

Syntax-Directed Translation

There are two notations for associating semantic rules with productions, which are:

- Syntax-directed definitions &
- Translation schema

Syntax-directed definition:

A syntax-directed definition is a context-free grammar together with semantic rules. In syntax-directed definition, attributes are associated with grammar symbol and semantic rules are associated with productions.

E.g.

	<u>Production</u>	<u>Semantic Rules</u>
1)	$E \rightarrow E_1 + T$	$E.\text{val} = E_1.\text{val} + T.\text{val}$
	$E \rightarrow T$	$E.\text{val} = T.\text{val}$

* The syntax directed definition for a simple desk calculator:

<u>Production</u>	<u>semantic Rules</u>
$L \rightarrow E_1$	$\text{print}(E_1.\text{val}) \quad / L.\text{val} = E_1.\text{val}$
$E \rightarrow E_1 + T$	$E.\text{val} = E_1.\text{val} + T.\text{val}$
$E \rightarrow T$	$E.\text{val} = T.\text{val}$
$T \rightarrow T_1 * F$	$T.\text{val} = T_1.\text{val} * F.\text{val}$
$T \rightarrow F$	$T.\text{val} = F.\text{val}$
$F \rightarrow (E)$	$F.\text{val} = E.\text{val}$
$F \rightarrow \text{digit}$	$F.\text{val} = \text{digit}.\text{textval}$

Annotated parse tree:

A parse tree constructed for a given input string in which each node showing the values of attributes is called an annotated parse tree.

- The process of computing the attributes values of the nodes is called annotating (or decorating) of the parse tree.

Example :

let's take a grammar;

$$L \rightarrow E \text{ return}$$

Print(E.val)

$$E \rightarrow E_1 + T$$

E.val = E₁.val + T.val

$$E \rightarrow T$$

E.val = T.val

$$T \rightarrow T * F$$

T.val = T.val * F.val

$$T \rightarrow E$$

T.val = E.val

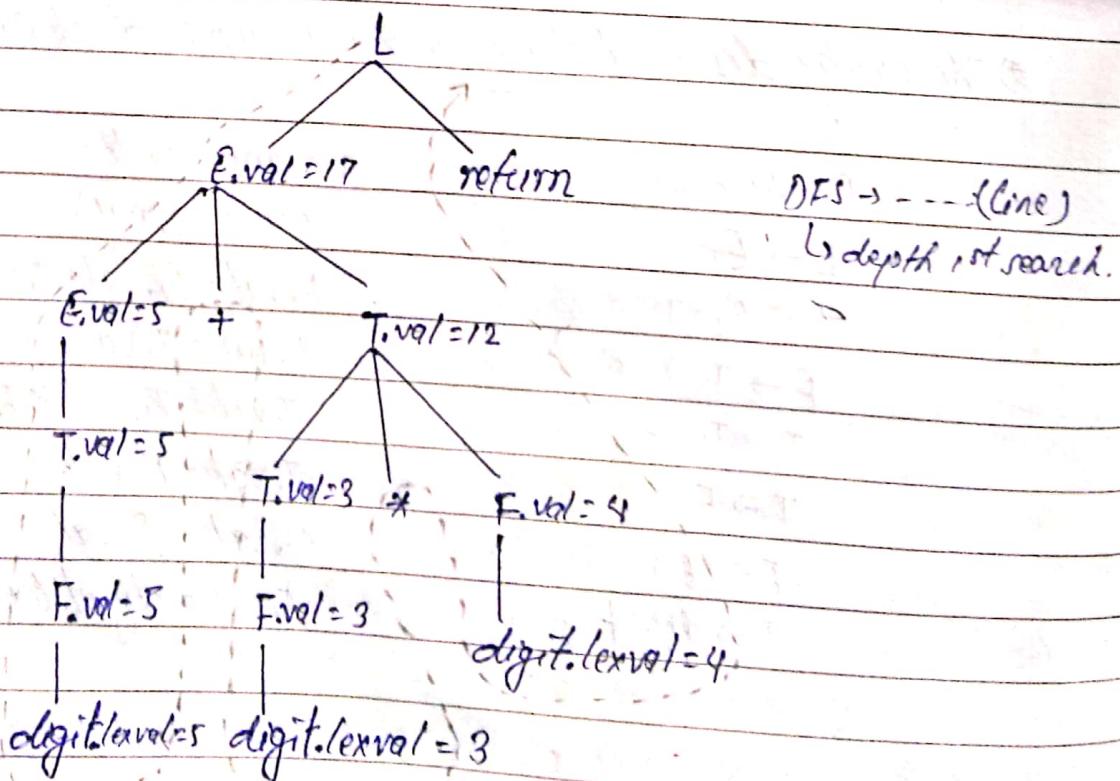
$$F \rightarrow (E)$$

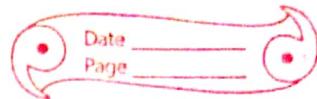
F.val = E.val

$$F \rightarrow \text{digit}$$

F.val = digit.lexval

Now, the annotated parse tree for the input string $5+3*4$ is,





Attribute grammar in Yacc / Bison

$E \rightarrow E \text{ retn}$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow (E) \mid \text{digit}$

% token DIGIT

q0%

L: $E \text{ '}' \ln'$ {printf ("%d\n", \$1); }
;

E: $E + T$ { \$\$ = \$1 + \$3; }
| T { \$\$ = \$1; }
;

T: $T * F$ { \$\$ = \$1 * \$3; }
| F { \$\$ = \$1; }
;

F: $'(' E ')'$ { \$\$ = \$2; }
| DIGIT { \$\$ = \$1; }
;

q0%

Inherited and synthesized Attributes (Types of attributes)

* Synthesized attributes:

The attributes of node that are derived from its children nodes are called synthesized attributes.

E.g.

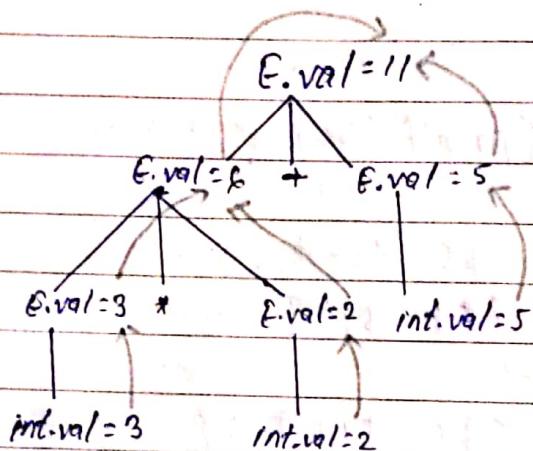
- ① $A \rightarrow BCD$, A be a parent node & B,C,D are children nodes
- | | |
|-------------|--|
| $A.s = B.s$ | } Parent node A taking value from its children
B,C,D. |
| $A.s = C.s$ | |
| $A.s = D.s$ | |



- (1) $E \rightarrow E_1 + E_2 \quad \{ E.val = E_1.val + E_2.val \}$
 $E \rightarrow E_1 * E_2 \quad \{ E.val = E_1.val * E_2.val \}$
 $E \rightarrow \text{int} \quad \{ E.val = \text{int}.val \}$

→ value owns from child to parent in the parse tree.

* For e.g. for string $3 * 2 + 5$



* Inherited attributes:

The attributes of node that are derived from its parent or sibling nodes are called inherited attributes.
 E.g.

(2) $A \rightarrow BCN$

C.i = A.i

C.i = B.i

(2)

Productions

semantic rules

$O \rightarrow TL$

L.in = T.type

$T \rightarrow \text{int}$

T.type = integer

$T \rightarrow \text{real}$

T.type = real

$L \rightarrow L_1, id$

L.in = L.in, addtype(id.entry, L.in)

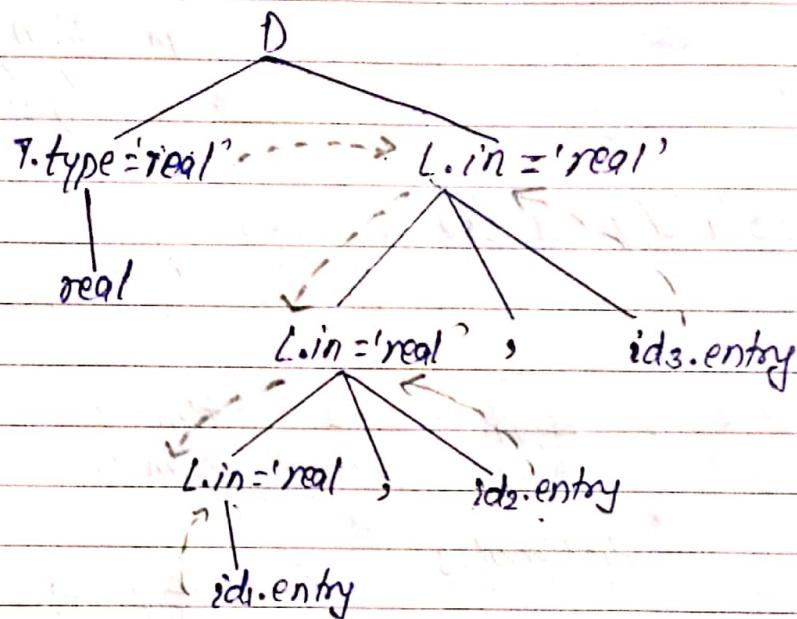
$L \rightarrow id$

addtype(id.entry, L.in)

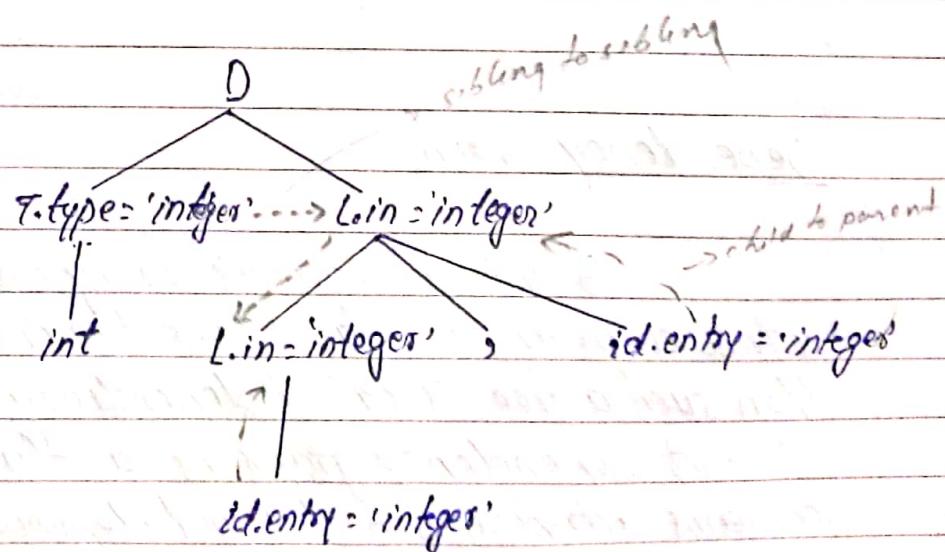
symbol T is associated with a synthesized attribute type,
 symbol L is associated with an inherited attribute in.

→ Values flows into a node in the parse tree from parents and/or siblings.

Input: real $\text{id}_1, \text{id}_2, \text{id}_3$



Input: int id, id



Production

1. $T \rightarrow FT'$

Semantic Rules

$T'.int = F.val$

in \rightarrow inherited attr.
syn \rightarrow synthesized attr.

2. $T' \rightarrow xFT'$

$T'.val = T'.syn$

$T'.in = T'.in \times F.val$

3. $F' \rightarrow e$

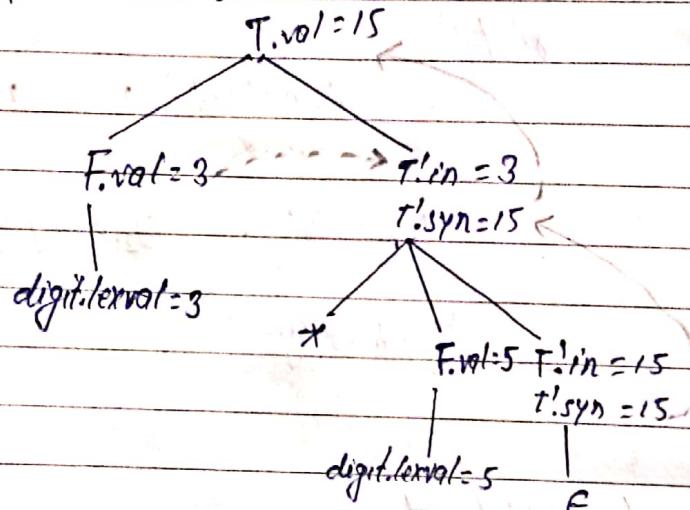
$F'.syn = T'.syn$

$T'.syn = T'.in$

4. $F \rightarrow digit$

$F.val = digit.lexval$

Annotated parse tree for 3×5



Dependency Graph

If interdependencies among the inherited and synthesized attributes in an annotated parse tree are specified by arrows then such a tree is called dependency graph.

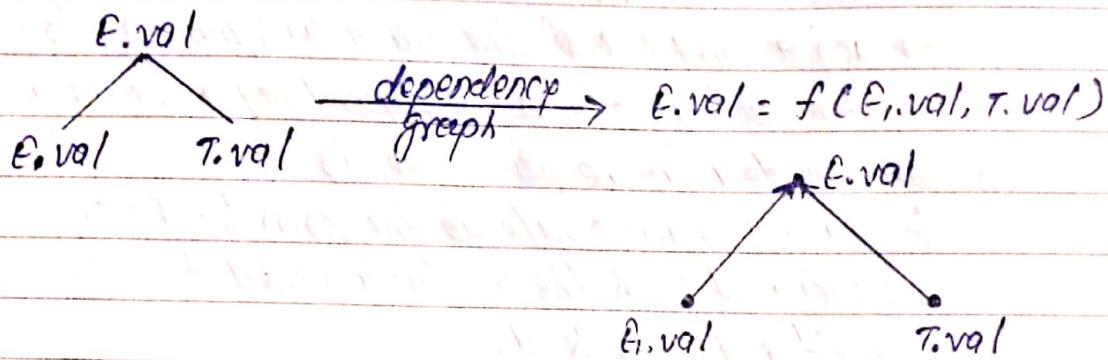
A dependency graph is a directed graph that contains attributes as nodes and dependencies across attributes as edge.

→ For synthesized attributes, each node has dependency to child nodes.

→ For inherited attributes, any node have dependency to its sibling or parent nodes.

for E.g.

$$\textcircled{1} \quad E \rightarrow E_1 + T \quad E.\text{val} = E_1.\text{val} + T.\text{val}$$



\textcircled{2}

$$D \rightarrow TL$$

$$L.\text{in} = T.\text{type}$$

$$T \rightarrow \text{int}$$

$$T.\text{type} = \text{integer}$$

$$T \rightarrow \text{real}$$

$$T.\text{type} = \text{real}$$

$$C \rightarrow (l_1, id)$$

$$L.\text{in} = L.\text{in}, \text{addtype}(id.\text{entry}, L.\text{in})$$

$$l \rightarrow id$$

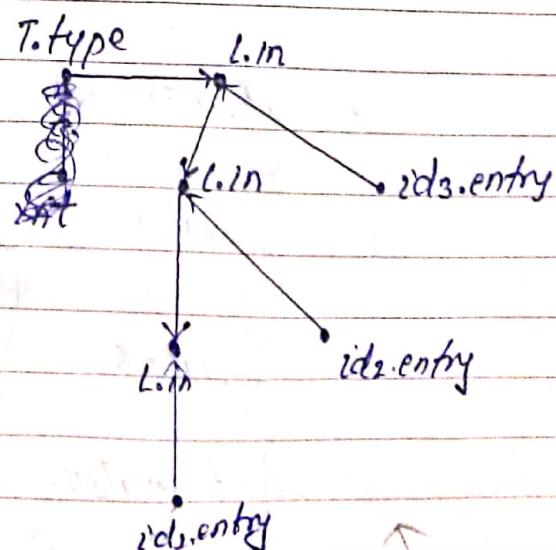
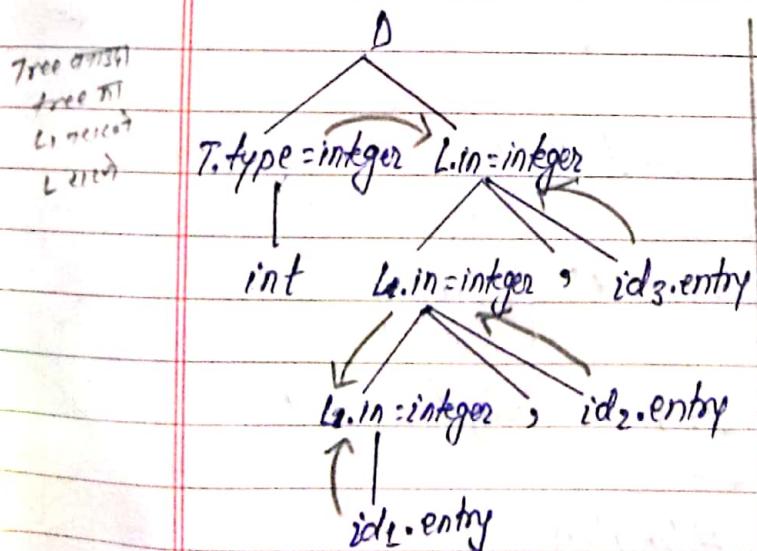
$$\text{addtype}(id.\text{entry}, L.\text{in})$$

Here type is synthesized and in is inherited attribute.

For int id1, id2, id3

The annotated parse tree :

Dependency graph :



xx wrong entry for start node

Algorithm for dependency graph:

for each node n in the parse tree do

for each attribute a of the grammar symbol n do

construct a node in the dependency graph for a .

for each node n in the parse tree do

for each semantic rule a of the form $b = f(c_1, c_2, \dots, c_k)$

associated with the production used at n do

for $i=1$ to k do

construct an edge from c_i to b .

Prod.

$E \rightarrow E + T$

$E \rightarrow T$

$T \rightarrow T * F$

$T \rightarrow F$

$F \rightarrow \text{digit}$

Semantic Rules

$E.\text{val} = E.\text{val} + T.\text{val}$

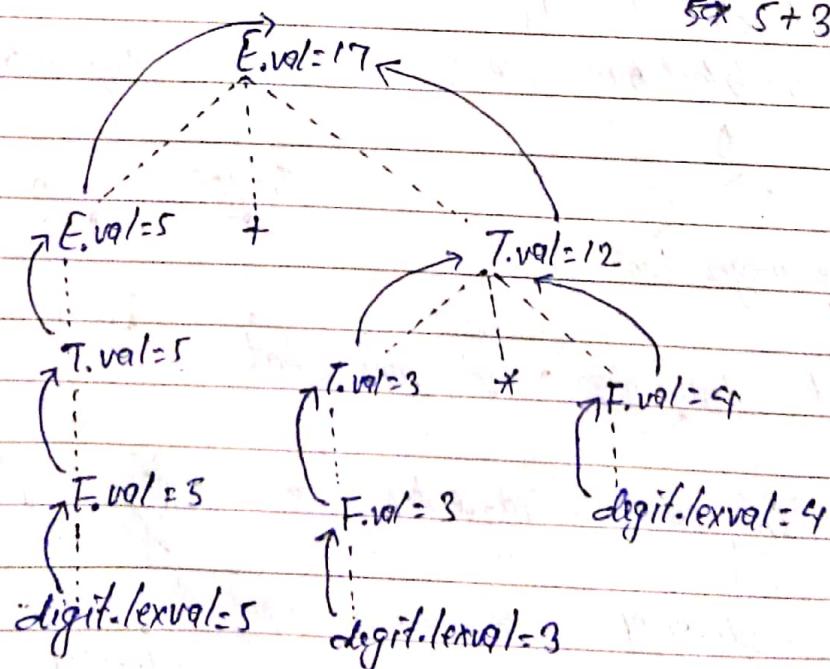
$E.\text{val} = T.\text{val}$

$T.\text{val} = T.\text{val} * F.\text{val}$

$T.\text{val} = F.\text{val}$

$F.\text{val} = \text{digit.lexval}$

$5 * 5 + 3 * 4$



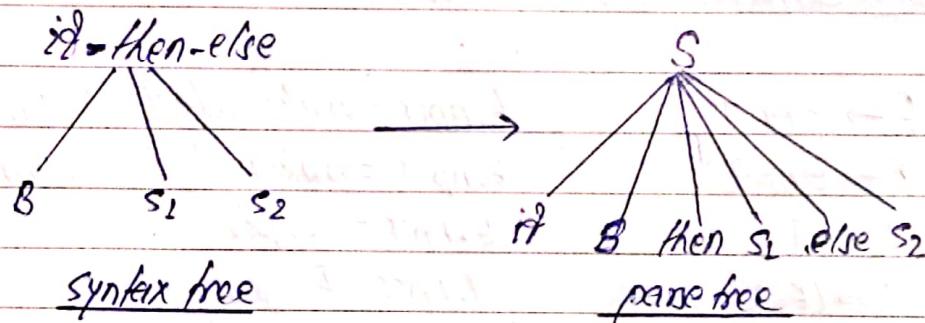
Here dotted line shows the parse tree and directed so solid line shows the dependency graph.

Construction of syntax tree

Syntax tree is an abstract representation of the language constructs. In the syntax tree, interior nodes are operators and leaves are operands. The syntax tree is used for syntax directed translation with the help of syntax directed definition.

E.g.

- ① $S \rightarrow \text{if } B \text{ then } S_1 \text{ else } S_2$ is a production.



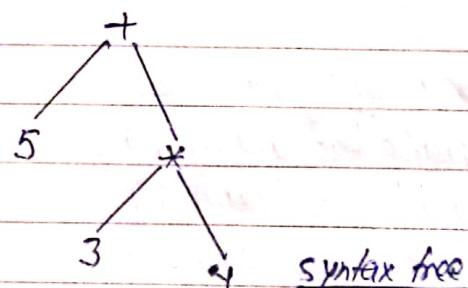
② Arithmetic

$$5 + 3 * 4$$

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid \text{digit}$$



To construct syntax tree we need following functions:

- ① `makenode (op, left, right)`: It creates an operator node with operator op . $left$ & $right$ points the $address$ of left and right child.

- ② `makeleaf (id, entry)`: It creates an identifier node with label id . $entry$ is a pointer to symbol table entry for that id .

- ③ `makeleaf (num, val)`: It creates a node with label num and val is the value of number.

Ex.

production

$$E \rightarrow E_1 + T$$

$$E \rightarrow E_1 - T$$

$$E \rightarrow T$$

$$T \rightarrow (E)$$

$$T \rightarrow id$$

$$T \rightarrow num$$

Semantic Rules

$$E.val = E_1.val + T.val$$

$$E.val = E_1.val - T.val$$

$$E.val = T.val$$

$$T.val = E.val$$

$$T.val = id.entry$$

$$T.val = num.val$$

Syntax directed defn for construction of syntax tree

$$E \rightarrow E_1 + T$$

E.nptr = makenode ('+', E₁.nptr, T.nptr)

$$E \rightarrow E_1 - T$$

E.nptr = makenode ('-', E₁.nptr, T.nptr)

$$E \rightarrow T$$

E.nptr = T.nptr

$$T \rightarrow (E)$$

T.nptr = E.nptr

$$T \rightarrow id$$

T.nptr = makeleaf(id, id.entry)

$$T \rightarrow num$$

T.nptr = makeleaf(num, num.val)

expression: 3 + 5 - 2

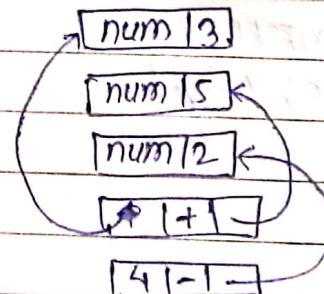
1. P₁ = makeleaf(num, 3);

2. P₂ = makeleaf(num, 5);

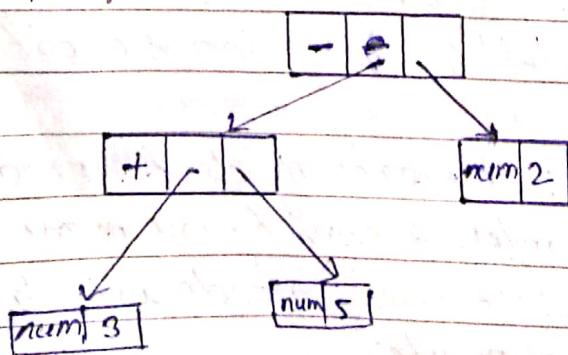
3. P₃ = makeleaf(num, 2);

4. P₄ = makenode('+', P₁, P₂);

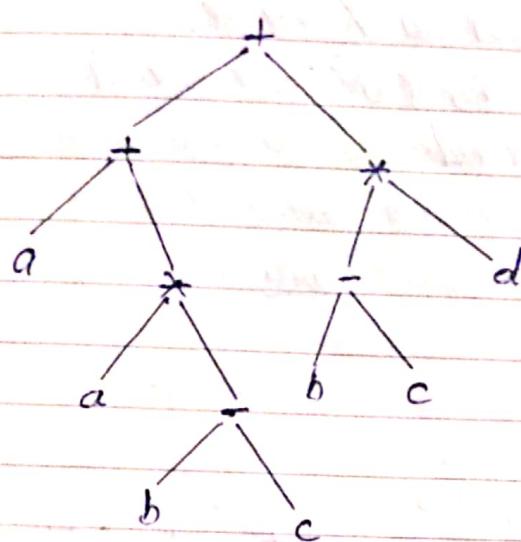
5. P₅ = makenode('-', P₄, P₃);



syntax tree:



$a + a * (b - c) + (b - c) * d$



code:

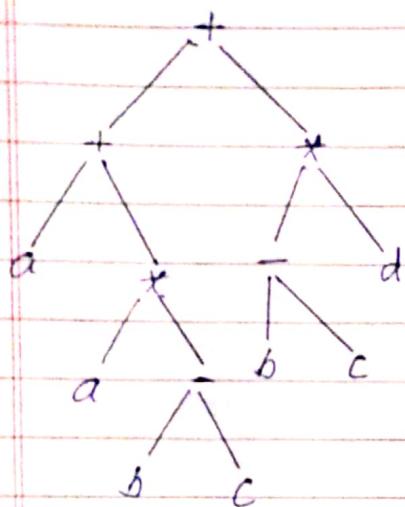
1. ~~makeleaf(a)~~
2. $P_1 = \text{makeleaf}(a, a.\text{entry})$;
3. $P_2 = \text{makeleaf}(a, a.\text{entry})$;
4. $P_3 = \text{makeleaf}(b, b.\text{entry})$;
5. $P_4 = \text{makeleaf}(c, c.\text{entry})$;
6. $P_5 = \text{makeleaf}(d, d.\text{entry})$;
7. $P_6 = \text{makeleaf}(b - c, b - c.\text{entry})$;
8. $P_7 = \text{makeleaf}(b - c, b - c.\text{entry})$;
9. $P_8 = \text{makeleaf}(a * (b - c), a * (b - c).\text{entry})$;
10. $P_9 = \text{makeleaf}(a * (b - c), a * (b - c).\text{entry})$;
11. $P_{10} = \text{makeleaf}(a + a * (b - c), a + a * (b - c).\text{entry})$;
12. $P_{11} = \text{makeleaf}(a + a * (b - c), a + a * (b - c).\text{entry})$;
13. $P_{12} = \text{makeleaf}(a + a * (b - c) + (b - c) * d, a + a * (b - c) + (b - c) * d).\text{entry}$;

~~*-* Directed Acyclic Graph (DAG):~~

A DAG for an expression identifies common sub-expressions in the expression.

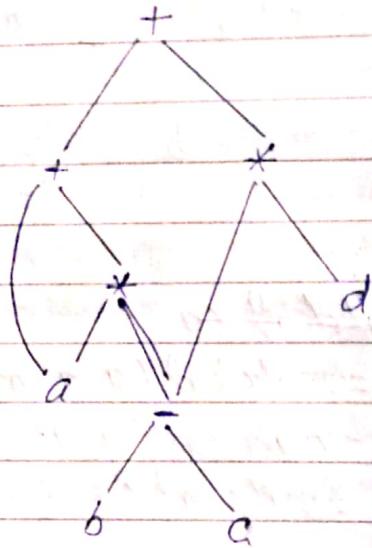
→ A directed acyclic graph (DAG) is an abstract syntax tree with unique node for each value.
 interior node → operator, child → operands
 $a + a * (b - c) + (b - c) * d$

Syntax tree:



DAG

DAG



sequence of instruction for DAG.

- | | |
|---|--|
| 1. $P_1 = \text{makeleaf}(a, a.\text{entry})$; | 6. $P_6 = \text{makennode}('x', P_1, P_5)$; |
| 2. $P_2 = \text{makeleaf}(b, b.\text{entry})$; | 7. $P_7 = \text{makennode}('+', P_3, P_6)$; |
| 3. $P_3 = \text{makeleaf}(c, c.\text{entry})$; | 8. $P_8 = \text{makennode}('x', P_5, P_4)$; |
| 4. $P_4 = \text{makeleaf}(d, d.\text{entry})$; | 9. $P_9 = \text{makennode}('+', P_7, P_8)$; |
| 5. $P_5 = \text{makennode}('-', P_2, P_3)$; | |

The only difference between syntax tree and DAG is that a node representing common sub-expression has more than one parent in the syntax tree.

s-attributed definition / grammar

A syntax directed definition that uses synthesized attributes exclusively is called an s-attributed definition. A parse tree of an s-attributed definition is annotated by evaluating the semantic rules for the attribute at each node in bottom-up manner.

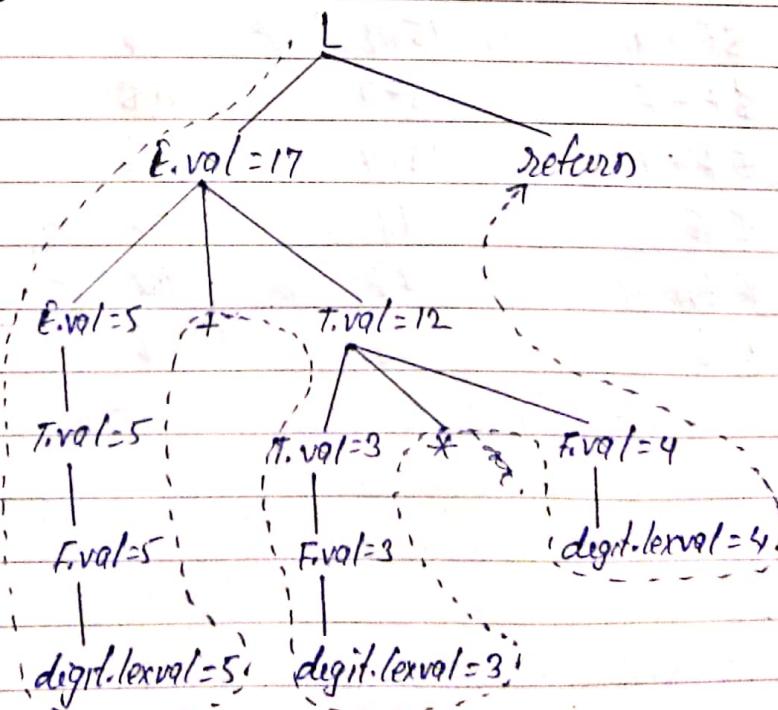
The evaluation of s-attributed definition is based on the depth first traversal of the annotated tree.

e.g.

<u>production</u>	<u>semantic rules</u>
$L \rightarrow E \text{ return}$	$\text{print}(E.\text{val})$
$E \rightarrow E_1 + T$	$E.\text{val} = E_1.\text{val} + T.\text{val}$
$E \rightarrow T$	$E.\text{val} = T.\text{val}$
$T \rightarrow T_1 * F$	$T.\text{val} = T_1.\text{val} * F.\text{val}$
$T \rightarrow F$	$T.\text{val} = F.\text{val}$
$F \rightarrow (E)$	$F.\text{val} = E.\text{val}$
$F \rightarrow \text{digit}$	$F.\text{val} = \text{digit.lexval}$

Q

Input string: $5 + 3 * 4$ return



Bottom-up evaluation of s-attributed defn:

- For bottom-up evaluation of s-attribute definition we use LR parser.
- For bottom-up evaluation of s-attribute definition we put the value of synthesized attribute of the grammar symbol in the stack.

E.g.

For the string $3 \times 5 + 4n$ using above grammar

stack	val	Input	Action
\$	-	$3 \times 5 + 4n \$$	shift
\$3	3	$\times 5 + 4n \$$	Reduce $F \rightarrow \text{digit}$
\$F	3	$\times 5 + 4n \$$	Reduce $T \rightarrow F$
\$T	3	$\times 5 + 4n \$$	shift
\$T*	3	$5 + 4n \$$	shift
\$T*5	385	$+ 4n \$$	Reduce $F \rightarrow \text{digit}$
\$T*F	385	$+ 4n \$$	Reduce $T \rightarrow T * F$
\$T	15	$+ 4n \$$	shift Red. $E \rightarrow T$
\$EF	15	$+ 4n \$$	shift
\$E+	15	$4n \$$	shift
\$E+4	15+4	$n \$$	Reduce $F \rightarrow \text{digit}$
\$E+F	15+4	$n \$$	Reduce $T \rightarrow F$
\$E+T	15+4	$n \$$	Reduce $E \rightarrow E + T$
\$E	19	$n \$$	shift
\$En	19	$\$$	Reduce $E \rightarrow E n$
\$L	19	$\$$	accept

x L-attributed definitions

A syntax-directed definition that uses both synthesized and inherited attribute but each inherited attribute is restricted to inherit from parent or left sibling only, is called L-attr. defn.
mathematically,

A syntax-directed definition is L-attributed if each inherited attribute of x_j on the right side of $A \rightarrow x_1, x_2, \dots, x_n$ depends only on

- the attributes of the symbols x_1, x_2, \dots, x_{j-1}
- the inherited attributes of A.

E.g.

$$A \rightarrow xyz \quad \{x.i = f_1(A.i), y.i = f_2(Y.s), z.i = f_3(Y.i)\} \quad \{y.i = f_4(z.i)\}$$

$$A \rightarrow LM \quad \{L.i = f(A.i), M.i = f(L.s), A.s = f(M.s)\}$$

↳ inherited synthesized not L-attributed

Evaluation of L-attributed definitions:

An inherited attribute can be evaluated in a left to right fashion using a depth first evaluation order.

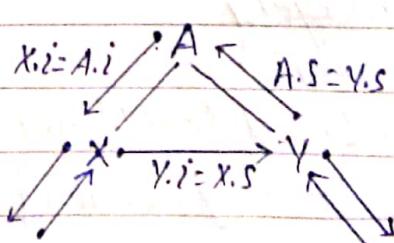
Procedure:

```
dfvisit(n; node); // depth-first evaluation
for each child m of n, from left to right do
    evaluate inherited attributes of m;
    dfvisit(m);
```

Evaluate synthesized attributes of n

E.g.

$$A \rightarrow XY$$



$$X.i = A.i$$

$$Y.i = X.s$$

$$A.s = Y.s$$

Translation scheme.

A translation scheme is a context-free grammar in which:

- attributes are associated with grammar symbols;
- semantic actions are inserted within the right sides of productions and are enclosed between braces {}.

E.g.

production

$$T \rightarrow T_1 * F$$

semantic Rules

$$T.\text{val} = T_1.\text{val} * F.\text{val}$$

The translation scheme is

$$T \rightarrow T_1 * F \quad \{ T.\text{val} = T_1.\text{val} * F.\text{val} \}$$

If both synthesized and inherited attributes are involved:

1. For synthesized attribute, for any production like

$$A \rightarrow x_1 x_2 x_3 \dots x_n$$

the translation actions are written at the right most part of the production.

$$\text{i.e. } A \rightarrow x_1 x_2 x_3 \dots x_n \quad \{ \dots \}$$

2. An inherited attribute, for a symbol in the RHS of a production must be computed in an action before that symbol.

E.g.

translation scheme for the L-attributed defn for "type declaration".

$$D \rightarrow T \quad \{ L.\text{in} = T.\text{type} \} \quad L$$

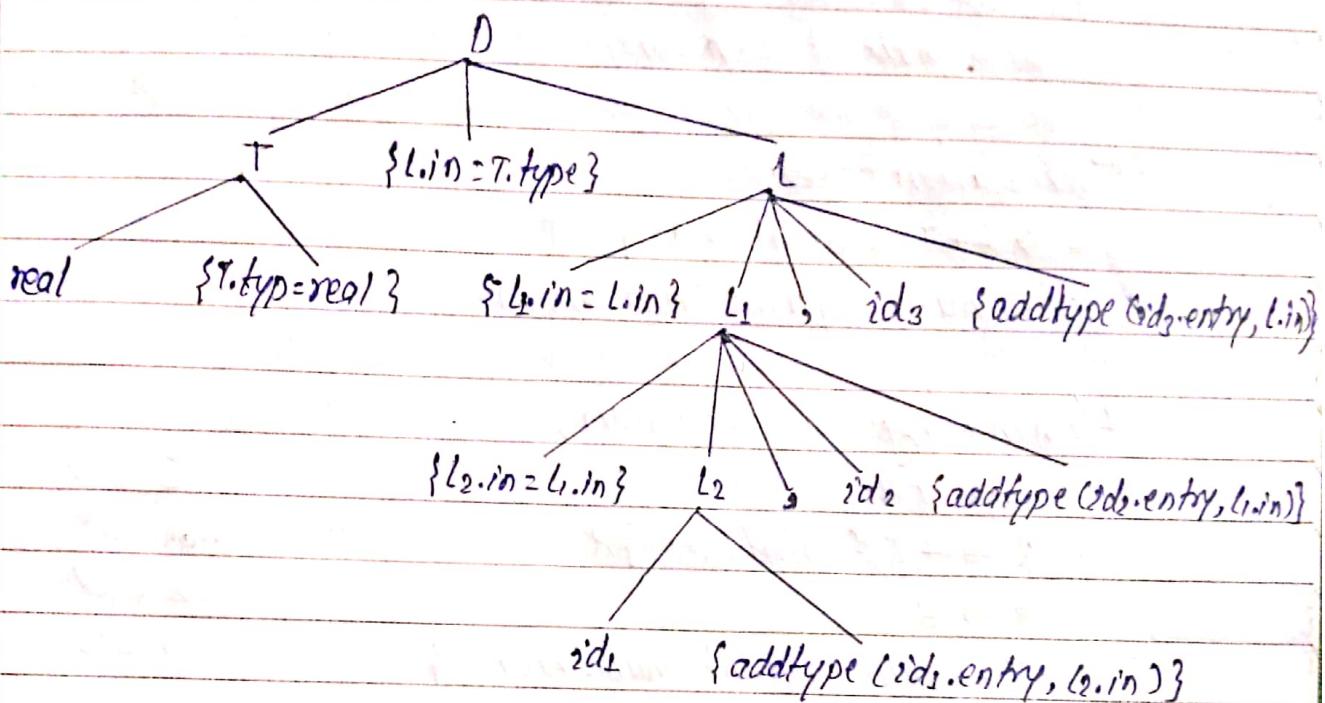
$$T \rightarrow \text{int} \quad \{ T.\text{type} = \text{integer} \}$$

$$T \rightarrow \text{real} \quad \{ T.\text{type} = \text{real} \}$$

$$L \rightarrow \{ L_1.\text{in} = L.\text{in} \} \quad L_1, \text{id} \quad \{ \text{addtype(id.entry, L.in)} \}$$

$$L \rightarrow \text{id} \quad \{ \text{addtype(id.entry, L.in)} \}$$

Parse tree for input : real id₁, id₂, id₃



Translation scheme that converts infix to postfix:

$2 + 3 * 4$

$E \rightarrow E + T \quad \{\text{print('+'});\}$

$E \rightarrow T$

$T \rightarrow T * F \quad \{\text{print('*')};\}$

$T \rightarrow F$

$F \rightarrow \text{num} \quad \{\text{print(num.lexval)};\}$

DFS

1st action $\rightarrow \text{print('2')}$

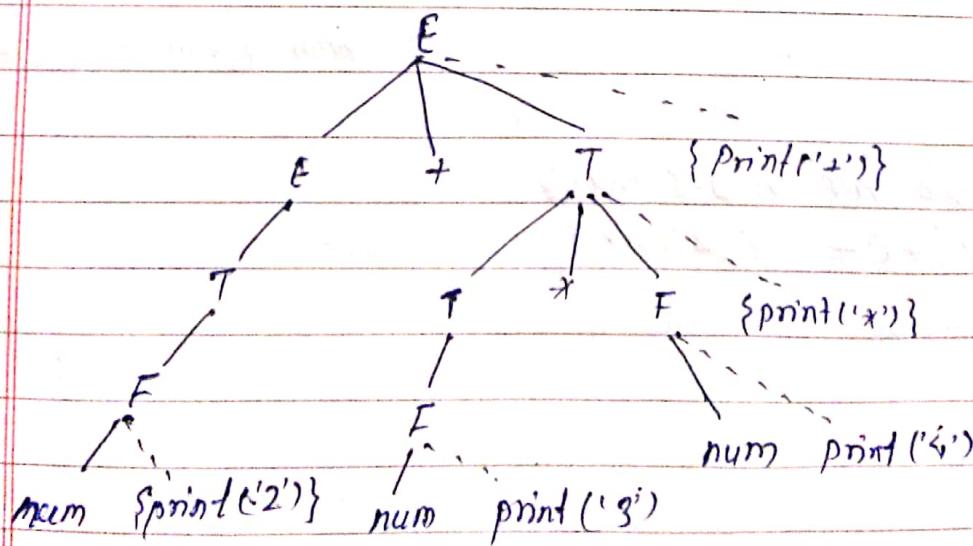
2nd action $\rightarrow \text{print('3')}$

3rd action $\rightarrow \text{print('4')}$

4th action $\rightarrow \text{print('*')}$

5th action $\rightarrow \text{print('+')}$

234*+ (Postfix)



(It only contains)

$$\text{E.g. } a+b+c \Rightarrow ab+c+$$

infix postfix

Translation scheme:

$$\begin{aligned} E &\rightarrow E + T \{ \text{print}(+) ; \} | T \\ T &\rightarrow \text{num} \{ \text{print}(\text{num}. \text{lexval}) : \} \end{aligned}$$

Eliminating left recursion,

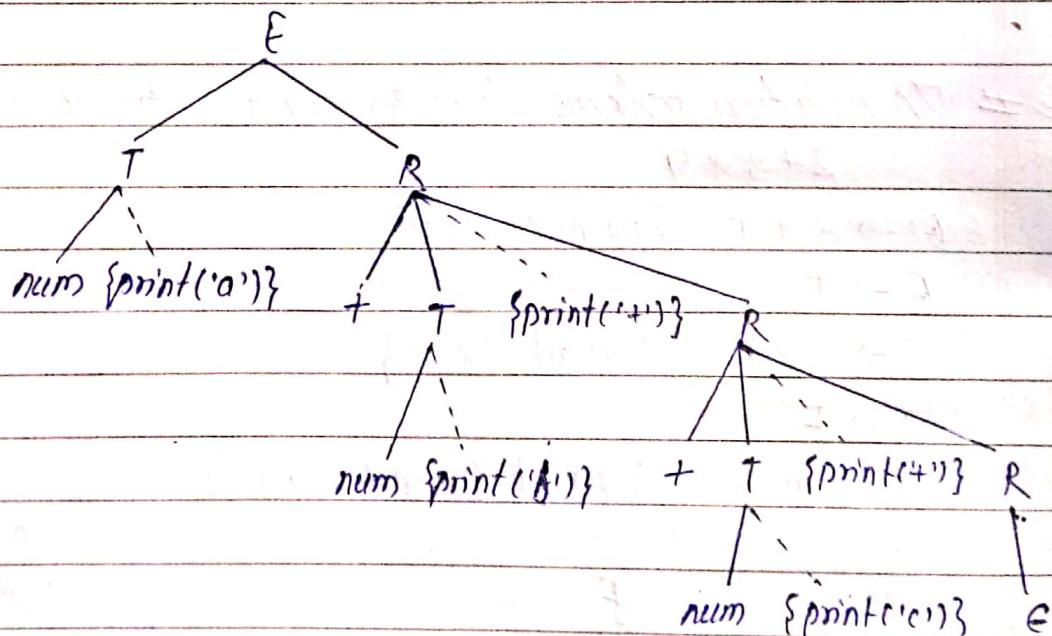
$$E \rightarrow TR$$

$$(E' = R)$$

$$R \rightarrow + T \{ \text{print}(+) \} R$$

$$R \rightarrow E$$

$$T \rightarrow \text{num} \{ \text{print}(\text{num}. \text{lexval}) \}$$



Traverse the tree in DFS order

$a b + c +$ (postfix)

Translation scheme Requirements:

If a translation scheme has to contain both synthesized and inherited attributes, we have to observe the following rules:

1. An inherited attribute of a symbol on the right side of a production must be computed in a semantic action before that symbol.
2. A semantic action must not refer to a synthesized attribute of a symbol to the right of that semantic action.
3. For synthesized attribute of non-terminal on LHS, the translation set actions are written at the right most part of the production.

Top-Down Translation

- L-attributed definitions can be evaluated in a top-down fashion (predictive parsing) with translation scheme.
- The algorithm for elimination of left recursion is extended to evaluate action & attribute.

eliminating left Recursion from a translation scheme

Consider a left recursive translation schema:

$$A \rightarrow A_1 Y \quad \{ A.a = g(A_1.a, Y.y) \}$$

$$A \rightarrow X \quad \{ A.a = f(X.z) \}$$

In this grammar each grammar symbol has synthesized attribute written using their corresponding lowercase letter.

Removing left recursion

$$A \rightarrow X R$$

$$R \rightarrow Y R \mid \epsilon$$

$$\boxed{A \rightarrow AY / X}$$

$$\textcircled{N-R}$$

Now,

Taking semantic action for each symbol as follows,

$$A \rightarrow x \{ R.i = f(x.z) \} R \{ A.a = R.s \}$$

$$R \rightarrow y \{ R_1.i = g(R.i, y.y) \} R_1 \{ R.s = R_1.s \}$$

$$R \rightarrow \epsilon \{ R.s = R.i \}$$

Evaluation of string xyy

$$A.a = g(g(f(x.z), y.y), y.y)$$

$$A.a = g(f(x.z), y.y) = y_2$$

$$A.a = f(x.z)$$

$$A.a = f(x.z)$$

x

These values are
computed according
to a left recursive
grammar.

$$A.a = R.s = g(g(f(x.z), y.y), y.y)$$

$$x.x \rightarrow R.i = f(x.z) \quad R.s = R.s$$

$$y.y \rightarrow R.i = g(f(x.z), y.y)$$

$$y.y \rightarrow R.i = g(g(f(x.z), y.y), y.y) = R.s$$

X By Given grammar

$$E \rightarrow E+E / E*E / (E) / id$$

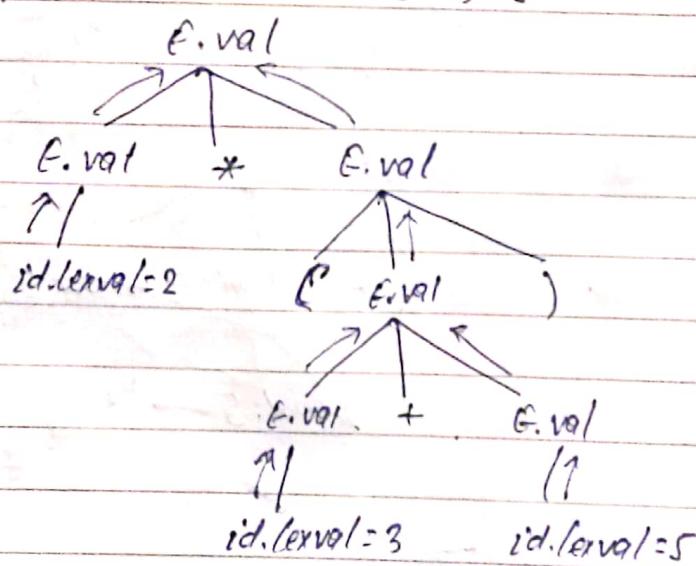
- Annotate the grammar with syntax directed defn using synthesized attributes.
- Remove left recursion from grammar & rewrite the attributes correspondingly.

Solⁿ

first part:

<u>E → E₁ + E₂</u>	<u>E.val = E₁.val + E₂.val</u>
<u>E → E₁ * E₂</u>	<u>E.val = E₁.val * E₂.val</u>
<u>E → (E₁)</u>	<u>E.val = E₁.val</u>
<u>E → id</u>	<u>E.val = id.lexval</u>

Annotated parse tree for $2 * (3+5)$ is



second part:

Removing left recursion as

$$E \rightarrow (E)R / idR$$

$$R \rightarrow +ER_1 / *ER_1 / E$$

Now add the attributes within this non-left recursive grammar as

$$E \rightarrow (E) \{ R.in = E1.val \} \quad R \{ E.val = R.sv \}$$

$$E \rightarrow id \{ R : in = id.lexval \} R \{ E.val = R.s \}$$

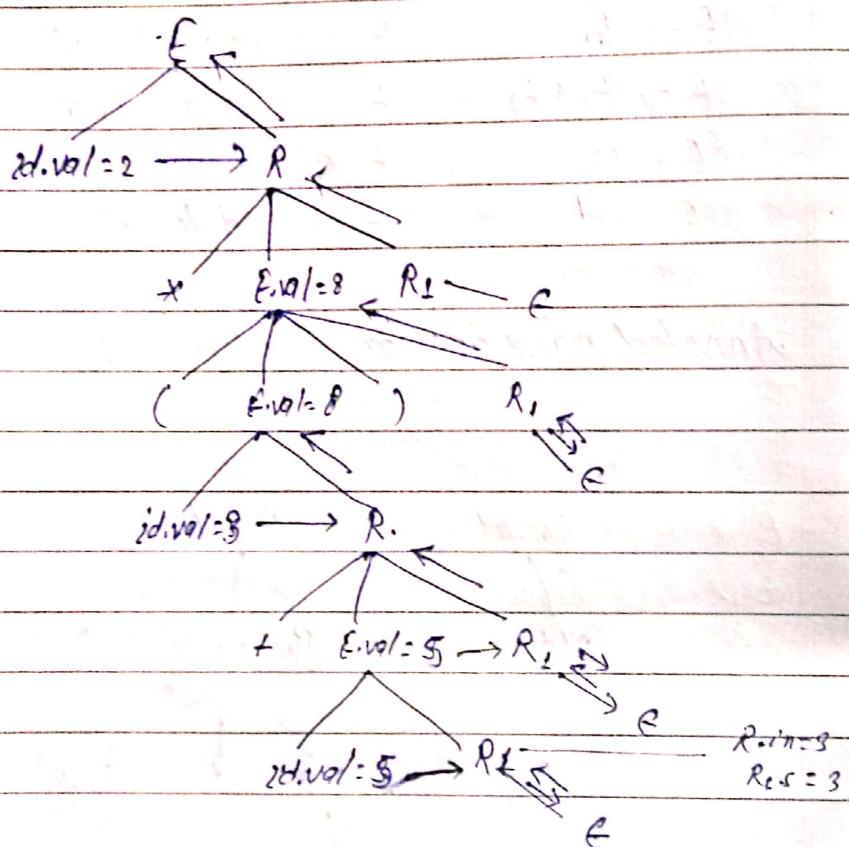
$$R \rightarrow +E \{ R.in = E.vol + R.in \} R_1 \{ R.s = R_1.s \}$$

$$R \rightarrow +E \{ R.i.n = E.vol + R.i.m \} R_1 \{ R.s = R.i.s \}$$

$$S \rightarrow +E \{ S.i.n = E.vol * R.i.m \} R_1 \{ R.s = R.i.s \}$$

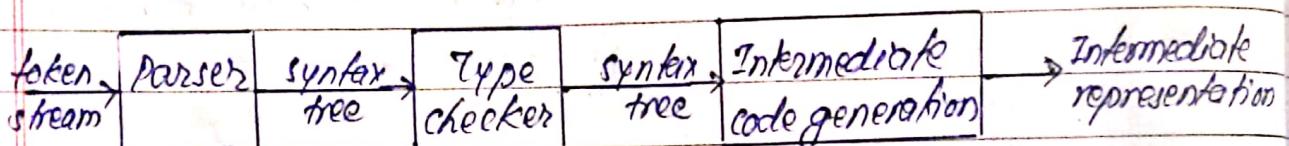
$R \rightarrow \exists E \{ R.i.n = E.val \wedge R.in \} \wedge \{ R.s = R.in \}$

The annotated parse tree for $2 * (8 + 5)$



Type checking

- Type checking is the process of verifying that each operation executed in a program respects the type system of the language.
- This generally means that all operands in any expression are of appropriate types and ~~are~~ number.
- Type checking is carried out in semantic phase.
- Type checking information added with the semantic rules.



e.g.: position of type checker

Two types of type checking

- static type checking
- Dynamic type checking

static type checking - checks at compile time.

static checking refers to the compile-time checking of programs in order to ensure that the semantic conditions of the language are being followed.

static checks include:

1. Type checks:

Report an error if an operator is applied to incompatible operand.

E.g. $2 + 2.5 = \text{Error}$

E.g.

```

int op(int), op(float); //overloading
int f(float);
int a, c[10], d;
d = c+d; //Error : type mismatch
*d = a; //Error : not a pointer type
a = op(d); //OK : overloading
a = f(d); //ok : Coersion of d to float
    
```

a. Flow-of-control ~~check~~ checks:

statements that results in a branch need to be terminated correctly. E.g. Break statement in C

- myfunc (int a)

{

```
cout << a;
```

```
break; //ERROR
```

statements:

}

misplaced break can't be used anywhere except case
 break can't be used in loop, if can be only used in loop

- myfunc()

{ ... }

```
switch(a)
```

```
{ case 0:
```

```
  break; //OK
```

```
case 1:
```

```
  break; //OK
```

```
default:
```

```
}
```

- myfunc (int a)

{

```
while (a)
```

{

```
  if (i>10)
```

```
    break; //OK
```

{

}

3. Uniqueness check:

In some context, an object must be defined exactly once.

E.g.

```
myfunc()  
{
```

```
int i, j, i; // ERROR : 'i' is multiple  
...  
}
```

4. Name-related checks:

~~some fun~~. sometimes the same name may be appeared five or more times.

Dynamic checking

- It is done at run-time.
- Implemented by including type information for each data location at run time.
- Compiler generates some verification code to enforce programming ~~dynamic~~ language's dynamic semantics.

If a programming language has no any dynamic checking, it is called strongly typed language. (i.e. there will be no type errors during run-time).

→ Compiler generates code to do the checks at run-time.

Type system

A type system is a collection of rules for assigning type expression to the part of a program. A type checker implements a type system.

e.g.

if both operands of addition are of type integer, then result is of type integer.

- A sound type system eliminates run time type checking for type errors.

Type Expression

- A basic type is type expression. e.g. integer, real, char etc.
- A type name is type expression. e.g. variable name, function name, constant etc.
 - if x is name of a variable, then x itself is also type expression.
- A type constructor applied to type expression is also type constructor expression. e.g.
 - array : if T is a type expression and I is a range of integers then $\text{array}(I, T)$ is a type expression.
 - record : if T_1, T_2, \dots, T_n are type expressions and f_1, f_2, \dots, f_n are field names, then $\text{record } (f_1, T_1), (f_2, T_2), \dots, (f_n, T_n)$ is a type expression.
 - If T_1 and T_2 are type expressions, then cartesian product $T_1 \times T_2$ is type expression product.
 - pointer : if T is a type expression, then $\text{pointer}(T)$ is a type expression. e.g. $\text{pointer}(\text{int})$

• Functions: mapping a domain type D to a range type R .

E.g. $\text{int} \rightarrow \text{int}$ represents the type of function which takes an int value as parameter and return type is also int.

Specification of a simple type checker

The specification of a type checker is defined by the translation scheme based on the syntax directed definitions associated with the type informations to each symbols.

E.g.

$$P \rightarrow D; E$$

$$D \rightarrow D; D$$

$$D \rightarrow \text{id} : T \quad \{ \text{addtype}(\text{id}.entry, T, \text{id}) \}$$

$$T \rightarrow \text{char} \quad \{ T.type = \text{char} \}$$

$$T \rightarrow \text{int} \quad \{ T.type = \text{int} \}$$

$$T \rightarrow \text{real} \quad \{ T.type = \text{real} \}$$

$$T \rightarrow * T_1 \quad \{ T.type = \text{pointer}(T, T_1) \}$$

$$T \rightarrow \text{array}[\text{intnum}] \text{ of } T_1 \quad \{ T.type = \text{array}(1.. \text{intnum}.val, T_1.val) \}$$

Q. q.

$a : \text{int}; ; b : \text{char};$

Q. Consider the following grammar for arithmetic expression using an operator op^n to integer or real/number.

$$E \rightarrow E_1 \text{ op } E_2 / \text{num}. \text{num} / \text{num} / \text{id}$$

Give syntax directed defⁿ as translation scheme to determine the type expression when two integers are used in exp^n , resulting type is integer otherwise real.

solⁿ

specification of type checker for this problem:

$$\begin{aligned}
 E \rightarrow id & \quad \{ E.type = \text{lookup}(id.entry) \} \\
 E \rightarrow \text{num} & \quad \{ E.type = \text{integer} \} \\
 E \rightarrow \text{num.num} & \quad \{ E.type = \text{real} \} \\
 E \rightarrow E_1 \text{ op } E_2 & \quad \{ E.type = \text{if } (E_1.type = \text{integer} \text{ and } E_2.type = \text{integer}) \\
 & \quad \text{then integer} \\
 & \quad \text{else if } (E_1.type = \text{integer} \text{ and } E_2.type = \text{real}) \\
 & \quad \text{then real} \\
 & \quad \text{else if } (E_1.type = \text{real} \text{ and } E_2.type = \text{integer}) \\
 & \quad \text{then real} \\
 & \quad \text{else if } (E_1.type = \text{real} \text{ and } E_2.type = \text{real}) \\
 & \quad \text{then real} \\
 & \quad \text{else typeerror} \} \\
 & \quad \}
 \end{aligned}$$

Type checking for boolean expr

$$\begin{aligned}
 E \rightarrow \text{true} & \quad \{ E.type = \text{boolean} \} \\
 E \rightarrow \text{false} & \quad \{ E.type = \text{boolean} \} \\
 E \rightarrow \text{literal} & \quad \{ E.type = \text{char} \} \\
 E \rightarrow \text{num} & \quad \{ E.type = \text{integer} \} \\
 E \rightarrow id & \quad \{ E.type = \text{lookup}(id.entry) \} \\
 E \rightarrow E_1 \text{ and } E_2 & \quad \{ E.type = \text{if } (E_1.type = \text{boolean} \text{ and } E_2.type = \text{boolean}) \\
 & \quad \text{then boolean else typeerror} \} \\
 E \rightarrow E_1 \text{ or } E_2 & \quad \{ E.type = \text{if } (E_1.type = \text{boolean} \text{ and } E_2.type = \text{boolean}) \\
 & \quad \text{then boolean else type-error} \} \\
 E \rightarrow E_1 + E_2 & \quad \{ E.type = \text{if } (E_1.type = \text{integer} \text{ and } E_2.type = \text{integer}) \text{ then} \\
 & \quad \text{integer} \\
 & \quad \text{else if } (E_1.type = \text{char} \text{ and } E_2.type = \text{integer}) \text{ then} \\
 & \quad \text{integer}
 \}
 \end{aligned}$$

```

        else if (E1.type = integer and E2.type = char) then
            integer
        else if (E1.type = char and E2.type = char) then
            integer
        else type-error;
    }
}

```

Type checking of expression:

#	E → literal	{ E.type = char }
	E → num	{ E.type = integer }
	E → id	{ E.type = lookup(id.entry) }
	E → E ₁ mod E ₂	{ E.type = if (E ₁ .type = integer and E ₂ .type = integer) then integer else type-error; }
	E → E ₁ [E ₂]	{ E.type = if (E ₂ .type = integer and E ₁ .type = array(s, t)) then t else type-error; }
(E → x E ₁)	E → E ₁ ↑	{ E.type = if (E ₁ .type = pointer(t)) then t else type-error; }

Type checking of statements

Assignment statement:

S → id = E { S.type = if (id.type = E.type) then void
else type-error; }

If then else statement:

S → if E then S₁ { S₁.type = if (E.type = boolean) then S₁.type
else type-error; }

While statement:

S → while E do S₁ { S₁.type = if (E.type = boolean) then S₁.type
else type-error; }

$\# S \rightarrow S_1; S_2 \quad \{ S.type = i \& (S_1.type = void \text{ and } S_2.type = void) \text{ then}$
 $\text{void} \text{ else type-error(); } \}$

Type checking of functions

$E \rightarrow E_1(E_2) \quad \{ E.type = i \& (E_2.type = s \text{ and } E_1.type = s \rightarrow t) \text{ then } t$
 $\text{else type-error(); } \}$

$T \rightarrow T_1 \rightarrow T_2 \quad \{ T.type = E_1.type \rightarrow T_2.type \}$

→ Function whose domains are functions from two characters and whose range is a pointer of integer

$T \rightarrow \text{int} \quad \{ T.type = \text{int} \}$

$T \rightarrow \text{char} \quad \{ T.type = \text{char} \}$

$T \rightarrow \text{pointer}[T_1] \quad \{ T.type = \text{pointer}(T_1.type) \}$

$E \rightarrow E_1[E_2] \quad \{ E.type = i \& (E_2.type = (\text{char}, \text{char}) \text{ and } E_1.type =$
 $(\text{char}, \text{char}) \rightarrow \text{pointer}(\text{int})) \text{ then } E_1.type \text{ else}$
 $\text{type-error(); } \}$

Type conversion and coercion

- Type conversion is explicit.

$$C = a + \text{int}(b)$$

- 1) Convert b into int
- 2) sum
- 3) assign

- Type conversion which happen implicitly is called coercion.
Compiler converts one type to another type automatically.

$\text{int } \text{int } \text{float}$
 $c = a + b;$

- 1) Conversion of 'a' from int to float
- 2) sum $a+b$ both in float, result = float
- 3) convert result into int from float
- 4) assign result to c.

Equivalence of Type Expression.

Two expressions are structurally equivalent if they are two expressions of same basic types and are formed by applying same constructor.

structural equivalence algorithm:

boolean sequival (s, t)
{

if s and t are same basic types

return true;

else if s=array (s₁, s₂) and t=array (t₁, t₂) then

return sequival (s₁, t₁) and sequival (s₂, t₂)

else if s=s₁ × s₂ and t=t₁ × t₂ then

return sequival (s₁, t₁) and sequival (s₂, t₂)

else if s=pointer (s₁) and t=pointer (t₁) then

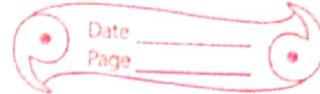
return sequival (s₁, t₁)

else if s=s₁ → s₂ and t=t₁ → t₂ then

return sequival (s₁, t₁) and sequival (s₂, t₂)

else return false

}



E.g.

`int a, b;`

Here a and b are structurally equivalent.

Q: Write the type expressions for the following types:

q. An array of pointers to real's, where the array index range from 1 to 100.

Sol

$T \rightarrow \text{real}$ { $T.\text{type} = \text{real}$ }

$E \rightarrow E_1[E_2]$ ~~{ $E.\text{type} \neq \text{int}$ ($E_1.\text{type} = \text{int}$) }~~

$E \rightarrow \text{array}[400, T]$ & $\text{if } T.\text{type} = \text{real} \text{ then}$

$T \rightarrow \text{real}$ { $T.\text{type} = \text{real}$ }

$E \rightarrow E_1[E_2]$ { $\text{if } (E_2.\text{type} = \text{int} \text{ and } E_1.\text{type} = \text{array}(1, 2, \dots, 100, E.\text{type})) \text{ then } E.\text{type} = \text{real} \text{ else } E.\text{type} = \text{type-error}();$ }

$E \rightarrow *E_1$ { $\text{if } (E_1.\text{type} = \text{pointer}(T.\text{type})) \text{ then } E.\text{type} = T.\text{type} \text{ else } E.\text{type} = \text{type-error}();$ }