Application of LSTM Neural Networks and Complex Network Analysis for Earthquake Forecasting in Colombia

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Abstract

Earthquakes are unpredictable and high-risk events that can cause significant human casualties and infrastructure damage. In recent years, there has been a surge in research on earthquake forecasting using machine learning and neural networks, yielding impressive results. This study addresses the earthquake forecasting problem by applying Long Short-Term Memory (LSTM) Neural Networks to historical seismic events along Colombia's Pacific coast, using data from the United States Geological Survey. We analyzed the seismic catalog over time, incorporated complex network features for each dataset, and trained multiple LSTM neural networks with hyper-parameter tuning. Features such as latitude, longitude, magnitude, days elapsed between events, and complex network properties were used. Models utilizing only earthquake features achieved 60-70% accuracy for 2-quantile classification, while models incorporating complex network features achieved similar accuracy for 3-quantile classification. These results are promising and offer a new perspective on the use of complex networks in earthquake forecasting.

Keywords: Earthquake Forecasting, LSTM Neural Networks, Machine Learning, Complex Networks

1 Introduction

Earthquakes are classified a high risk event due to their unexpected nature and the limited time available to take preventive actions. Furthermore, the earthquakes may cause the human casualties and infrastructure damage. Over the past few years, numerous papers have explored the use of machine learning algorithms and neural networks for earthquake forecasting [1–6]. The growing interest in the use of machine learning has been documented, as well as the use of artificial intelligence to forecast seismic events, indicating future work and various challenges to be addressed.

One approach involves the application of deep neural networks to learn from data directly to identify complex patterns. However, forecasting features such as magnitude is limited by the lack of events that exceed certain thresholds. A more promising approach uses a set of different characteristics and regions as input to the neural network in a moving window of time [7].

Some of the documented features in literature are magnitude, frequency of events [8–12], occurrence of aftershocks [13], probability of detection and rate of false alarms [14], geomagnetic field variation, soil temperature and relative humidity [15], seismic indicators [16], location [17], Gutenberg-Richter b-value [18–20], gravity, georesistivity and water level [21], elapsed days, mean magnitude, mean time between characteristic events, coefficient of variation of the mean time [22], and electronic signals captured on seismographs [23–28].

Artificial intelligence and machine learning algorithms are powerful tools for addressing a wide range of classification and forecasting problems. They have the potential to learn from hidden patterns within the provided data [6]. As seen in [6, 23], their application in earthquake forecasting is useful for risk assessment and early prevention.

In [4], it is stated that studies in seismology are carried out for the following objectives: actions to reduce long-term disasters generated by earthquakes, preparation and adjustment to disasters, disaster response strategies, and post-disaster recovery planning. According to Satriano et al. [29], information systems focused on the early warning of seismological events must quickly and reliably provide information on different parameters such as location, time, and size to improve emergency response. Espinosa et al. [30] mention that the Mexican SAS (seismic alert system), an early warning system implemented in Mexico, has allowed seismic waves to be detected up to 60 seconds in advance, a time frame that allows security procedures to be executed to protect equipment susceptible to damage, such as power plants, computer systems, and communication networks.

Additionally, there has been increasing interest in representing data through graphs, as complex relationships can be modeled using nodes and edges [31]. Earthquakes can be modeled as a complex network, representing locations as nodes and sequences as edges [32]. Learning from these structures has been successfully applied in particle interaction, recommendation systems, molecular properties, natural language processing, and other fields [33].

As stated by León et al. [32], representing seismological events as complex networks allows for the study of seismicity in a region and helps to unravel the relationships among these events. Earthquake networks are based on the temporal sequence of

events and their specific locations. Different network features, such as path length, degree distribution, and clustering, help define the relationships between events, hubs, and small-world network properties. Thus, integrating the analysis of complex networks to structure the relationships between seismic events seems to be helpful in improving forecast results.

In this study, we processed earthquake data from Colombia and trained LSTM neural network models. The models achieved 60-70% accuracy for 2-quantile classification and similar accuracy for 3-quantile classification when using complex network features. These findings suggest that complex networks can enhance earthquake forecasting.

2 Methods

In this section, we take a look at the training and test data, and the steps to generate the earthquake features used later for training.

The earthquake events used in this study were obtained from the U.S. Geological Survey (USGS) for the Colombian region, with latitudes ranging from -0.132° to 9.796° and longitudes from -80.343° to -72.466°. The events are plotted by magnitude and depth in **Figure 1**. The retrieved dataset contained 5462 events since 1975, which was reduced to 4042 events after processing. The data cleaning process involved removing empty values, converting string values to numerical values for certain features, and filtering out events that were not validated by multiple sources, had missing data points, or had zero values. The selected events were of the mb type, representing the body wave magnitude, and included the depth of the event.

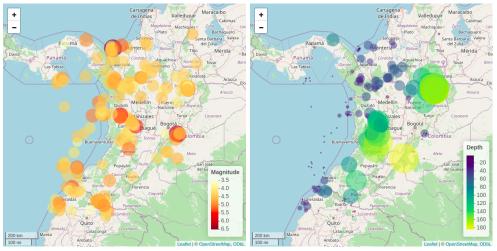
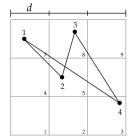


Fig. 1 Earthquake events visualization by Magnitude (left) and Depth (right)

2.1 Earthquake Networks

Following the methodology proposed by Leon et al. [32], constructing an Earthquake Complex Network involves dividing the selected geographical area into a grid of cells,

we'll call them nodes from now on, each representing a specific distance in kilometers. Sequential earthquake events are then used to establish connections between these nodes, forming the network. In 2 we can see a diagram of the process of creating an earthquake network.



t	latitude	longitude		node
1	lat_1	$long_1$		7
2				5
3				8
4				3
o_node	(latitude,	longitude)	\Rightarrow	n

Fig. 2 Quick overview of the creation of an earthquake network. A geographical region is divided into nodes of equal size in kilometers, then each event is clasified in each node by its latitude and longitude, we later connect each node by the time sequence of the events. We can observe nodes 7, 5, 8, 3 are connected in that order, first (7,5), then (5,8), and finally (8,3).

2.2 Dataset

After processing and cleaning the data, we assigned each earthquake event to a node based on its geographical location. We then normalized the features to ensure they were consistent and comparable across the dataset. To analyze the data at different levels of detail, we divided the features into 2, 3, and 4 quantiles. Next, we created the sequences needed for training the LSTM network. This involved generating rolling windows of events, where each window contained a sequence of features used as input to the model, and a feature of the following event as the target.

Table 1 Dataset Statistics

Feature	Min	Max	Median	Mean	SD	Variance	Range
Latitude	-0.13	9.79	6.73	5.73	2.08	4.31	9.92
Longitude	-80.34	-72.47	-75.68	-75.55	2.49	6.20	7.88
Depth	0.00	436.50	68.10	89.68	65.50	4290.78	436.50
Magnitude	0.00	7.80	4.40	4.19	0.99	0.97	7.80

Resume of the features used in the dataset, we can see the minimum, maximum, median, mean, standard deviation, variance, and range of the features.

Following the methodology proposed by Lin et al. [34], multivariate time-series forecasting involves using a rolling window approach. In this context, the input to the model is a sequence of values $\{y_1, y_2, \ldots, y_l\}$, and the output is the value y_{l+l} , where l represents the lookback number of events. We applied this approach to the earthquake

data, using the features within each window as inputs to the LSTM network, then selecting features of the following event as the target.

The sequences were explored according to the lookback parameter, we generated different matrices of size (S, L) resulting in a dataset of size (N, S, L). The following figure shows the structure of the dataset for the LSTM network.

Fig. 3 Dataset for the LSTM neural network.

In the figure above, we can identify the variables F, S, L, W, t, N, and C where:

- 1. $F_{S,L}$ is a time-series sequence of a feature
- 2. S is the sequence identifier that matches the number of features in the catalog plus the augmented features
- 3. L is the lookback or length of the sequence
- 4. W is the window of events with time index t, which ranges from 0 to N, where N is the total number of events minus the lookback
- 5. C is the class of the target feature that follows the previous sequence

To calculate the complex network properties, as we've discussed in 2.1, we took each moving window and built their respective network, we took into account different node distance values of 10, 50, and 100 kilometers, per each event sequence of 50 and 100 events. The networks features we calculated from the resulting networks were degree centrality, clustering, betweenness centrality, closeness centrality, and page rank.

3 Results

In this section, we present the results of the LSTM neural networks trained with the earthquake data. We trained multiple models tuning for hyperparameters, including the number of LSTM layers, hidden size, learning rate, and maximum number of epochs. We also included the complex network features in the training process to evaluate their impact on the forecast results.

Multiple experiments were conducted as shown in Table 2. We categorized the target magnitude into 2, 3, and 4 quantiles as follows:

- 1. 2 quantiles: The feature is divided into two sections, each containing 50% of the data, corresponding to the categories low and high.
- 2. 3 quantiles: The feature is divided into three sections, containing data from 0%-33.3%, 33.3%-66.6%, and 66.6% onwards, corresponding to the categories low, medium, and high.
- 3. 4 quantiles: The feature is divided into four sections, each containing 25% of the data, corresponding to the categories low, low-medium, medium-high, and high.

It was observed that the best model with 2 quantiles achieved 64% accuracy, followed by the best model with 3 quantiles with 46% accuracy, and the model with 4 quantiles with 41% accuracy.

To incorporate complex network features into the training process, we calculated network properties for each window of events. The LSTM network was then trained using both earthquake features and network properties, with quantiles and node sizes varied for each case, and the selection of network properties determined through hyperparameter tuning. The results are presented in Table 3. The best model with 2 quantiles achieved 65% accuracy, followed by the best model with 3 quantiles at 48% accuracy, and the best model with 4 quantiles at 43% accuracy.

4 Discussion

In this study, we investigated the application of LSTM neural networks for earthquake forecasting in Colombia by leveraging both seismic event features and complex network metrics. The experiments highlight that models classifying earthquake magnitude into 2 quantiles consistently achieved higher accuracy (up to 67%) compared to those using 3 or 4 quantiles, which obtained 48% and 43% accuracy respectively. This suggests that reducing the number of classes simplifies the classification task, resulting in more reliable predictions.

Furthermore, the inclusion of complex network features—such as degree centrality, clustering, betweenness, closeness, and page rank—provided additional insight into the spatial-temporal relationships among earthquake events. While the improvements were moderate, the network-enhanced models underscored the potential benefits of incorporating structural information beyond traditional seismic indicators.

These findings indicate that integrating complex network analysis can enhance the performance of neural network-based forecasting. However, one of the main challenges we faced was the limited amount of data available. With more extensive datasets, we could potentially achieve even better results. Future research should focus on further refining these models through advanced hyperparameter tuning, exploration of alternative feature combinations, and validation using larger datasets to achieve more robust and accurate earthquake predictions.

Additionally, the study opens up several avenues for future work. One potential direction is the exploration of other machine learning models and architectures, such as convolutional neural networks (CNNs) or transformer models, which might capture different aspects of the data more effectively. Another area worth investigating is the integration of real-time data streams to continuously update and improve the

Table 2 Results of the LSTM Neural Networks

loss	test loss	lookback	test size	test size batch size	hidden size	lstm layers	lr	max epochs	accuracy	quantiles
1014.889	449.927	33	0.176	2	80	4	0.000	09	0.640	2
823.150	733.873	144	0.282	2	26	2	0.000	25	0.634	2
133.589	690.542	102	0.268	14	129	∞	0.001	19	909.0	2
126.626	367.758	147	0.139	18	144	7	0.000	58	0.582	2
409.568	525.436	78	0.117	7	22	4	0.002	45	0.463	3
150.548	1386.181	54	0.270	12	105	2	0.003	48	0.447	3
38.531	1464.909	124	0.119	19	33	4	0.001	33	0.430	3
165.997	1109.243	13	0.263	19	113	2	0.000	53	0.413	3
405.722	1245.538		0.227	∞	129	ಬ	0.000	25	0.411	4
173.115	848.971	106	0.134	19	101	2	0.001	28	0.397	4
266.301	790.450		0.158	16	92	2	0.000	52	0.387	4
249.980	902.233		0.156	15	22	2	0.008	36	0.382	4

Top 4 models for 2 quantiles, 3 quantiles, and 4 quantiles, respectively. The table shows the loss, test loss, lookback, test size, batch size, hidden size, LSTM layers, learning rate, maximum epochs, accuracy, quantiles, network features, and node size.

Table 3 Results of the LSTM Neural Networks with Network Features

loss	test loss	lookback	test size	batch size	hidden size	lstm layers	lr	max epochs	accuracy	quantiles	quantiles network features	node size
112.576 114.802 513.069	433.087 248.123 273.118	82 104 122	0.173 0.103 0.110	18 19 4	20 133 106	6 7 2 2	0.003	39 18 58	0.648 0.647 0.644	222	betweenness clustering degree	30 30 30
705.396	1115.538	149	0.276	4 0	19	4 6	0.002	388	0.473	. 80	degree	30
404.635	416.466	145 79	0.102	5 6	04 138	6	0.000	18 55	0.464	3 0	betweenness betweenness	30
269.973 527.298	$1138.736 \\ 1006.915$	105 75	$0.225 \\ 0.166$	14 6	73 68	∞ c	0.001	38 30	0.408	4 4	clustering clustering	30 30
212.685	813.492	148	0.161	19	64	9	0.000	29	0.375	4	pagerank	30
1063.339	456.658	13	0.152	2 -	36	8 4	0.007	12	0.651	2.2	pagerank	50
249.543	417.286	82	0.162	, «	12	5 2	0.001	45	0.640	1 (2)	pagerank	20
402.819	1202.975	36	0.300	-1	124	4	0.002	52	0.487	8	closeness	50
406.882 192.634	$1182.266 \\ 1022.804$	139 20	0.293 0.184	7	101	2 7	0.000	92 32	0.480 0.464	3 3	pagerank betweenness	50 50
308.907 350.506 664.843	959.463 836.819 1094.966	137 10 10	0.194 0.165 0.212	13 12 6	70 116 117	7 7 8 8	0.001 0.000 0.000	45 39 46	0.432 0.429 0.409	4 4 4	closeness clustering closeness	50 50 50
294.545 297.019 720.330	355.232 685.403 352.685	49 18 84	0.142 0.280 0.145	3 6 7	128 114 56	6 6	0.000 0.001 0.003	26 57 39	0.671 0.662 0.657	000	betweenness closeness pagerank	100 100 100
254.312 191.379 183.231	846.157 1270.860 497.836	94 140 116	0.202 0.289 0.106	11 12 16	62 51 27	4 2 5	0.001 0.001 0.000	11 23 23	0.467 0.466 0.461	3 3 3	betweenness clustering degree	100 100 100
696.927 300.884 231.743	832.365 1110.282 1483.400	53 13 128	0.163 0.219 0.296	6 13 16	140 35 140	88 89	0.000 0.004 0.004	41 62 32	0.417 0.403 0.381	4 4 4	pagerank degree closeness	100 100 100

Top 4 models for 2 quantiles, 3 quantiles, and 4 quantiles, respectively. The table shows the loss, test loss, lookback, test size, batch size, hidden size, LSTM layers, learning rate, maximum epochs, accuracy, quantiles, network features, and node size.

forecasting models. Moreover, incorporating additional external factors, such as geological and environmental data, could provide a more comprehensive understanding of the factors influencing earthquake occurrences.

In conclusion, this study demonstrates the feasibility and potential of using LSTM neural networks combined with complex network analysis for earthquake forecasting. The promising results encourage further research and development in this area, with the ultimate goal of improving earthquake prediction accuracy and contributing to disaster preparedness and risk mitigation efforts.

5 Conclusion

In this study, we explored the application of LSTM neural networks combined with complex network analysis for earthquake forecasting in Colombia. By leveraging seismic event features and complex network metrics, we aimed to improve the accuracy of earthquake magnitude classification. Our experiments demonstrated that models classifying earthquake magnitude into 2 quantiles achieved the highest accuracy, reaching up to 67%. Models using 3 and 4 quantiles achieved lower accuracies of 48% and 43%, respectively.

The inclusion of complex network features provided additional insights into the spatial-temporal relationships among earthquake events, enhancing the performance of the neural network models. However, the improvements were moderate, indicating that while complex network analysis is beneficial, there is still room for further refinement and optimization.

One of the main challenges faced in this study was the limited amount of data available. Future research should focus on utilizing larger datasets, exploring alternative machine learning models and architectures, and incorporating additional external factors to achieve more robust and accurate earthquake predictions.

Overall, this study demonstrates the potential of combining LSTM neural networks with complex network analysis for earthquake forecasting. The promising results encourage further research and development in this area, with the ultimate goal of improving earthquake prediction accuracy and contributing to disaster preparedness and risk mitigation efforts.

Declarations

Not applicable

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