# Assignment 2

# AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

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### Chapter 16, Exercise 16.4

#### Question 9:

If 4-digit numbers greater than 5,000 are randomly formed from the digits 0,1,3,5 and 7, what is the probability of forming a number divisible by 5 when :

- 1) the digits are repeated?
- 2) the repetition of digits are not allowed?

#### **Solution:**

Let W, X, Y, Z be 4 random variables representing Thousandths, Hundredths, Tenths and Units place respectively.

Since 4-digit numbers greater than 5,000 are formed, The thousands place is either 7 or 5.

1) Digits are repeated

$$W \in \{5, 7\} \tag{1}$$

$$X \in \{0, 1, 3, 5, 7\} \tag{2}$$

$$Y \in \{0, 1, 3, 5, 7\} \tag{3}$$

$$Z \in \{0, 1, 3, 5, 7\} \tag{4}$$

'A' = Event representing all the 4-digits numbers greater than 5,000 divisible by 5 when digits are repeated.

$$Pr(A) = Pr(W = 5, Z = 0) + Pr(W = 5, Z = 5) + Pr(W = 7, Z = 0) + Pr(W = 7, Z = 5)$$

(5)

$$= \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{5} - \frac{1}{2} \times \frac{1}{5} \times \frac{1}{5} \times \frac{1}{5}\right) + \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{5}\right) + \left(\frac{1}{2} \times \frac{1}{5}\right) + \left(\frac{1}{2} \times \frac{1}{5}\right) + \left(\frac{1}{2} \times \frac{1}{5}\right)$$
 (6)

$$=\frac{24}{250} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10} \tag{7}$$

$$=\frac{99}{250}$$
 (8)

## 2) Digits are not repeated

$$W \implies 2 \text{ options}$$
 (9)

$$Z \implies 4 \text{ options}$$
 (10)

$$X \implies 3 \text{ options}$$
 (11)

$$Y \implies 2 \text{ options}$$
 (12)

'B' = Event representing all the 4-digits numbers greater than 5,000 divisible by 5 when digits are not repeated.

$$Pr(B) = Pr(W = 5, Z = 0) + Pr(W = 7, Z = 0) + Pr(W = 7, Z = 5)$$
(13)

$$= \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{4}\right) + \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{4}\right) + \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{4}\right) \tag{14}$$

$$= \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

$$= \frac{3}{8}$$
(15)

$$=\frac{3}{8}\tag{16}$$