

22/02/23

Closure of an attribute

→ given a (FD) set

Set of all attributes which are implied by the attribute.

$$X^+ = X$$

do {

$$\text{old } X^+ = X^+$$

for each F.D f_i in F.D set F ,

IF LHS of $f \subseteq X^+$

$$X^+ = X^+ \cup \text{RHS of } f$$

} while (old $X^+ \neq X^+$)

~~if old X^+~~

Candidate key : $K \Rightarrow K^+ = \underline{U}$ (Universal Set of Attributes \rightarrow Relation)

Cover of a FD set : A FD set F_c covers the FD set F if each F.D $f \in F$ is in F_c^+

<u>F</u>	<u>F_c</u>
$A \rightarrow B$	$A \rightarrow B$
$B \rightarrow C$	$B \rightarrow C$
$A \rightarrow C$	

Minimal cover : by removing the redundancy in F.D

Canonical form of a functional dependency

$$XYZ \rightarrow C_1, C_2$$

$$\begin{aligned} XYZ &\rightarrow C_1 \\ XYZ &\rightarrow C_2 \end{aligned}$$

(decomposition)

① PUT F.Ds in canonical form.

② Find & redundancy in F.Ds.

(a) If there is any redundant attribute on RHS of FD, then remove those.

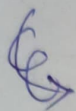
$$X \rightarrow Y \Rightarrow [X - \{A\}] \rightarrow Y$$

if A is dependent on X

(b) F.D is redundant $\Rightarrow F \Rightarrow (F - \{X \rightarrow Y\})^+$

Normalisation : The formal approach for designing database based on the concept of key and functional dependency.

Prime attribute : An attribute which is part of at least one candidate key.



↓
To minimize update anomalies occurrence of NULL values and redundancies



A complex structure will be broken into number of simple schema/relation.

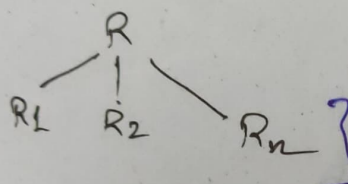
ER Diagram



Relations (R. model)



Normalization : Check with individual relation.



} Lossy loss join : while joining the decomposed relation

must be dependency preserving

- it must not give rise to spurious tuples

X normal form : Highest normal form it satisfies.

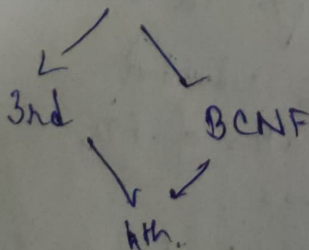
Designer may restrict the design to lower normal form.

↳ denormalisation

Eg: Roll & grade → roll number to grade often req.

1st NF (Not related with FD, each attr. must be atomic & single valued)

↓
2nd



∴ Roll → ~~score~~ → grade
① ← one table → ②

Node NORMALIZATION

27/02

Full

For every student unique roll number

↓ store

student(roll, Name, ph-no, city, [scode, sname, stype, FM,
PH, SCORE, FAC-ID, FAC-NAME,
FAC-PH])

1st normal form : F.D has no role.

→ Every attribute must be atomic and single valued
if composite, break it into components
if multivalued
↓
remove from original relation.

Eg: DOB → DT-DOB
 ↓
 MON-DOB
 ↓
 YR-DOB

for
Each such independent
set, create
relations

For RELATED ATTR
that
RELATE together

In new relation
copy the primary
key (FK in
new relation)

FK

∴ Student → 1st normal form

Student (Roll, Name, Ph-no, CITY, DOB)

NEW → SUBJECT (Roll, score, SName, SType, ...)
(FK)

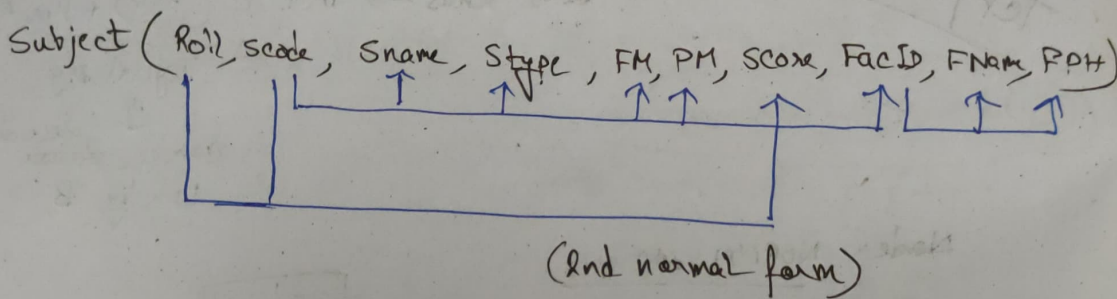
∴ **FDS**

ROLL → Name, Ph-no, city, dob

SCORE → SName, SType, FM, P.M, Fac-ID

Fac-ID → FName, F-ph

ROLL, SCORE → Score



2NF : Partial dependency

$X \rightarrow Y$ if $A \subset X$ & $X - \{A\} \rightarrow Y$ holds

then $\nexists Y$ is partially dependent on X

otherwise → fully functionally dependent.

A relation is in 2NF if every non prime attribute is fully functionally dependent on key.

→ if key is simple → already in 2NF

∴ **Student is in 2NF**

→ Subject: only score is fully functionally dependent on both roll & score

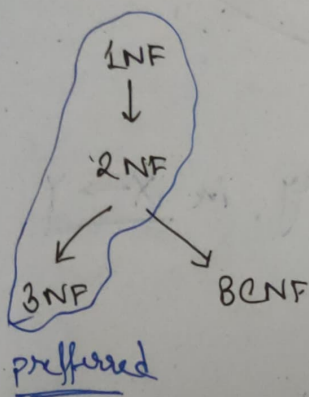
→ Not in 2NF (remove others)
and copy part of key on which they depend

∴ 2NF : ~~SDNF~~

Student (Roll, Name, Ph-no, City, dob)
Subject (Scode, Sname, Stype, FM, PM, EID, FName, F-PH)

Result (Roll, Scode^(FK), Score)

(new)



2NF : new relation has referenced key

1NF : new relation has referencing key

3NF : relation is in 3NF, if for every F.D, $X \rightarrow Y$ that holds on the relation, either of the following is true

→ X is super key

→ Y is prime.

Violating condition

! (X (super) ~~or~~ Y (prime))

⇒ X is not candidate and Y is not prime.



(2NF vio) XX X is part of cand (prime)

or

X is not prime attr.

∴ X & Y are both non prime

∴ $Z \rightarrow X \rightarrow Y$

non prime

To be in 3NF, relation must be in 2NF and

∄ no transitive dependencies

∴ reduce transitive dependency

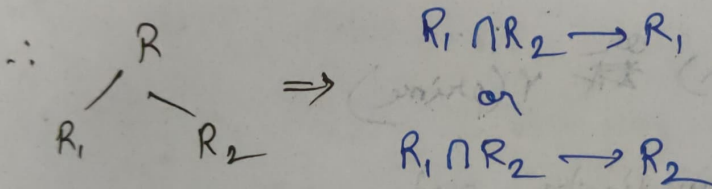
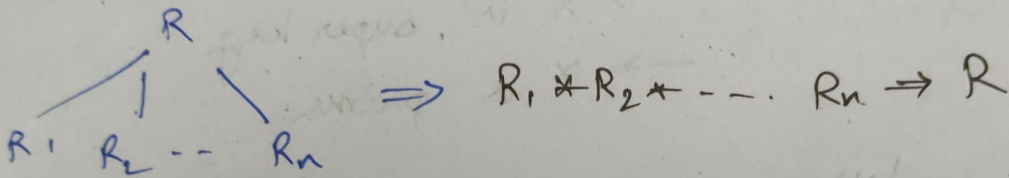
$\text{Subject} (\text{SCODE}, \text{SNAME}, \text{STYPE}, \text{FM}, \text{PM}, \text{F-ID})$
 $\text{Faculty} (\text{FID}, \text{FAC-NAME}, \text{F-PH})$

Fk

BCNF : Holds, only if $X \rightarrow \text{superkey}$ in $X \rightarrow Y$
 (more strict)

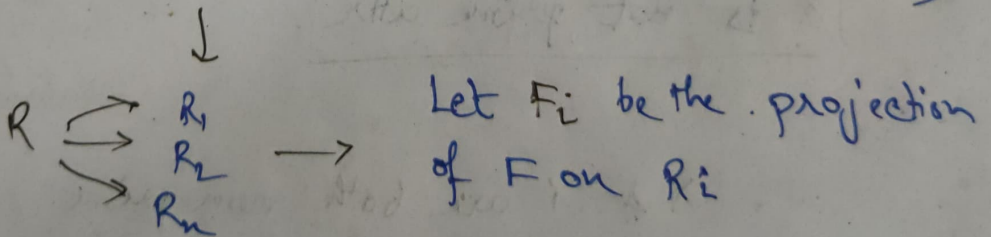
so from the relation, remove Y , in a new rel,
~~copy~~ copy X
 X is PK in new relation.
 X is FK in old relation

Decomposition must be loss less.



Upto BCNF \rightarrow Decomposition preserving

F.D set F defined on universal relation R (all attr)



$$UF_i = F'$$

Set of F.D in F whose
 LHS & RHS attributes are in R_i

$\therefore F'^+ = F^+ \Rightarrow F' \text{ \& } F \text{ are equivalent.}$

\therefore F.D preserving then.

3NFBCNF

Both removes ~~dep~~ redundancy
 Both are lossless.

Dep
preserving

may not
 be dep. pres.

Attribute preservation

Each attribute of R
 must appear once
 in the decomposed.

What if ph no, not separated

↳

Roll

PH

Scode

Reason

Multiple 1:N

1

P1

S1

1

P2

S2

1

P1

S3

1

P2

S1

1

P1

S2

1

P2

S3

meaningless

↳ 4th NF