4-4.2-1

EE24BTECH11005 - Arjun Pavanje

Ouestion:

Find the direction and normal vectors of the given line 2x + 3y = 9

Variable	Description
2x + 3y = 9	given line

TABLE I: Variables Used

Solution: The equation of the line is given by,

$$y = mx + c \tag{1}$$

$$\mathbf{x} = \begin{pmatrix} 0 \\ c \end{pmatrix} + x \begin{pmatrix} 1 \\ m \end{pmatrix} \tag{2}$$

$$\mathbf{x} = \mathbf{h} + k\mathbf{m} \tag{3}$$

here, $\mathbf{m} = \begin{pmatrix} 1 \\ m \end{pmatrix}$ where \mathbf{m} is direction vector given line can be written as

$$\mathbf{x} = \begin{pmatrix} 0 \\ 3 \end{pmatrix} + k \begin{pmatrix} 3 \\ -2 \end{pmatrix}$$
$$\mathbf{m} = \begin{pmatrix} 3 \\ -2 \end{pmatrix}$$

equation of line in terms of normal vector \mathbf{n} is,

$$\mathbf{n}^T \mathbf{x} = c \tag{4}$$

$$\mathbf{n} = \begin{pmatrix} -m \\ 1 \end{pmatrix} \tag{5}$$

Here,

$$\mathbf{n} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

Direction vector:
$$\mathbf{m} = \begin{pmatrix} 3 \\ -2 \end{pmatrix}$$

Normal Vector:
$$\mathbf{n} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

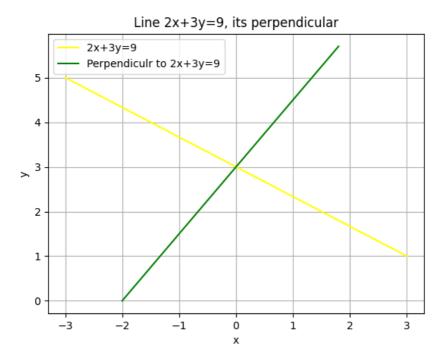


Fig. 1: Plot of the triangle