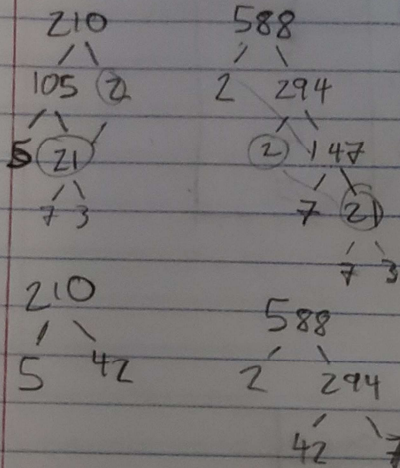


1.18, 1.20, 1.27

Taylor Whitlock
Section 002
HW #3

1.18) $\gcd(210, 588)$



| A | B |
|-----|-----|
| 588 | 210 |
| 210 | 168 |
| 168 | 42 |
| 42 | 0 |

EUCLID'S
ALGORITHM

1.20) $20 \bmod 79$:

$AX + BY = D$

INVERSE = 4

| A | B | X | Y | D | RETURN | CALL # |
|----|----|------|------|------|--------------|--------|
| 79 | 20 | 1 | -4 | 1 | $(-1, 4, 1)$ | 1 |
| 20 | 19 | 0 | 1 | 1 | $(1, -1, 1)$ | 2 |
| 19 | 1 | 1 | 0 | 1 | $(0, 1, 1)$ | 3 |
| 1 | 0 | NONE | NONE | NONE | $(1, 0, 1)$ | 4 |

$3 \bmod 62$

| A | B | X | Y | D | RETURN | CALL # |
|----|---|------|------|------|---------------|--------|
| 62 | 3 | 1 | -1 | 1 | $(-1, 21, 1)$ | 1 |
| 3 | 2 | 0 | 1 | 1 | $(1, -1, 1)$ | 2 |
| 2 | 1 | 1 | 0 | 1 | $(0, 1, 1)$ | 3 |
| 1 | 0 | NONE | NONE | NONE | $(1, 0, 1)$ | 4 |

INVERSE = 21

$21 \bmod 91$

| A | B | X | Y | D | RETURN | CALL # |
|----|----|------|------|------|--------------|--------|
| 91 | 21 | 0 | 1 | 7 | $(1, -4, 7)$ | 1 |
| 21 | 7 | 1 | 0 | 7 | $(0, 1, 7)$ | 2 |
| 7 | 0 | NONE | NONE | NONE | $(1, 0, 7)$ | 3 |

INVERSE DOES NOT EXIST

1.20 CONT

5 MOD 23

| A | B | X | Y | D | RETURN | CALL # |
|----|---|------|------|------|------------|--------|
| 23 | 5 | -1 | 2 | 1 | (2, -9, 1) | 1 |
| 5 | 3 | 1 | -1 | 1 | (-1, 2, 1) | 2 |
| 3 | 2 | 0 | 1 | 1 | (1, -1, 1) | 3 |
| 2 | 1 | 1 | 0 | 1 | (0, 1, 1) | 4 |
| 1 | 0 | NONE | NONE | NONE | (1, 0, 1) | 5 |

INVERSE = 14

1.27

3 MOD 352

| A | B | X | Y | D | RETURN | CALL # |
|-----|---|---|---|---|--------------|--------|
| 352 | 3 | 0 | 1 | 1 | (1, -117, 1) | 1 |
| 3 | 1 | 1 | 0 | 1 | (0, 1, 1) | 2 |
| 1 | 0 | ∅ | ∅ | ∅ | (1, 0, 1) | 3 |

$$-117 \text{ MOD } 352 = 235 \text{ (MOD } 352)$$

d = 235

$$y = M^e \text{ (MOD } 391) = 68421 \% 391 = 105$$

Encryption = 105