

Naive Bayes

It is a probabilistic supervised ML algo based on Bayes Theorem, used mainly for classification problem.

Bayes Formula

$$P(C|X) = \frac{P(X|C) \cdot P(C)}{P(X)}$$

C = class label

X = Input data (Feature)

$P(C|X)$ = Posterior Probability (what we want)

$P(X|C)$ = Likelihood

$P(C)$ = Prior Probability

$P(X)$ = Evidence (constant).

If input features $\rightarrow X = (x_1, x_2, x_3, \dots, x_n)$.

Naive Bayes Assumes.

$$P(X|C) = P(x_1|C) \cdot P(x_2|C) \dots P(x_n|C)$$

Each feature is independent.

Working

1. Calculate Prior Probability $P(C)$

2. Calculate Likelihood $P(x_i|C)$

↳ Probability of each feature given in class.

3. Apply Naive Bayes Assumption

$$\hookrightarrow P(X|C) = P(x_i|C)$$

4. Calculate Posterior Score

$$P(C|X) \propto P(C) \times \prod P(x_i|C)$$

5. Predict class

↳ with maximum Probability.

→ three types of Naive Bayes.

↳ Multinomial

↳ Gaussian

↳ Bernoulli

① Multinomial

Used when feature / data is text.

When features show how many times something appears.

ex →

Day	Outlook	temp	Decision
1	Sunny	Hot	No
2	Sunny	Hot	No
3	Overcast	Hot	Yes
4	Rain	Mild	Yes
5	Rain	Cool	Yes
6	Rain	Cool	No
7	Overcast	Cool	Yes
8	Sunny	Mild	No
9	Sunny	Cool	Yes
10	Rain	Mild	Yes
11	Sunny	Mild	Yes
12	Overcast	Mild	Yes
13	Overcast	Hot	Yes
14	Rain	Mild	No
15	Sunny	Cool	?

$$P(\text{Yes}) = \frac{9}{14}$$

$$P(\text{No}) = \frac{5}{14}$$

{ Prior Probability }

Likelihood Probability of feature (X) given class c

(Yes)

$$P(\text{Sunny} | \text{Yes}) = \frac{2}{9}$$

$$P(\text{Cool} | \text{Yes}) = \frac{3}{9}$$

(No)

$$P(\text{Sunny} | \text{No}) = \frac{3}{5}$$

$$P(\text{Cool} | \text{No}) = \frac{1}{5}$$

Posterior Probability

$$P(\text{Yes} | \text{Sunny, Cool}) = P(\text{Sunny} | \text{Yes}) \times P(\text{Cool} | \text{Yes}) \times P(\text{Yes})$$

$$= \frac{2}{9} \times \frac{3}{9} \times \frac{9}{14} \approx 0.0476$$

$$P(\text{No} | \text{Sunny, Cool}) = \frac{3}{5} \times \frac{1}{5} \times \frac{5}{14} \approx 0.0425$$

Normalizing them

$$0.0476 + 0.0425 = 0.0905$$

$$P(\text{Yes} | \text{Sunny, Cool}) = \frac{0.0476}{0.0905} \approx 0.526$$

$$P(\text{No} | \text{Sunny, Cool}) = \frac{0.0425}{0.0905} \approx 0.474$$

High Posterior Probability Score = 0.526,

So Prediction is (Yes)

Like in this way this naive Bayes works.

② Gaussian Naive Bayes

↳ Used when features are continuous.

$$\text{Formula} \rightarrow P(x|c) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

$\mu \rightarrow \text{mean}$, $\sigma^2 \rightarrow \text{variance}$.

In this Likelihood Probability is using this formula rest remains same.

③ Bernoulli Naive Bayes

↳ Used when features are binary (0 or 1).
Feature indicates presence or absence.

$$P(x|c) = p^n (1-p)^{1-n}$$

ex → dataset

mail	Free	Win	Hello	Spam / Not
Free win	1	1	0	1
win Hello	0	1	1	1
Hello	0	0	1	0
Free Hello	1	0	1	0

For these type Bernoulli used.