EE24BTECH11005 - Arjun Pavanje

Question:

If the points A(1,2), O(0,0) and B(a,b) are collinear, then find the relation between a and b.

Solution:

Variable	Description
A	Point (1, 2)
0	(0,0) point
В	(a,b) point

TABLE I: Variables Used

First we should construct the collinearity matrix with the given points A,O,B

$$\begin{pmatrix} O - A \\ B - O \end{pmatrix} \tag{1}$$

$$\begin{pmatrix} -1 & -2 \\ a & b \end{pmatrix} \xrightarrow{R_2 \to R_2 - aR_1} \begin{pmatrix} -1 & -2 \\ 0 & b - 2a \end{pmatrix}$$
 (2)

rank should be 1 for collinearity, for that R_2 must be 0, so

$$b - 2a = 0 \tag{3}$$

$$\therefore b = 2a \tag{4}$$

The required relation between a, and b is, b = 2a

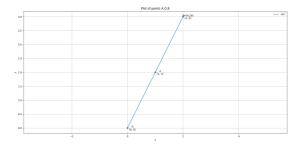


Fig. 1: Plot of the points A,O,B