Matrix Theory (EE5609) Assignment 2

Arkadipta De MTech Artificial Intelligence Roll No - AI20MTECH14002

Abstract—This assignment finds the equation of a straight line given two points on that line.

From the theory, using equation 2.0.1, the direction vector for the line through the points \mathbf{O} and \mathbf{P} is

1 Problem Statement

Find the equation of the line passing through the origin and the point $\begin{pmatrix} 5 \\ -2 \\ 3 \end{pmatrix}$.

2 Theory

The direction vector **A** for a line through the points $\begin{pmatrix} x_1 \\ y_1 \\ z_1 \end{pmatrix}$ and $\begin{pmatrix} X_2 \\ y_2 \\ z_2 \end{pmatrix}$ is given by

$$\mathbf{A} = \begin{pmatrix} a \\ b \\ b \end{pmatrix} = \begin{pmatrix} x_2 - x_1 \\ y_2 - y_1 \\ z_2 - z_1 \end{pmatrix}$$
 (2.0.1)

The vector form of equation of a line passing through a point with position vector \mathbf{a} and along the direction vector \mathbf{b} is given by

$$\mathbf{r} = \mathbf{a} + k\mathbf{b} \tag{2.0.2}$$

where k is a constant multiple.

3 Solution

Let the points be $\mathbf{O} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$ which is the origin and (5)

$$\mathbf{P} = \begin{pmatrix} 5 \\ -2 \\ 3 \end{pmatrix}.$$

$$\mathbf{A} = \mathbf{P} - \mathbf{O} \tag{3.0.1}$$

$$\implies \mathbf{A} = \begin{pmatrix} 5 \\ -2 \\ 3 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \tag{3.0.2}$$

$$\implies \mathbf{A} = \begin{pmatrix} 5 \\ -2 \\ 3 \end{pmatrix} \tag{3.0.3}$$

From equation 2.0.2, the vector form of the line passing through **O** and **P**, which is the line passing through the point **O** and along direction vector **A** is given by

$$\mathbf{r} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + k \begin{pmatrix} 5 \\ -2 \\ 3 \end{pmatrix} \tag{3.0.4}$$

$$\implies \mathbf{r} = k \begin{pmatrix} 5 \\ -2 \\ 3 \end{pmatrix} \tag{3.0.5}$$

(2.0.1) where k is a constant multiple.

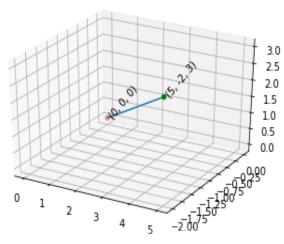


Fig. 1: Line passing through origin and point (5,-2,3)

Python Code: The code for generating the Figure 1 can be found at https://github.com/Arko98/EE5609/blob/master/Assignment_2/Codes/Figure.py