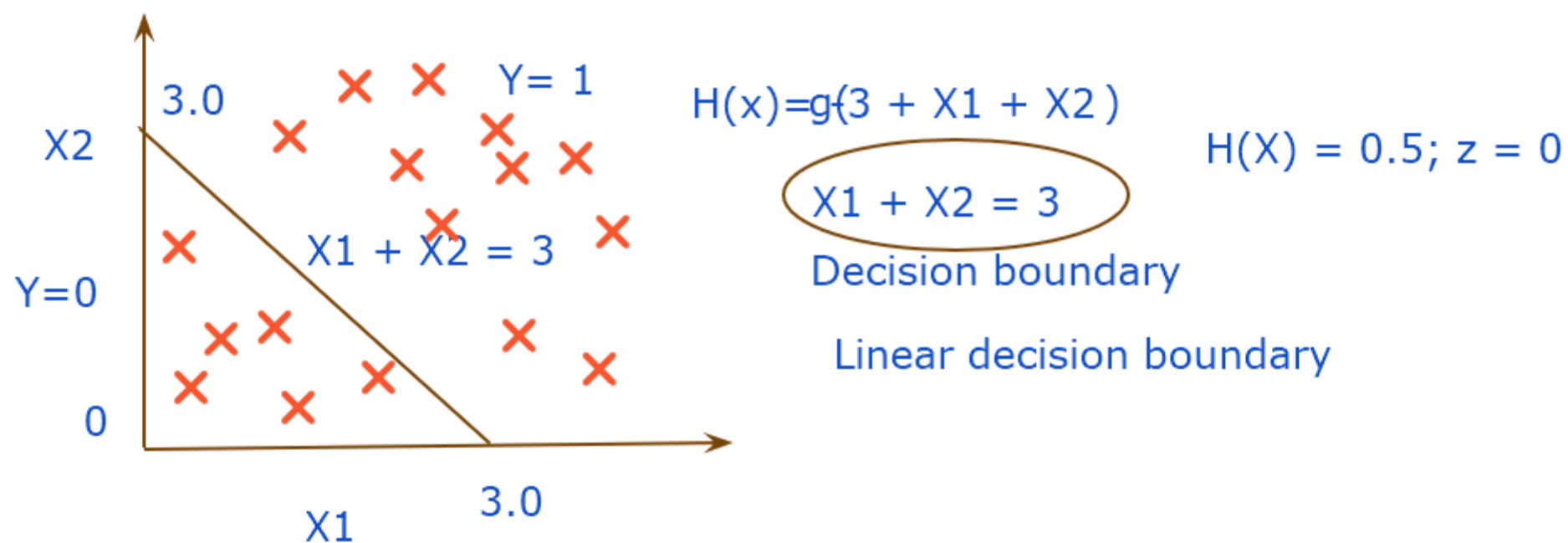


$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

$$\theta_0 = -1; \theta_1 = \theta_2 = 0; \theta_3 = 1 \text{ \& } \theta_4 = 1$$

$$H(X) = g(-1 + 0 + 0 + X_1^2 + X_2^2)$$

$$X_1^2 + X_2^2 = 1 \quad \text{Decision boundary; non-linear}$$

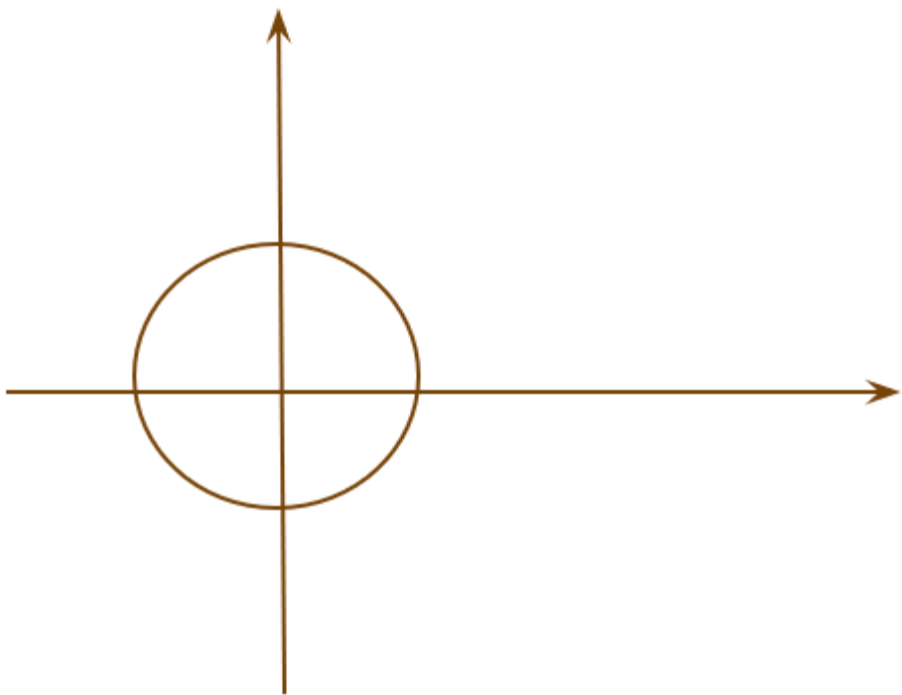


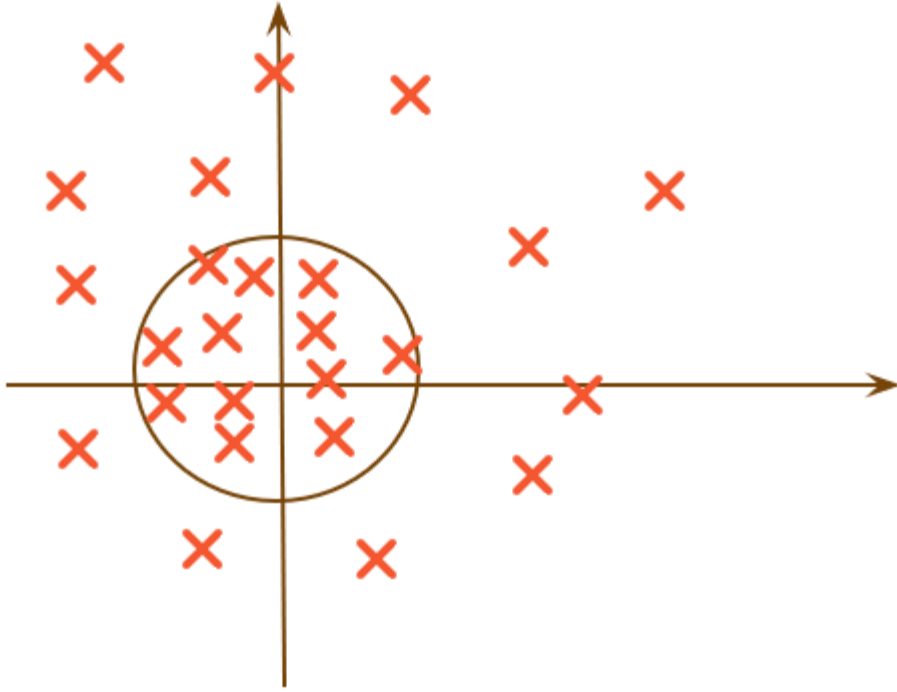
$$H(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

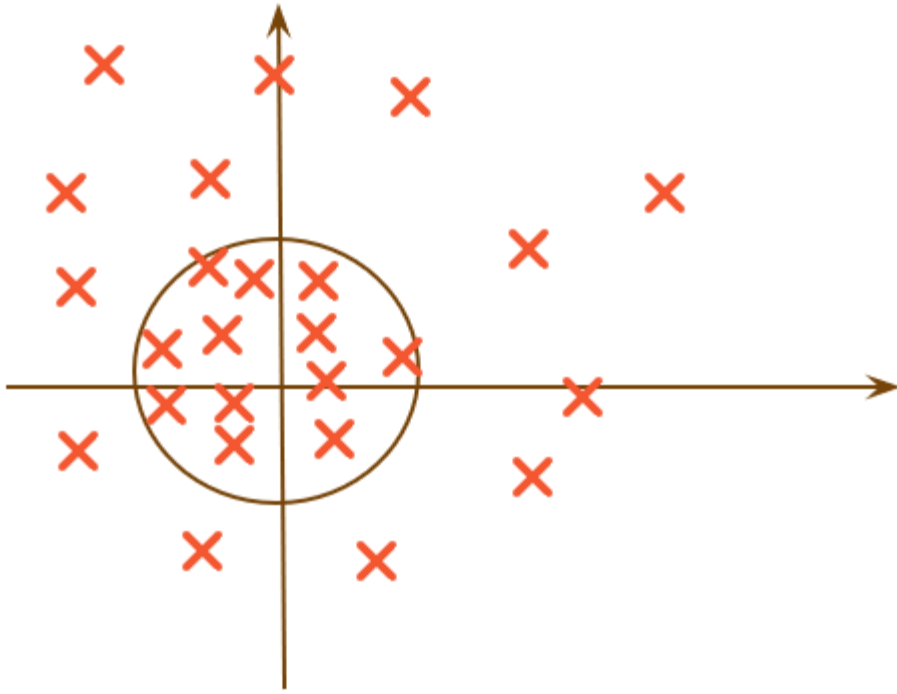
$$\theta_0 = -1; \theta_1 = \theta_2 = 0; \theta_3 = 1 \text{ \& } \theta_4 = 1$$

$$H(X) = g(-1 + 0 + 0 + X_1^2 + X_2^2)$$

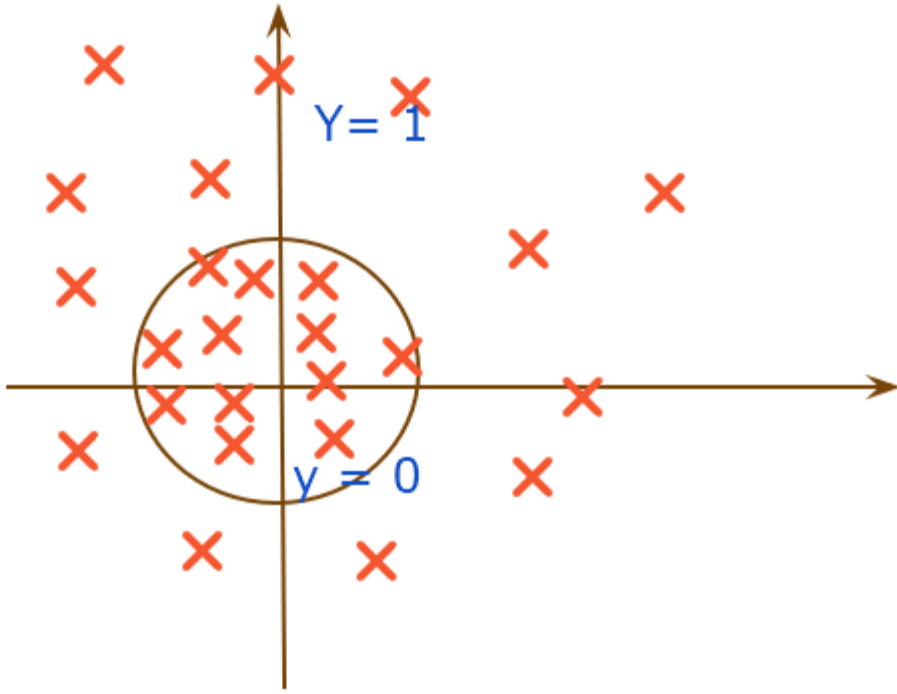
$$X_1^2 + X_2^2 = 1 \quad \text{Decision boundary; non-linear}$$



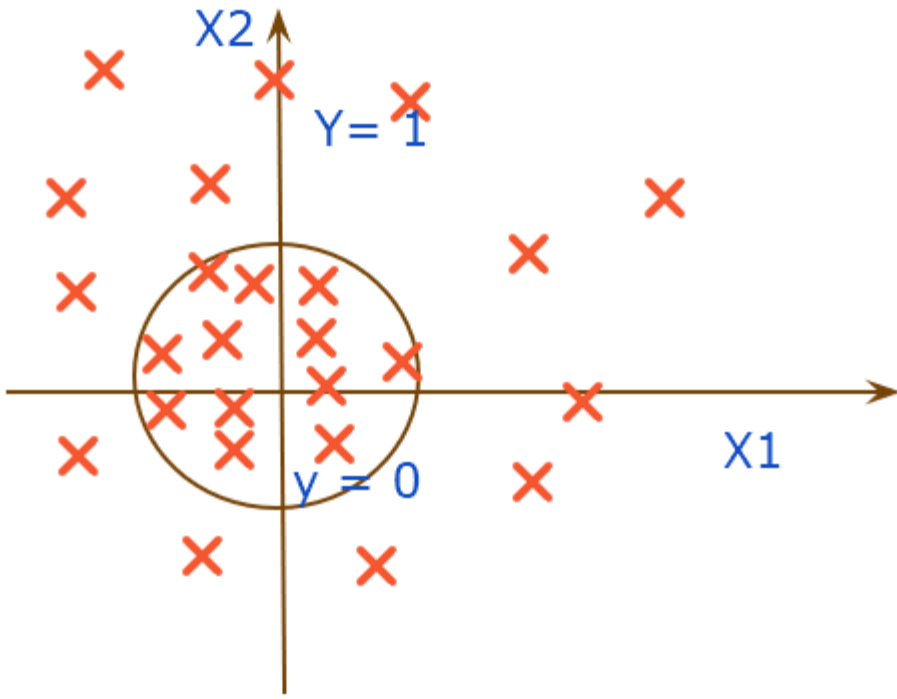




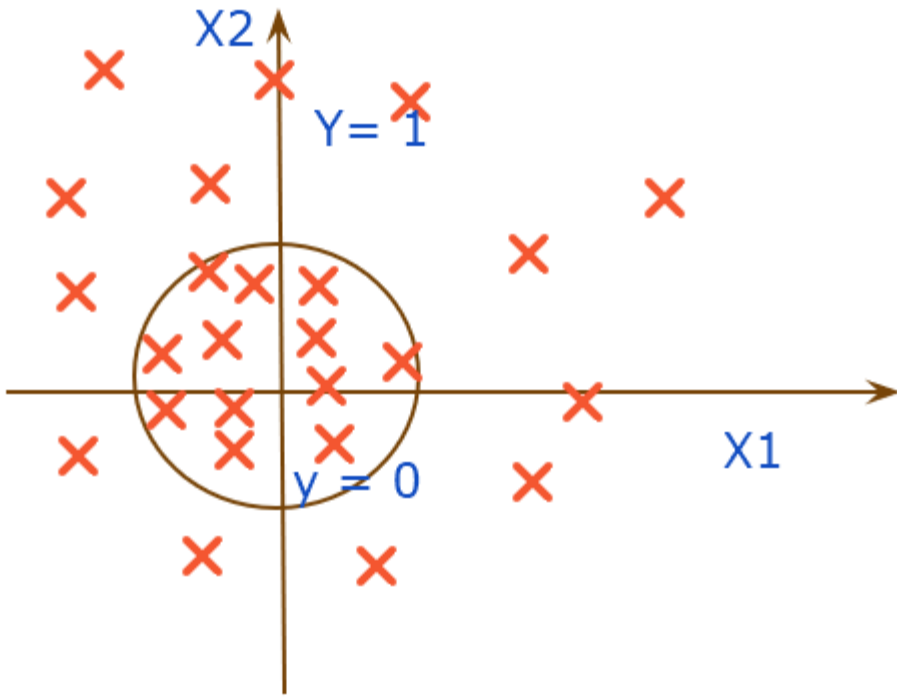
decision boundary
 $X_1^2 + X_2^2 = 1$



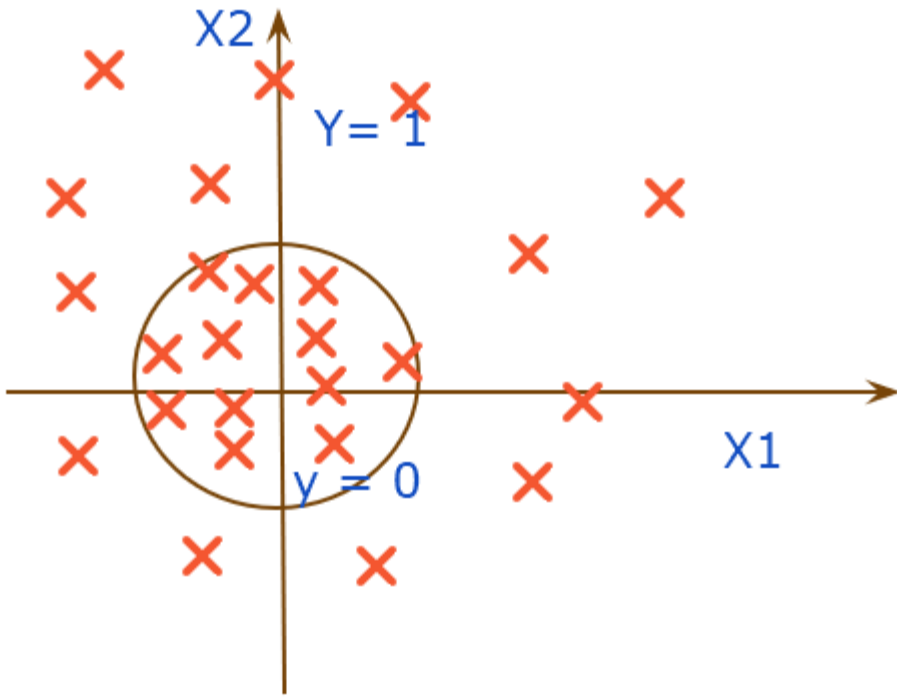
decision boundary
 $X_1^2 + X_2^2 = 1$



decision boundary
 $X_1^2 + X_2^2 = 1$



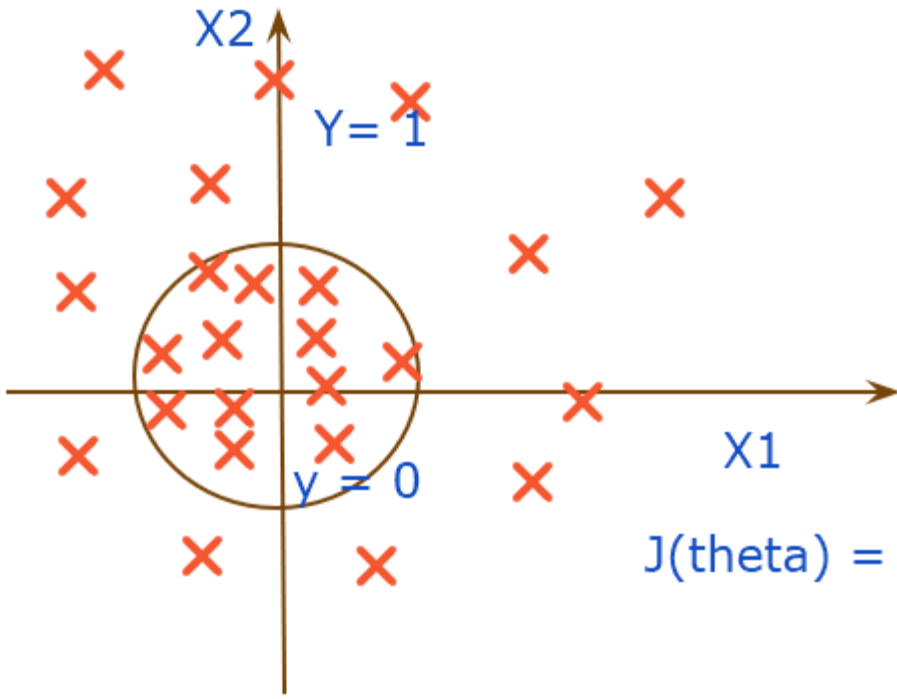
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$



decision boundary
 $X_1^2 + X_2^2 = 1$

$$X_1 + X_2 = 3$$

$\theta_0, \theta_1, \theta_2, \theta_n$

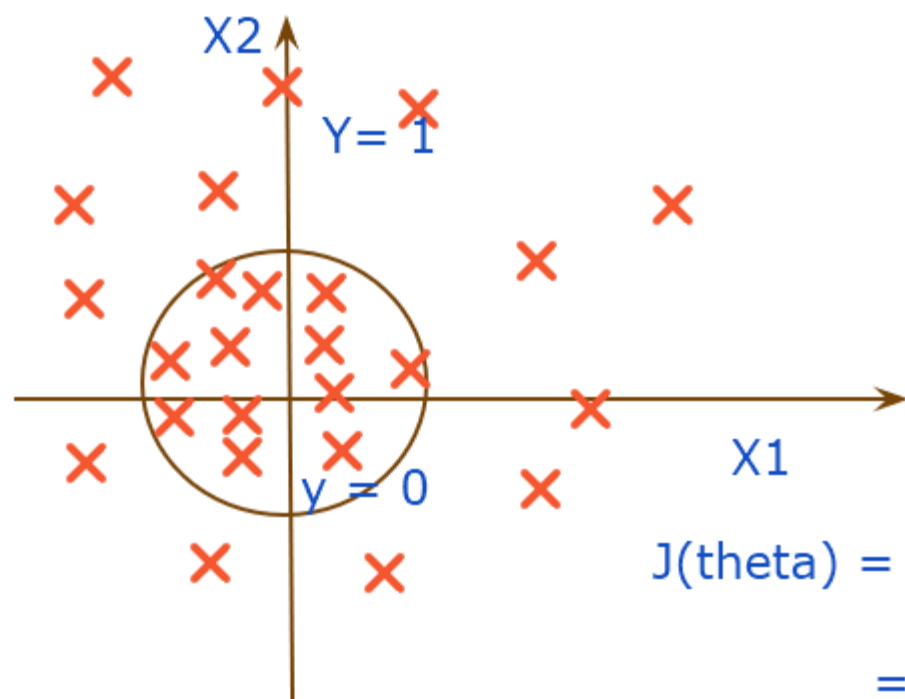


decision boundary
 $X_1^2 + X_2^2 = 1$

$$X_1 + X_2 = 3$$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$



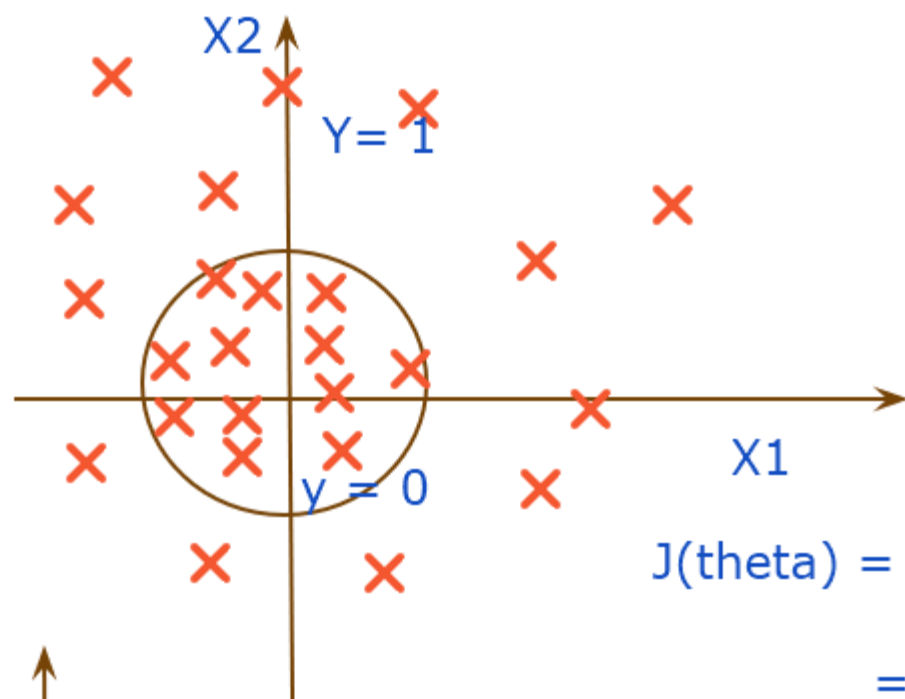
decision boundary
 $X1^2 + X2^2 = 1$

$$X1 + X2 = 3$$

theta 0, theta 1, theta 2, theta n

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$

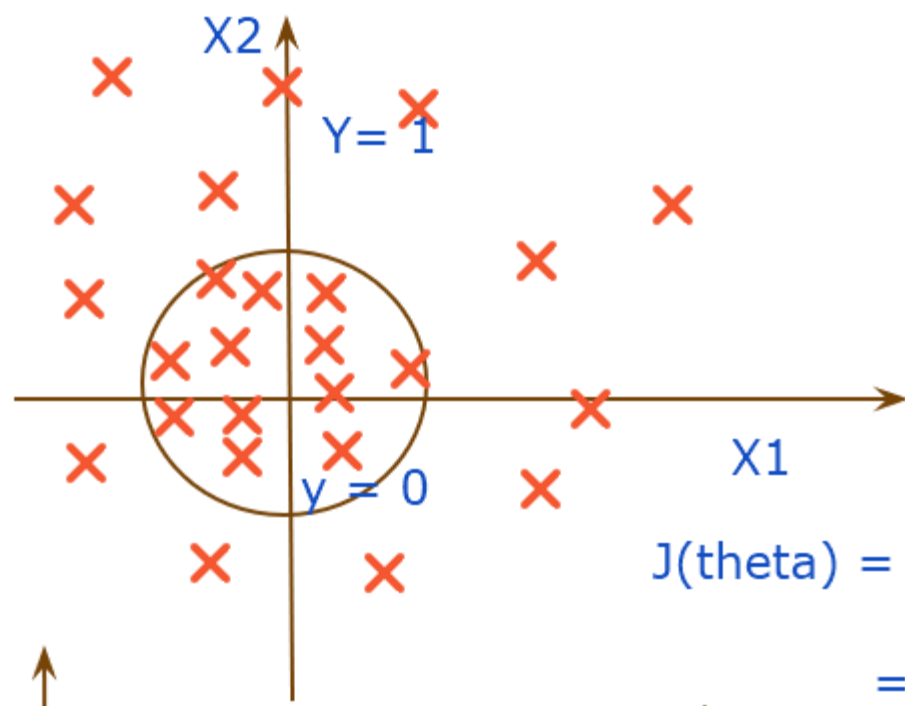


decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$

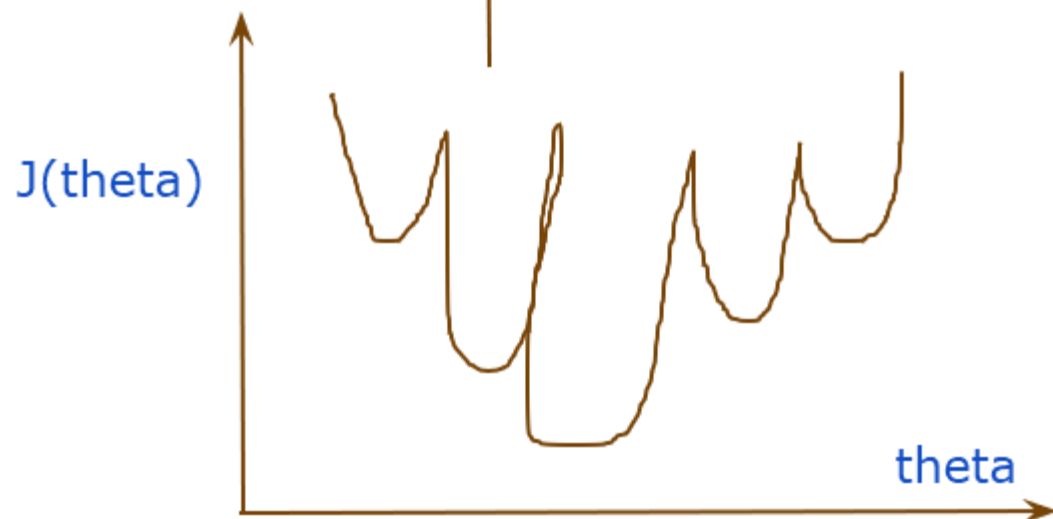


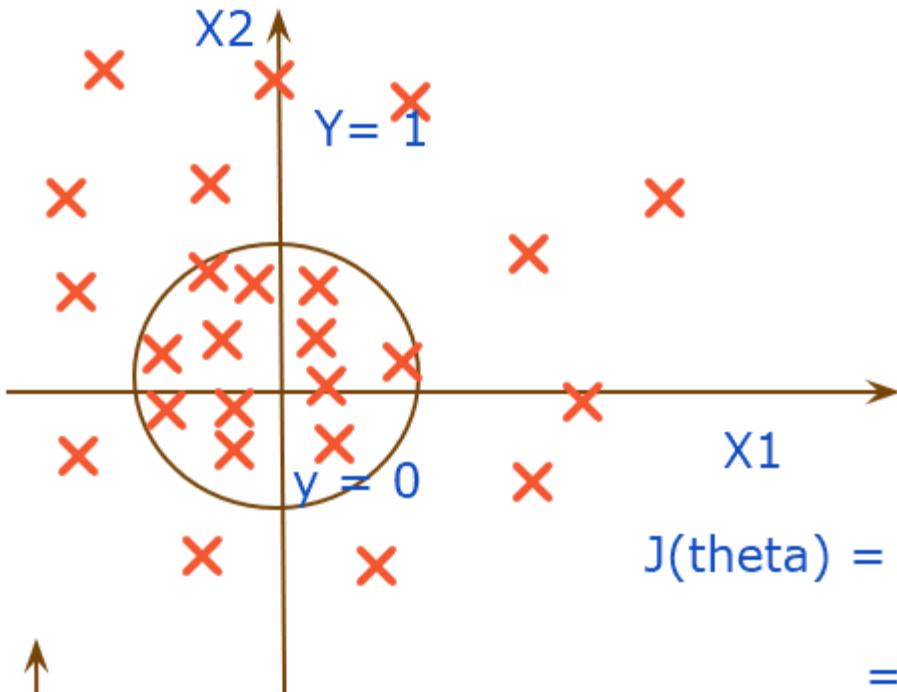
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$





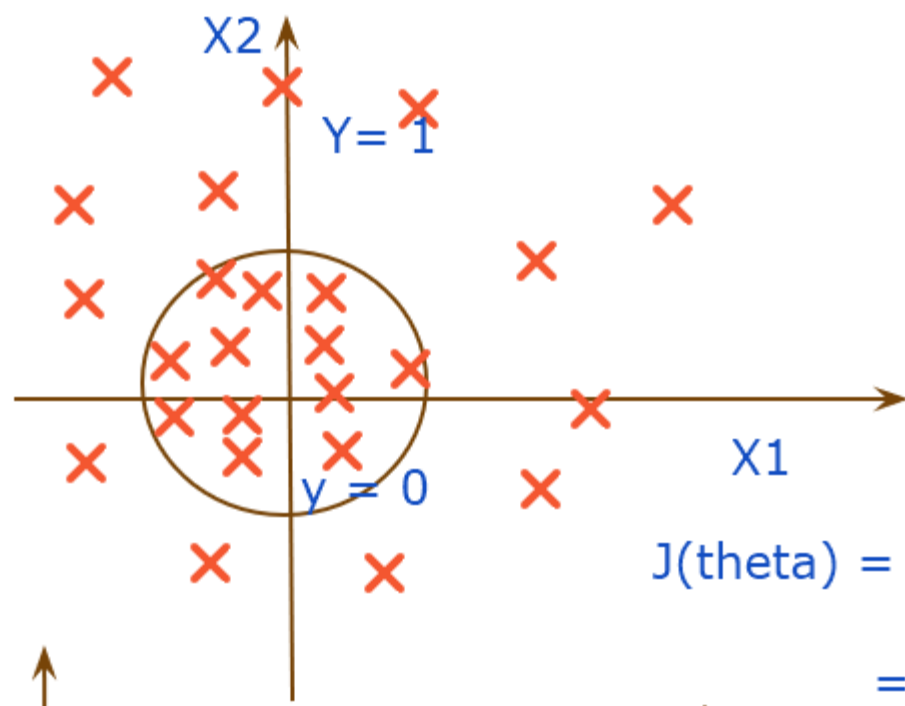
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



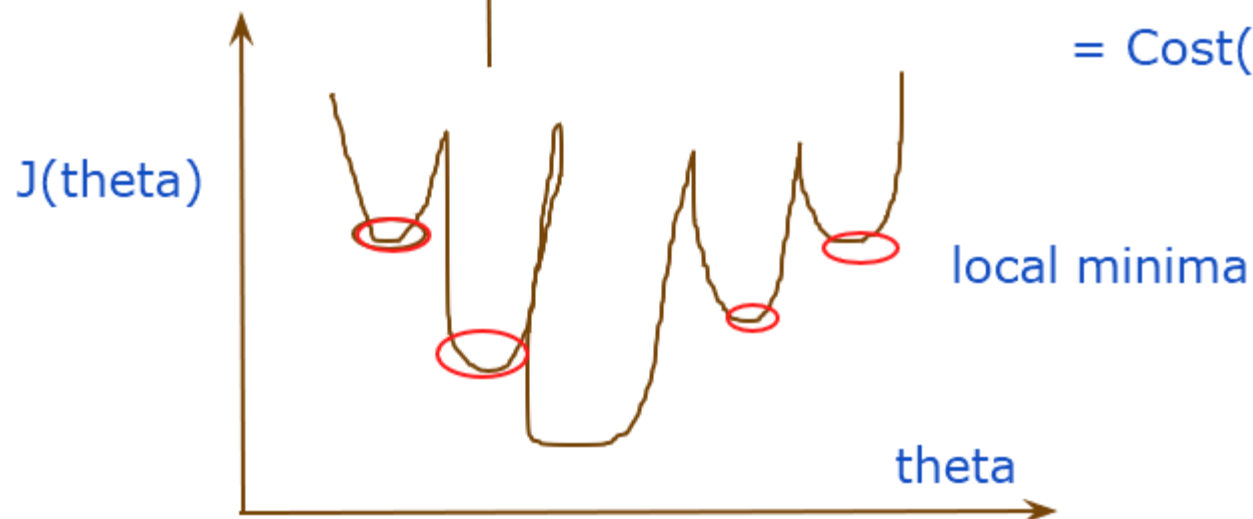


decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

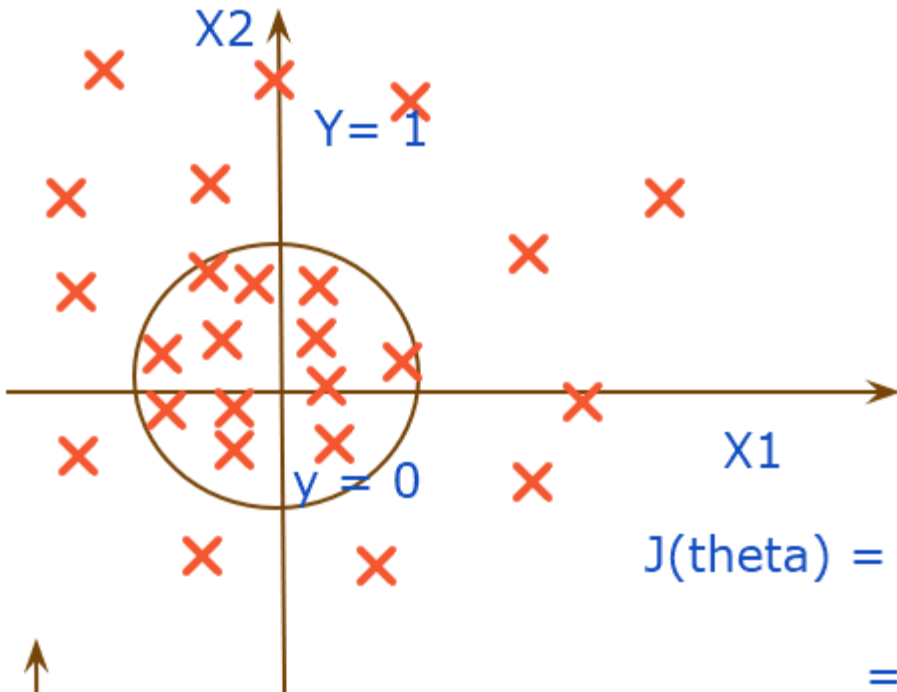
$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



local minima

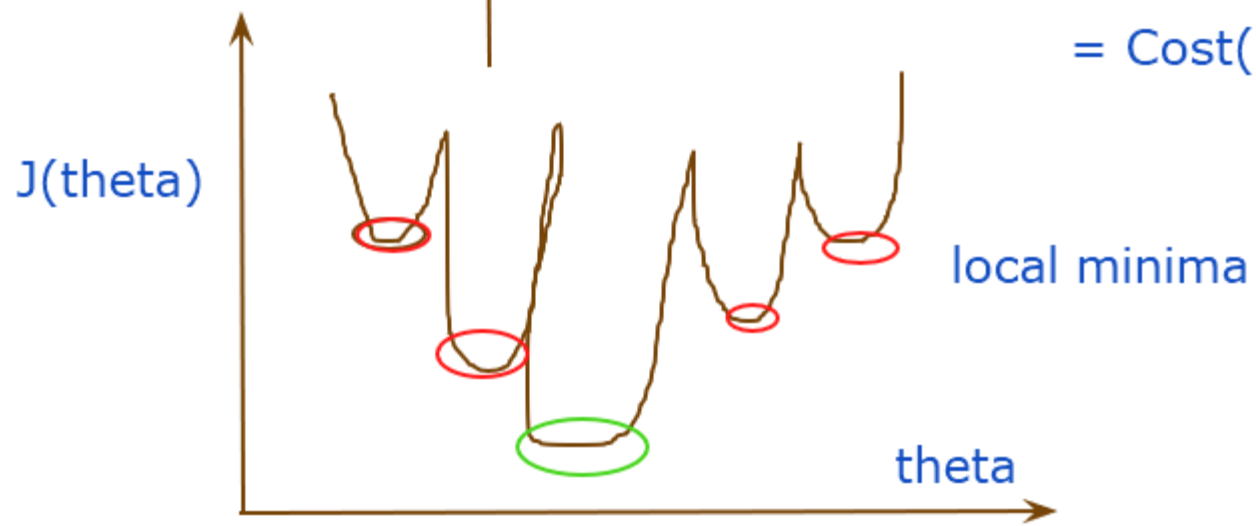


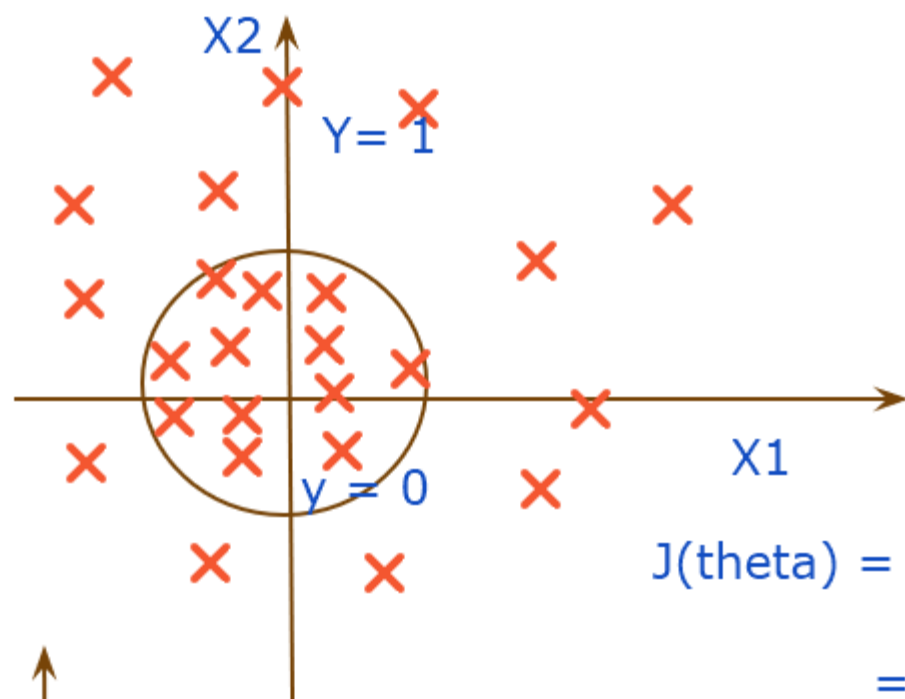
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$= \text{Cost}(h(x), y)$



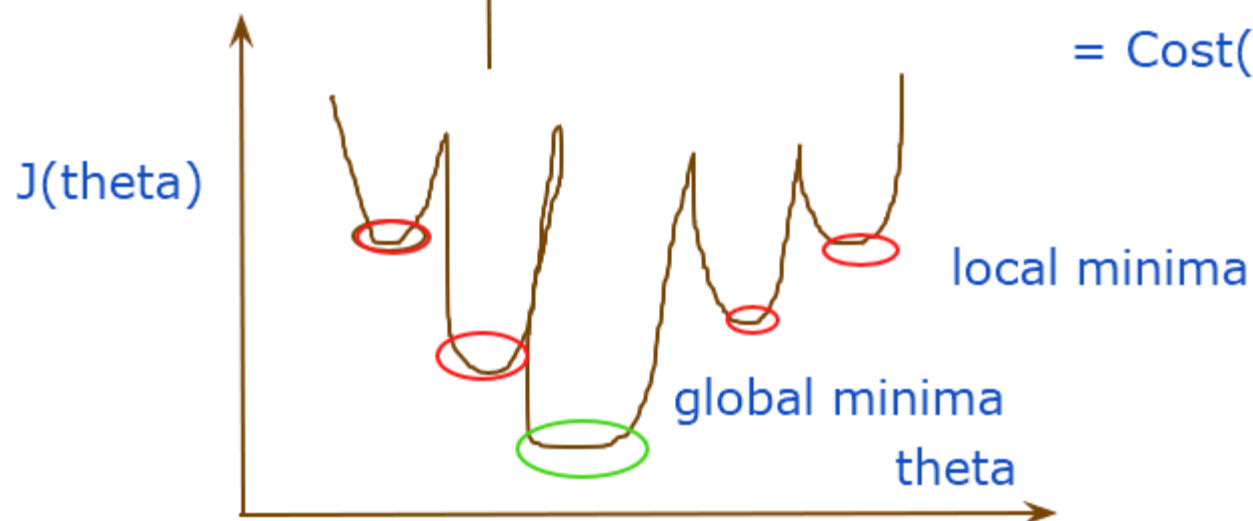


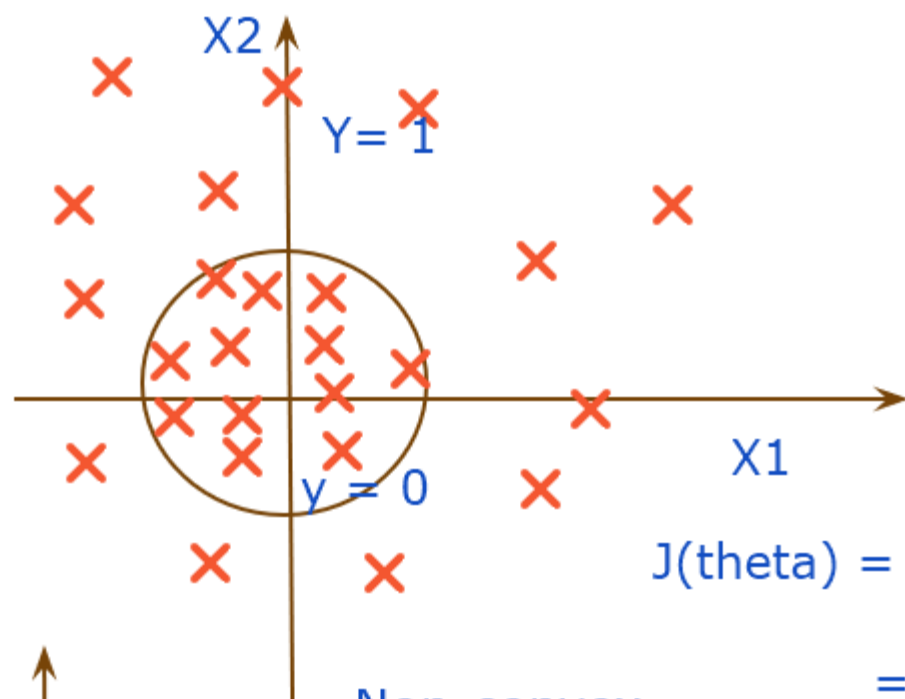
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



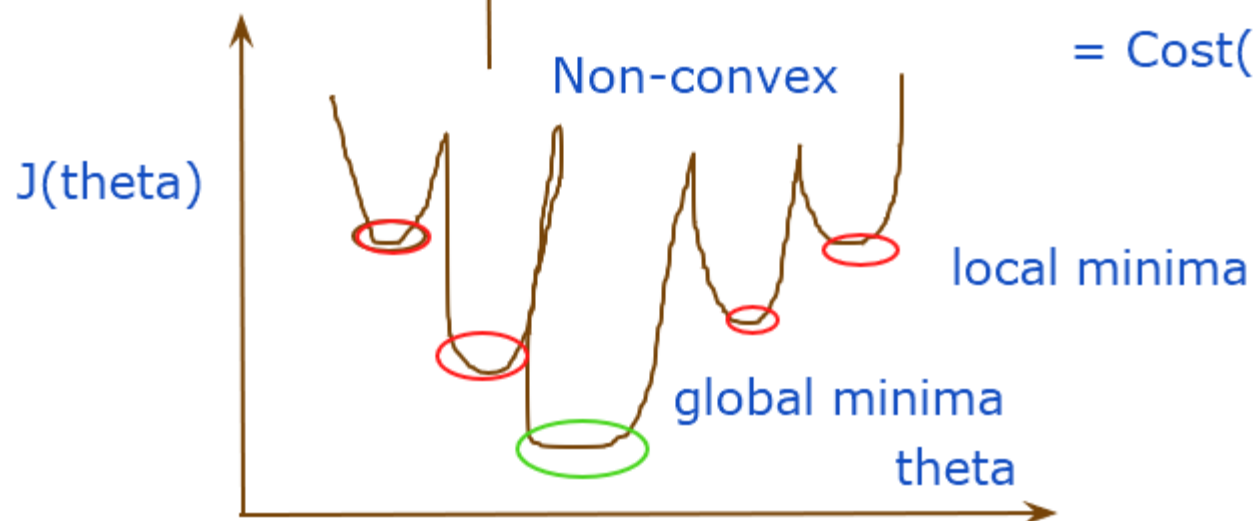


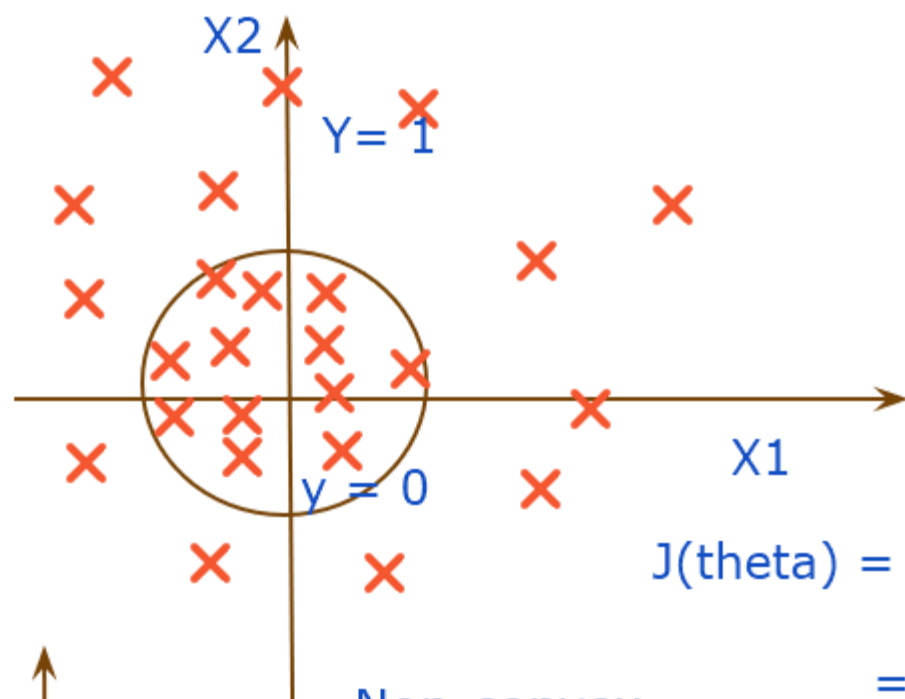
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



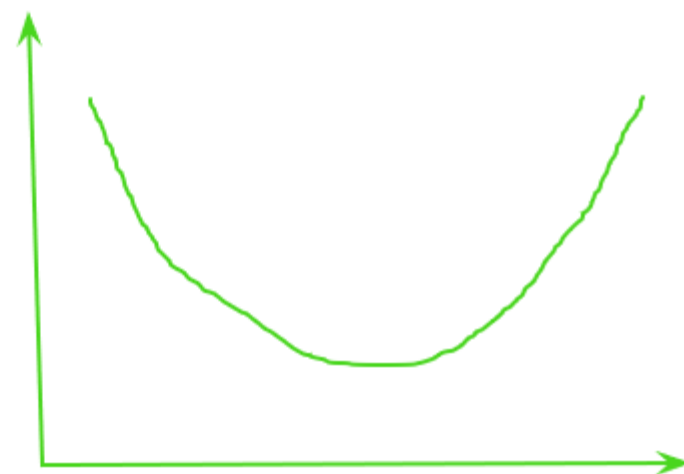
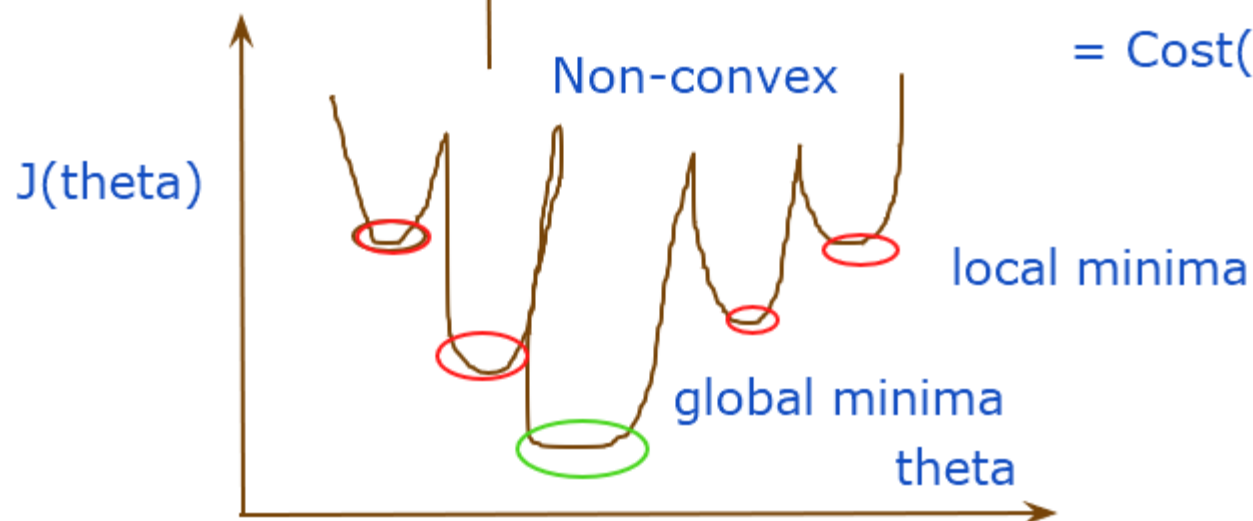


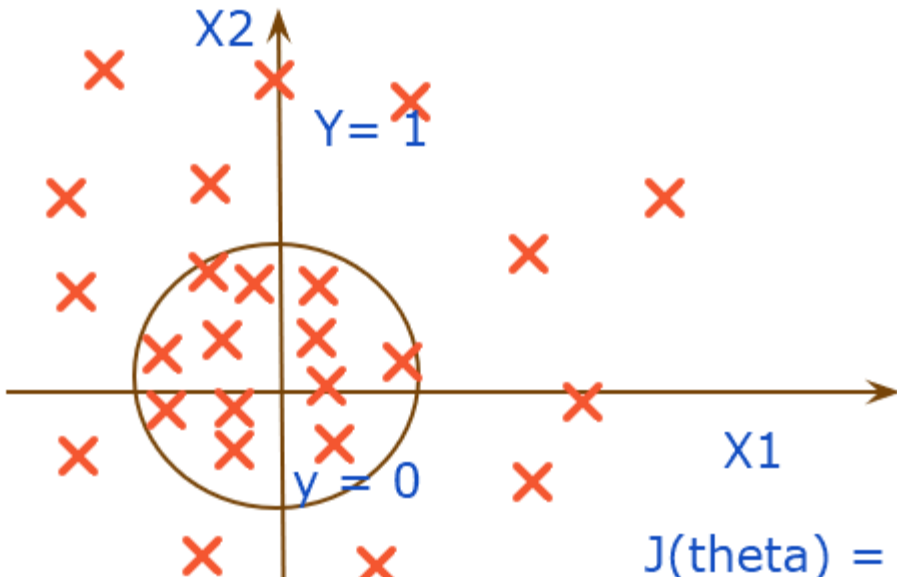
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



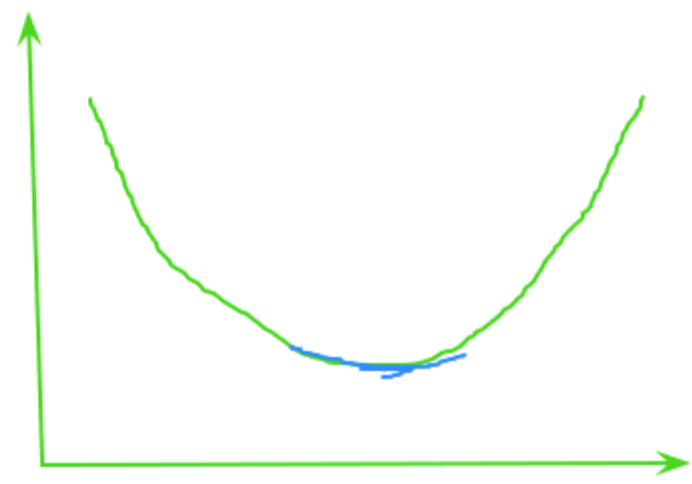
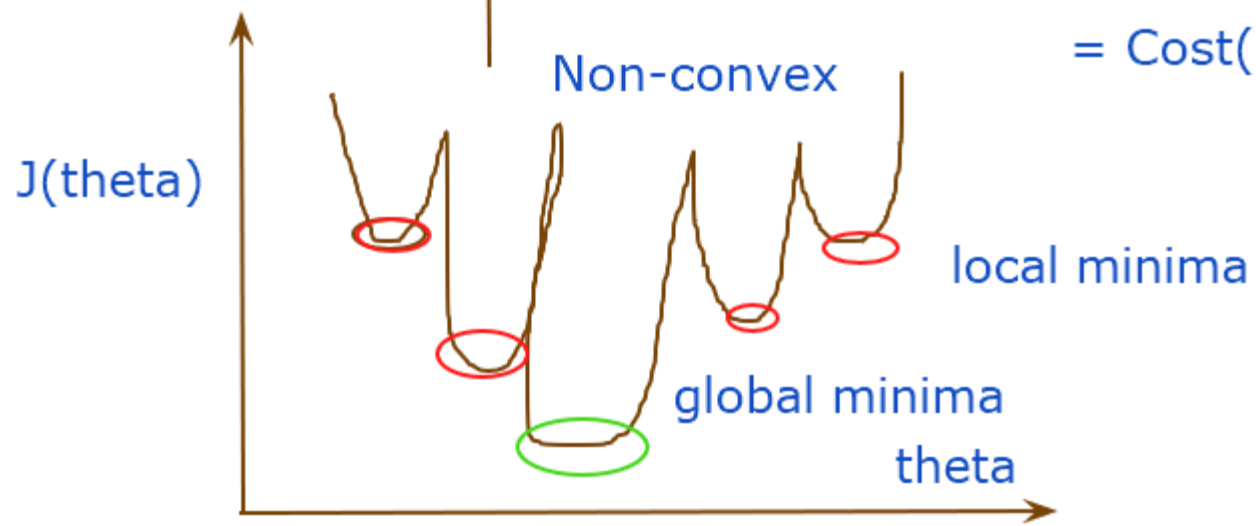


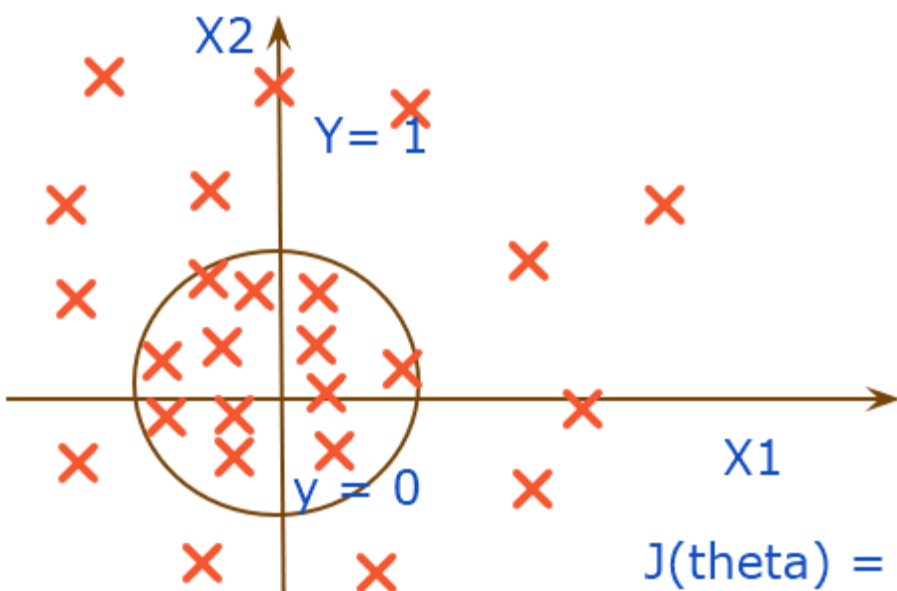
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



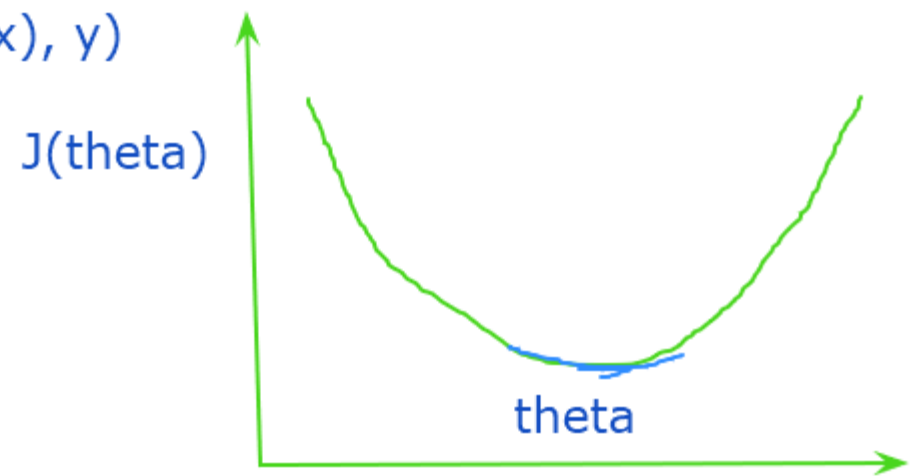
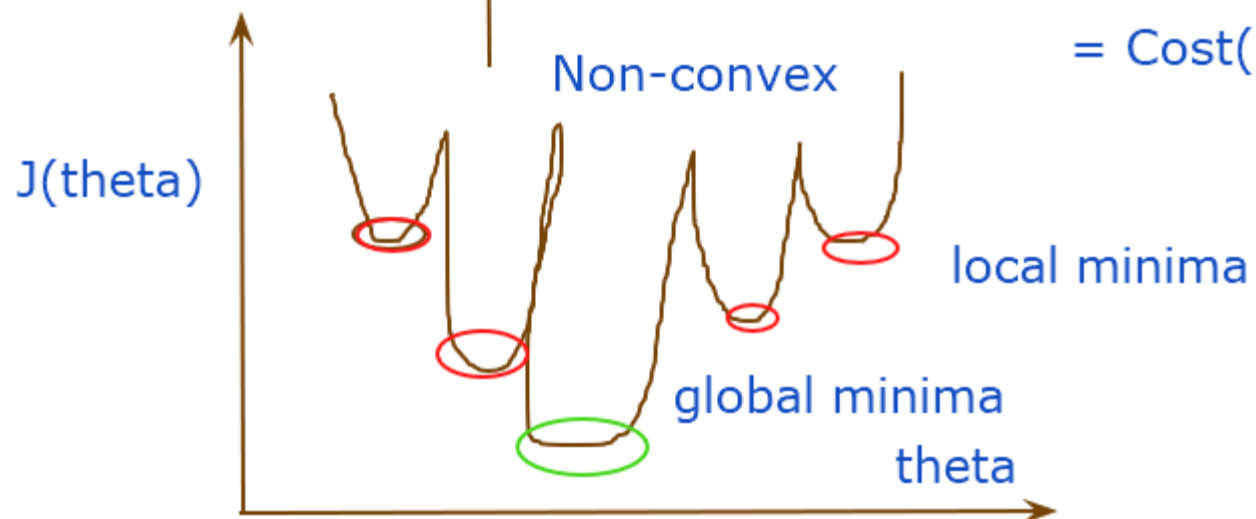


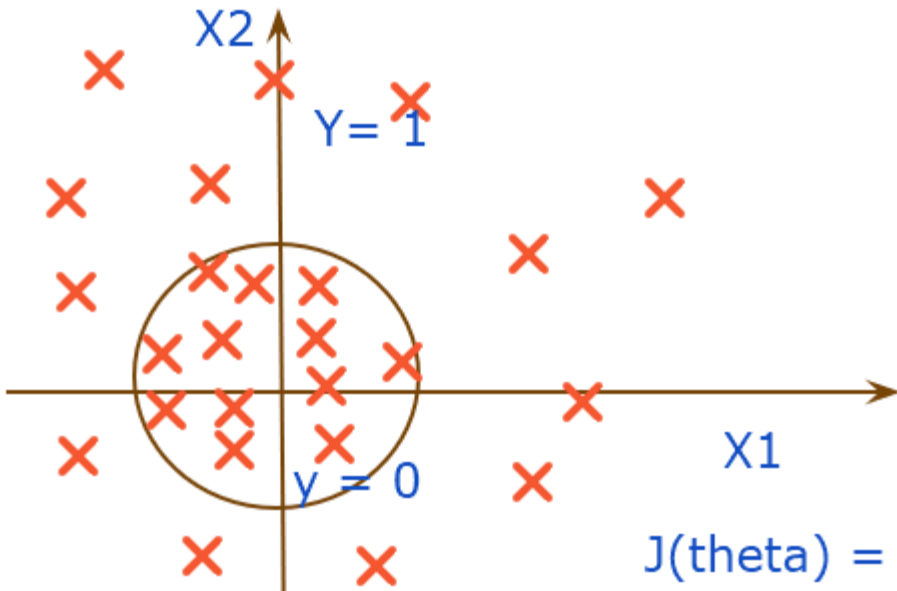
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

$\theta_0, \theta_1, \theta_2, \theta_n$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m [h(x_i) - y_i]^2$$

$$= \text{Cost}(h(x), y)$$



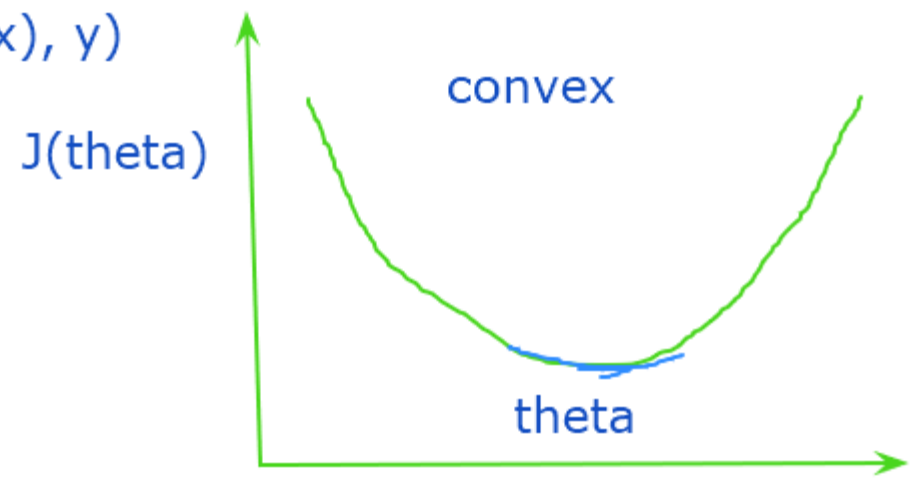
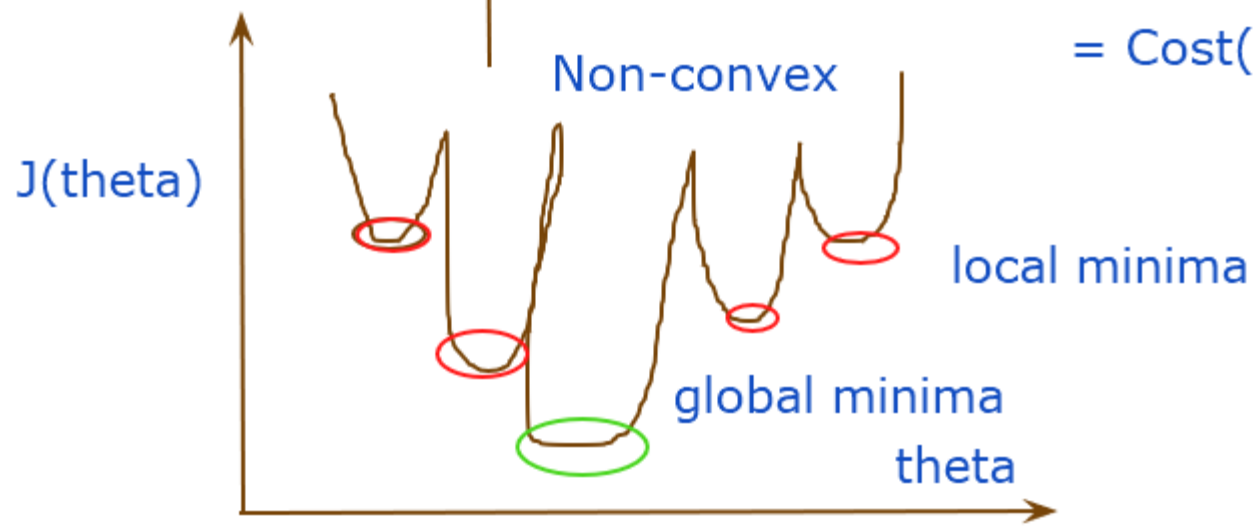


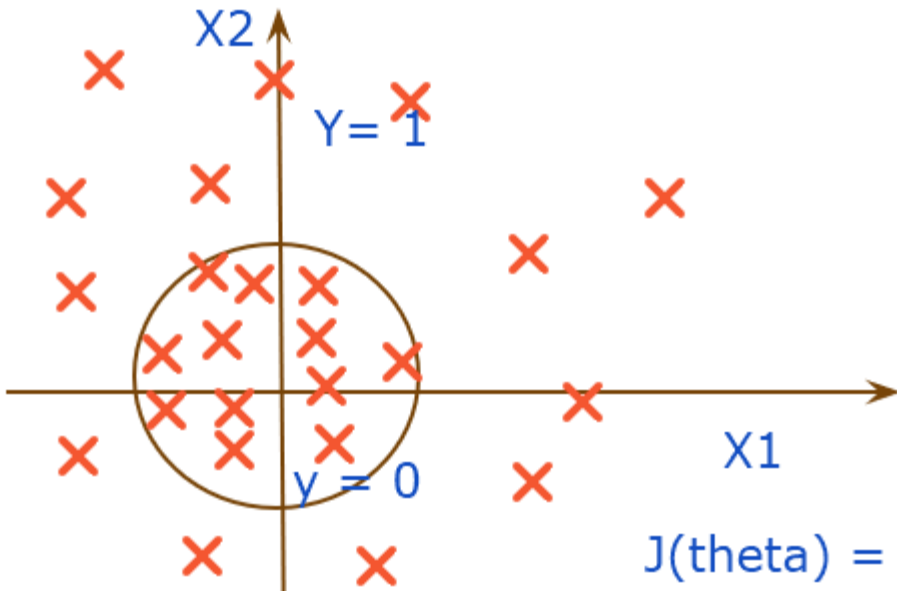
decision boundary
 $X_1^2 + X_2^2 = 1$
 $X_1 + X_2 = 3$

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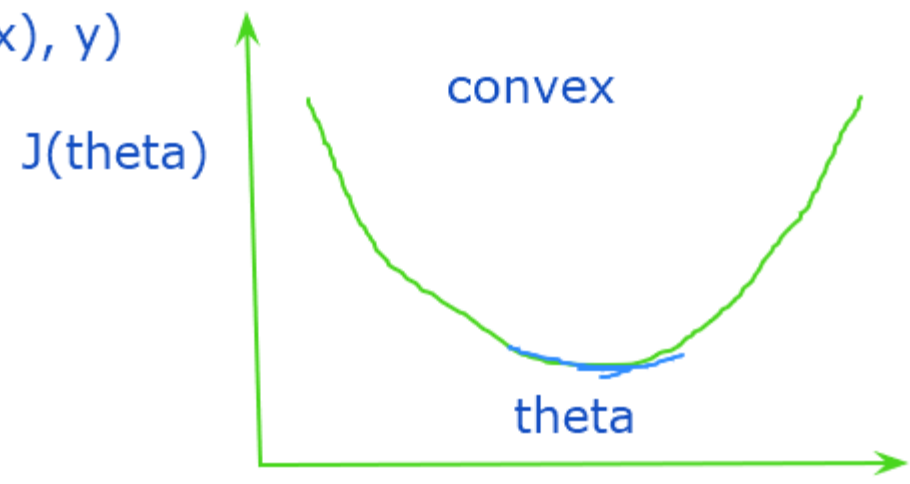
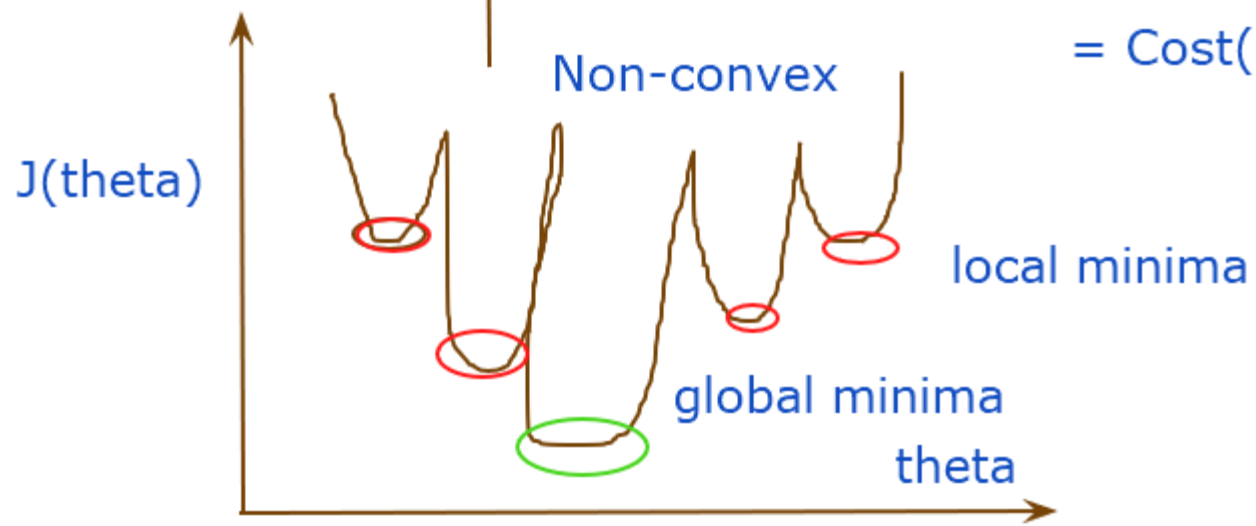


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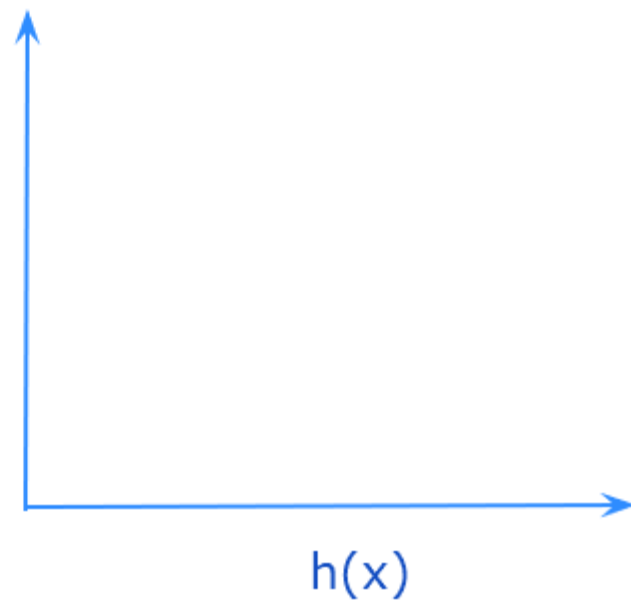
theta 0, theta 1, theta 2, theta n

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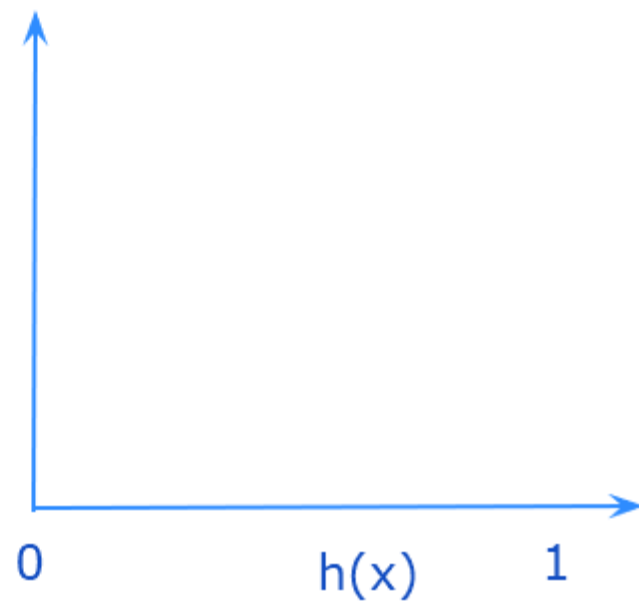
= Cost(h(x), y)



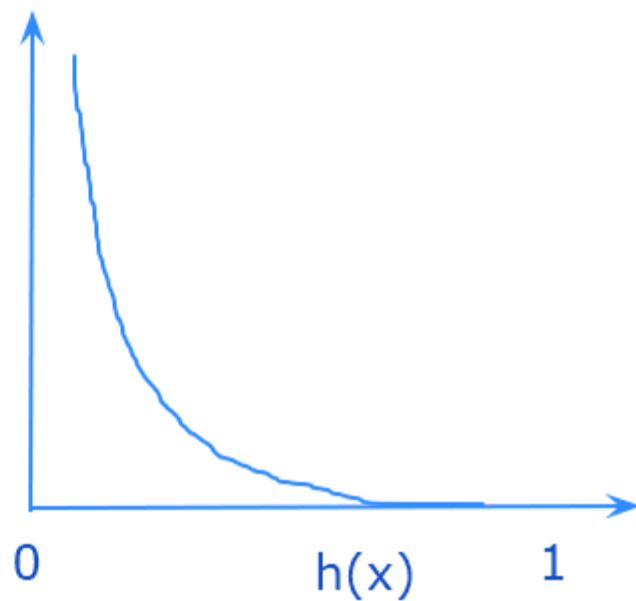
$$\text{cost}(h(x), y) = \begin{cases} -\log h(x) & \text{if } y = 1 \\ -\log(1-h(x)) & \text{if } y = 0 \end{cases}$$



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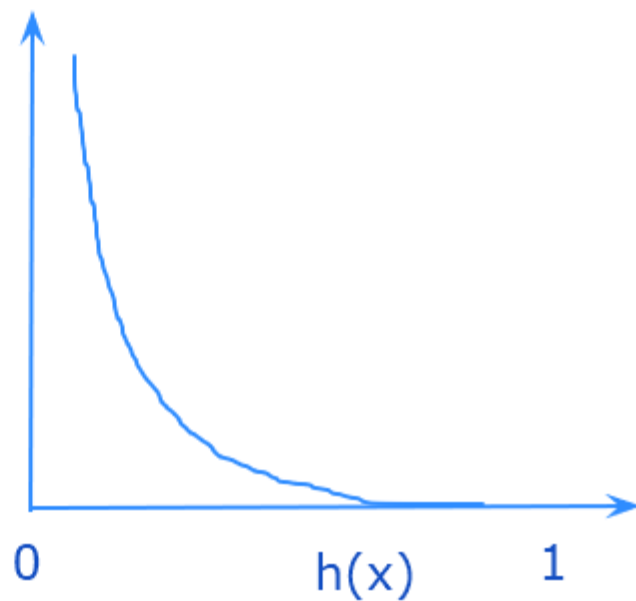


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if $h(x) = 1$; then cost = 0
if $h(x) = 0$; then cost = infinity

$$\text{cost}(h(x), y) = \begin{cases} -\log h(x) & \text{if } y = 1 \\ -\log(1-h(x)) & \text{if } y = 0 \end{cases}$$

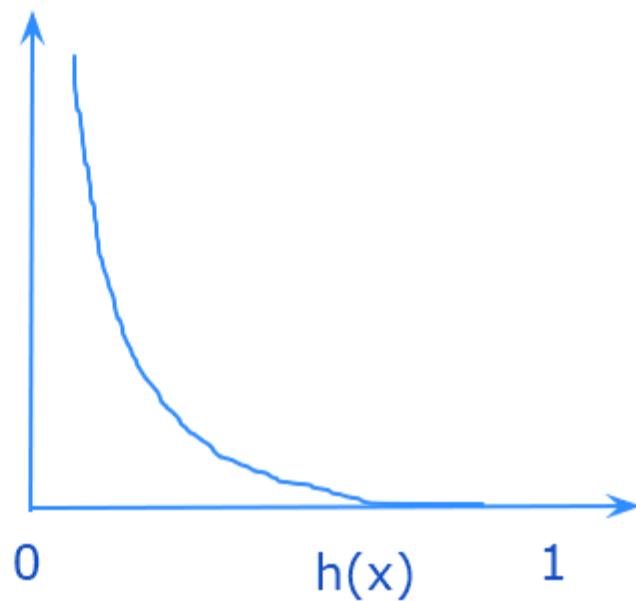


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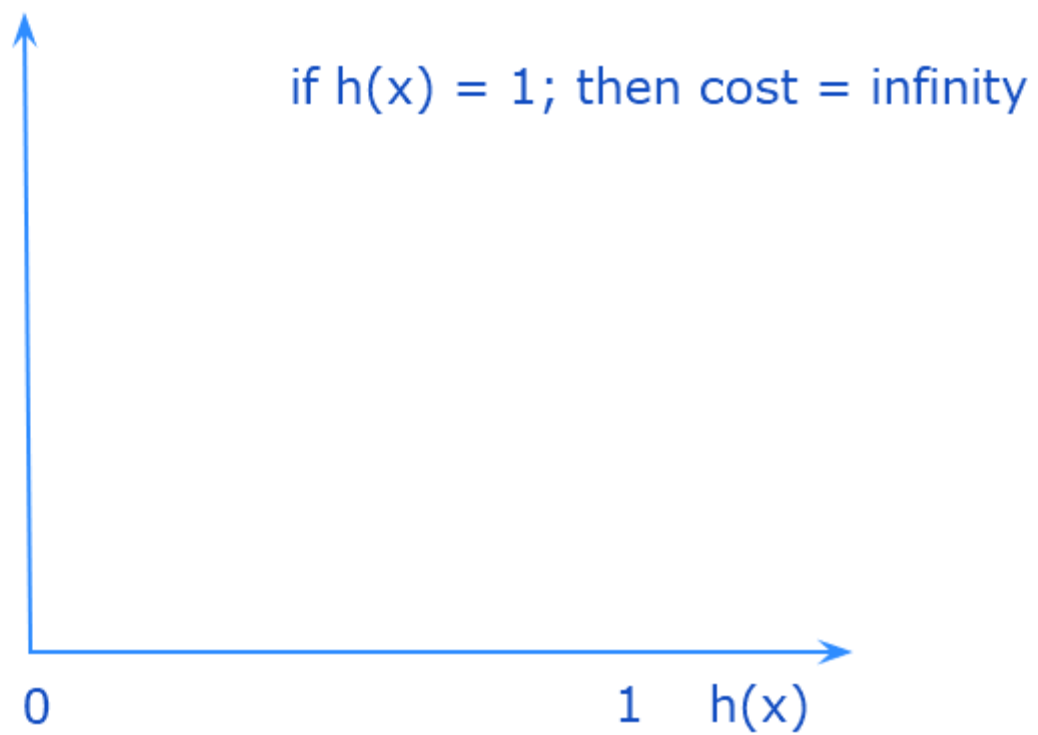
$$\text{cost}(h(x), y) = \begin{cases} -\log h(x) & \text{if } y = 1 \\ -\log(1-h(x)) & \text{if } y = 0 \end{cases}$$

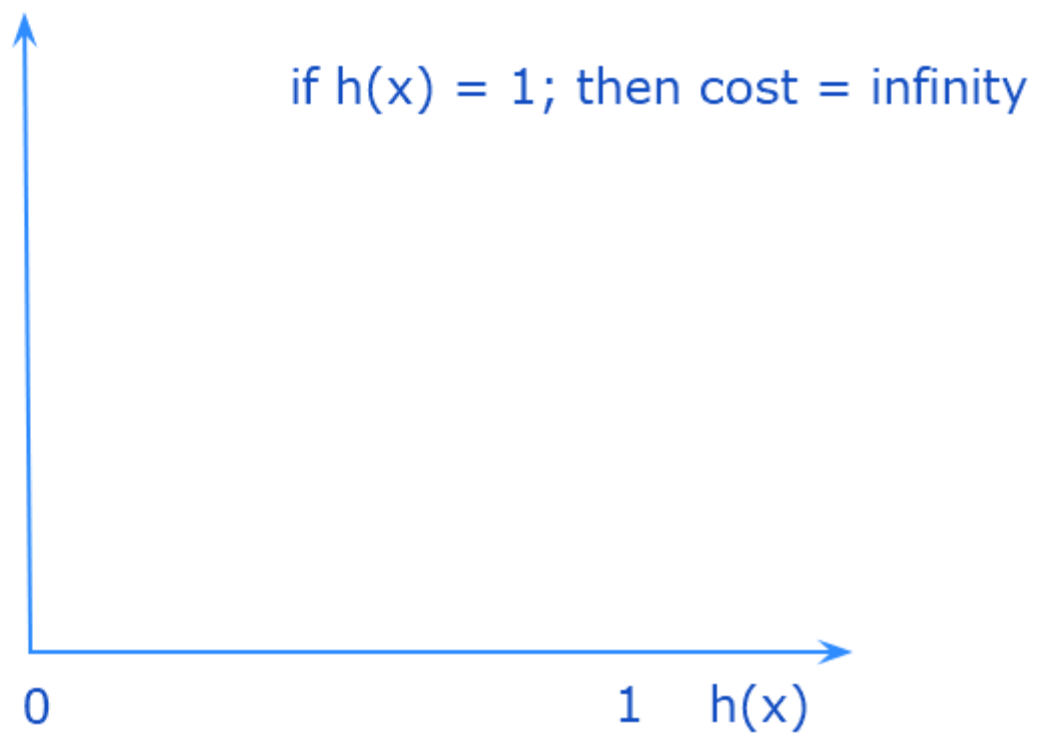


if $h(x) = 1$; then cost = 0

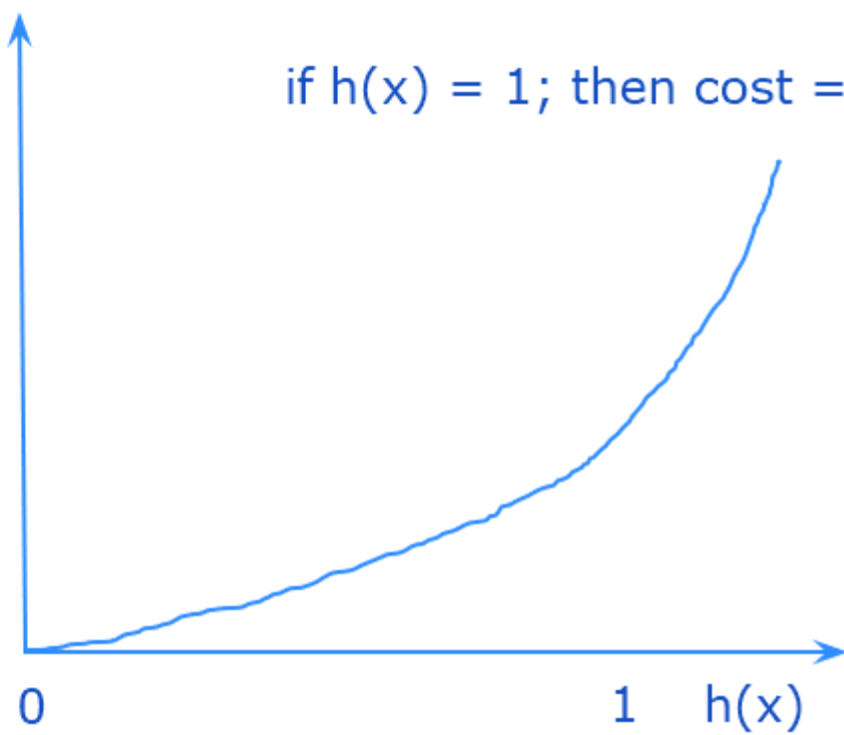
if $h(x) = 0$; then cost = infinity

if $h(x) = 0$; then cost = 0

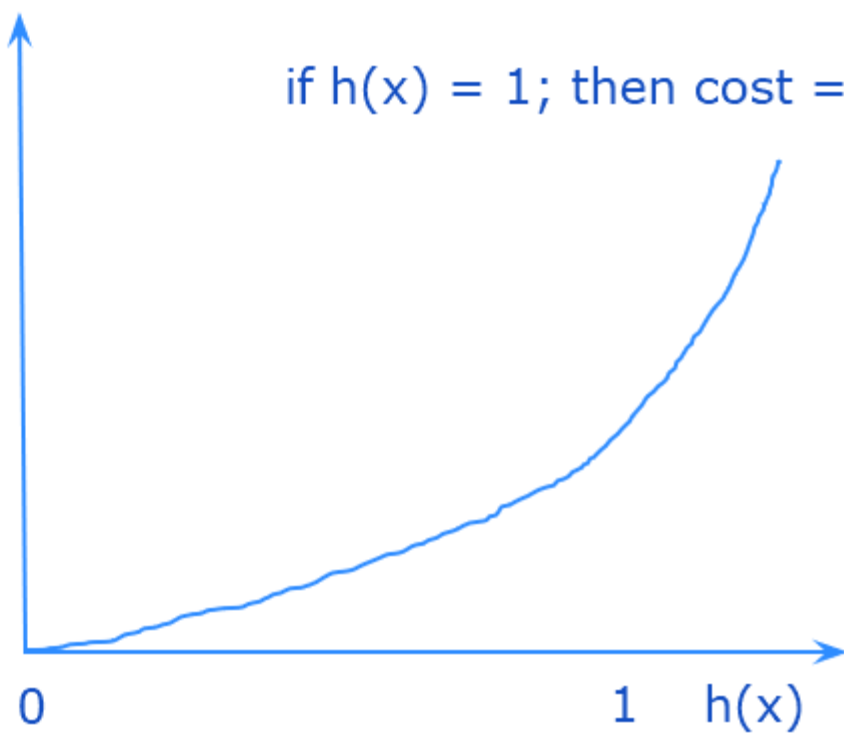


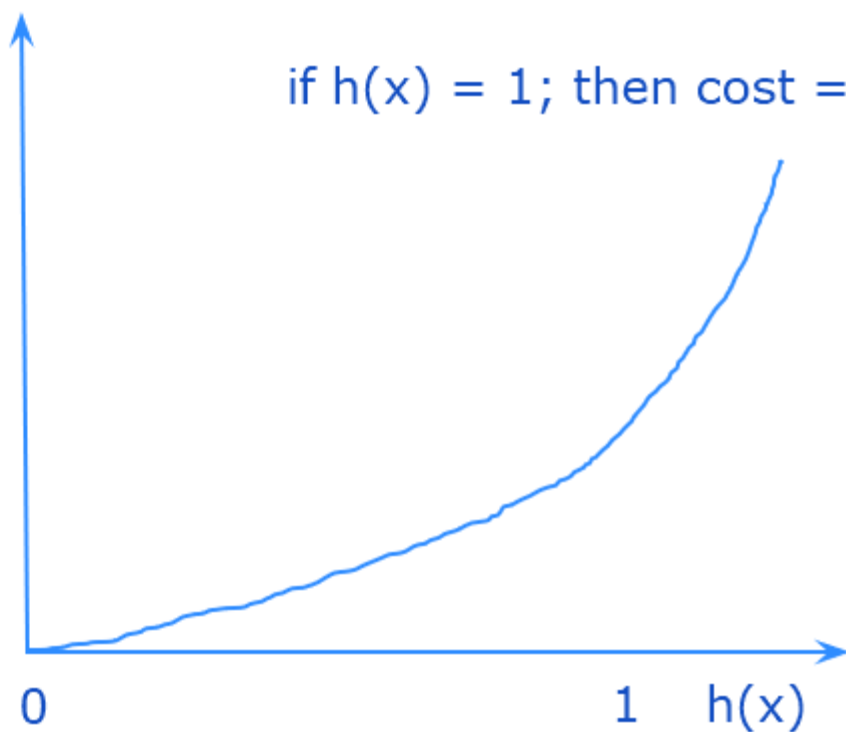


if $h(x) = 1$; then cost = infinity



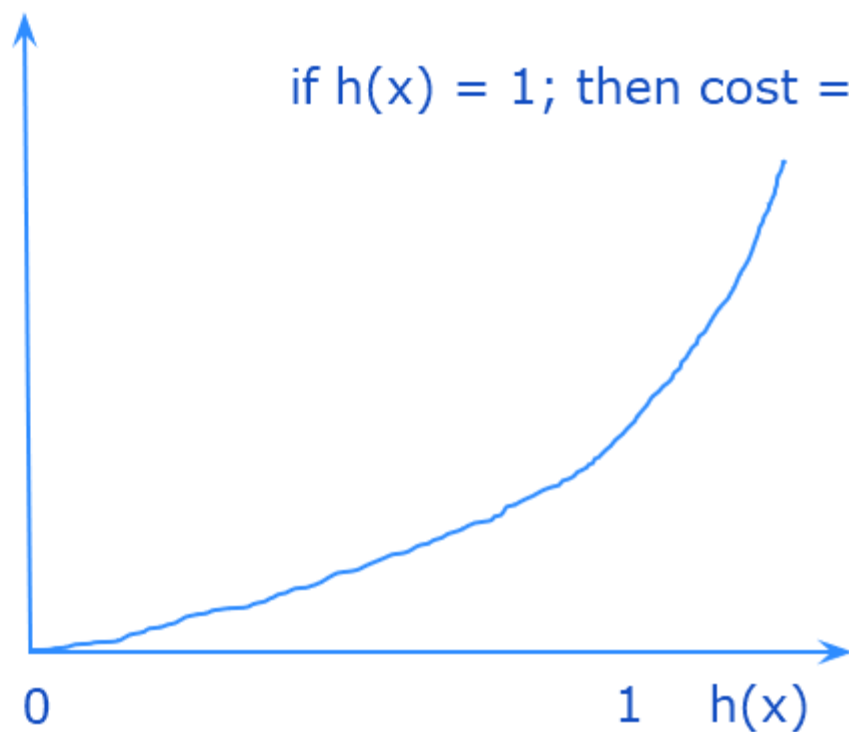
if $h(x) = 1$; then cost = infinity





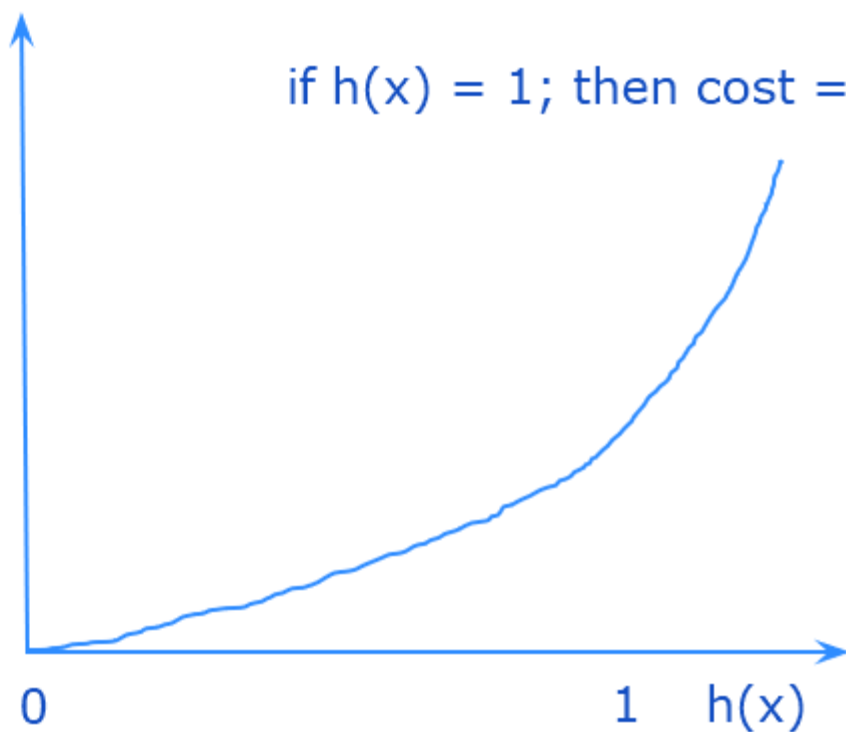
if $h(x) = 1$; then cost = infinity

$$\text{cost}(h(x), y) = \begin{cases} -\log(h(x)) & \text{if } y = 1 \\ -\log(1-h(x)) & \text{if } y = 0 \end{cases}$$

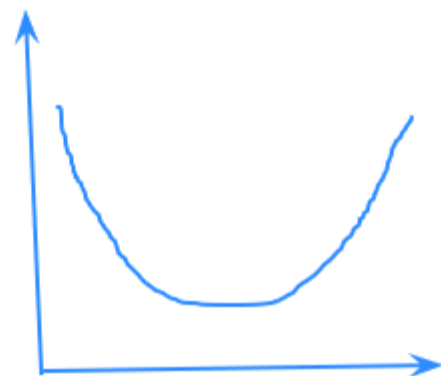


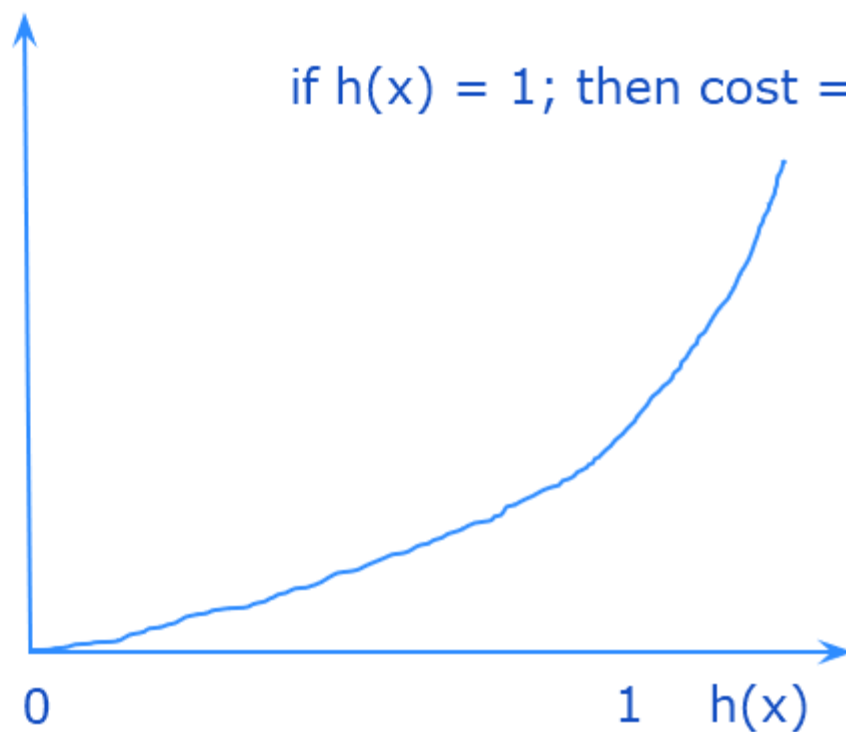
$$\text{cost}(h(x), y) = \begin{cases} -\log(h(x)) & \text{if } y = 1 \\ -\log(1 - h(x)) & \text{if } y = 0 \end{cases}$$

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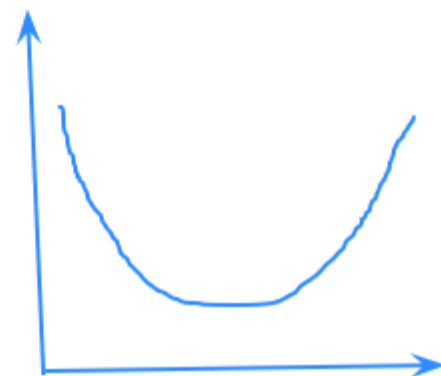
$$\text{cost}(h(x), y) = \begin{cases} -\log(h(x)) & \text{if } y = 1 \\ -\log(1-h(x)) & \text{if } y = 0 \end{cases}$$



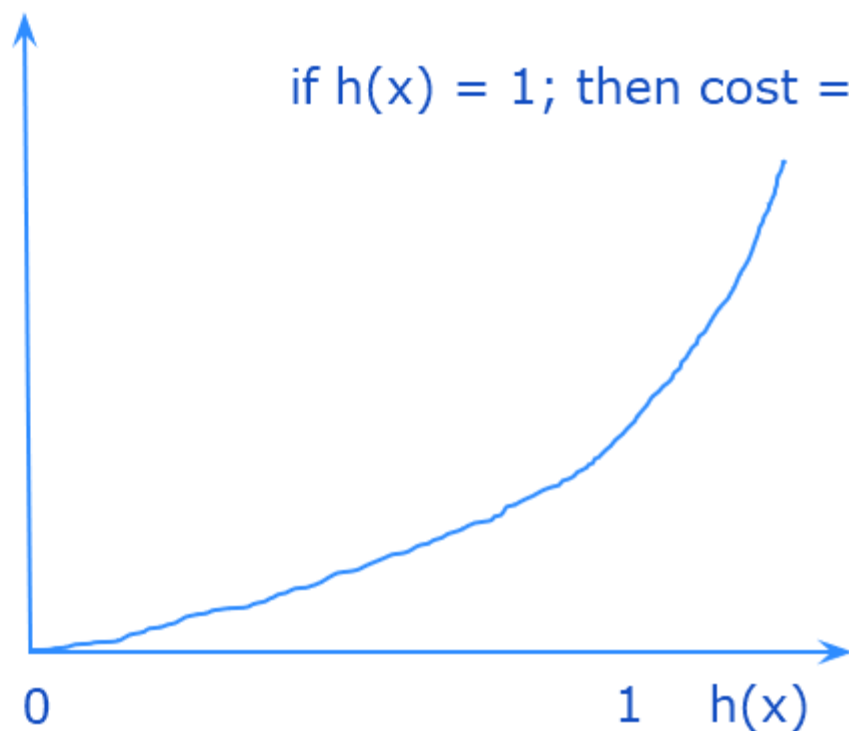


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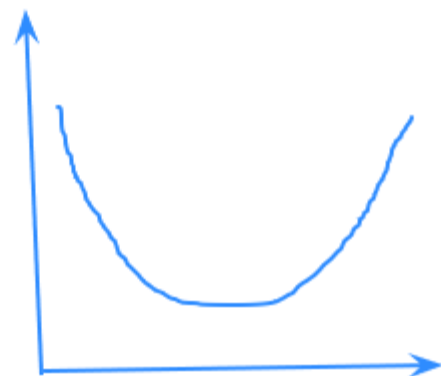


$$\text{cost}(h(x), y) = -y \log(h(x)) - (1-y) \log(1-h(x))$$



if $h(x) = 1$; then cost = infinity

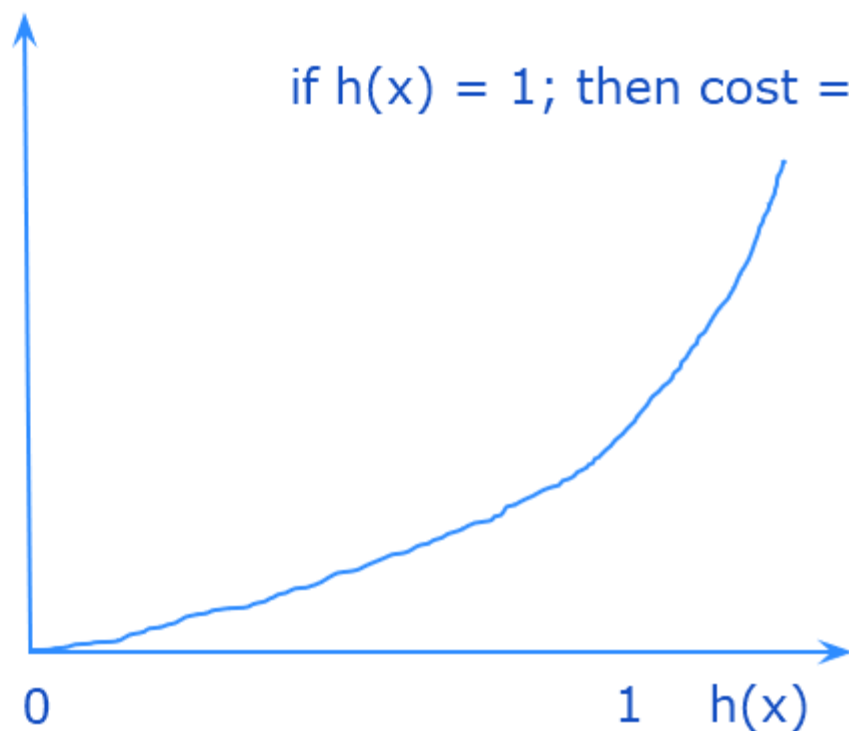
$$\text{cost}(h(x), y) = \begin{cases} -\log(h(x)) & \text{if } y = 1 \\ -\log(1-h(x)) & \text{if } y = 0 \end{cases}$$



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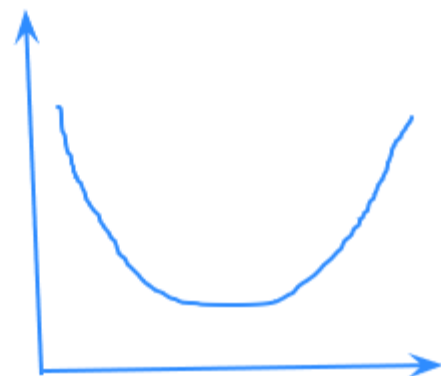
$$\text{if } y = 1; \text{cost}(h(x), y) = -\log(h(x))$$

$$\text{if } y = 0; \text{cost}(h(x), y) = -\log(1-h(x))$$



if $h(x) = 1$; then cost = infinity

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$$\text{if } y = 1; \text{cost}(h(x), y) = -\log(h(x))$$

$$\text{if } y = 0; \text{cost}(h(x), y) = -\log(1-h(x))$$