

Working Document for the Improvement to `nls()` GSOC project

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TODOS

- See how `dir` works in `nlsalt::numericDeriv()`; need some examples/tests

Abstract

`nls()` is the primary nonlinear modeling tool in base R. It has a great many features, but it is about two decades old and has a number of weaknesses, as well as some gaps in documentation. This document is an ongoing record of work under the Google Summer of Code 2021 of the first author. As such it is NOT meant to be a finished academic report, but a form of extended diary of activity, issues and results.

2021-5-18

By email, a Google Meet was set up for May 19 at noon Ottawa time. JN downloaded the latest version of `R-devel.tar.gz` and unpacked it into a directory `~/vmshare/R-devel` which is shared with a VirtualBox VM of Kubuntu 20.04 (Focal Fossa), a long-term support version of Linux. Opening a terminal inside this VM, it was possible to build and run this version of R.

```
cd /media/sf_vmshare/R-devel/  
./configure  
make  
sudo make install  
[admin password]  
R
```

This launched the development version of R correctly.

JN also set up this document.

Agenda for May 19

- check Meet is working
- introductions
- start linux VM install if an iso is available. May want to check that VirtualBox Guest additions is available and that the shared directory works, as these sometimes require some attention to permissions and ownership etc.
- Consider early goals to for possible `nls()` changes. See below.
- Set objectives for next two weeks
- Set next online meeting

Possible early goals

- Get a VM running under VirtualBox and install build tools. See <https://support.rstudio.com/hc/en-us/articles/218004217-Building-R-from-source> I did NOT need more than `./configure` in my build, as I am not building a server version.
 - Try the build. (Cheer loudly when it works!)
 - Explore and document the R source for `nls`-related code. In particular, we want
 - to list the files that have such code or calls to it
 - to note, if possible, what each does
 - to note, in particular, where `nls()` solves the Gauss-Newton equations, as we will want to modify these sections to augment them to allow a Marquardt stabilization.
 - to note, in particular, where `nls()` computes the Jacobian and/or Hessian for the nonlinear least squares problem. In package `nlsr`, there are tools that allow an expression for the model to be parsed and processed to compute the Jacobian using symbolic or automatic derivatives. This may or may not be feasible for `nls()`. However, we may be able to improve the approximation used.
- [2021-5-27] first draft `DerivsNLS.Rmd`. Note discovered “central” control for `numericDeriv()` function. It does NOT appear that the ‘`dir`’ control is actually used. This would likely change from forward to backward differences for SOME components of the step to compute first order finite difference approximation to the Jacobian.
- Augment this document to record what has been done and results or problems.
 - Add to the bibliography file specified. This is taken from another work, but as Rmarkdown only uses the references it needs, it will serve as a template.
 - AB can ask for pointers to references to add to this document or to subsidiary documents we will create as necessary to describe parts of the work if required.

[2021-5-25] Meet session. AB got Linux Mint 20.1 VM going and verified. SOME questions sorted out. JN added some material re: linear least squares solutions to the Variety document.

Some thoughts on how `nls()` code might be modified [JN: 2021-5-19]

- R-core will veto any changes that do not leave existing tests and examples as they are. Therefore we will be always thinking of ways to leave the default behaviour as it is now. In the relative offset convergence test that was causing small-residual problems to fail, JN suggested a small change to the test. In very simplified terms, the test is a ratio of (**new sum of squares**)/(**baseline sum of squares**) When both these quantities are small, we risk zero/zero situation. Therefore, a new control parameter `convTeestAdd` that has a default of 0 was introduced. This can be set in the `nls.control()` function. It is added to the denominator and allows the `nls()` function to complete satisfactorily when we have problems where the fit is nearly exact. Thus we are seeking similar modifications that are invoked by setting new control parameters to non-default settings to get new behaviour.
- In the material below on implementing nonlinear least squares, it should be possible to have a zero valued default for the Marquardt parameter λ . As long as this zero value is preserved, the legacy behaviour is used. Our decisions need to be careful in situations where we really do need the Marquardt stabilization. That is, should we simply fail (legacy behavior), should we override the legacy behaviour, since the user almost certainly does not want an avoidable failure, or should we seek an additional control that allows for more nuanced outcomes. Clearly thought is needed, and we will need to find some examples to illustrate our arguments.
- Note that `nls()` is a mix of several codes, using different solution tools. We will need to decide where our modifications apply and document carefully. JN opinion: we may want to postpone consideration

of “port” and “plinear” algorithms, but it would be useful to document what they do. The current documentation suggests that bounds on parameters can only be used with “port.”

- The derivative code to generate the Jacobian in `nls()` is (JN believes??) a simple forward-difference code. This may be in C rather than R. It is well-known that central differences, while they cost twice the computing effort, do a better job. Can we find a way to allow that easily?
- If there are bounds on parameters, the “step” taken in estimating differences may violate bounds. This is an issue well-known to workers in optimization, but not on the radar of most users. Clearly a “nasty.” Can we do anything to at least warn users in a way that is useful?

[2021-5-31] Notes on investigations

- 1) AB managed to get R built from an R-devel expanded tarball. JN had managed this earlier. There appear to be some transient glitches (HT has noted also). These are likely due to R-core members making trial changes. MASS package in particular noted.
- 2) Investigations of using subversion or git repo of the code so we can track any changes in files relevant to `nls()`. JN tried from <https://github.com/wch/r-source/wiki> which has some instructions. These seemed to work, but we note the need for `texinfo` and `git-svn` packages to be installed. Also standard “git pull” cannot be used. “git sv rebase” followed by “git svn fetch” tried and seem to work, but JN does not feel he understands what is going on.
- 3) Started to look into development of replacement code for parts of `nls()`. Created `ReplaceNLS.R` and `RestoreNLS.R` with the intention that `source()` of these files would replace the functions. However, first attempt, which simply added a `cat()` output to `numericDeriv()` function got

```
Error in numericDeriv(rexpr, theta, rho = weedenv) :  
  object 'C_numeric_deriv' not found
```

[2021-6-1] nlspkg package created

Thanks to Duncan Murdoch who created `nlspkg` from the R source files. This is a package version of the files in the source tree that will let us work with the code and change it. When we issue

```
library(nlspkg)
```

once we have installed it, the objects in the package will replace (mask) those in base-R.

To build `nlspkg`, I needed the `inconsolata.sty` font that is in the `texlive-fonts-extra` package of Linux Mint. In other systems, this font may reside elsewhere.

As of June 1, the package builds and mostly checks. There are two warnings:

- a number of function objects are NOT documented. We may or may not wish to add `man` files (of type `.Rd`). The list of objects is quite long, but they seem not to be needed by the user. Note that `nlminb` is present, likely for the PORT option of the “algorithm” parameter of `nls()`.
- There is a non-standard license specification. Checking in the Writing R Extensions manual (file `r-exts.pdf`), suggests dropping one of the two licenses listed (GPL-2 and GPL-3). Dropping the latter removed one warning.

The package `nlspkg` is to provide the EXISTING `nls()` functionality, while the package `nlsalt` is for our replacement. I plan to make this all-R. If we want to use C (or something else) later, then we will create another “alternate” package.

Note that each of these packages needs its own “project.” In Rstudio we choose to create a project using an existing directory (copy of that for `nlspkg`). This sets up the control files for the project and allows the package to be built and checked with the Rstudio tools. The umbrella `ImproveNLS` project handles the `git` version control.

[2021-6-1] nlsalt package mods started

numericDeriv first cut at pure R. JN incorporated C code into the R code of the numericDeriv function as comments, then tried to provide R statements to do what it appears the C is doing. Some steps and checks likely left out.

[2021-6-2] Converting codes to All-R – numericDeriv

In the `ExDerivs.R` script, JN tested a forward difference code in R against a call to `numericDeriv()`. On a single example, it tests OK, so next step is to modify `nls.R` in package `nlsalt`.

Note that `ExDerivs.R` is in flux. “Old” tests will be commented out. Look for the double question mark (??) for things that may need to be checked.

Some concerns:

- the code requires us to `get()` and `assign()` values in the environment `rho` that is used to evaluate the nonlinear residual functions. There may or may not be ways to make this more efficient.
- the C code uses explicit loops. A very preliminary use of R’s vectorization in the difference between two residual vectors (i.e., without subscripts or looping) worked fine, but there are almost certainly further optimizations. By contrast, we MAY want to leave either explicit loops or commented code that contains such loops as a way to provide explanation of what is happening.

The code from the trials in `ExDerivs.R` was ported to `nls.R` in `nlsalt` package and tested with `TestnumericDeriv1.R` (added to repo). Things seem to work OK. I have NOT tried changing `dir`. ??

[2021-6-4]

- Code for `numericDeriv()` in `nls.R` was extracted to `numericDeriv20210603CommentedWithC.txt`.
- The code for `numeric__deriv` was removed from `nls.c`
- The line in `init.c` that mentions `numeric__deriv` was commented out so it would not be linked into the shared library for `nlsalt` (`nlsalt.so`)
- By launching Rstudio from the `nlsalt.Rproj` file, the package `nlsalt` could be rebuilt using “clean and rebuild.” `nlsalt.Rproj` can be initiated from the “Files” menu of Rstudio. Note that rebuild is probably necessary on each machine on which `nlsalt` is used. (?? Do we need to check this is the case?)

[2021-6-5]

- created script `tnlsModel.R` as first step to create and produce an “m” object
- Current understanding (JN): `nlsModel` (and `nlsModel.plinear` too probably) creates an R object that it labels as class “`nlsModel`.” This object contains functions that are called from `nls.c::nls__iter` to run the iteration and estimate the parameters in the model. There seem to be some extraneous functions, and we can hopefully learn enough to remove the extras.
- The current structure is to particularize the functions in “m” so the (essentially) external `nls.c` code acts on these. As a first goal, and part of learning how things work, we will want to replace the `nls.c::nls__iter` with all-R equivalent.
- Started document `nlsModel.Rmd` to document this function. ?? AB: in our documents, I am currently copying and pasting material. However, it would be sensible to do an “include” of the material from the `nlsalt` package, but to do that cleanly, we will want to separate the functions into different files. This will mean we have to be careful that the package still builds OK.

From `nlsr vignette nlsr-devdoc.Rmd` [2021-5-23 onwards]

[2021-6-6]

Wanted package benchmarkme.

install failed. Needed dependencies.

So in linux, install `libssl.dev libcurl4-openssl-dev`

Then benchmarkme installed OK.

We can use this within our benchmarking in addition to `sessionInfo()`.

[2021-6-6] → [2021-6-11]

Had online meeting and got Rstudio more or less set up to deal with version control and package building, BUT ...

hit a big problem with 32 bit Windows architecture NOT linking to BLAS. A posting to R-package-devel list got a suggestion from Dirk Eddelbeutel to check `sessionInfo()` and this shows that on the Windows R side, BLAS and LAPACK are not listed, while they are in Linux. Duncan Murdoch pointed to `makevars.win`, but several tries with some possible `PKG_LIBS` settings did not give any change. Noted that command line `CMD.exe` use of “R CMD build” and “R CMD INSTALL” showed the issue to be at the INSTALL stage, and it is clear that the 32 bit architecture is NOT finding the BLAS routines, but

Then found <https://stackoverflow.com/questions/42118561/error-in-r-cmd-shlib-compiling-c-code> and this shows what to use for `makevars.win`, which is the single line file

```
PKG_LIBS = $(LAPACK_LIBS) $(BLAS_LIBS) $(FLIBS)
```

[2021-6-12] → [2021-6-14]

Document `PkgFromRbase` written to document the packaging effort and report on the `Makevars.win` issue.

JN diverted to update `optimx` package.

[2021-6-15] chunk code from file

The **R Markdown Cookbook** is quite useful in giving hints on some features of R Markdown. In particular, sections 16.1 to 16.3 of

<https://bookdown.org/yihui/rmarkdown-cookbook/>

show how to use R scripts saved in files within chunks of R Markdown documents. This is important, as we may wish to list such files, but copying the script into the text of the document means that this copy and the original file can become unsynchronized.

From work on the Gramps genealogy software (and some local setup issues), JN found that the following chunk will allow listings in a nice format. Note the “comment=NA” to avoid line prefixing with hash symbols. The code which follows needs surrounding by the usual three ticks before and after.

```
{r lscript, comment=NA, echo=FALSE}
cat(readLines('/home/gramps/GrampsSetup/FrohnGramps'), sep = '\n')
```

[2021-6-15] - [2021-6-20]: `nlsalt` issues

- 1) Need to ensure the name “nlsalt” is fixed DESCRIPTION, NAMESPACE (dynload line), .gitignore (.so line can be *.so), `init.c` (dynload line, `R_init` line)
- 2) appears new all-R `numericDeriv` not quite right for all nls examples. Probably (to be determined??) whether example uses a function or expression in the definition of the model.

«««< HEAD During this time did some work on splitting nls.R into separate files where major functions were in their own file. In particular, nlsModel() was separated out so that nlsModel and nlsModel.plinear did not get confused in editing, since they are largely the same.

The file `nls-noc.R` has the ongoing work to try to build an all-R `nls_iter` function. This is gradually proceeding, but not functional at the time of our June 21 online meeting.

JN took a brief look at 2010 UseR! tutorial on nonlinear models. This may give us some ideas for documentation and tests.

Week of [2021-6-21]

Online meeting on June 21 talked about `nls-noc.R` as well as testing schemes. AB will try to develop a short appraisal of testing schemes and suggest a path for us. Some discussion of tools.

JN started `nlsModelDoc.Rmd`. There are many functions, seemingly without documentation. Also quite complex codes and reuse of names. In some codes the “«-” assignment is used. We will need to be very careful to document and understand this. ===== ### [2021-6-21] Meeting etc.

Met online.

- discussed testing schemes. AB will see if he can develop a short appraisal and suggestions for our use.
- talked about `nls-noc.R` process. This is ongoing by JN
- later in day, JN contacted Doug Bates to ask if there are developer notes or other information, as there seem to be extra features in the `nlsModel()` output and the `nls_iter` code in `nls.c`

[2021-6-22] Answering some of the TODOS / nls-noc.R / nlsModelDoc.Rmd

- Do we need to update `nlsalt` and `nlspkg` separately from `improvenls` on a machine when there are changes imported via git? Answer is that git within `improvenls` directory seems sufficient.
- response from Doug Bates. Added him to gitlab project.
- Expanded document `nlsModelDoc.Rmd` to show what different objects created actually do. There are still plenty of questions, especially about `setPars()`.
- AB: in our documents, I am currently copying and pasting material. However, it would be sensible to do an “include” of the material from the `nlsalt` package, but to do that cleanly, we will want to separate the functions into different files. This will mean we have to be careful that the package still builds OK.

This can be accomplished via (following commented in the `Rmd` file). Note that the issue is addressed in several ways in `/home/gramps/GrampsSetup/GrampsSetup.Rmd`, which needs to be better explained here.

<https://towardsdatascience.com/rtest-pretty-testing-of-r-packages-50f50b135650>

<https://towardsdatascience.com/unit-testing-in-r-68ab9cc8d211>

<https://r-pkgs.org/tests.html>

JN contacted Doug Bates who indicated he may be able to provide some input on the code. There does not appear to be any developer documentations. Ongoing work with `nlsModel()` seems to indicate that the “m” object is set up to provide all the infrastructure for the rest of the code to work with for a particular nonlinear model.

[2021-6-23] [2021-6-24] Tidying

- JN cleaned up `DerivsNLS`. Extracted `ssasymptot` model and tested in `nlsalt`. `numericDeriv` must be working, but not explicitly tested. Note that the encapsulated version in the examples of `nls()` seem to fail.??

- used file import of nls.R and nls.c parts (which are now separated out in improvnls)
- nlsModelDoc proceeding slowly. There are many undocumented features and pieces of code in nlsModel() that need careful understanding, particularly the scoping assignment “«-” in some lines of the code. In minpack.lm there is a version of nlsModel() that uses assign rather than <<-, and some documentation points out that this may be a more explicit mechanism (and therefore easier to understand and keep correct). Note the R documentation ?assignOps as well as the assign() and get() functions.
-

=====end diary only portion =====

5. Implementation of nonlinear least squares methods

This section is a review of approaches to solving the nonlinear least squares problem that underlies nonlinear regression modelling. In particular, we look at using a QR decomposition for the Levenberg-Marquardt stabilization of the solution of the Gauss-Newton equations.

Gauss-Newton variants

Nonlinear least squares methods are mostly founded on some or other variant of the Gauss-Newton algorithm. The function we wish to minimize is the sum of squares of the (nonlinear) residuals $r(x)$ where there are m observations (elements of r) and n parameters x . Hence the function is

$$f(x) = \sum_i (r_i^2)$$

Newton’s method starts with an original set of parameters $x[0]$. At a given iteration, which could be the first, we want to solve

$$x[k+1] = x[k] - H^{-1}g$$

where H is the Hessian and g is the gradient at $x[k]$. We can rewrite this as a solution, at each iteration, of

$$H\delta = -g$$

with

$$x[k+1] = x[k] + \delta$$

For the particular sum of squares, the gradient is

$$g(x) = 2 * r[k]$$

and

$$H(x) = 2(J'J + \sum_i (r_i * Z_i))$$

where J is the Jacobian (first derivatives of r w.r.t. x) and Z_i is the tensor of second derivatives of r_i w.r.t. x). Note that J' is the transpose of J .

The primary simplification of the Gauss-Newton method is to assume that the second term above is negligible. As there is a common factor of 2 on each side of the Newton iteration after the simplification of the Hessian, the Gauss-Newton iteration equation is

$$(J'J)\delta = -J'r$$

This iteration frequently fails. The approximation of the Hessian by the Jacobian inner-product is one reason, but there is also the possibility that the sum of squares function is not “quadratic” enough that the unit step reduces it. Hartley (1961) introduced a line search along delta, while Marquardt (1963) suggested replacing $J'J$ with $(J'J + \lambda * D)$ where D is a diagonal matrix intended to partially approximate the omitted portion of the Hessian.

Marquardt suggested $D = I$ (a unit matrix) or $D = (\text{diagonal part of } J'J)$. The former approach, when λ is large enough that the iteration is essentially

$$\delta = -g/\lambda$$

gives a version of the steepest descents algorithm. Using the diagonal of $J'J$, we have a scaled version of this (see https://en.wikipedia.org/wiki/Levenberg%E2%80%93Marquardt_algorithm; Levenberg (1944) predated Marquardt, but the latter seems to have done the practical work that brought the approach to general attention.)

Nash (1977) found that on low precision machines, it was common for diagonal elements of $J'J$ to underflow. A very small modification to solve

$$(J'J + \lambda(D + \phi I))\delta = -g$$

where ϕ is a small number avoids most of these conditions. $\phi = 1$ seems to work quite well. We note that this modification would likely not have been recognized had I not been working on machines with mediocre floating-point arithmetic – a little more than 6 decimal digits of precision and no extended precision.

Choices

Both `nlsr::nlxb()` and `minpack.lm::nlsLM` use a Levenberg-Marquardt stabilization of the iteration described above, with `nlsr` using the modification involving the ϕ control parameter. The complexities of the code in `minpack.lm` are such that I have relied largely on the documentation to judge how the iteration is accomplished. `nls()` uses a straightforward Gauss-Newton iteration, but rather than form the sum of squares and cross-products, uses a QR decomposition of the matrix J that has been found by a forward difference approximation.

(Nash (1979)), solving

$$(J^T J + \lambda D)\delta = -J^T r$$

where D is some diagonal matrix and λ is a number of modest size initially. Clearly for $\lambda = 0$ we have a Gauss-Newton method. Typically, the sum of squares of the residuals calculated at the “new” set of parameters is used as a criterion for keeping those parameter values. If so, the size of λ is reduced. If not, we increase the size of λ and compute a new δ . Note that a new J , the expensive step in each iteration, is NOT required.

As for Gauss-Newton methods, the details of how to start, adjust and terminate the iteration lead to many variants, increased by different possibilities for specifying D . See Nash (1979).

Using matrix decompositions [2021-5-23 onwards]

In Nash (1979), the iteration equation was solved as stated. However, this involves forming the sum of squares and cross products of J , a process that loses some numerical precision. A better way to solve the linear equations is to apply the QR decomposition to the matrix J itself. However, we still need to incorporate the

λI or λD adjustments. This is done by adding rows to J that are the square roots of the “pieces.” We add 1 row for each diagonal element of I and each diagonal element of D .

In each iteration, we reduce the λ parameter before solution. If the resulting sum of squares is not reduced, λ is increased, otherwise we move to the next iteration. Various authors (including the present one) have suggested different strategies for this. My current opinion is that a “quick” increase, say a factor of 10, and a “slow” decrease, say a factor of 0.2, work quite well. However, it is important to check that λ has not got too small or underflowed before applying the increase factor. On the other hand, it is useful to be able to set $\lambda = 0$ in the code so that a pure Gauss-Newton method can be evaluated with the program(s). The current code `nlfb()` uses the line

```
if (lamda<1000*.Machine$double.eps) lamda<-1000*.Machine$double.eps
```

to ensure we get an increase. To force a Gauss-Newton algorithm, the controls `laminc` and `lamdec` are set to 0.

The Levenberg-Marquardt adjustment to the Gauss-Newton approach is the second major improvement of `nlslr` (and also its predecessor `nlmrt` and the package `minpack-lm`) over `nls()`.

`nls()` attempts to minimize a sum of squared residuals by a Gauss-Newton method. If we compute a Jacobian matrix J and a vector of residuals r from a vector of parameters x , then we can define a linearized problem

$$J^T J \delta = -J^T r$$

This leads to an iteration where, from a set of starting parameters x_0 , we compute

$$x_{i+1} = x_i + \delta$$

This is commonly modified to use a step factor `step`

$$x_{i+1} = x_i + \text{step} * \delta$$

It is in the mechanisms to choose the size of `step` and to decide when to terminate the iteration that Gauss-Newton methods differ. Indeed, though I have tried several times, I find the very convoluted code behind `nls()` very difficult to decipher. Unfortunately, its authors have now (as far as I am aware) all ceased to maintain the code.

We could implement the methods using the equations above. However, the accumulation of inner products in $J^T J$ occasions some numerical error, and it is generally both safer and more efficient to use matrix decompositions. In particular, if we form the QR decomposition of J

$$QR = J$$

where Q is an orthonormal matrix and R is Right or Upper triangular, we can easily solve

$$R\delta = -Q^T r$$

for which the solution is also the solution of the Gauss-Newton equations. But how do we get the Marquardt stabilization?

If we augment J with a square matrix $\sqrt{\lambda D}$ whose diagonal elements are the square roots of λ times the diagonal elements of D , and augment the vector r with n zeros where n is the column dimension of J and D , we achieve our goal.

Typically we can use $D = I_n$ (the identity of order n), but Marquardt (1963) showed that using the diagonal elements of $J^T J$ for D results in a useful implicit scaling of the parameters. Nash (1977) pointed out that

on computers with limited arithmetic (which now are rare since the IEEE 754 standard appeared in 1985), underflow might cause a problem of very small elements in D and proposed adding ϕI_n to the diagonals of $J^T J$ before multiplying by λ in the Marquardt stabilization. This avoids some awkward cases with very little extra overhead. It is accomplished with the QR approach by appending $\sqrt{\phi\lambda}$ times a unit matrix I_n to the matrix already augmented matrix. We must also append a further n zeros to the augmented r .

[2021-5-27] JN added some notes on LU and Cholesky to “Variety” document.

===== End of extract on approaches to solving Gauss Newton equations =====

Early explorations and setup of project [2021-5-24]

This is essentially a diary entry. (?? AB you may want to add some notes too.)

- AB working to secure his computer, set up VirtualBox and prepare a linux guest VM
- AB has been looking at documents JN posted. Gitlab repo seems to be working OK. On comment from HT, JN discovered (very overdue!) that Rstudio support for git is very useful.
- JN set up nls-flowchart.txt for use by team. This is looking at R-devel.tar.gz downloaded May 18, 2021. It is likely we can use any recent version, though at some point we may need to be more precise. The purpose of this is to describe what is going on in the nls() operations.
- JN added document **VarietyInNonlinearLeastSquaresCodes.Rmd**. This is tangential to the project, but is an attempt to provide a panorama of the different ways in which nonlinear least squares software has been set up over the years. JN will respond to questions from other team members to try to make this explanatory document helpful in understanding the existing nls() code and proposed changes.
- Section added above “From nlsr vignette nlsr-devdoc.Rmd”
- In the “VarietyInNonlinearLeastSquaresCodes.Rmd” document, JN added a section on different approaches to solving LINEAR least squares problems, since the inner iteration of almost all nonlinear least squares methods involves such a sub-problem. AB has been looking at this. It is currently a messy DRAFT section at 2021-5-25.
- Meet scheduled for May 25;

Attempts to understand numericDeriv() [2021-5-24 to 27]

JN has found it quite difficult to get a good understanding of the `numericDeriv()` function that appears in `nls.R` and calls material in `nls.c`. That this has proved difficult to use suggests the documentation is less than wonderful. However, the main reason is to set up tests and timings and compare to other approaches to computing the Jacobian in nonlinear least squares. ??Gut feeling: `numericDeriv` is really only set up to compute a Jacobian. ?? Note: there is a “central” option. Can this be used with `nls()`? Why or why not?

A file `ExDerivs.R` has been added to the repo.

[2021-5-26] JN sorted out one approach that allows `numricDeriv`, `nlsr::model2rjfun` and `numDeriv::jacobian` to be compared. [2021-5-27] `DerivsNLS.Rmd` first draft done. Problems with `system()` and `system2()` and calling `bash` from `rmarkdown` document led to email sent to Yihui Xie, as the output of a Linux command (`inxi -F`) to get machine properties was returned with extra characters.

Tangential issues raised during the project

Output from bash scripts in rmarkdown files

In trying to capture the output of the Linux command-line program `inxi` (which reports hardware and software information), JN found `rmarkdown` failed to knit correctly.

```
system('inxi -F >t.txt')
```

and

```
system2("inxi -F >tlinux.txt")
```

both failed, as did specifying the chunk as `{bash inxi2}` and trying `inxi -F >t2.txt`.

The outputs had strange characters that were indecipherable by the LaTeX processor and caused a crash. Indeed files of substantially differing sizes were generated.

We also tried

```
system2("inxi," -F," stdout="tlinux2.txt")
```

The issue was reported on `community.rstudio`.

`\url{https://community.rstudio.com/t/bash-output-causes-trouble-for-latex-and-hence-no-pdf/106502}`

where a workaround is reported. This puts the `inxi` command in a script which uses the preamble ``#!/bin/sh``. That is, we use the ``sh`` shell. For example, let us call it `myscript.sh` and it contains

```
#!/bin/sh # myscript.sh – push hw info to thw.txt one directory above inxi -F >../thw.txt echo “done”
```

This command script is then run from R using

```
system(“mate-terminal -e ./myscript.sh”) ““
```

JN tested this with `mate-terminal`, `xterm` and `konsole` as the terminal programs.

References

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