

## Feature Scaling ML GURU

← X → Y

Size	no of bedrooms	price
1000	2	-
1500	3	-
1400	2	-
2000	5	-
⋮	⋮	⋮

$$\hat{y}_i = w_1 x_{i1} + w_2 x_{i2} + b$$

From Previous video,

$$\frac{\partial L}{\partial w_j} = \frac{1}{n} \left[ (\hat{y}_1 - y_1) x_{1j} + (\hat{y}_2 - y_2) x_{2j} + \dots + (\hat{y}_m - y_m) x_{mj} \right]$$

$$\frac{\partial L}{\partial w_j} \propto (\hat{y}_i - y_i) x_{ij}$$

eg)

$$\frac{\partial L}{\partial w_1} \propto (\hat{y}_i - y_i) x_{i1}$$

$$\frac{\partial L}{\partial w_2} \propto (\hat{y}_i - y_i) x_{i2}$$

(1000's)

$x_{i1} \Rightarrow$  (size)

$x_{i2} \Rightarrow$  (no. of bedrooms)

$$\frac{\partial L}{\partial b} = (\hat{y}_i - y_i) (1)$$

$$\therefore \left| \frac{\partial L}{\partial w_1} \right| \gg \left| \frac{\partial L}{\partial w_2} \right|$$

update rule:

$$w_1 = w_1 - lr \left( \frac{\partial L}{\partial w_1} \right)$$

$$w_2 = w_2 - lr \left( \frac{\partial L}{\partial w_2} \right)$$

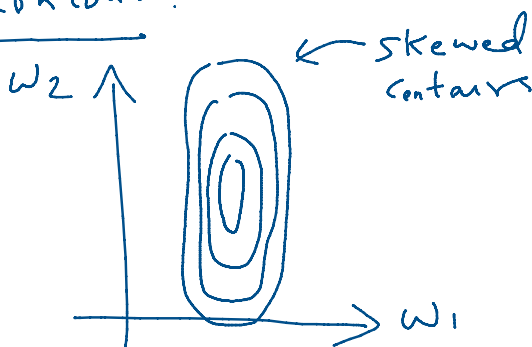
$$\Delta w_1 \propto \frac{\partial L}{\partial w_1}$$

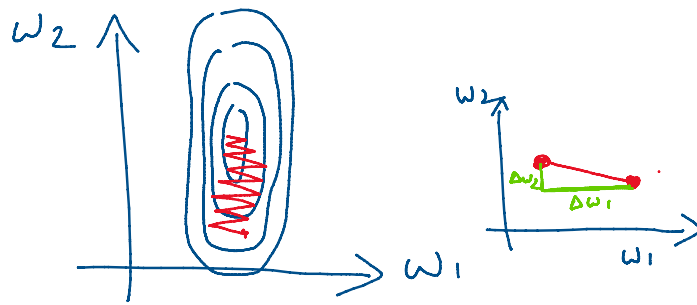
$$\Delta w_2 \propto \frac{\partial L}{\partial w_2}$$

Hence,

$$\Delta w_1 \gg \Delta w_2$$

Loss contour:





Hence, All the features must be in same range

## Feature Scaling

### ① Feature normalization (MinMax Scaler)

→ It scales all the features (columns) to  $[0, 1]$  range

eg)

no. of bedrooms
1
3
5
2

$$X_{\min} = 1$$

$$X_{\max} = 5$$

$$X = \frac{X - X_{\min}}{X_{\max} - X_{\min}}$$

eg)  $X = 5$

$$\therefore X_{\text{scaled}} = \frac{X - X_{\min}}{X_{\max} - X_{\min}} = \frac{5 - 1}{5 - 1} = 1$$

$$X = 3$$

$$X_{\text{scaled}} = \frac{3 - 1}{5 - 1} = \frac{2}{4} = 0.5$$

### ② Feature Standardisation

→ scales all features to 0 mean and unit variance

$$X = \frac{X - \mu}{s} \quad \left\{ \begin{array}{l} \mu = \text{mean} \\ s = \text{standard deviation} \end{array} \right.$$