Newton's Third haw

From observations, Newton concluded that all forces in nature act in pairs.

· Impossible to have a single isolated force.

Fig. (a) Tugboat pushes on barge (action). (b) Barge pushes on tugboat (reaction).





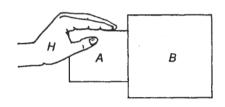
Action Reaction

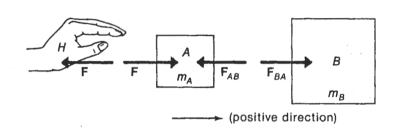
Newton: "To every action (force) there is always opposed an egual reaction (force); or, the mutual actions of two bodies upon early other are always egual, and directed to contrary parts.

Note:-The two forces in an action-reaction pair act on different objects.

- A body is accelerated only by the forces acting on it. Forces it exerts on another body do not affect its motion.

Example F= 2N is applied to block A which is in contact with B Identify all action-reaction pairs:





$$m_{A} = 1 kq$$
 $m_{B} = 2 kq$

$$\vec{a} = ?$$

[contact Force]

choose coordinate system, x-axis positive to night. Apply Newton's 2ND Law for motion of B:

Forces acting on A:

(a)

Since both blocks stay in contact

.. a = a = a [Constraint in problem]

Add Eq.
$$0+0$$

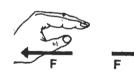
 $F-F_{AB}+F_{BA}=(m_A+m_B)$ 0

|FAB| = | FBH | Magnitudes equal due to Newton's 3'nd Law.

$$\therefore F = (m_A + m_B) \alpha$$

Single mass M= mA+mB on which only external force F is important.

$$a = \frac{F}{m_{H} + m_{B}} = \frac{2N}{(1+2)kq} = \frac{2}{3} \frac{m}{s^{2}}$$



Contact Force

$$F_{BA} = m_B \alpha_B = m_B \alpha$$

$$= 2 \times \frac{2}{3} = \frac{4}{3} N$$

Newton's Postulate: Every pair of particles in the universe exerts on one another a mutual gravitational force of attraction. This force is proportional to the product of the masses and inversely proportional to the square of the distance between them.

$$F_{q} = G m_{1} m_{2}$$

$$m_{1}$$

$$K = K_{12}$$

$$m_{2}$$

$$K = K_{12}$$

G = 6.673 × 10 1 N·m²/kg² Universal Gravitation Constant.

Consider a mass m at the surface of the earth which has a mass = ME and radius = RE.

$$\frac{F}{g} = m \left(\frac{M_E G}{R_E^2} \right) = m g$$

Gravitation constant G can be determined by measuring the force with known masses that are separated by a known distance. [Cavendish Expt.]

Gravitational acceleration quby observing the fall of dojects. is measured

ME = 9 RE

"weighing the earth"

Object in resting on surface of the earth.

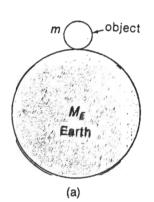
Object:
Two forces acting.

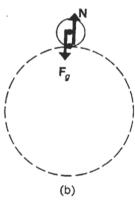
Earth's attractive gravitational force

Fq. Contact force N with ground. Since object is at vest: $\frac{1}{N} + \frac{1}{F_q} = 0$

Earth:

Two forces acting. Attractive gravitational force fg due to object. Contact force w with object. No relative motion: $\vec{w} = -f_q$





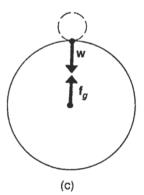


Fig. (a) An object at rest on the Earth's surface. (b) The forces acting on the object. (c) The forces acting on the Earth. The forces shown together in (b) and (c) are not action-reaction pairs.

Action - Reaction Force Pairs:

$$F_{q} = -f_{q}$$

$$N = -3$$

All four forces have equal magnitudes $F_q = f_q = N = w = mq$

Weight

The contact force \vec{w} that an object exerts on whatever is supporting it is called the weight of the object.

For above example $\vec{F_q}$ acts on the object and \vec{w} acts on the earth. For this case of zero acceleration

$$\vec{\omega} = m\vec{q}$$

Accelerating Elevator

-Object on floor of elevator that is accelerating upward with acceleration a.

For forces acting on m:

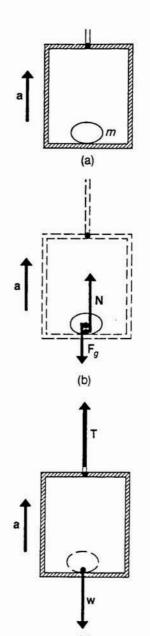
N: Face elevator exerts on object Fq: Force earth exerts on object

-weight is increased by the amount ma over weight at rest.

For elevator moving dowward with acceleration a:

-weight is decreased by ma'.

Free Fall: $a'=q \Rightarrow w=0$ Object is weightless — exerts no contact force on support.

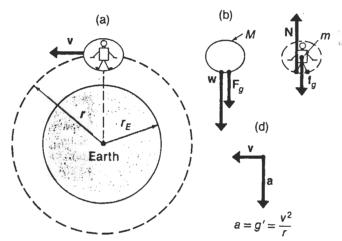


- (a) An object with a mass m is on the floor of an elevator that is accelerating upward.
- (b) Forces acting on the object.
- (c) Forces acting on the elevator.

Example: Astronaut/Satellite

An artificial satellite is in a circular orbit around the Earth. At position of orbit acceleration due to gravity is $g' = \frac{v^2}{R}$

[Free-fall motion]



An astronaut in an orbiting artificial satellite is weightless.

Force acting on satellite:

$$F_5 = F_g + \omega = Mg'$$

[F=ma]

Forces acting on astronaut:

[F=ma]

Fq = Mg | Gravitational Force on each fq = mg | object by definition.

: W = N = 0 [No contact force/No weight]

Astronaut is weightless - can exert no net force on satellite.

Note: Weight of an object is always equal to the vector force exerted on the supporting object or system.

Mass plays essentially two different roles in mechanics.

1. Inertial Mass:

In Newton's haws the quantity m connects the force applied to an object with its acceleration.

The mass measured in this way is called the inertial mass, MI.

2. Gravitational Mass:

Mass is also the property of matter that causes bodies to exert attractive gravitational forces on each other. eg. Measure force on object due to the earth.

$$\overrightarrow{F} = G \underbrace{M_E M_G}_{R_E^2} = \overrightarrow{g} M_G$$

This mass is called the gravitational mass.

Question: Is MI = MG for all bodies?

Experiment: Must provide the ultimate answer. Do all bodies fall due to gravity with the same acceleration?

Body #1:
$$M_{\pm}(1) Q(1) = \frac{GM_E}{R_E^2} M_G(1) = g M_G(1)$$

Body
$$^{\pm}\lambda$$
: $M_{\pm}(2) \alpha(2) = q M_{G}(2)$ (2)

$$\frac{m_{\pm}(1) q(1)}{m_{\pm}(2) q(2)} = \frac{m_{G}(1)}{m_{G}(2)}$$

$$\frac{M_{I}(1)}{M_{G}(1)} = \frac{M_{I}(2)}{M_{G}(2)} \times \frac{Q_{I}(2)}{Q_{I}(1)}$$

Experiment finds that a(2)/a(1) = constant. Tested for many different materials.

Galileb Eötvös } < 1×10⁻¹² difference.

Ratio $\frac{M_{\rm I}}{M_{\rm G}} = 1$ by a proper choice of G.

Newtonian Theory: MI & MG not required

General Relativity: MI & MG absolutely a must

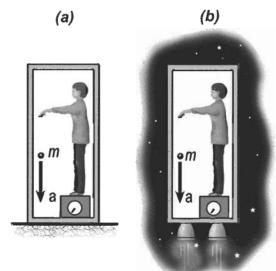
Principle of Equivalence

Principle of Equivalence'
-gravitation is equivalent to acceleration.

Principle of Equivalence

-A fundamental postulate of Einstein's General Theory of Relativity. In this theory gravity is interpreted as a correture in space and time

-Equivalence Physicist in a box cannot tell the difference between gravity and acceleration.



- (a) A physicist-in-a-box, resting on the earth.
- (b) The same, accelerating in deep space at 9.8 m/s². It is not possible, by doing experiments within the box, for the physicist to tell which box he is in.

Ex: Suppose $\left(\frac{M_q}{M_{\perp}}\right)_A = 2\left(\frac{M_q}{M_{\perp}}\right)_B$. Release both objects

in an Einstein elevator. If they fall with same acceleration then elevator must be accelerating upwards. If A falls with twice acceleration of B then it must be due to gravitational field. Violation of Principle of Equivalence! Predicted bending of light by a massive object.

Hooke's Law - Springs

All bodies are elastic to varying degrees. When a stretching or compressing force is applied they deform.

- steel balls
 - rubber bands
 - -springs

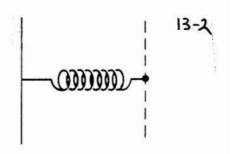
A body nesists deformation by means of a nestoring force.

Pull on a spring - it pulls back.

In many cases the relationship between the resulting restoring force and the deformation obeys a simple empirical law known as Hooke's Law.

"The magnitude of the restoring force is directly proportional to the deformation"

- -approximate
- empirical description
- -good for small deformations



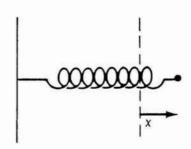
Spring, relaxed.

Hooke's Law:

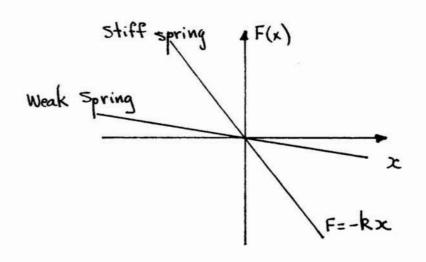
$$F = -k x$$

Spring constant

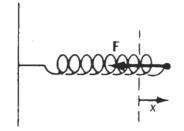
4 Negative sign means the restoring force opposes the deformation.

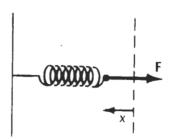


Spring, stretched by a length x.

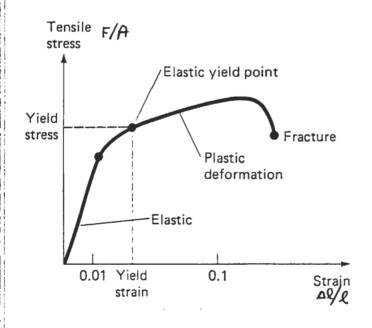


k large: stiff spring large force/Unit displacement k small: soft spring small force/unit displacement





+x -elongation; Force negative opposes stretching -x -compression; Force positive opposes compression



Parallel Springs

$$-k_1x - k_2x + Mg = 0$$

$$x(k_1+k_2) = mq$$

$$\frac{Mq}{(k_1+k_2)} = \frac{Mq}{k_{eff}}$$

Series Springo

$$2(=Mq\left[\frac{1}{k_1}+\frac{1}{k_2}\right]$$

Let
$$\frac{1}{k_{eff}} = \frac{1}{k_1} + \frac{1}{k_2}$$

Weaker Spring

If
$$k_1 = k_2 = k$$

 $k_1 = k_2 = k$
 $k_2 = k$
weaker