EE24BTECH11005 - Arjun Pavanje

Question:

The coordinates of the point \mathbf{P} dividing the line segment joining the points $\mathbf{A}(1,3)$ and $\mathbf{B}(4,6)$ in the ratio 2:1 are (10, 2012)

Solution: If P divides AB in the ratio k:1,

Variable	Description
P	Point to be found
A	(1, 3) point
В	(4, 6) point
k	ratio in which P divides AB

TABLE I: Variables Used

$$\mathbf{P} = \frac{k\mathbf{B} + \mathbf{A}}{k+1} \tag{1}$$

From equation 1 we have

$$P = \frac{k\binom{4}{6} + \binom{1}{3}}{k+1} \tag{2}$$

$$=\frac{\binom{4k+1}{6k+3}}{k+1}\tag{3}$$

here, k = 2, so putting the k value into 3 we get

$$P = \frac{\binom{9}{15}}{3} \tag{4}$$

$$= \begin{pmatrix} 3 \\ 5 \end{pmatrix} \tag{5}$$

The coordinates of the required point P are $\begin{pmatrix} 3 \\ 5 \end{pmatrix}$

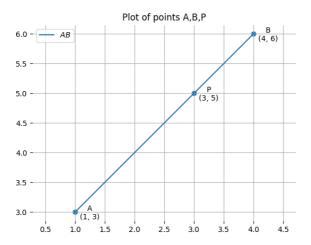


Fig. 1: Plot of the points A,B,P