11/1/23

RELATIONAL ALGEBRA & RELATIONAL CALCULUS

→ To work with Relational Database

→ RA → Procedural | RC → Non-Procedural
(Expressions → Sequence of Operations) | → What data we need (No opⁿ given)

- **Relational Algebra** → ✓ Provides the foundation to work with Relᴺ dB
  ✓ Useful for implementing & optimising the query
  ✓ Some of the concepts of Relᴺ Alg is implemented in SQL.

eg:— DEPT (DCODE, DNAME, ...)
STUDENT (ROLL, NAME, ---, DCODE) (FK)

In an expression →
1 or more Relᴺ → I/P
Operations → Applied
Relᴺ(s) → O/P

(Pred^e is check on every Tuple)

(#) SELECT Operation → [COMMUTATIVE ($\sigma_1\sigma_2 R = \sigma_2\sigma_1 R$)]

$\sigma_{\text{predicate}}(R)$

eg:— $\sigma_{DCODE='D1'}(STUDENT)$

predicate:
> >=
< <=
= AND OR NOT
!=

O/P Relᴺ →
→ Schema → Same as I/P Relᴺ
→ State → Set of tuples satisfying the predicate

[CONJUNCTIVE ($\sigma_{P1}\sigma_{P2} R = \sigma_{P1 \text{ AND } P2} R$)]

(#) PROJECT OPERATION → [NOT COMMUTATIVE]

$\pi_{\text{list\_of\_attributes}}(R)$

$\langle t \rangle \; \forall t \in R$

eg:— $\pi_{ROLL, NAME}(STUDENT)$

O/P →
→ Schema → ROLL, NAME
→ #Tuples → likely to be same as #tuples in I/P Relᴺ

[eg:— $\pi_{SCORE}(ST^D)$
→ Same scores are merged into 1]

(#) DUPLICATE ELIMINATING PROJECT Op^n → If projected Aff^n doesnot contain Superkey, after projection, multiple tuples maybe taken as 1.

$$\Pi_{a_1,a_2}\left(\sigma_{a_3>30}(R)\right) = \Pi_{a_1,a_2}\left(\sigma_{a_3>30}\left(\Pi_{a_1,a_2,a_3}(R)\right)\right)$$

[Broader Table narrowed → In Memory (Not Disk) → Faster → Optimisation]

(#) RENAME Operation →

$\rho_{R2(X,Y,Z,W)}(R1(A,B,C,D))$ (Can use assignment for changing name also)

General: $R2(W,X,Y,Z) \leftarrow Op^n(R)$

$R2(X,Y,Z,W) \leftarrow \Pi_{A,B,C,D}(R1(A,B,C,D))$

First 4 are Fundamental Operations

(#) CARTESIAN PRODUCT →

R1 × R2

A, B A, B

R1.A, R1.B, R2.A, R2.B

O/P Rel^n →
- Schema → Sch(R1) ∪ Sch(R2)
- State → |R1| × |R2| Relations

eg:— $\Pi_{ROLL,NAME,DNAME}\left(\sigma_{STD.DCODE=DEPT.DCODE}(STUDENT \times DEPT)\right)$

→ Qualification needed as conflicting attributes

Derived Operations

(#) JOIN →

$R1 \bowtie_{Condition} R2$ eg:— $STD \bowtie_{STD.DCODE=DEPT.DCODE} DEPT$

If Condition is not given, equality of all common attributes is checked...

(Use RENAME to remove conflicting attⁿ on which = not done, if cond^n not given) eg:— $STD \bowtie \rho_{DCODE,DNAME}(DEPT)$

(*) If not based on '=' (equality) of attⁿ, (>, <, >=, etc.) → θ (Theta Join)

Later, choose any 1 attⁿ (common) (maybe (Cannot join unequal attⁿ)) To avoid (2,3) (3,2)

Same Score Students Pairs → $\left(\sigma_{STUDENT.SCORE=T.SCORE \text{ AND } STUDENT.ROLL<>T.ROLL}(STUDENT \times \rho_T(STUDENT))\right)$ → Can give < / or / >

FUNDM OP → Select, Project, Rename, Cart Prdt, Union, Minus

DERV OP → Intersection, Join, Natural Join