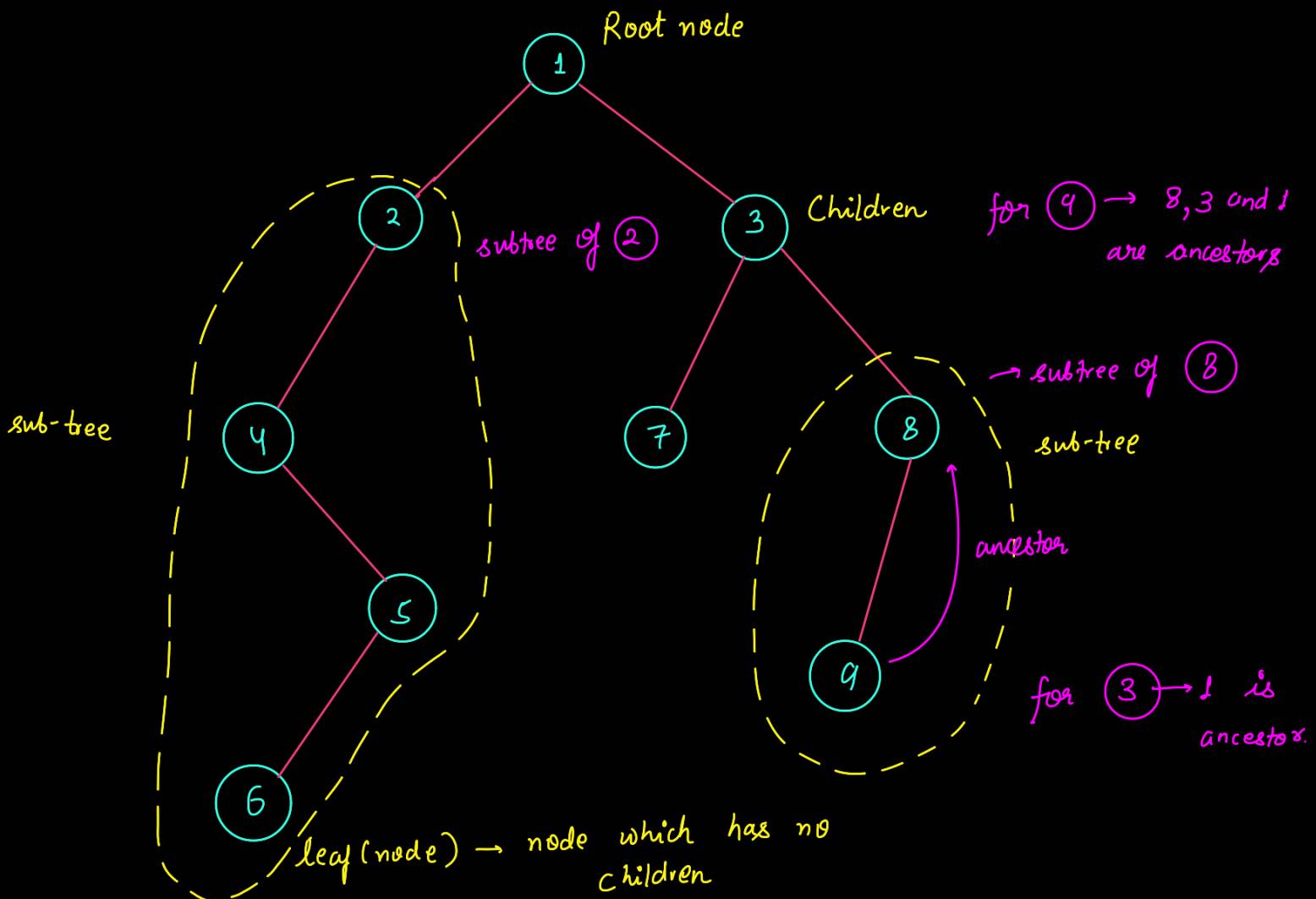
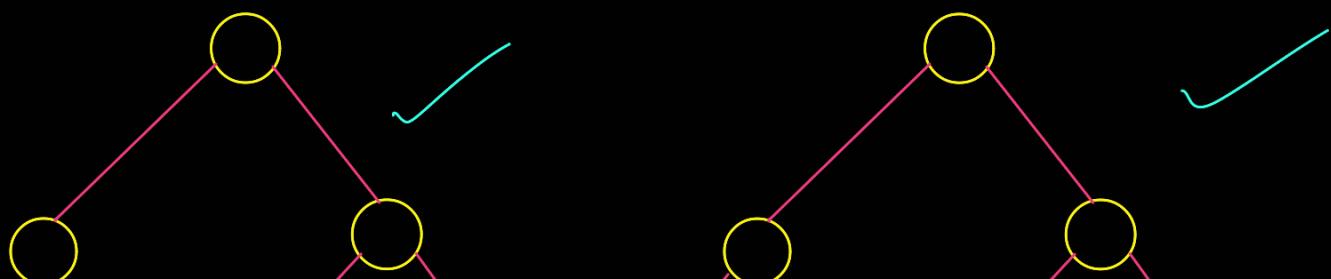


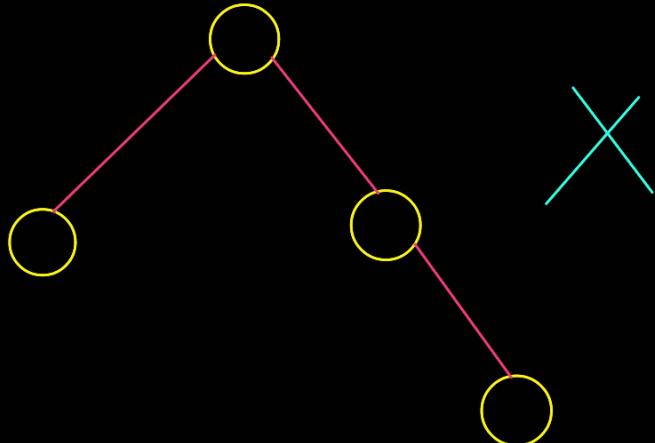
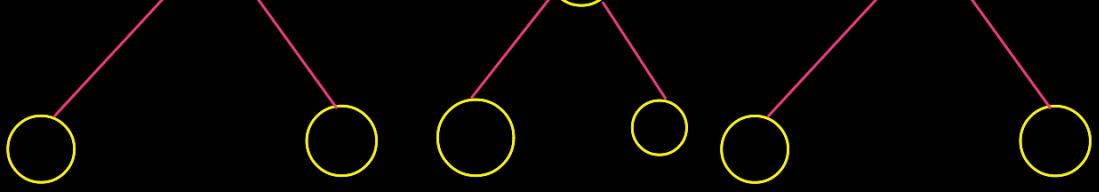
# TREES:



# Types of Binary Trees:

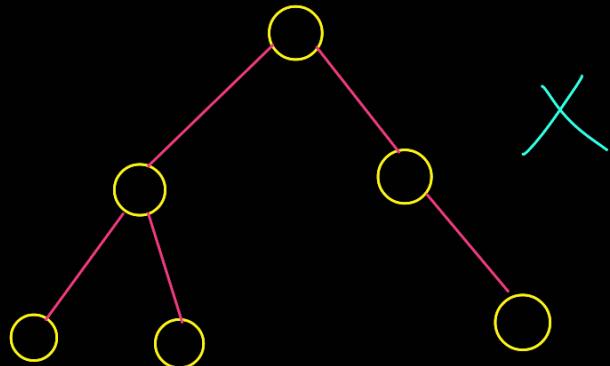
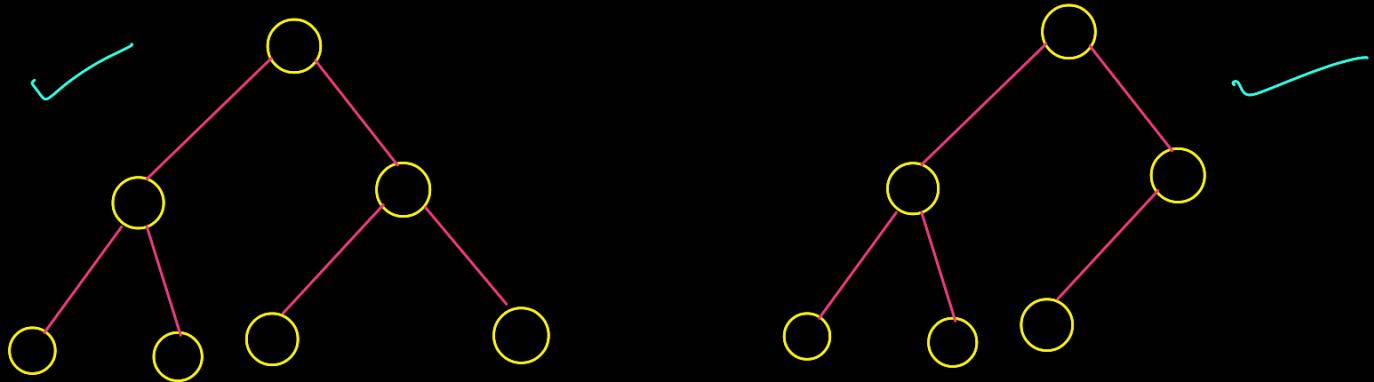
① Full Binary Tree: either has 0 or 2 children



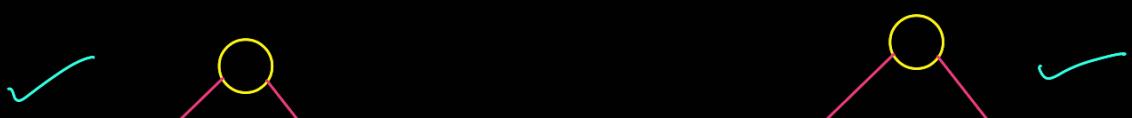


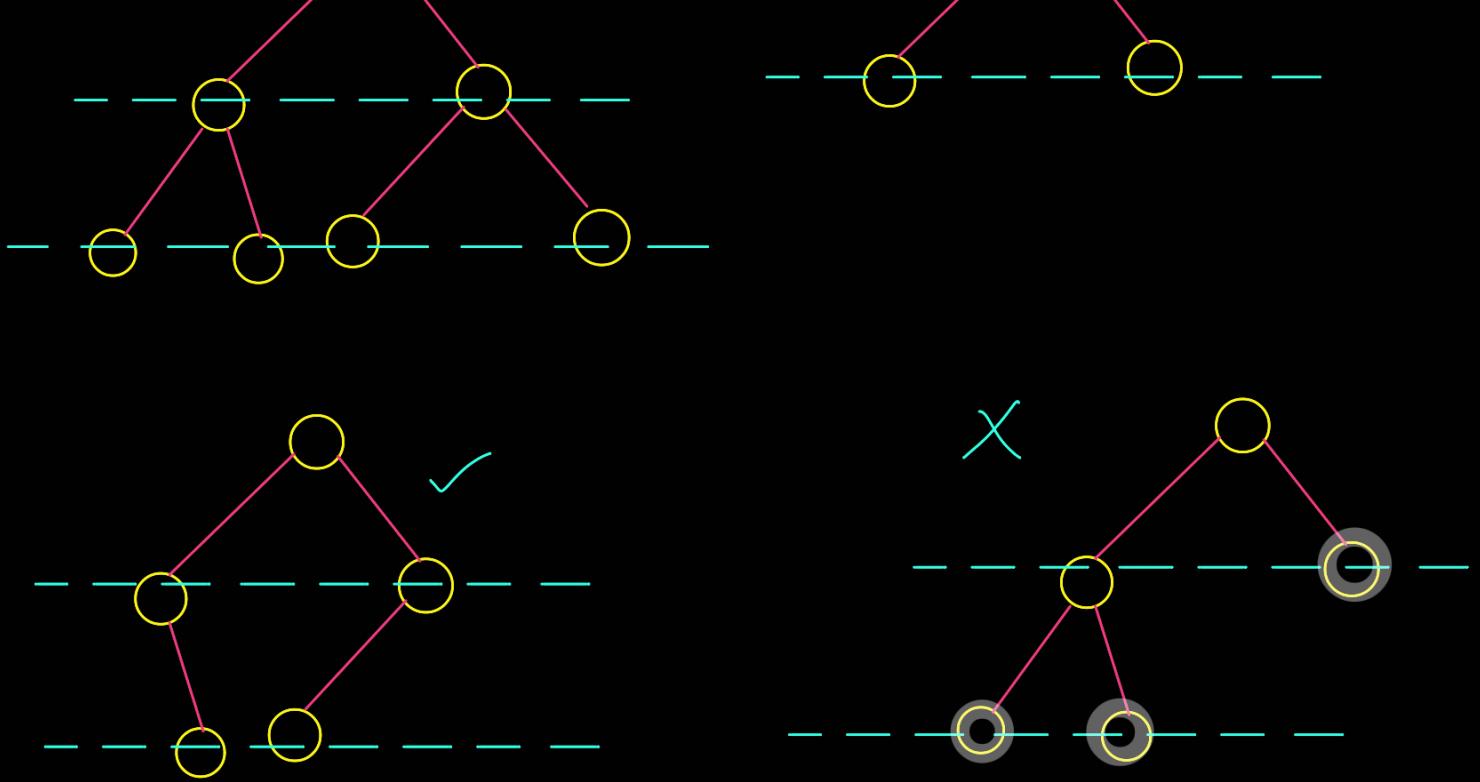
possibly.

- ② Complete Binary Tree  $\Rightarrow$  1) all levels are filled except, the last level.  
 2) the last level has all nodes on left as possible.



- ③ Perfect Binary tree : all leaf nodes are at same level.

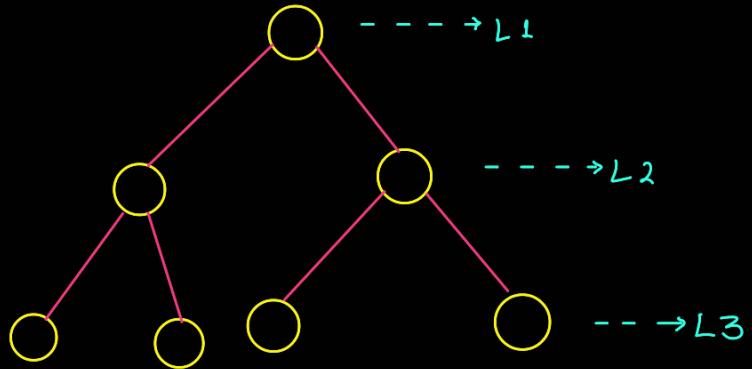




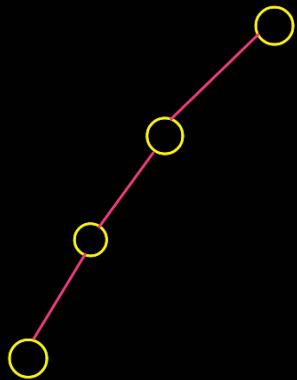
4. Balanced Binary tree: height of tree can at max be  $\log_2(N)$   
where  $N \rightarrow$  no. of nodes.

$n = 8$  nodes.

levels =  $\log_2 8 = 3$

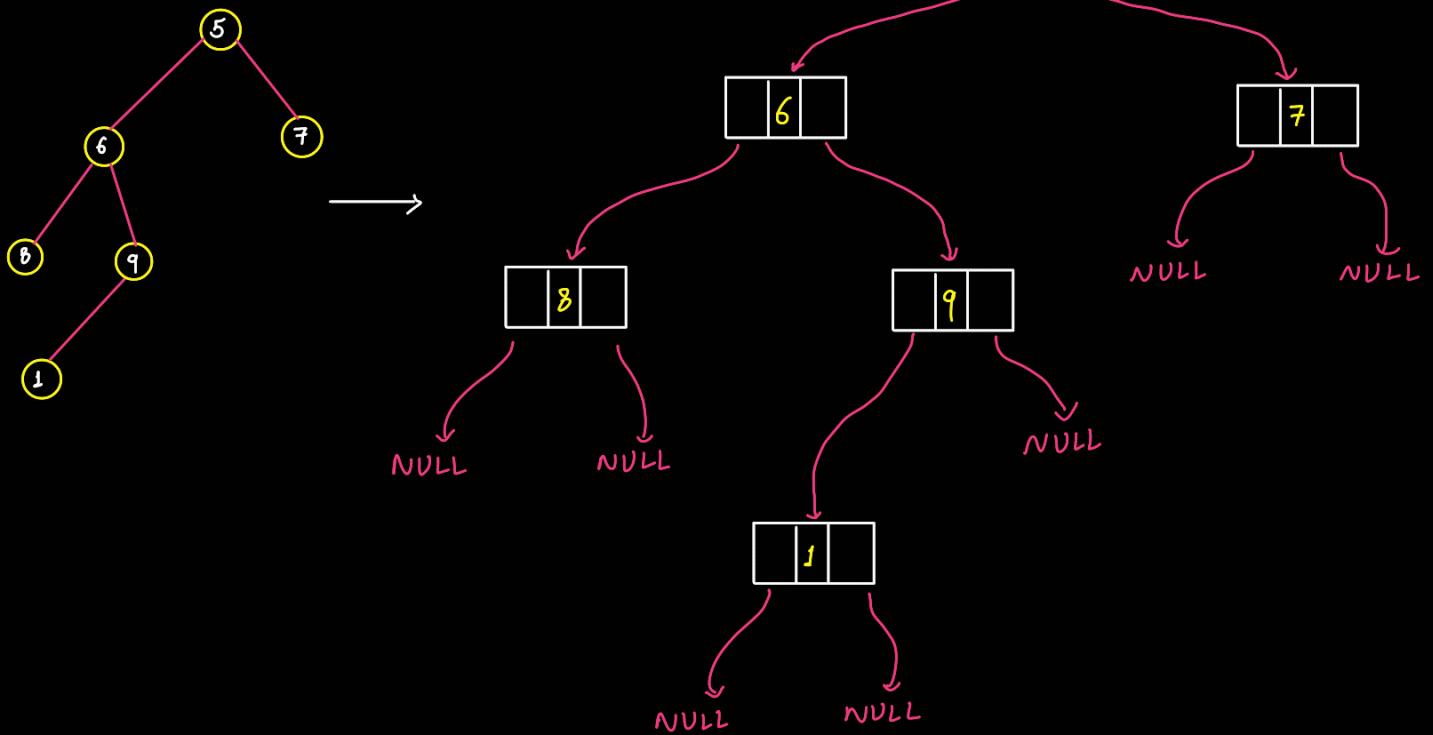


5. Degenerate trees  $\rightarrow$  (linked list)



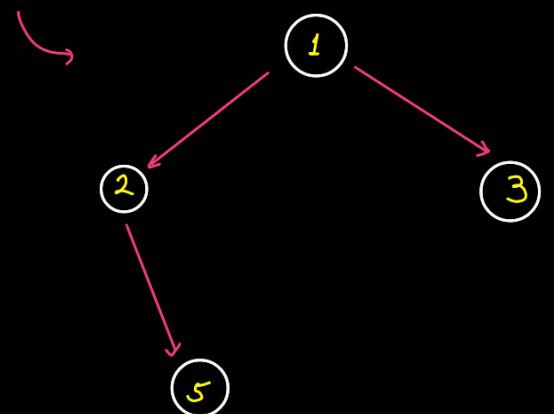
\* Representation of Binary tree:

left	data	right
------	------	-------



```
Code → Struct node {
    int data;
    struct node *left;
    struct node *right;
    node (int val) {
        this->data = val;
        this->left = this->right = NULL;
    }
};
```

eg → main () {  
 struct node \*root = new node(1);  
 root -> left = new node(2);  
 root -> right = new node(3);  
 root -> left -> right = new node(5);  
}



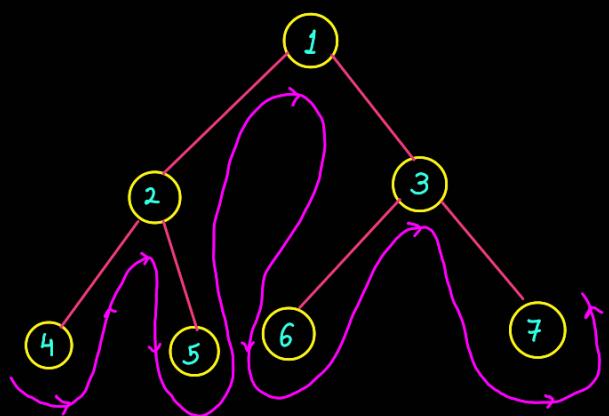
# Tree Traversals : (BFS/DFS) → (Breadth first search/depth first search)

DFS → types

- inorder traversal (left root right)
- pre-order traversal (root left right)
- post-order traversal (left right root)

I) Inorder Traversal : (left root right)

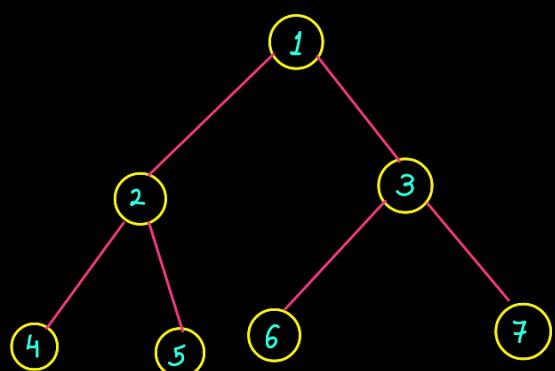
$\Rightarrow 4 \ 2 \ 5 \ 1 \ 6 \ 3 \ 7$



(extreme left pe Left Root Right)



(extreme right pe left root right)

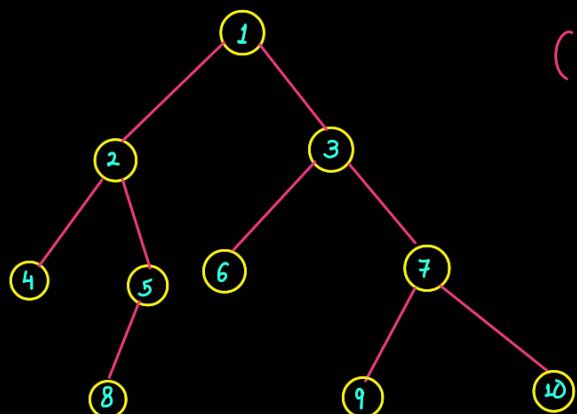


Pre-order traversal  $\rightarrow$  (Root left right)

1 2 4 5 3 6 7

post order  $\rightarrow$  (left right Root)

4 5 2 6 7 3 1



(LROR)

Inorder: 4 2 8 5 1 6 3 9 7 10

(RDLR)

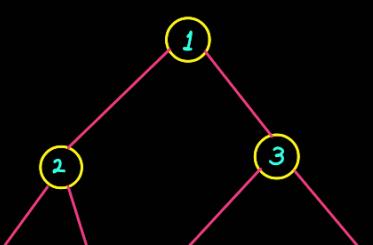
Pre-order: 1 2 4 5 8 3 6 7 9 10

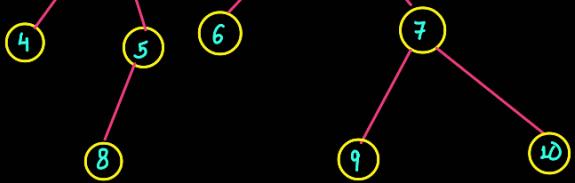
(LRRD)

Post order: 4 8 5 2 6 9 10 7 3 1

# Breadth first Traversal  $\rightarrow$  horizontally.

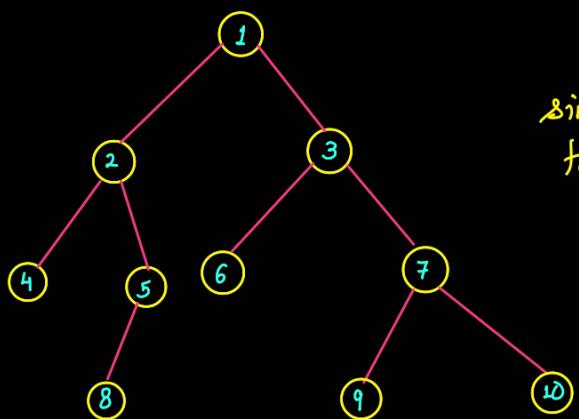
BFS: 1 2 3 4 5 6 7 8 9 10





## # BFS (level order traversal)

O/P  $\Rightarrow$  1 2 3 4 5 6 7 8 9 10



simple steps  $\rightarrow$  to follow

1. keep pointing the nodes one by one and simultaneously, if the curr. node has any left/right, add it to the queue)

```

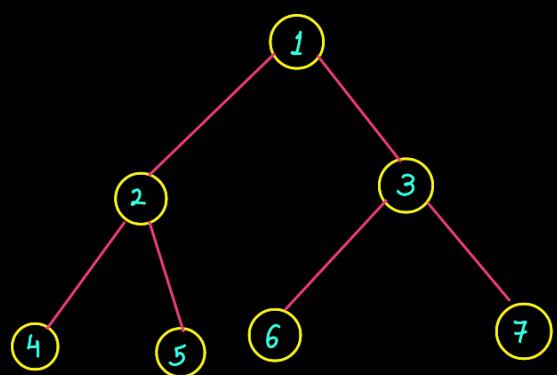
vector<vector<int>> level( node* root) {
    vector<vector<int>> ans;
    queue<node> q;
    q.push(root);
    while ( !q.empty() ) {
        int size = q.size();
        vector<int> level;
        for( int i = 0; i < size; i++ ) {
            TreeNode * node = q.front();
            q.pop();
            if ( node->left ) q.push( node->left );
            if ( node->right ) q.push( node->right );
            level.push_back( node->val );
        }
        ans.push_back( level );
    }
    return ans;
}
  
```

```

    ans.push_back(level);
}
return ans;
}

```

## # Iterative traversals:



Pre-order traversal  $\rightarrow$  (Root Left Right)

1 2 4 5 3 6 7

hint  $\rightarrow$  use stack and  
push right node before  
left node because you have  
to process left node first.

l  
r

post order  $\rightarrow$  (Left Right Root)

4 5 2 6 7 3 1

y

5

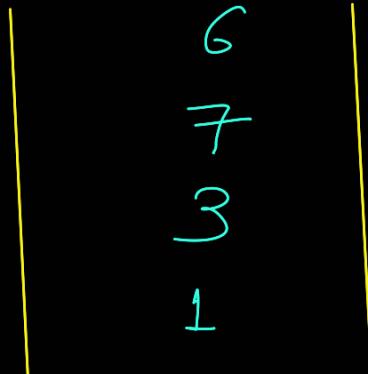
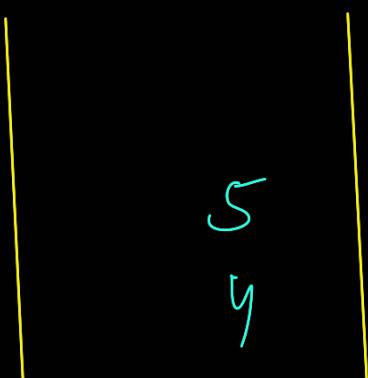
2

6

7

3

1



st1

curr = st2.top(); st2.pop();

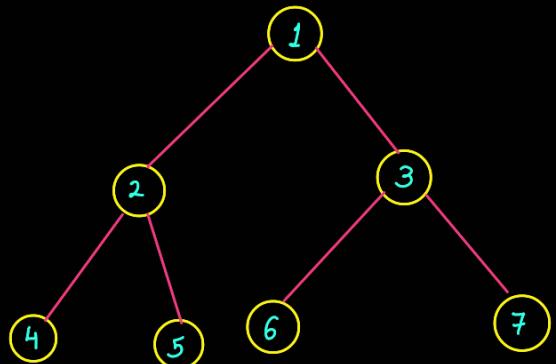
curr->left ? st1.push(curr->left);

curr->right ? st1.push(curr->right);

(LROR)

inorder:

4 2 5 1 6 3 7



curr = null.

temp = null.

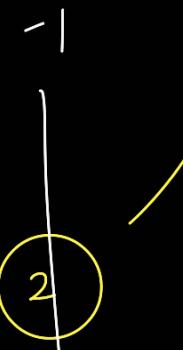
hint keep filling left  
nodes and moving  
to node = node->left  
until you find leaf node  
then print stack's top  
and move to node's  
right.

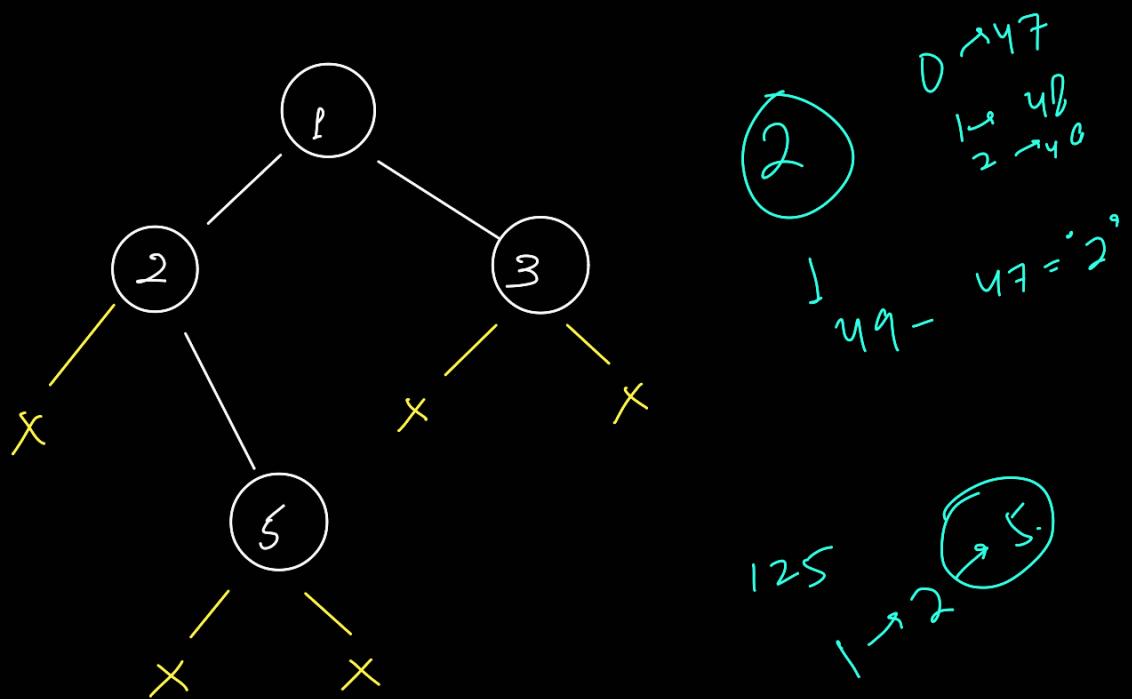
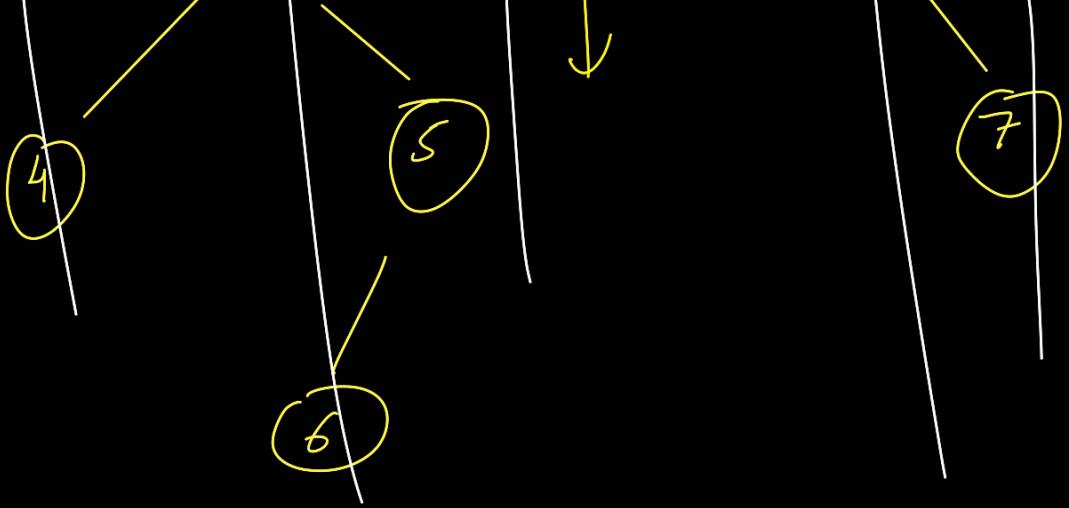
queue <  $\emptyset$ , value).

map<int, map<int, multiset<int>>;

1 val

- 2





```

1 { } 1
f( root, ans, temp) {
    if (!root) ret;
    if (leaf) ans.push(stoi);
    temp += root->val; 1
    f( root->left, ans, temp); 0
    f( root->right, ans, temp); 2
}
  
```

```

3
2 { } 12
f( root, ans, temp) {
    if (!root) ret;
    if (leaf) ans.push(stoi);
    temp += root->val; 12
    f( root->left, ans, temp); ✓
    f( root->right, ans, temp); ✓
}
  
```

```

5 { } 125
f( root, ans, temp) {
    if (!root) ret;
    if (leaf) ans.push(stoi);
    temp += root->val;
    f( root->left, ans, temp);
    f( root->right, ans, temp);
}
  
```

```

f( root, ans, temp) {
    if (!root) ret;
}
  
```

```

f( root, ans, temp) {
    if (!root) ret;
}
  
```

```

f( root, ans, temp) {
    if (!root) ret;
}
  
```

```

if (leaf) ans.push(stoi);
temp += root->val;
f (root->left, ans, temp);
j (root->right, ans, temp);

```

```

f (root, ans, temp) {
    if (!root) ret;
    if (leaf) ans.push(stoi);
    temp += root->val;
    f (root->left, ans, temp);
    j (root->right, ans, temp);
}

```

```

if (leaf) ans.push(stoi);
temp += root->val;
f (root->left, ans, temp);
j (root->right, ans, temp);

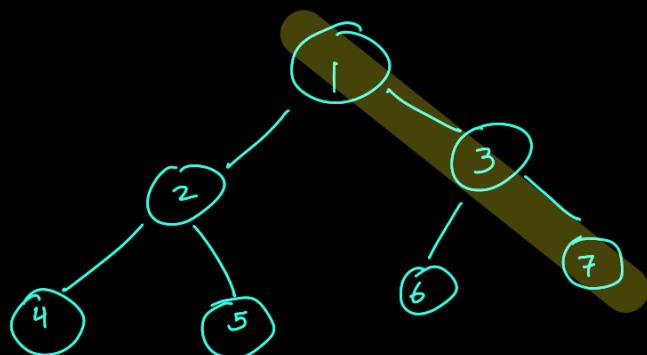
```

```

if (leaf) ans.push(stoi);
temp += root->val;
f (root->left, ans, temp);
j (root->right, ans, temp);

```

$n = 7$



1  
f (root, n, ans, final)

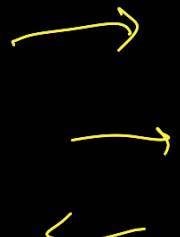
```

if (!root) ret;
if (root->val == n) {
    final = ans;
    return;
}

```

ans.push(root);      ans = 1

helper(root->left, n, ans, final);



2      1 3  
f (root, n, ans, final)

```

if (!root) ret;
if (root->val == n) {
    final = ans;
    return;
}

```

ans.push(root);      1 2

helper(root->left, n, ans, final);      0

```

    helper(root->right, z, ans, final);
ans.pop();

```

null 124

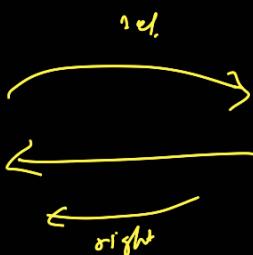
```
f( root, x, ans, final)
```

```
if (!root) set;
```

```
if (root->val == x) {
```

```
final = ans;
return; }
```

```
ans.push(root);
```



```

helper(root->left, z, ans, final);
ans.push();

```



13

```
f( root, x, ans, final)
```

```
if (!root) set;
```

```
if (root->val == x) {
```

```
final = ans;
return; }
```

```
ans.push(root);
```

```
helper(root->left, x, ans, final);
helper(root->right, x, ans, final);
ans.pop();
```

```
helper(root->left, x, ans, final);
helper(root->right, x, ans, final);
ans.pop();
```

```
f( root, x, ans, final)
```

```
if (!root) set;
```

```
if (root->val == x) {
```

```
final = ans;
return; }
```

```
ans.push(root);
```

```
helper(root->left, x, ans, final);
helper(root->right, x, ans, final);
ans.pop();
```

```
f( root, x, ans, final)
```

```
if (!root) set;
```

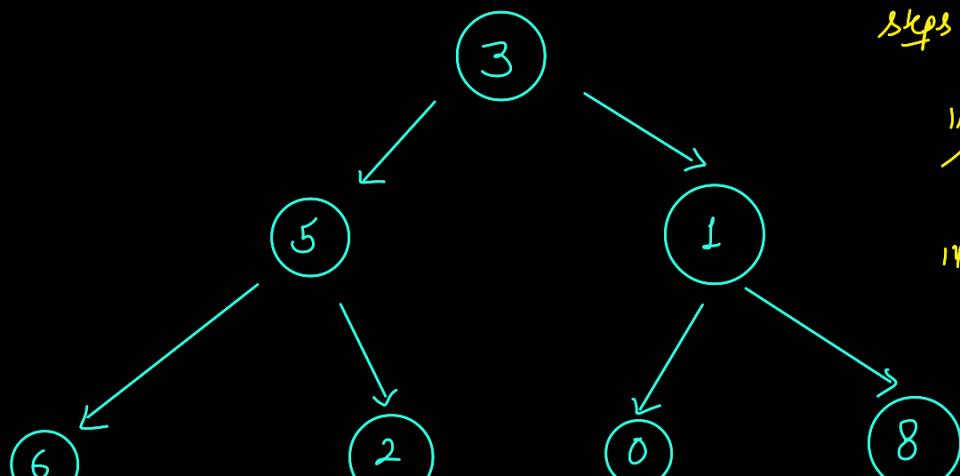
```
if (root->val == x) {
```

```
final = ans;
return; }
```

```
ans.push(root);
```

```
helper(root->left, x, ans, final);
helper(root->right, x, ans, final);
ans.pop();
```

# [Print nodes at a distance of K in Binary Tree]:

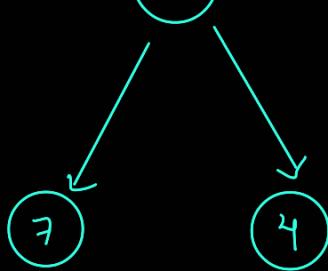


steps → 1) parent store in map

2) move ↑

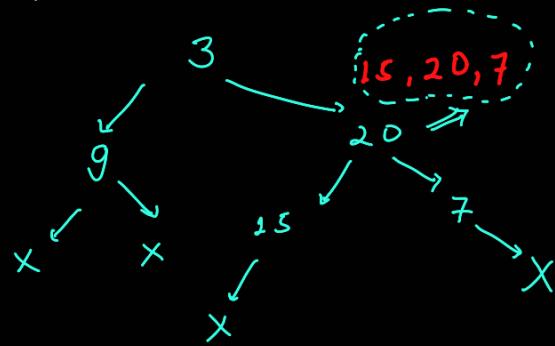
3) if dis == k { v.push(queue)}

return v;



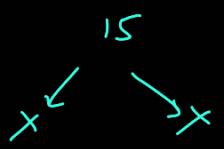
Ques: Imp - Topic → Construct Binary Tree From In-Order and Post/Pre-Order Traversals:

eg → pre Order:  $[ \underline{3}, 9, 20, 15, 7 ]$     inorder:  $[ 9, \underline{3}, 15, 20, 7 ]$   
pstart                                  pend                                  instant                                  inend:



15, 20, 7  
Pre: 20, 15, 7  
In: 15, 20, 7

Pre: 15  
In: 15



pre =  $\underline{1}, 2, 4, 7, 3$   
 $\downarrow$      $\downarrow$      $\downarrow$      $\downarrow$      $\downarrow$   
 $\text{ps} \quad \text{pstart} \quad \text{pstart + numleft} \quad \text{pend} \quad (n-1)$   
 $\text{instant} \quad \text{inroot} \quad \text{inroot} \quad \text{inend}$

inroot =  
numleft = inroot - instant.  
= 3

Step 1 → map inorder to index;

root = new Tree(preord[ps])

1

f ( preord, 0, n-1, inorder, 0, n-1, map )

left =

f ( pre, pstart+1, pstart + numleft, inorder, 4, 7 )

3

Pyu → becz hume	
preorder	inorder
4	0
2	1
7	2
1	3
3	4

2. dhundha hai.

right = f ( pre, numleft+1, pend, inorder, inroot+1, inend )

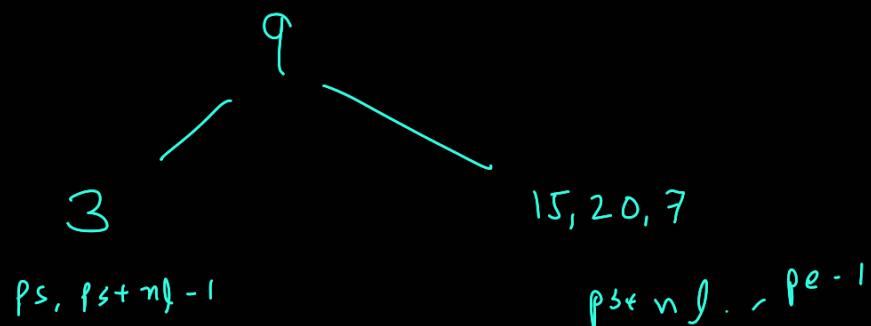
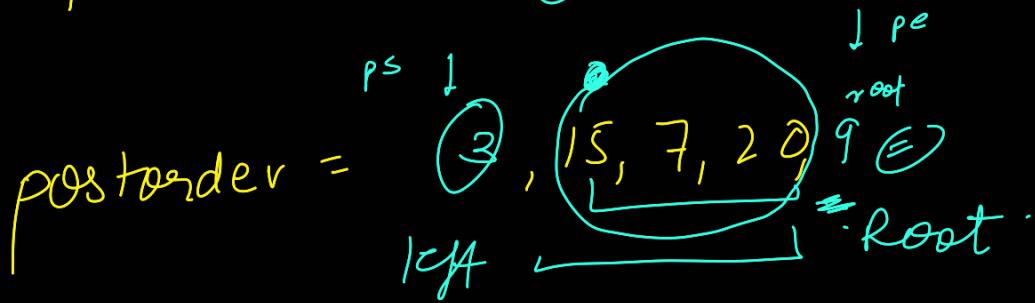
inroot

inroot

inend

inorder =

3 9, 15, 20, 7



## Morris Traversal : (Pre-order and inorder)

Recursive | Iterative traversal :

time:  $O(N)$   
space:  $O(N)$

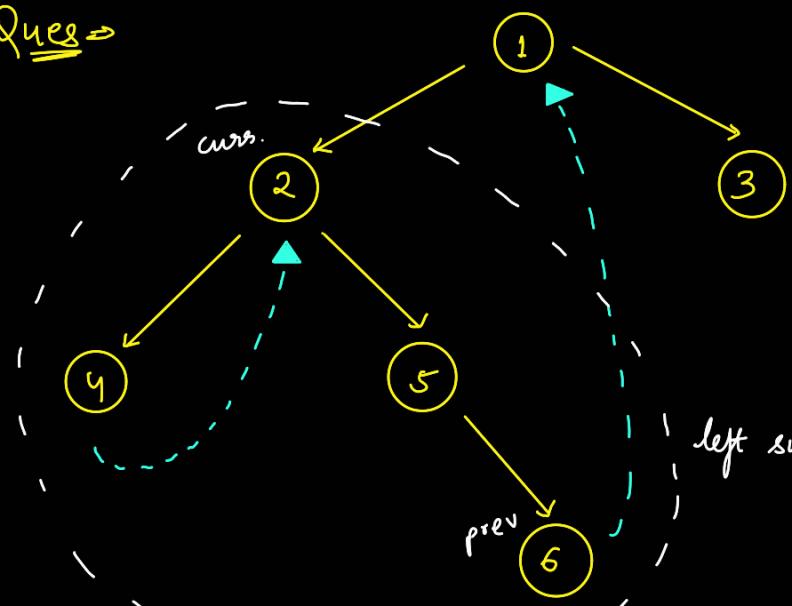
Morris traversal

time:  $O(N)$

space:  $O(1)$

\* uses the concept of threaded binary tree.

Ques →



leftRootRight  
inorder → 4 2 5 6 + 3

★ Morris-Traversal :  $O(1)$  space  
 $O(N)$  time

Observations :

if ( $\text{left} \rightarrow \text{null}$ )  
 $\text{print}(\text{curr})$   
 $\text{move} \rightarrow \text{right}$

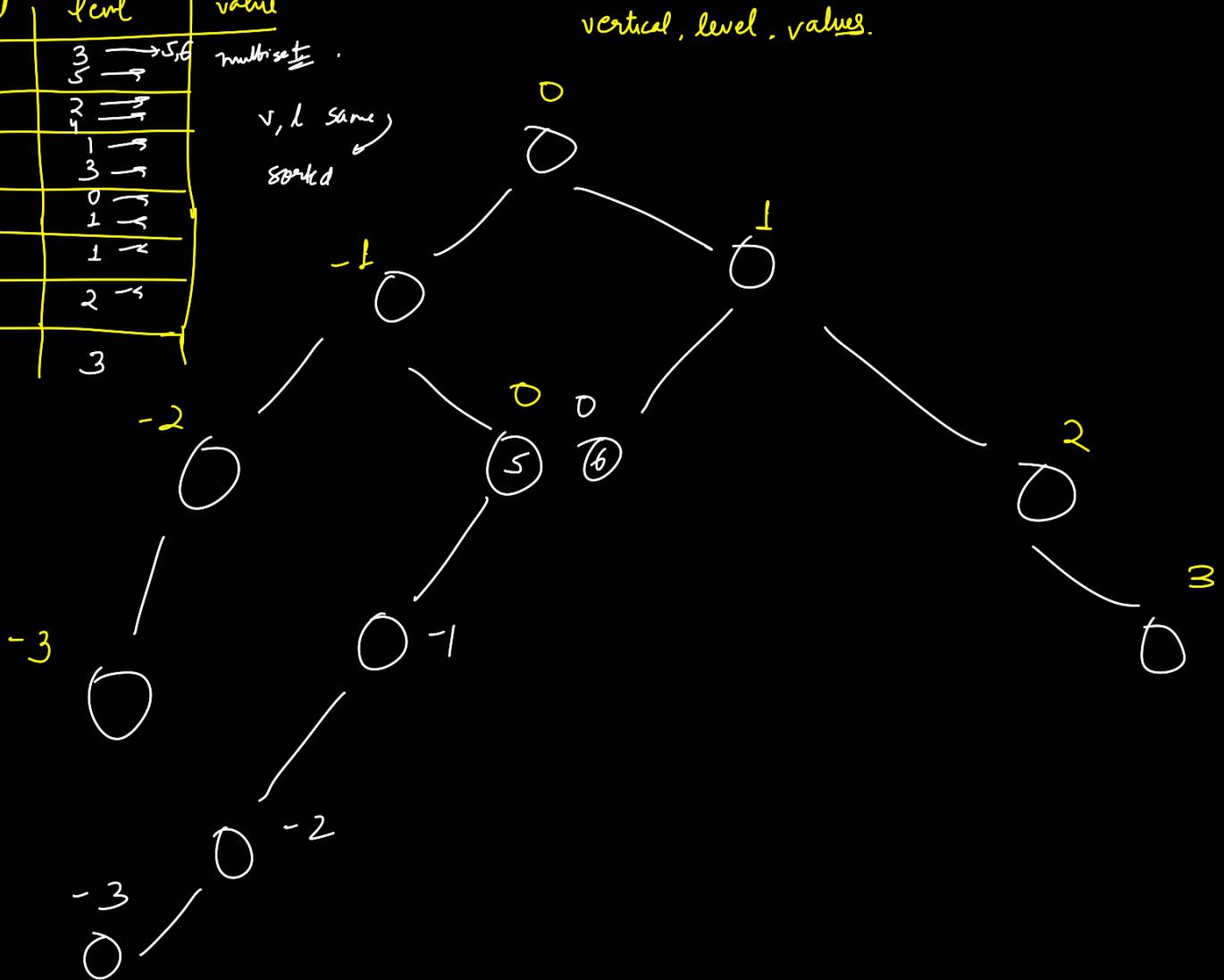
2.  $\text{left} \rightarrow$  rightmost gray thread current  
on left



1. move

then move  
 curr → left  
 subtree  
 If thread already  
 exists, remove  
 gt and move  
 curr → right.

sorted vertical	sorted level	value	sorted multiset
-3	3 → 5, 6		
-2	5 →		
-1	2 →		
0	1 →		
1	3 →		
2	0 →		
3	1 →		
	2 →		
	3		

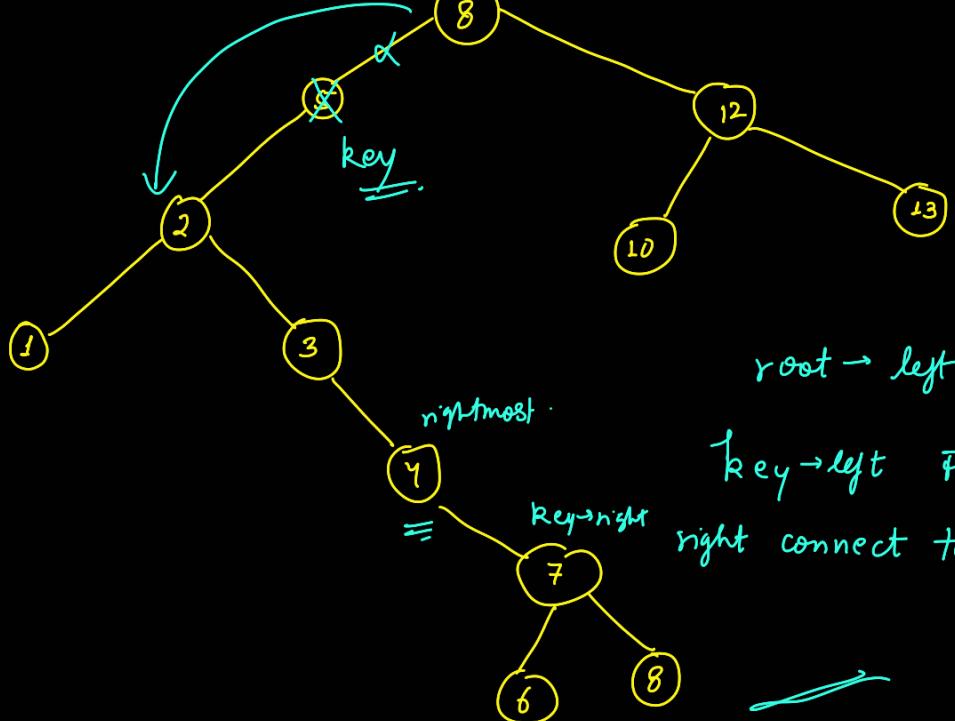


## [Binary Search Tree]:

↳ Height is generally kept  $\log_2 N$

- ↳ i)  $L < N < R$
- ii) Left subtree  $\rightarrow$  BST
- iii) Right subtree  $\rightarrow$  BST

key = 5

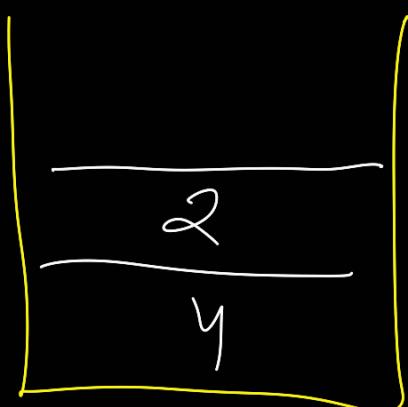


$\text{root} \rightarrow \text{left} = \text{key} \rightarrow \text{left}$

$\text{key} \rightarrow \text{left} \rightarrow \text{rightmost} \rightarrow$   
 $\text{right connect to key} \rightarrow \text{right}.$

$\text{array} = 1, 3, 4, 2$

$\text{mge} = 3, 4, -1, -1$



If  $a[i] > st.top()$  {  
 while ( $!st.empty()$ ) { and  $a[i] > st.top()$   
 $mge[i] = a[i];$   
 $st.pop();$   
 $st.push(a[i])$ }

0 1 2 3 4 5 6 7 8 9

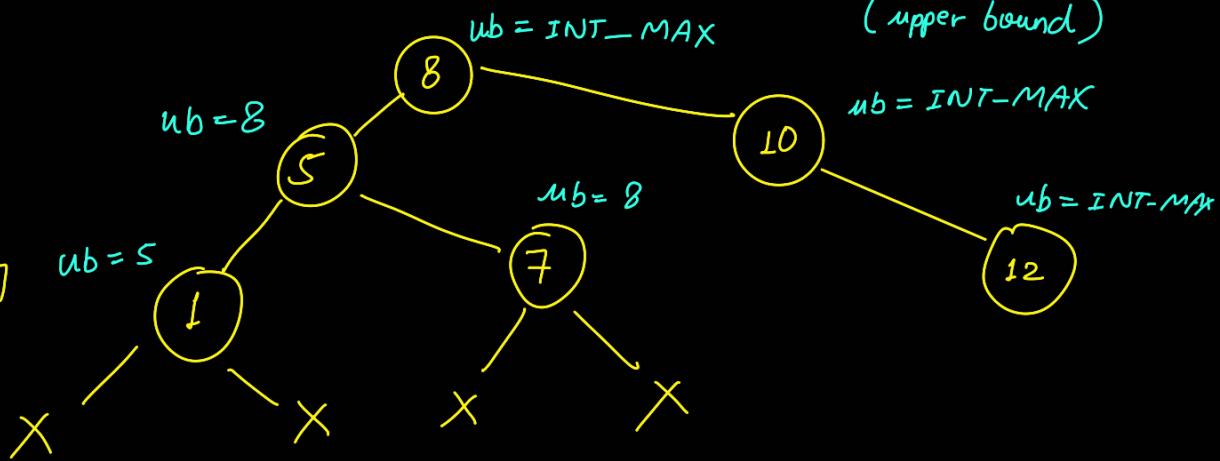
1, 2, 3, 7, 6, 5, 4, 9, 2, 0

7 3 9 9 6

2 3 2 7 9 9 7

Ques:

inorder: [2, 5, 1, 7, 10, 12]

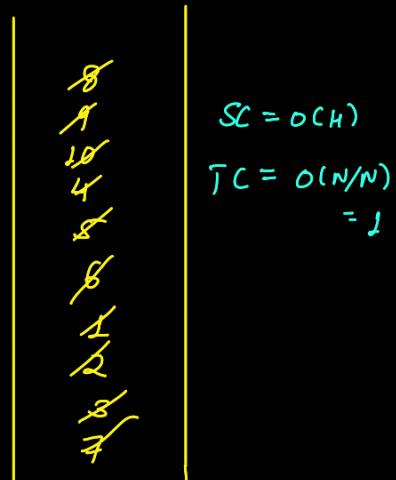
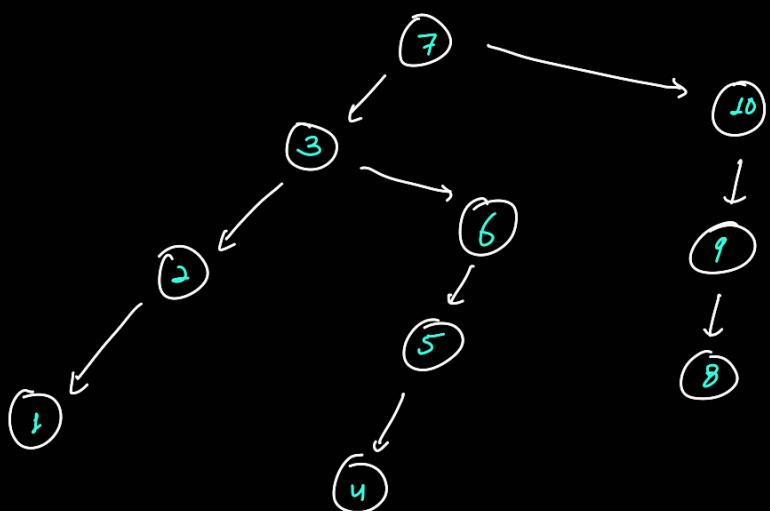


node  $\rightarrow$  left  $\rightarrow$  passing node  $\rightarrow$  val as upperbound.  
 node  $\rightarrow$  right  $\rightarrow$  passing prev ub as new upperbound.

# BST iterator of inorder       $S.C \Rightarrow O(H) \xrightarrow{\log_2 N}$  and  $T.C. = O(1)$

left      Root      Right

Stack  $\rightarrow$  sare  
 y      right      ho  
 left      daal  
 to      do  
 right      jake  
 sare      left  
 daal  
 do.



1, 2, 3, 4, 5, 6, 7, 8, 9, 10

Ques:

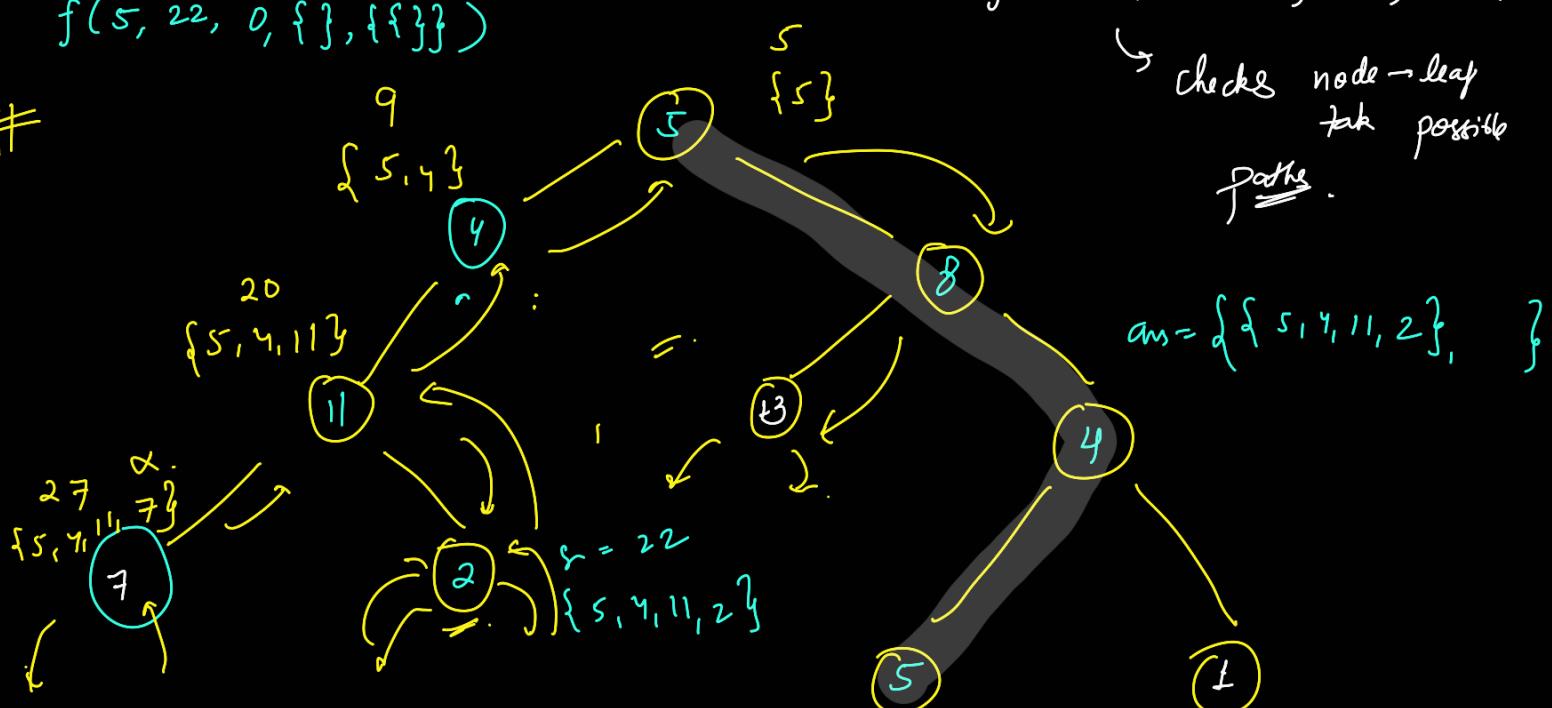
$$TC = O(n) + O(n) \Rightarrow O(n)$$

$$SC = O(n)$$

f (arr, matrix, sum, node)

$f(5, 22, 0, \{\}, \{\})$

#



- requirements:
- vector
  - 2d vector
  - sum variable

base case: if root = null return

remember → while backtracking, remove the node from sum,