Lexical Analysis

Responsibilities

Scans the input program
Removes white spaces
Removes comments
Extracts and identifies tokens
Generates lexical errors
Passes tokens to parser

Terminologies

Token: classification for a common set of strings

Examples: Identifier, Integer, Float, Operator,....

Pattern: The rules that characterize the set of

strings for a token

Examples: [0-9]+

Lexeme: Actual sequence of characters that matches a pattern and has a given Token class

Examples:

Identifier: sum, data, x

Integer: 345, 2, 0, 629,....

Lexical Errors

Error Handling is localized with respect to the input source code

For example: fi(a == f(x)) ... generates no lexical error in C

In what situations do errors occur?

Prefix of remaining input does not match any defined token

Possible error recovery actions:

- 1.Deleting or Inserting Input Characters
- 2. Replacing or Transposing Characters
- 3.Or, skip over to next separator to ignore problem

Overall strategy

Use one character of look-ahead

Perform a case analysis

- 1)Based on lookahead char
- 2)Based on current lexeme

Outcome

- 3)If char can extend lexeme, continue.
- 4)If char cannot extend lexeme, find what the complete lexeme is (upto the previous character) and return its token. Put the lookahead back into the symbol stream.

Regular expressions

 ϵ is a regular expression, $L(\epsilon) = \{\epsilon\}$ If a is a symbol in Σ , then a is a regular expression, $L(a) = \{a\}$

(r) | (s) is a regular expression denoting the language L(r) \cup L(s)

(Strings from both languages)

(r)(s) is a regular expression denoting the language L(r)L(s)

(Strings constructed by concatenating a string from the first language with a string from the second language)

(r)* is a regular expression denoting (L(r))*

(Each string in the language is a concatenation of any number of strings in the language of s)

(r) is a regular expression denoting L(r)

Regular expressions

Examples:

```
\begin{array}{c|c} letter \rightarrow A \mid B \mid ... \mid Z \mid a \mid b \mid ... \mid Z \mid \_\\ digit \rightarrow 0 \mid 1 \mid ... \mid 9\\ id \rightarrow letter \ (letter \mid digit)* \end{array}
```

Regular expressions

Extensions

```
One or more instances: (r)+
```

Zero of one instances: r?

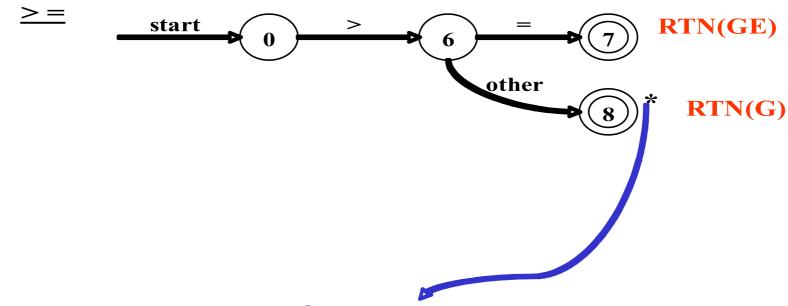
Character classes: [abc]

Example:

```
letter \rightarrow [A-Za-z]
```

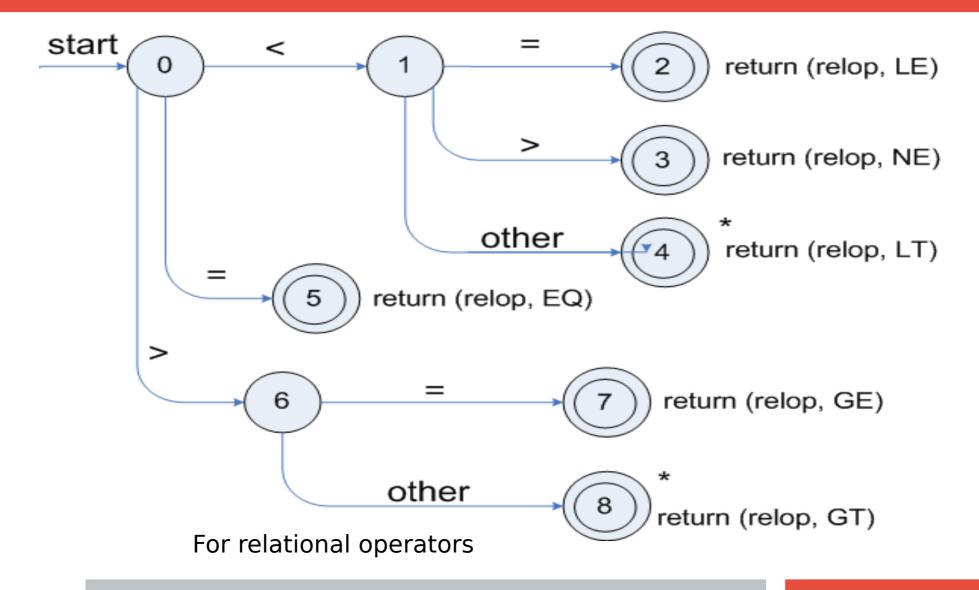
digit
$$\rightarrow$$
 [0-9]

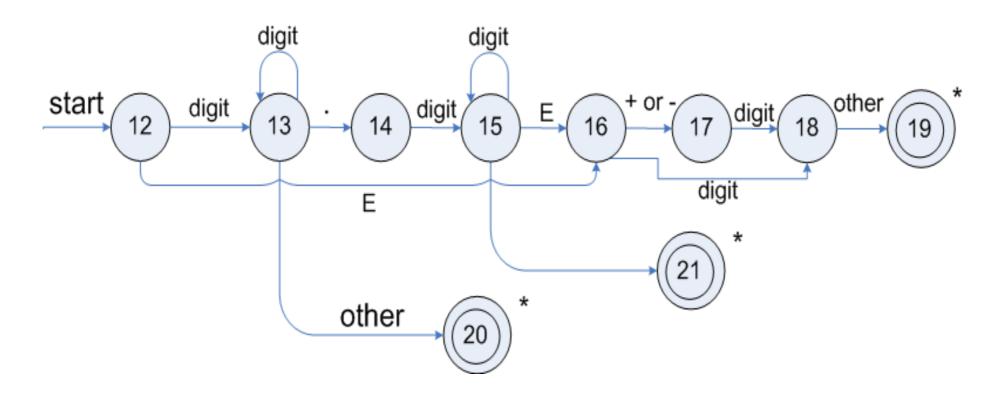
id → letter(letter|digit)*



Weoe accepted N>Oand have read other char that must be unread.

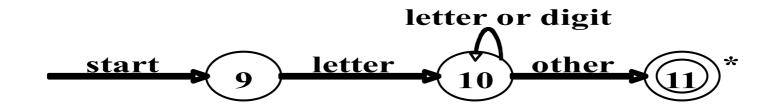
An additional character is read, that needs to be unread(return to input buffer





For unsigned numbers

id:



For identifiers

What to do for keywords?

- Use the "Identifier" token
- After a match, lookup the keyword table
- If found, return a token for the matched keyword
- If not, return a token for the true identifier

Recognising Tokens

Regular expressions provide specifications for the tokens in a language

Finite automaton is used to recognise a token - implementation

A finite automaton consists of

An input alphabet ¬

A set of states S

A start state n

A set of accepting states F = S

A set of transitions state cinput state

Finite Automaton

Deterministic Finite Automata (DFA)

One transition per input per state

No _{=n}-moves

Nondeterministic Finite Automata (NFA)

Can have multiple transitions for one input in a given state Can have __ moves

Finite automata have finite memory

Need only to encode the current state

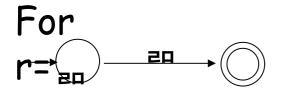
Conversion can be automated

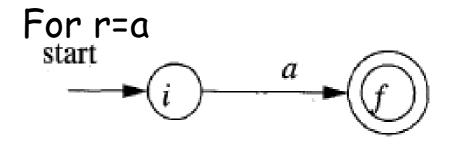
NFAs and DFAs recognize the same set of languages (regular languages)

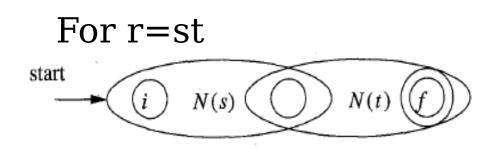
DFAs are easier to implement

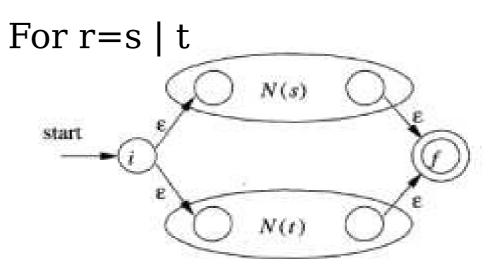
McNaughton-Yamada-Thompson Algorithm

For each kind of regular expression, define an NFA

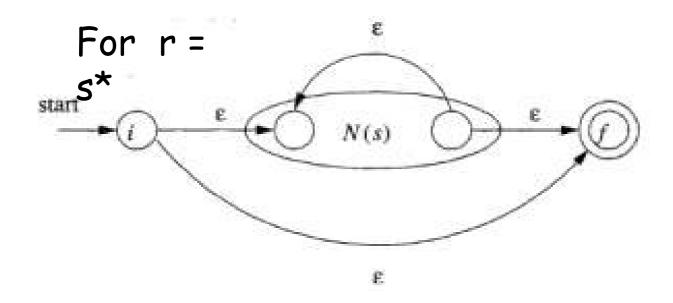




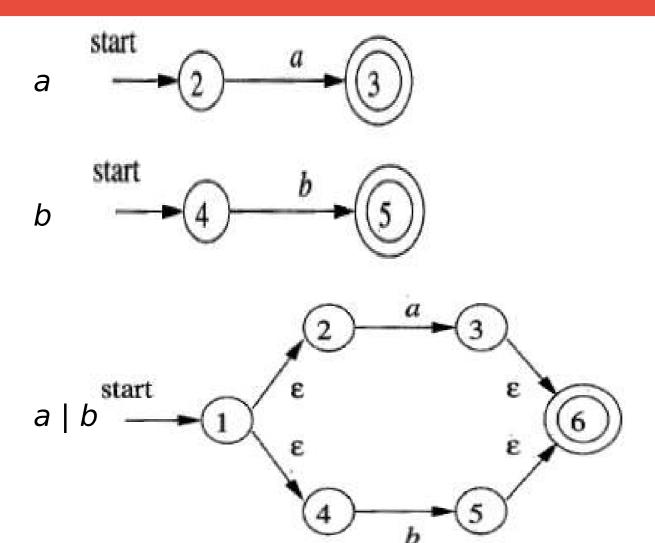




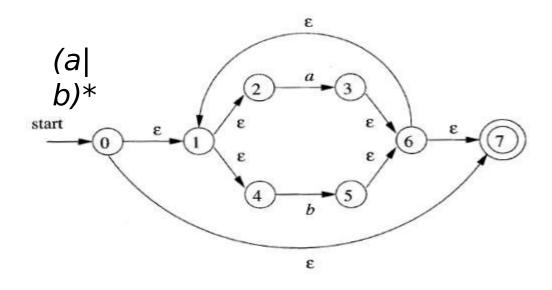
McNaughton-Yamada-Thompson Algorithm

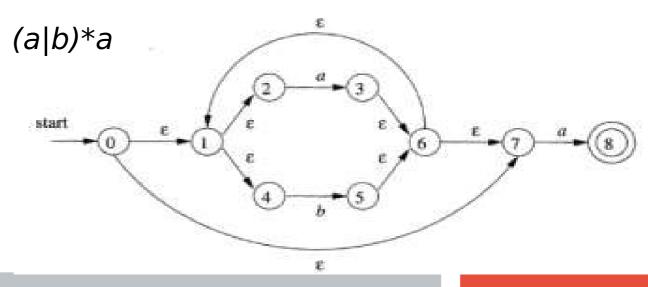


Example: (a|b)*abb



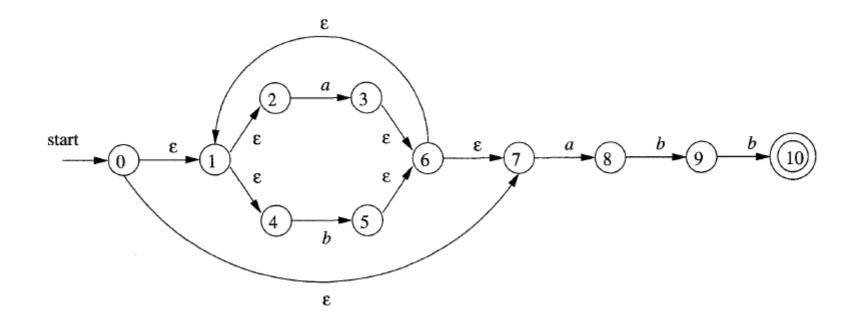
Example: (a|b)*abb





Example: (a|b)*abb

(a|b)*abb



Converting NFA to DFA

- Subset construction: each state of DFA corresponds to a set of NFA states
- For real languages NFA and DFA have approximately the same number of states (though not theoretically)

Definitions

OPERATION	DESCRIPTION
ϵ -closure(s)	Set of NFA states reachable from NFA state s
	on ϵ -transitions alone.
ϵ -closure (T)	Set of NFA states reachable from some NFA state s
	in set T on ϵ -transitions alone; = $\cup_{s \text{ in } T} \epsilon$ -closure(s).
move(T, a)	Set of NFA states to which there is a transition on
	input symbol a from some state s in T .

Simulating NFA

```
    S = ε-closure(s<sub>0</sub>);
    c = nextChar();
    while (c!= eof) {
    S = ε-closure(move(S, c));
    c = nextChar();
    }
    if (S ∩ F!= ∅) return "yes";
    else return "no";
```

Computing ε-closure

```
    Push all states of T onto stack;

    Initialize ε-closure(T) to T;

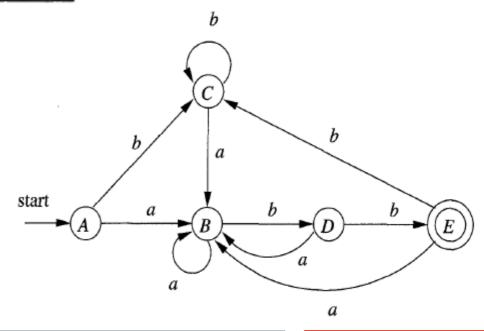
while (stack is not empty) {
    pop t, the top element of the stack
    for (each state u with an edge from t to u
         labeled ε)
     • if (u is not in ε-closure(T))
     • { add u to ε-closure(T))
     push u onto stack
```

Subset Constructions

```
initially, \epsilon-closure(s_0) is the only state in Dstates, and it is unmarked;
while ( there is an unmarked state T in Dstates ) {
      \max T;
      for (each input symbol a) {
             U = \epsilon-closure(move(T, a));
             if ( U is not in Dstates )
                    add U as an unmarked state to Dstates;
             Dtran[T, a] = U;
                                                           States of the
                                                           DFA we are
                                                           constructing
```

The resulting DFA

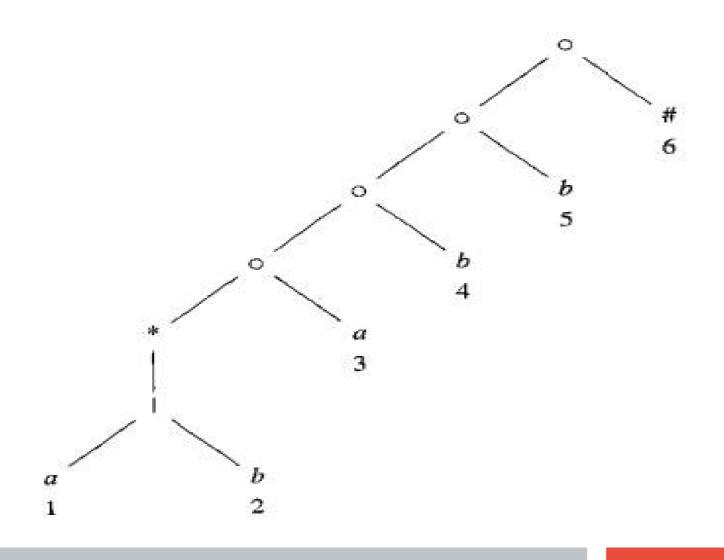
NFA STATE	DFA STATE	a	b
$\{0, 1, 2, 4, 7\}$	A	B	C
$\{1, 2, 3, 4, 6, 7, 8\}$	B	В	D
$\{1, 2, 4, 5, 6, 7\}$	C	B	C
$\{1, 2, 4, 5, 6, 7, 9\}$	D	B	E
$\{1, 2, 3, 5, 6, 7, 10\}$	E	B	C



Construction of DFA directly from RE

- Augment the regular expression r with a special end symbol # to make accepting states important
 - the new expression is r#
- Construct a syntax tree for r#
- Attach a unique integer to each node that is not labeled by ε

Syntax tree for regular expression (a|b)*abb

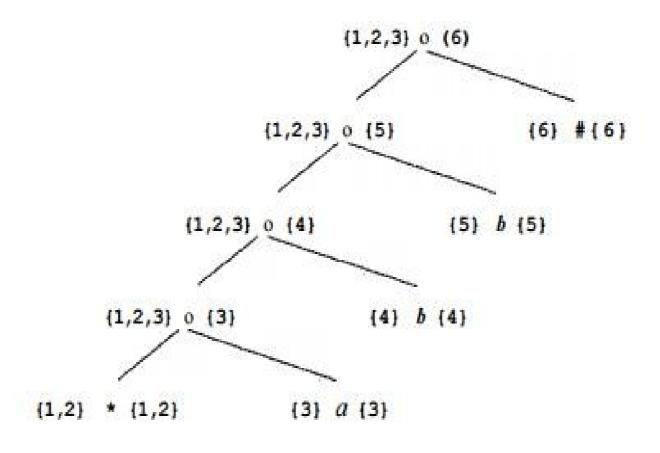


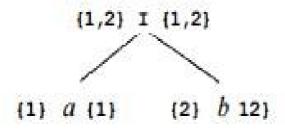
Annotating the tree

- Traverse the tree to construct functions nullable, firstpos, lastpos, and followpos
- For a node n, let L(n) be the language generated by the subtree with root n
- nullable(n): L(n) contains the empty string ε
- firstpos(n): set of positions under n that can match the first symbol of a string in L(n)
- lastpos(n): the set of positions under n that can match the last symbol of a string in L(n)
- followpos(i): the set of positions that can follow position i in any generated string

Computation of nullable, firstpos, lastpos

Node n	nullable(n)	firstpos(n)	lastpos(n)
Leaf ε	true	Ø	Ø
Leaf i	false	{ <i>i</i> }	$\{i\}$
ľ	$nullable(c_1)$	$firstpos(c_1)$	$lastpos(c_1)$
/ \	or	U	U
$c_1 c_2$	$nullable(c_2)$	$firstpos(c_2)$	$lastpos(c_2)$
· / \ c ₁ c ₂	$nullable(c_1)$ and $nullable(c_2)$	if $nullable(c_1)$ then $firstpos(c_1) \cup$ $firstpos(c_2)$ else $firstpos(c_1)$	if $nullable(c_2)$ then $lastpos(c_1) \cup \\ lastpos(c_2)$ else $lastpos(c_2)$
* c ₁	true	$firstpos(c_1)$	$lastpos(c_1)$



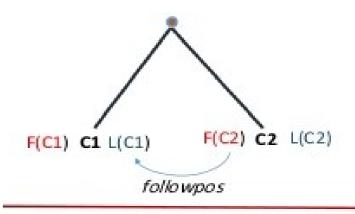


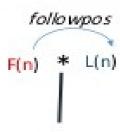
C(L|D)*LLS

- 1) Construct NFA and then DFA using subset construction
- 2) Construct DFA directly from the RE

Evaluating followpos

- Two-rules for followpos:
 - If n is concatenation-node with left child c_1 and right child c_2 , and i is a position in lastpos (c_1) , then all positions in firstpos (c_2) are in followpos(i).
 - If n is a star-node, and i is a position in lastpos(n), then all positions in firstpos(n) are in followpos(i).
- After computing firstpos and lastpos for each node, followpos of each position can be computed by making one depthfirst traversal of the syntax tree.





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NODE n	followpos(n)
1	{1,2,3}
2	{1,2,3}
3	{4}
4	{5}
5	{6}
6	0

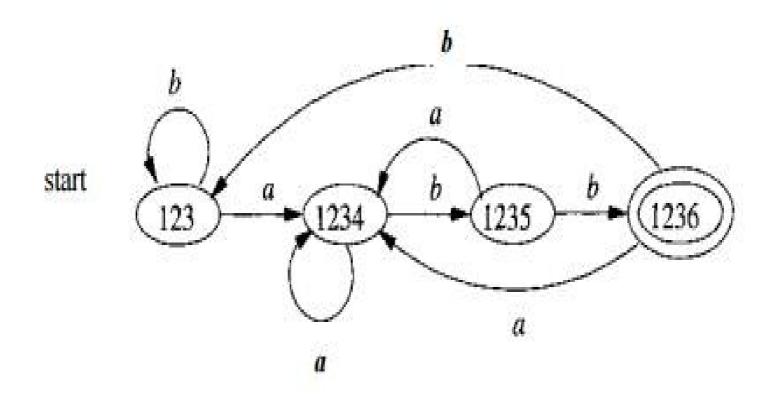
The Algorithm

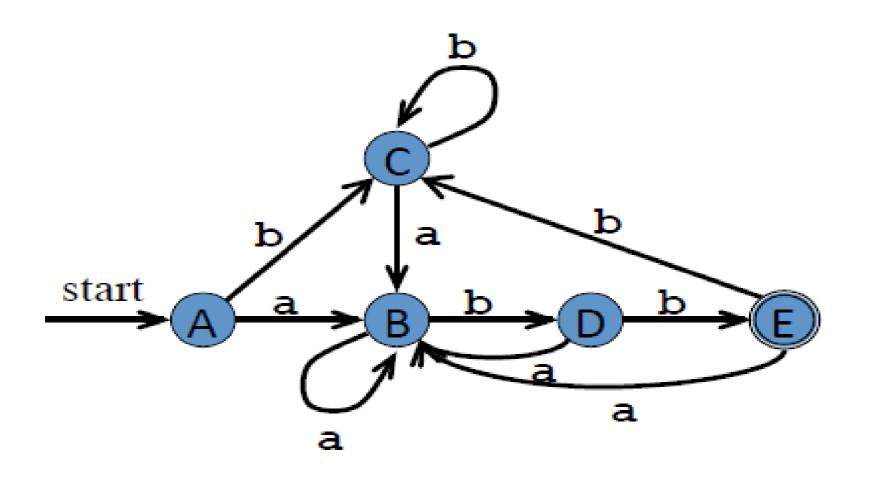
• Initialize Dstates to contain only the unmarked state firstpos(n_o), where n_o is the root of syntax tree T for (r) #

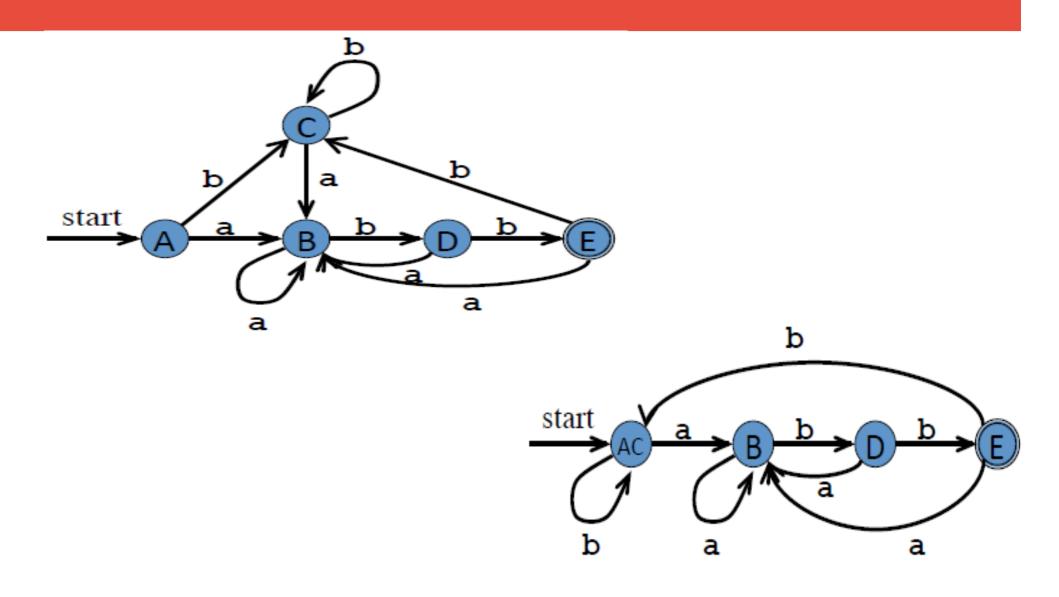
```
while (there is an unmarked state S in Dstates) {
   mark S;
   for (each input symbol a) {

    let U be the union of followpos(p) for all p in S

      that correspond to a;
    if (U is not in Dstates)
          add U as an unmarked state to Dstates; Dtran[S, a] = U;
```







Minimizing number of DFA states

• For any regular language, there is always a unique minimum state DFA, which can be constructed from any DFA of the language.

Algorithm:

Partition the set of states into two groups:

G 1 : set of accepting states

G 2 : set of non accepting states

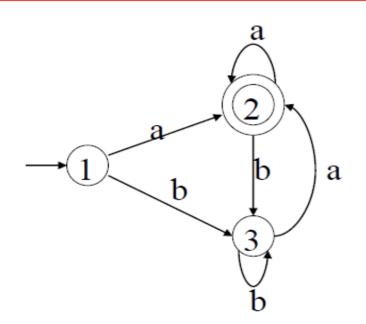
For each new group G

partition G into subgroups such that states s1 and s2 are in the same group, iff for all input symbols a, states s1 and s2 have transitions to states in the same group

Start state of the minimized DFA is the group containing the start state of the original DFA

Accepting states of the minimized DFA are the groups containing the accepting states of the original DFA.

Minimizing DFA – Example (1)



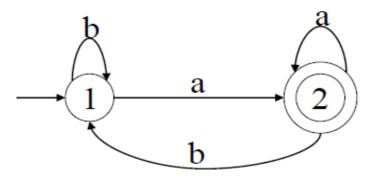
$$G_1 = \{2\}$$

 $G_2 = \{1,3\}$

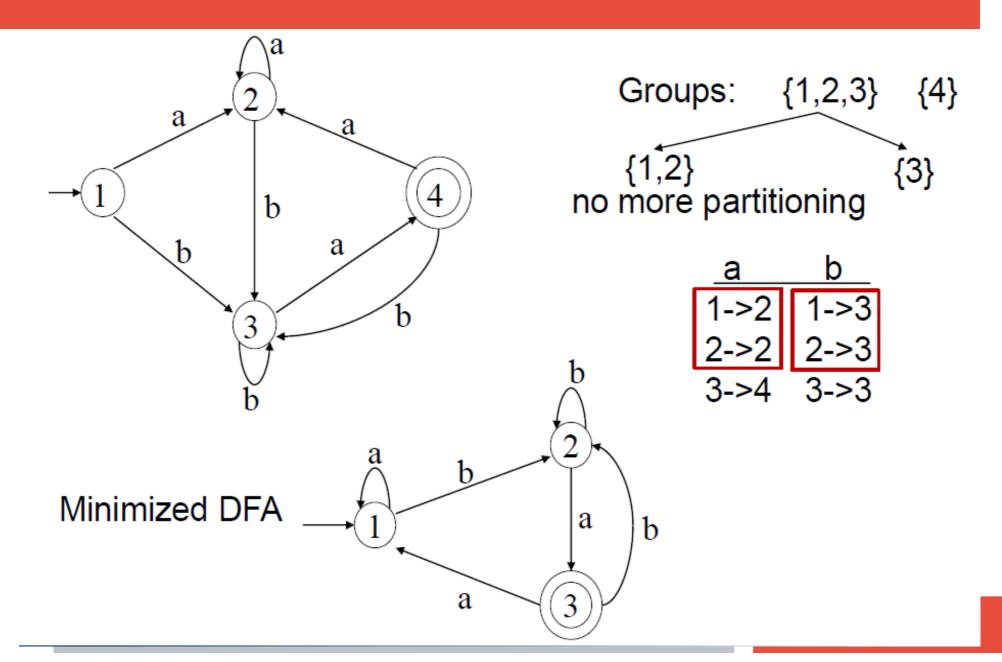
G₂ cannot be partitioned because

Dtran[1,a]=2 Dtran[1,b]=3 Dtran[3,a]=2 Dtran[3,b]=3

So, the minimized DFA (with minimum states) is



Minimizing DFA – Example (2)



Architecture of a Lexical Analyzer

