

- (1) Because it is too low level.
complex to write code.
time consuming.

(Any thing reasonable should be fine)
As Answer.

$$\begin{array}{r} \text{(2)} \quad A = \quad 1111 \quad \leftarrow \text{carry} \\ \quad \quad \quad 11110100 \\ B = \quad 10110111 \quad (+) \\ \hline A+B = 1 \boxed{10101011} \\ \quad \quad \downarrow \\ \quad \quad \text{carry (discarded).} \end{array}$$

$$\text{(3)} \quad 3 \Rightarrow 0011 \quad (4\text{-bit})$$

-3 is 2's complement of 3:

1) Step1: Flip the bits = 1100

2) Step2: Add 1 = 1100 + 1 = 1101

$$\Rightarrow (-3)$$

1 is in 4-bit binary: 0001

-1 is 2's complement of 1:

1) flip the bits = 1110

2) Add 1 = 1110 + 1 = 1111

$$\Rightarrow (-1)$$

Now, $-3-1 \Rightarrow (-3) + (-1)$:

$$\begin{array}{r} \\ -3: 1101 \\ -1: 1111 \quad (+) \\ \hline \textcircled{1} 1100 \\ \swarrow \\ \text{Discard.} \end{array}$$

Now $(-3-1) - 1 = (-3-1) + (-1)$

$$\begin{array}{r} \\ -3-1: 1100 \\ -1: 1111 \quad (+) \\ \hline \textcircled{1} 1011 \\ \swarrow \\ \text{Discard} \end{array}$$

Ans is negative : 1011

To get the absolute value, do a 2's complement

1) Flip the bits = 0100

2) Add 1 $\Rightarrow 0100 + 1 = 0101$

0101 is 5

Answer is $\boxed{-5}$

④

1	000	10100	1010	1011	110000	110011	0111
↓	↓	↓	↓	↓	↓	↓	↓
1	1	4	A	B	C	3	3
							7

⑤ - 58

it can be done in many ways:

Approach 1: (1) Convert the number to Hex.
(2) perform a compliment.

Approach 2: (1) Convert the number to binary
(2) Perform 2's complement
(3) Convert back to Hexadecimal.

See next page



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Approach-1

58 to Hexadecimal:

Division	Result	Remainder
58/16	3	10 → (A)
3/16	0	3

58 is 3A.

58 in 16 bit = 003A.

complement of 003A.

(1) $FFFF - 003A = FFC5$

(2) Add 1 : $FFC5 + 1 = \boxed{FFC6}$.

give full points if answer is C6

Ans: FFC6

Approach-2

58 in binary $\Rightarrow 111010$

58 in 16-bit = 0000 0000 0011 1010

2's complement :

1) Flip : 1111111111000101

2) Add 1 : 1111111111000110

In Hexadecimal:

F F C 6

Ans: FFC6

Answer C6 also gets full points

6

(a)

0111011

msb is 0 here. So, the number is positive.

Diagram showing the binary number 0111011 with arrows pointing from each bit to its corresponding power of 2 in the expansion:

$$0 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$= 0 + 64 + 32 + 16 + 0 + 4 + 2 + 1$$

$$= 119$$

⑥ ⑥

1111 0001

MSB is 1, so number is negative.

Do a 2's complement:

1) flip the bits = 0000 1110

2) Add 1 = 0000 1110 + 1 = 0000 1111

Convert to binary:

$$\begin{array}{cccccccc} & & & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ & \swarrow & \swarrow & \swarrow & \swarrow & \downarrow & \searrow & \searrow & \searrow & \searrow & \searrow \\ 0 \times 2^7 & + & 0 \times 2^6 & + & 0 \times 2^5 & + & 0 \times 2^4 & + & 1 \times 2^3 & + & 1 \times 2^2 & + & 1 \times 2^1 & + & 1 \times 2^0 \end{array}$$

$$= 0 + 0 + 0 + 0 + 8 + 4 + 2 + 1$$

$$= 15$$

Answer is -15

⑦

$$\begin{array}{r} A1C \\ + CCF \\ \hline 16EB \end{array}$$

$$\begin{array}{r} 16EB \\ - FFE \\ \hline 6ED \end{array}$$

⑧ The signed range of 4-bit storage is

$$\begin{aligned} & -2^{n-1} \text{ to } +2^{n-1}-1 \\ \Rightarrow & -2^{4-1} \text{ to } +2^{4-1}-1 \\ \Rightarrow & -2^3 \text{ to } +2^3-1 \\ \Rightarrow & -8 \text{ to } +7 \end{aligned}$$

So, -10 is out of range for 4-bit.

No possible to store -10

⑨ The smallest 120-bit signed integer $= -2^{n-1}$
 $= -2^{120-1}$
 $= -2^{119}$

⑩

$$P = (\neg x \wedge \neg y \wedge \neg z) \vee (\neg x \wedge y \wedge z) \vee (x \wedge y \wedge \neg z)$$

