

GlobalSetup

$$\begin{aligned} gp &= (g, G_1, G_T, e, H, H_1, H_2, sk_{KGC}, sk_{svr}, pk_{svr}) \\ sk_{KGC} &= x \in Z_p^*, sk_{svr} = l \in Z_p^*, pk_{svr} = L = g^l \\ H: Z_p^* &\rightarrow G_1, H_1: G_T \rightarrow Z_p^*, H_2: \{0,1\}^* \rightarrow Z_p^* \end{aligned}$$

KeyGen_o

$$\begin{aligned} ID_o, s &\in Z_p^*, V \in G_1 \\ sk_o &= (sk_{co}, sk_{ao}) = (s, H(ID_o)^x) \text{ [} x \text{ 在 GlobalSetup 里]} \\ pk_o &= (V, pk_{co}, pk_{ao}) = (V, g^s, H(ID_o)) \end{aligned}$$

KeyGen_u

$$\begin{aligned} ID_u, t &\in Z_p^* \\ sk_u &= (sk_{tu}, sk_{au}) = (t, H(ID_u)^x) \\ pk_u &= (pk_{tu}, pk_{au}) = (g^t, H(ID_u)) \end{aligned}$$

Ciphertext

$$\begin{aligned} r &\in Z_p^* \\ T &= e(L, V)^{sk_{co}} \\ C_w &= (C_{w1}, C_{w2}) = ((pk_{co})^r, e(g, g^{H_2(w)})^r \cdot T) \\ C_{ID_o} &= H_1(e(H(ID_o)^x, H(ID_u))) \end{aligned}$$

Re-enc

$$C'_w = (C'_{w1}, C'_{w2}) = ((C_{w1})^{(sk_{tu}/sk_{co})}, C_{w2})$$

Trapdoor

$$\begin{aligned} k &\in Z_p^* \\ T_q &= (T_{q1}, T_{q2}) = ((g^{H_2(q)})^{1/sk_{tu}} \cdot L^k, g^k) \\ C_{ID_u} &= H_1(e(H(ID_o), H(ID_u)^x)) \end{aligned}$$

Test

$$\begin{aligned} T &= e(V, pk_{co})^{sk_{svr}} \\ e(C'_{w1}, T_{q1}/(T_{q2})^{sk_{svr}}) \cdot T &= C'_{w2} \end{aligned}$$