1-1.8-3

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EE24BTECH11005 - Arjun Pavanje

Question:

Find the lengths of the medians of the triangle with vertices ${\bf A}(0,0,6), {\bf B}(0,4,0), {\bf C}(6,0,0)$

Solution:

Variable	Description
A	(0,0,6) point
В	(0,4,0) point
С	(6,0,0) point
D	Midpoint of BC
E	Midpoint of CA
F	Midpoint of AB

TABLE I: Variables Used

1)

$$D = \frac{B+C}{2} = \begin{pmatrix} 3\\2\\0 \end{pmatrix} \tag{1}$$

$$\left\| \frac{B+C}{2} - A \right\| = \sqrt{\left(\frac{B+C}{2} - A \right)^T \left(\frac{B+C}{2} - A \right)} = \sqrt{49}$$
 (2)

Length of median AD = 7 units

2)

$$E = \frac{C+A}{2} = \begin{pmatrix} 3\\0\\3 \end{pmatrix} \tag{3}$$

$$\left\| \frac{C+A}{2} - B \right\| = \sqrt{\left(\frac{C+A}{2} - B\right)^T \left(\frac{C+A}{2} - B\right)} = \sqrt{34}$$
 (4)

Length of median $BE = \sqrt{34}$ units

$$F = \frac{A+B}{2} = \begin{pmatrix} 0\\2\\3 \end{pmatrix} \tag{5}$$

$$\left\| \frac{A+B}{2} - C \right\| = \sqrt{\left(\frac{A+B}{2} - C \right)^T \left(\frac{A+B}{2} - C \right)} = \sqrt{49}$$
 (6)

Length of median CF = 7 units

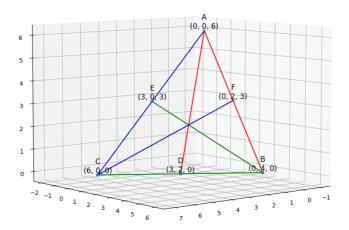


Fig. 1: Plot of Triangle ABC, medians