Improvement to nls(): Solution to Tests(Easy)

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Theory:

The logistic sigmoid growth curve is given by -

$$y = f(t) = \frac{L}{1 + e^{-k(t - x_0)}}...(\Delta)$$

Here, the growth y = f(t) is a function of time t.

 x_0 : the x value of the sigmoid's midpoint.

L: the curve's maximum value.

k: the logistic growth rate or steepness of the curve.

Now, given the test data, we need to estimate a logistic sigmoid growth curve of the form as in Eq. Δ .

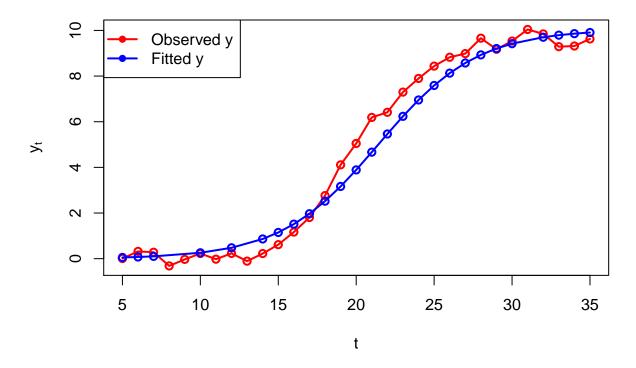
R Code:

```
### "Improvements to nls()" - GSOC'21
## Easy
# test data
time <- c( 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16,
17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29,
30, 31, 32, 33, 34, 35)
y \leftarrow c(0.0074203, 0.3188325, 0.2815891, -0.3171173, -0.0305409, 0.2266773,
  -0.0216102, 0.2319695, -0.1082007, 0.2246899, 0.6144181, 1.1655192,
  1.8038330, 2.7644418, 4.1104270, 5.0470456, 6.1896092, 6.4128618,
 7.2974793, 7.8965245, 8.4364991, 8.8252770, 8.9836204, 9.6607736,
  9.1746182, 9.5348823, 10.0421165, 9.8477874, 9.2886090, 9.3169916,
  9.6270209)
# Plot y vs. time
plot(time,y,xlab="t",ylab=expression(y[t]),
main="Plot of Observed and Fitted y against Time", lwd=2, col="red", type="o")
# clean the data
time <- time [y>=0]
```

```
y \leftarrow y[y \ge 0]
## Approximate estimation of x0,k, L based on above plot
#approximate value of x0
x0 <- mean(time)</pre>
# approximate value of L
L < -max(y)
\# approximate value of k
# we remove y for which ln(L/y-1) is NA
time<-time[-which(L/y<=1)]</pre>
y < -y[-which(L/y <= 1)]
k \leftarrow log(L/y-1)/(x0-time)
k<-mean(k)
# plot of the fitted values
lines(time, L/(1+exp(-k*(time-x0))),type="o",lwd=2,col="blue")
legend("topleft",legend=c("Observed y","Fitted y"),
col=c("red","blue"),lwd=2,,pch=16)
# print the parameter values
cat("The estimated value of x0 is : ",x0,"\n")
cat("The estimated value of L is : ",L,"\n")
cat("The estimated value of k is : ",k,"\n")
```

Output:





The estimated value of x0 is : 21.44444

The estimated value of L is : 10.04212

The estimated value of k is : 0.3175419

Explanation:

We first plot the graph to know how the given y's look as a function of time. Since, the logistic function is strictly positive, I first discard the negative y values from the data and the corresponding time points. Then, to estimate x_0 we take the mean of the time points as the mid-value of y should correspond to the mid-value of time.Now, L being the maximum value of the growth curve, I take L to be the maximum of the given y's. Finally, given y, time and estimated x_0 , L, I compute k's by plugging these values in Eq. Δ and then take the mean of the resulting vector of k's.

Using the above procedure, my estimated logistic growth function is -

$$\hat{y} = \hat{f}(t) = \frac{10.04212}{1 + e^{-0.3175419(t - 21.44444)}}$$