ASSIGNMENT 1

EE24BTECH11005 - Arjun Pavanje*

E: Subjective Questions

- 6. Without using tables prove that $\left(\sin\left(12^{()}\right)\right)\left(\sin\left(48^{()}\right)\right)\left(\sin\left(54^{()}\right)\right) = \frac{1}{8}$ (1982 2*Marks*)
- 7. Show that $16\left(\cos\left(\frac{2\pi}{15}\right)\right)\left(\cos\left(\frac{4\pi}{15}\right)\right)\left(\cos\left(\frac{8\pi}{15}\right)\right)$ $\left(\cos\left(\frac{16\pi}{15}\right)\right) = 1$

(1983 - 2Marks)

- 8. Find all the solution of $4\cos^2(x)\sin(x) 2\sin^2(x) = 3\sin(x)$ (1983 2*Marks*)
- 9. Find the values of $x \in (-\pi, +\pi)$ which satisfy the equation $8^{(1+|\cos(x)|+|\cos^2(x)|+|\cos^3(x)|+...}) = 4^3$

(1984 - 2Marks)

10. Prove that $\tan(\alpha) + 2\tan(2\alpha) + 4\tan(4\alpha) + 8\cot(8\alpha) = \cot(\alpha)$

(1988 - 2Marks)

11. ABC is a triangle such that $\sin(2A + B) = \sin(C - A) = -\sin(B + 2C) = \frac{1}{2}$ If A, B and C are in arithmetic progression, determine the values of A, B and C.

(1990 - 5Marks)

12. If $exp\{\left(\sin^2(x) + \sin^4(x) + \sin^6(x) + \dots \infty\right) \ln 2\}$ satisfies the equation $x^2 - 9x + 8$, find the value of $\frac{\cos(x)}{\cos(x) + \sin(x)}$, $0 < x < \frac{\pi}{2}$

(1991 - 4Marks)

13. Show that the value of $\frac{\tan(x)}{\tan(3x)}$, wherever defined never lies between $\frac{1}{3}$ and 3

(1992 - 4Marks)

14. Determine the smallest positive value of x (indegrees) for which $\tan(x + 100^{\circ}) = \tan(x + 50^{\circ})\tan(x)\tan(x - 50^{\circ})$

(1993 - 5Marks)

15. Find the smallest positive number p for which the equation $\cos(p\sin(x)) = \sin(p\cos(x))$ has a solution $x \in [0, \pi]$

(1995 - 5Marks)

- 16. Find all values of θ in the interval $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ satisfying the equation $(1 \tan(\theta))(1 + \tan(\theta))\sec^2(\theta) + 2^{\tan^2(\theta)} = 0$ (1996 2Marks)
- 17. Prove that the values of the function $\frac{\sin(x)\cos(3x)}{\sin(3x)\cos(x)}$

does not lie between $\frac{1}{3}$ and 3 for any real x (1997 – 5Marks)

18. Prove that $\sum_{k=1}^{n-1} (n-k) \cos\left(\frac{2k\pi}{n}\right) = -\frac{n}{2}$, where $n \ge 3$

(1997 - 5Marks)

- 19. In any triangle *ABC*, prove that $\cot\left(\frac{A}{2}\right) + \cot\left(\frac{B}{2}\right) + \cot\left(\frac{C}{2}\right) = \cot\left(\frac{A}{2}\right)\cot\left(\frac{B}{2}\right)\cot\left(\frac{C}{2}\right)$ (2000 3Marks)
- 20. Find the range of values oft for which $2 \sin(t) = \frac{1-2x+5x^2}{3x^2-2x-1}$, $t \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ (2005 2*Marks*)