



CHAPTER 3: PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

1-Mark Questions

Question 1: Write the general form of a pair of linear equations in two variables.

Question 2: How many solutions can a pair of linear equations have?

Question 3: What is meant by a consistent pair of linear equations?

Question 4: If two lines intersect at one point, how many solutions are possible?

Question 5: If two lines are parallel, how many solutions are possible?

2-Mark Questions

Question 6: Write the condition for a pair of linear equations to have

- (a) unique solution
- (b) no solution

Question 7: Check whether the pair of equations

$$2x + 3y = 11$$

$$4x + 6y = 22$$

has infinitely many solutions or not.

Question 8: Find the value of k for which the system

$$kx + y = 4$$

$$6x + 2y = 8$$

has infinitely many solutions.

Question 9: Write the condition for a pair of linear equations to be inconsistent.

Question 10: What is the graphical representation of two coincident lines?

Question 11: Solve using **substitution method**

$$x + y = 7$$

$$x - y = 1$$

Question 12: Solve using **elimination method**

$$2x + 3y = 13$$

$$x + y = 5$$

Question 13: Solve using **substitution method**

$$2x - y = 4$$

$$x + y = 5$$

Question 14: Find k for which the pair has **no solution**

$$kx + 2y = 5$$

$$3x + ky = 10$$

Question 15: Solve **graphically**

$$x + y = 6$$

$$x - y = 2$$

Question 16: Solve by elimination method

$$3x - 2y = 5$$

$$2x + y = 4$$

Question 17: Solve by substitution method

$$x = y + 3$$

$$2x + y = 11$$

Question 18: Solve by elimination method

$$5x - y = 9$$

$$3x + 2y = 7$$

Question 19: Solve

$$4x - 3y = -5$$

$$2x + y = 7$$

Question 20: Solve

$$x + 2y = 10$$

$$2x - y = 1$$

PYQ / CASE-BASED / HIGH WEIGHTAGE

Question 21: The sum of two numbers is 27 and their difference is 3. Find the numbers.

Question 22: The larger of two numbers is 5 more than the smaller. Their sum is 25. Find the numbers.

Question 23: Solve

$$2x + 5y = 14$$

$$4x + 10y = 28$$

Question 24: Solve

$$3x + y = 8$$

$$6x + 2y = 16$$

Question 25: Find k for which the pair has **no solution**

$$kx + y = 2$$

$$3x + 3y = 6$$

Question 26: Solve by elimination

$$7x - 3y = 5$$

$$3x + y = 11$$

Question 27: Solve by substitution

$$x - 2y = 4$$

$$2x + y = 1$$

Question 28: Solve graphically

$$2x + y = 6$$

$$x - y = 1$$

Question 29: Solve

$$3x + 4y = 10$$

$$2x - y = 1$$

Question 30: Solve

$$x + y = 8$$

$$2x - y = 1$$

Question 31: The sum of two numbers is 20 and their difference is 4. Find the numbers.

Question 32: Two numbers differ by 6 and their sum is 24. Find the numbers.

Question 33: Find the value of k for which the pair of equations has **infinitely many solutions**

$$kx + 4y = 8$$

$$2x + ky = 4$$

Question 34: Find the value of k for which the pair of equations has **no solution**

$$kx + y = 5$$

$$3x + 3y = 9$$

Question 35

(A) If α, β are the zeroes of the polynomial

$3x^2 - 5x + 2$, find the value of $\alpha^2 + \beta^2$. (3)

OR

(B) Find a quadratic polynomial whose sum of zeroes is 6 and product is 8. Also find its zeroes. (3)

Question 36

(A) If α, β are the zeroes of $4x^2 + 7x - 5$, find $\alpha^2 + \beta^2$. (3)

OR

(B) Find a quadratic polynomial whose sum of zeroes is -1 and product is -12 . Also find its zeroes. (3)

Question 37

(A) If α, β are the zeroes of $2x^2 - 9x + 4$, find the value of $(\alpha + \beta)^2 - 2\alpha\beta$. (3)

OR

(B) Find a quadratic polynomial whose zeroes are 3 and -5 . (3)

Question 38

(A) If α, β are the zeroes of $5x^2 - 3x - 1$, find $\alpha^2 + \beta^2$. (3)

OR

(B) Find a quadratic polynomial whose sum of zeroes is 2 and product is -15 . Also find its zeroes. (3)

Question 39

(A) If α, β are the zeroes of $x^2 - 6x + 1$, find the value of $1/\alpha + 1/\beta$. (3)

(B) Find a quadratic polynomial whose zeroes are -2 and 7 . (3)

Question 40

(A) If α, β are the zeroes of
 $2x^2 - 5x - 7$, find $(\alpha - \beta)^2$. (3)

OR

(B) Find a quadratic polynomial whose zeroes are $1/2$ and 3 . (3)

Question 41

(A) If α, β are the zeroes of
 $5x^2 + x - 6$, find $1/\alpha^2 + 1/\beta^2$. (3)

OR

(B) Find a quadratic polynomial whose sum of zeroes is 1 and product is -6 .
Also find its zeroes. (3)

HINTS/SOLUTIONS

Solution 1:

A pair of linear equations in two variables is written as:

$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

where a_1, b_1, a_2, b_2 are not zero simultaneously.

Solution 2:

A pair of linear equations can have **three types of solutions**:

1. **One solution** (unique solution)
2. **Infinitely many solutions**
3. **No solution**

Solution 3:

A pair of linear equations is called **consistent** if it has

- **one solution** or
- **infinitely many solutions**

That is, at least one solution exists.

Solution 4:

If two lines intersect at **one point**, then the pair of linear equations has **only one solution**.

Solution 5:

If two lines are **parallel**, they never intersect.
So, the pair of linear equations has **no solution**.

Solution 6:

Consider the pair of linear equations:

$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

(a) Condition for unique solution:

$$a_1 \div a_2 \neq b_1 \div b_2$$

(Is case me lines intersect karti hain)

(b) Condition for no solution:

$$a_1 \div a_2 = b_1 \div b_2 \neq c_1 \div c_2$$

(Is case me lines parallel hoti hain)

Solution 7:

Given equations:

$$2x + 3y - 11 = 0$$

$$4x + 6y - 22 = 0$$

Q8 (Infinitely many solutions)

Given:

$$kx + y = 4$$

$$6x + 2y = 8$$

Standard form:

$$kx + y - 4 = 0$$

$$6x + 2y - 8 = 0$$

Condition:

$$a_1 / a_2 = b_1 / b_2 = c_1 / c_2$$

$$\begin{aligned} \frac{k}{6} &= \frac{1}{2} = \frac{-4}{-8} \\ \frac{k}{6} &= \frac{1}{2} \\ k &= 3 \end{aligned}$$

 **Answer:** $k = 3$

Q9 (Inconsistent condition)

Pair of linear equations is **inconsistent** if:

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

)Parallel lines, no solution)

Q10 (Coincident lines)

Two coincident lines overlap completely and have **infinitely many solutions**.

Q11 (Substitution method)

$$x + y = 7$$

$$x - y = 1$$

From first equation:

$$y = 7 - x$$

Substitute in second:

$$x - (7 - x) = 1$$

$$2x = 8$$

$$x = 4$$

$$y = 3$$

 **Answer:** (4, 3)

Q12 (Elimination method)

$$2x + 3y = 13$$

$$x + y = 5$$

Multiply second by 2:

$$2x + 2y = 10$$

Subtract:

$$y = 3$$

$$x = 2$$

 **Answer:** (2, 3)

Q13 (Substitution method)

$$\begin{aligned}2x - y &= 4 \\x + y &= 5\end{aligned}$$

$$\begin{aligned}y &= 5 - x \\2x - (5 - x) &= 4 \\x = 3, y &= 2\end{aligned}$$

 **Answer:** (3, 2)

Q14 (No solution)

$$kx + 2y = 5$$

$$3x + ky = 10$$

Condition for no solution:

$$\begin{aligned}\frac{k}{3} &= \frac{2}{k} \neq \frac{5}{10} \\k^2 &= 6 \\k &= \sqrt{6}, -\sqrt{6}\end{aligned}$$

 **Answer:** $k = \pm\sqrt{6}$

Q15 (Graphical)

$$x + y = 6$$

$$x - y = 2$$

Intersection point:

$$x = 4, y = 2$$

Solution 16

Given:

$$3x - 2y = 5 \dots\dots(1)$$

$$2x + y = 4 \dots\dots(2)$$

Multiply equation (2) by 2:

$$4x + 2y = 8 \dots\dots(3)$$

Add (1) and (3):

$$7x = 13$$

$$x = \frac{13}{7}$$

Put value of x in (2):

$$2\left(\frac{13}{7}\right) + y = 4$$

$$y = \frac{2}{7}$$

Answer:

$$x = \frac{13}{7}, y = \frac{2}{7}$$

Solution 17

Given:

$$x = y + 3 \dots\dots(1)$$

$$2x + y = 11 \dots\dots(2)$$

Put value of x from (1) into (2):

$$2(y+3)+y=11$$

$$\begin{aligned}3y &= 5 \\y &= \frac{5}{3}\end{aligned}$$

Now,

$$x = y + 3 = \frac{5}{3} + \frac{9}{3} = \frac{14}{3}$$

Answer:

$$x = \frac{14}{3}, y = \frac{5}{3}$$

Solution 18

(Elimination Method)

Given:

$$5x - y = 9 \dots\dots(1)$$

$$3x + 2y = 7 \dots\dots(2)$$

Multiply (1) by 2:

$$10x - 2y = 18 \dots\dots(3)$$

Add (2) and (3):

$$13x = 25$$

$$x = \frac{25}{13}$$

Put x in (1):

$$5\left(\frac{25}{13}\right) - y = 9$$

y=138

Answer:

$$x = \frac{25}{13}, y = \frac{8}{13}$$

Solution 19

Given:

$$4x - 3y = -5 \dots\dots(1)$$

$$2x + y = 7 \dots\dots(2)$$

Multiply (2) by 3:

$$6x + 3y = 21 \dots\dots(3)$$

Add (1) and (3):

$$10x = 16$$

$$x = \frac{8}{5}$$

Put x in (2):

$$2\left(\frac{8}{5}\right) + y = 7$$

$$y = \frac{19}{5}$$

Answer:

$$x = \frac{8}{5}, y = \frac{19}{5}$$

Solution 20

Given:

$$x + 2y = 10 \dots\dots(1)$$

$$2x - y = 1 \dots\dots(2)$$

Multiply (2) by 2:

$$4x - 2y = 2 \dots\dots(3)$$

Add (1) and (3):

$$5x = 12$$

$$x = \frac{12}{5}$$

Put x in (1):

$$\frac{12}{5} + 2y = 10$$

$$y = \frac{19}{5}$$

Answer:

$$x = \frac{12}{5}, y = \frac{19}{5}$$

Solution 21 (PYQ)

Let numbers be x and y

$$x + y = 27 \dots\dots(1)$$

$$x - y = 3 \dots\dots(2)$$

Add (1) and (2):

$$2x = 30$$

$$\begin{aligned}x &= 15 \\y &= 12\end{aligned}$$

Solution 22 (PYQ)

Let smaller number = x

Larger number = $x + 5$

$$x + (x + 5) = 25$$

$$\begin{aligned}2x &= 20 \\x &= 10\end{aligned}$$

Larger number = 15

Answer:

Numbers are **10 and 15**

Solution 23 (PYQ)

Given:

$$2x + 5y = 14 \dots\dots(1)$$

$$4x + 10y = 28 \dots\dots(2)$$

Multiply (1) by 2:

$$4x + 10y = 28$$

This is same as equation (2)

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

Infinite solutions

Solution 24

Given:

$$3x + y = 8 \dots\dots(1)$$

$$6x + 2y = 16 \dots\dots(2)$$

Multiply (1) by 2:

$$6x + 2y = 16$$

Equation (2) and new equation are same

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

Answer:

Pair has **infinitely many solutions**

Solution 25

Given:

$$kx + y = 2 \dots\dots(1)$$

$$3x + 3y = 6 \dots\dots(2)$$

Rewrite (2):

$$x + y = 2 \dots\dots(3)$$

For **no solution**:

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

From (1) and (3):

$$\frac{k}{1} = \frac{1}{1} \Rightarrow k = 1$$

But

$$\frac{2}{2} = 1$$

So equations become coincident

👉 To make **no solution**, coefficients same but constants different

Hence **no value of k**

Answer:

✗ **No such value of k**

Solution 26

(Elimination Method)

Given:

$$7x - 3y = 5 \dots\dots(1)$$

$$3x + y = 11 \dots\dots(2)$$

Multiply (2) by 3:

$$9x + 3y = 33 \dots\dots(3)$$

Add (1) and (3):

$$16x = 38$$

$$x = \frac{19}{8}$$

Put x in (2):

$$3\left(\frac{19}{8}\right) + y = 11$$

$$y = \frac{31}{8}$$

Answer:

$$x = \frac{19}{8}, y = \frac{31}{8}$$

Solution 27

(Substitution Method)

Given:

$$x - 2y = 4 \dots\dots(1)$$

$$2x + y = 1 \dots\dots(2)$$

From (1):

$$x = 4 + 2y$$

Put in (2):

$$2(4 + 2y) + y = 1$$

$$5y = -7 \Rightarrow y = -\frac{7}{5}$$

$$x = \frac{6}{5}$$

Answer:

$$x = \frac{6}{5}, y = -\frac{7}{5}$$

Solution 28

(Graphical Method)

Equations:

$$2x + y = 6$$

$$x - y = 1$$

Convert to y form:

$$y = 6 - 2x$$

$$y = x - 1$$

Intersection point:

$$x = \frac{7}{3}, y = \frac{4}{3}$$

Answer:

$$\text{Solution} = \left(\frac{7}{3}, \frac{4}{3} \right)$$

Solution 29

Given:

$$3x + 4y = 10 \dots\dots (1)$$

$$2x - y = 1 \dots\dots (2)$$

Multiply (2) by 4:

$$8x - 4y = 4 \dots\dots (3)$$

Add (1) and (3):

$$11x = 14$$

$$x = \frac{14}{11}$$

Solution 30

Given:

$$x + y = 8 \dots\dots(1)$$

$$2x - y = 1 \dots\dots(2)$$

Add (1) and (2):

$$3x = 9$$

$$x = 3$$

$$y = 5$$

Answer:

$$x = 3, y = 5$$

Solution 31

Let the two numbers be **x** and **y**

Given:

$$x + y = 20 \dots\dots(1)$$

$$x - y = 4 \dots\dots(2)$$

Add (1) and (2):

$$2x = 24$$

$$x=12$$

Put **x** = 12 in (1):

$$12 + y = 20 \Rightarrow y = 8$$

Answer:

Numbers are **12 and 8**

Solution 32

Let the two numbers be x and y

Given:

$$x - y = 6 \dots\dots(1)$$

$$x + y = 24 \dots\dots(2)$$

Add (1) and (2):

$$2x = 30$$

$$x = 15$$

Put $x = 15$ in (2):

$$15 + y = 24 \Rightarrow y = 9$$

Answer:

Numbers are 15 and 9

Solution 33

Given equations:

$$kx + 4y = 8 \dots\dots(1)$$

$$2x + ky = 4 \dots\dots(2)$$

For infinitely many solutions:

$$\begin{aligned}\frac{a_1}{a_2} &= \frac{b_1}{b_2} = \frac{c_1}{c_2} \\ \frac{k}{2} &= \frac{4}{k} = \frac{8}{4} \\ \frac{8}{4} &= 2\end{aligned}$$

So,

$$2k=2 \Rightarrow k=4$$

Check:

$$\frac{4}{2} = \frac{4}{4} = 2$$

✓ condition satisfied

Answer:

$$k = 4$$

Solution 34

Given equations:

$$kx + y = 5 \dots\dots(1)$$

$$3x + 3y = 9 \dots\dots(2)$$

Rewrite (2):

$$x + y = 3 \dots\dots(3)$$

For no solution:

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

From (1) and (3):

$$\frac{k}{1} = \frac{1}{1} \Rightarrow k = 1$$

But,

$$\frac{5}{3} \neq 1$$

✓ condition satisfied

Answer:

$$k = 1$$

Solution 35 (A)

Given polynomial:

$$3x^2 - 5x + 2$$

If α, β are zeroes, then

$\alpha + \beta = \text{coefficient of } x \text{ (with sign changed) upon coefficient of } x^2$

$$\alpha + \beta = \frac{5}{3}$$

$\alpha\beta = \text{constant term upon coefficient of } x^2$

$$\alpha\beta = \frac{2}{3}$$

We know,

$$\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$$

Substitute values:

$$\begin{aligned}\alpha^2 + \beta^2 &= \left(\frac{5}{3}\right)^2 - 2\left(\frac{2}{3}\right) \\ &= \frac{25}{9} - \frac{4}{3} \\ &= \frac{25}{9} - \frac{12}{9} \\ &= \frac{13}{9}\end{aligned}$$

Answer:

$$\alpha^2 + \beta^2 = \frac{13}{9}$$

Solution 35 (B)

Given:

$$\text{Sum of zeroes} = 6$$

$$\text{Product of zeroes} = 8$$

Let the zeroes be α and β .

Standard quadratic polynomial:

$$x^2 - (\text{sum})x + (\text{product})$$

So required polynomial is:

$$x^2 - 6x + 8$$

Now find its zeroes:

$$x^2 - 6x + 8 = 0$$

Factorization:

$$(x - 2)(x - 4) = 0$$
$$x = 2, 4$$

Answer:

Quadratic polynomial: $x^2 - 6x + 8$

Zeroes are **2 and 4**

Question 36 (A)

Given polynomial:

$$4x^2 + 7x - 5$$

$$\alpha + \beta = -7 \text{ upon } 4$$

$$\alpha\beta = -5 \text{ upon } 4$$

Formula:

$$\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$$

$$\begin{aligned} &= \left(\frac{-7}{4}\right)^2 - 2\left(\frac{-5}{4}\right) \\ &= \frac{49}{16} + \frac{10}{4} \\ &= \frac{49}{16} + \frac{40}{16} \\ &= \frac{89}{16} \end{aligned}$$

Answer: 89 upon 16

Question 36 (B)

Sum of zeroes = -1

Product of zeroes = -12

Quadratic polynomial:

$$\begin{array}{c} x^2 - (\text{sum})x + (\text{product}) \\ x^2 + x - 12 \end{array}$$

Factorization:

$$(x + 4)(x - 3) = 0$$

Zeroes: -4 and 3

Question 37 (A)

Given polynomial:

$$2x^2 - 9x + 4$$

$$\alpha + \beta = 9 \text{ upon } 2$$

$$\alpha\beta = 2$$

Expression given:

$$(\alpha + \beta)^2 - 2\alpha\beta$$

$$\begin{aligned} &= \left(\frac{9}{2}\right)^2 - 2(2) \\ &= \frac{81}{4} - 4 \\ &= \frac{81 - 16}{4} \\ &= \frac{65}{4} \end{aligned}$$

Answer: 65 upon 4

Question 37 (B)

Zeroes are: 3 and -5

Sum = -2

Product = -15

Quadratic polynomial:

$$\begin{aligned} &x^2 - (-2)x + (-15) \\ &x^2 + 2x - 15 \end{aligned}$$

Question 38 (A)

Given polynomial:

$$5x^2 - 3x - 1$$

$$\alpha + \beta = 3 \text{ upon } 5$$

$$\alpha\beta = -1 \text{ upon } 5$$

Formula:

$$\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$$

$$\begin{aligned} &= \left(\frac{3}{5}\right)^2 - 2\left(\frac{-1}{5}\right) \\ &= \frac{9}{25} + \frac{2}{5} \\ &= \frac{9}{25} + \frac{10}{25} \\ &= \frac{19}{25} \end{aligned}$$

Answer: 19 upon 25

Question 38 (B)

Sum of zeroes = 2

Product = -15

Quadratic polynomial:

$$x^2 - 2x - 15$$

Factorization:

$$(x - 5)(x + 3) = 0$$

Zeroes: 5 and -3

Question 39 (A)

Given polynomial:

$$x^2 - 6x + 1$$

$$\alpha + \beta = 6$$

$$\alpha\beta = 1$$

Formula:

$$\begin{aligned}\frac{1}{\alpha} + \frac{1}{\beta} &= \frac{\alpha + \beta}{\alpha\beta} \\ &= \frac{6}{1} \\ &= 6\end{aligned}$$

Answer: 6

Question 39 (B)

Zeroes: -2 and 7

$$\text{Sum} = -2 + 7 = 5$$

$$\text{Product} = -14$$

Quadratic polynomial:

$$\begin{aligned}x^2 - (\text{sum})x + (\text{product}) \\ x^2 - 5x - 14\end{aligned}$$

Answer: $x^2 - 5x - 14$

Question 40 (A)

Given polynomial:

$$2x^2 - 5x - 7$$

$$\alpha + \beta = 5 \text{ upon } 2$$

$$\alpha\beta = -7 \text{ upon } 2$$

Formula:

$$\begin{aligned}(\alpha - \beta)^2 &= (\alpha + \beta)^2 - 4\alpha\beta \\&= \left(\frac{5}{2}\right)^2 - 4\left(\frac{-7}{2}\right) \\&= \frac{25}{4} + 14 \\&= \frac{25}{4} + \frac{56}{4} \quad = \frac{81}{4}\end{aligned}$$

Question 40 (B)

Zeroes: 1 upon 2 and 3

$$\text{Sum} = 1 \text{ upon } 2 + 3 = 7 \text{ upon } 2$$

$$\text{Product} = 3 \text{ upon } 2$$

Quadratic polynomial:

$$x^2 - \frac{7}{2}x + \frac{3}{2}$$

Multiply by 2 to remove fraction:

$$2x^2 - 7x + 3$$

$$\text{Answer: } 2x^2 - 7x + 3$$

Question 41(A)

Given polynomial:

$$5x^2 + x - 6$$

$$\alpha + \beta = -1 \text{ upon } 5$$

$$\alpha\beta = -6 \text{ upon } 5$$

Formula:

$$\frac{1}{\alpha^2} + \frac{1}{\beta^2} = \frac{(\alpha + \beta)^2 - 2\alpha\beta}{(\alpha\beta)^2}$$

$$= \frac{\left(\frac{-1}{5}\right)^2 - 2\left(\frac{-6}{5}\right)}{\left(\frac{-6}{5}\right)^2}$$

$$= \frac{\frac{1}{25} + \frac{12}{5}}{\frac{36}{25}}$$

$$= \frac{\frac{61}{25}}{\frac{36}{25}}$$

$$= \frac{61}{36}$$