

# Assignment 2

## AI1110: Probability and Random Variables

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#### Chapter 16 , Exercise 16.4

##### Question 9 :

If 4-digit numbers greater than 5,000 are randomly formed from the digits 0,1,3,5 and 7, what is the probability of forming a number divisible by 5 when :

- 1) the digits are repeated?
- 2) the repetition of digits are not allowed?

##### Solution:

Let W , X , Y , Z be 4 random variables representing Thousandths , Hundredths , Tenths and Units place respectively.

Since 4-digit numbers greater than 5,000 are formed , The thousands place is either 7 or 5.

- 1) Digits are repeated

Parameter	Value	Description
W	{5, 7}	2 choices
X	{0, 1, 3, 5, 7}	5 choices
Y	{0, 1, 3, 5, 7}	5 choices
Z	{0, 1, 3, 5, 7}	5 choices

TABLE 1

'A' = Event representing all the 4-digits numbers greater than 5,000 divisible by 5 when digits are repeated.

$$\Pr(A) = \Pr(W = 5, Z = 0) + \Pr(W = 5, Z = 5) + \Pr(W = 7, Z = 0) + \Pr(W = 7, Z = 5) \quad (1)$$

$$= \left( \frac{1}{2} \times 1 \times 1 \times \frac{1}{5} - \frac{1}{2} \times \frac{1}{5} \times \frac{1}{5} \times \frac{1}{5} \right) + \left( \frac{1}{2} \times 1 \times 1 \times \frac{1}{5} \right) + \left( \frac{1}{2} \times \frac{1}{5} \right) + \left( \frac{1}{2} \times \frac{1}{5} \right) \quad (2)$$

$$= \frac{24}{250} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10} \quad (3)$$

$$= \frac{99}{250} \quad (4)$$

## 2) Digits are not repeated

Parameter	Description
W	2 choices
Z	4 choices
X	3 choices
Y	2 choices

TABLE 2

'B' = Event representing all the 4-digits numbers greater than 5,000 divisible by 5 when digits are not repeated.

$$\Pr(B) = \Pr(W = 5, Z = 0) + \Pr(W = 7, Z = 0) + \Pr(W = 7, Z = 5) \quad (5)$$

$$= \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{4}\right) + \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{4}\right) + \left(\frac{1}{2} \times 1 \times 1 \times \frac{1}{4}\right) \quad (6)$$

$$= \frac{1}{8} + \frac{1}{8} + \frac{1}{8} \quad (7)$$

$$= \frac{3}{8} \quad (8)$$