

3
4 1.7)

5 It takes $O(m \cdot n)$ time complexity. There will be m function calls because y will get halved each time, and though bit shifting left/right (adding/multiplying) as well as checking the last bit are all $O(1)$ operations, addition is $O(n)$ time since it has to go through each bit of n , thus the combination is $O(m \cdot n)$.

7
8 1.25)

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9 def modexp(x, y, n):
10     if y == 0:
11         return 1
12     z = modexp(x, y/2, n)
13     return (z**2) % n if y % 2 == 0 else ((z**2) % n)*x % n
14
15 modexp(2, 125, 127)
16     modexp(2, 62, 127)
17         modexp(2, 31, 127)
18             modexp(2, 15, 127)
19                 modexp(2, 7, 127)
20                     modexp(2, 3, 127)
21                         modexp(2, 1, 127)
22                             modexp(2, 0, 127)
23                                 z = null, returns 1
24                                 z = 1, returns  $2 \cdot (1^2) \% n = 2$ 
25                                 z = 2, returns  $2 \cdot (2^2) \% n = 8$ 
26                                 z = 8, returns  $2 \cdot (8^2) \% n = 1$ 
27                                 z = 1, returns  $2 \cdot (1^2) \% n = 2$ 
28                                 z = 2, returns  $2 \cdot (2^2) \% n = 8$ 
29                                 z = 8, returns  $(8^2) \% n = 64$ 
30                                 z = 64, returns  $2 \cdot (64^2) \% n = 64$ 
31
32
33 2**125 (mod 127) = 64
34
```

35 Problem 3)

	x	y	z	n	return value	call level
36	2	21	16	18	8	1
37	2	10	14	18	16	2
38	2	5	4	18	14	3
39	2	2	2	18	4	4
40	2	1	1	18	2	5
41	2	0	None	18	1	6