Design and Analysis of Algorithms Lab Assessment-3

Name: Armaan Indani

Reg. No.: 22BCE3347

Slot: L41+42

Faculty: Dr. Joshva Devdas T – 16700

Question 1:

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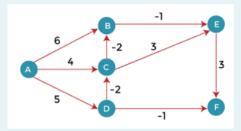
Question 1

Correct

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ℙ Flag question

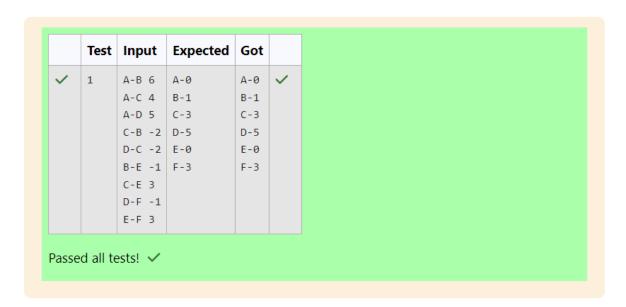
Write a program to compute the shingle source shortest path algorithm using Bellman Ford Algorithm



Test	Input	Result
1	A-B 6	A-0
	A-C 4	B-1
	A-D 5	C-3
	C-B -2	D-5
	D-C -2	E-0
	B-E -1	F-3
	C-E 3	
	D-F -1	
	E-F 3	

```
Answer: (penalty regime: 0 %)
       #include <stdio.h>
        #include <limits.h>
    2
    3
    4
        int min(int a, int b)
    5 1
    6
             return a > b ? b : a;
    8
    9
        int main()
   10 🔻
        {
             int x = INT_MAX;
   11
             int n = 6;
   12
   13
             int c[6][6] = {
   14
                  \{x, x, x, x, x, x\},\
   15
                  \{x, x, x, x, x, x\},\
   16
                  \{x, x, x, x, x, x\},\
   17
                  \{x, x, x, x, x, x\},\
   18
                  \{x, x, x, x, x, x\},\
   19
                  \{x, x, x, x, x, x\},\
   20
             };
   21
   22
             int d[6] = \{0, x, x, x, x, x\};
   23
   24
             for (int i = 0; i < 9; i++)
   25
   26
                  char s, d, dash;
                  int wt;
scanf("%c%c%c", &s, &dash, &d);
scanf("%d", &wt);
   27
   28
   29
   30
                  getchar();
   31
   32
                  int src = (int)s - 65;
   33
                  int dest = (int)d - 65;
   34
   35
                  if (src > 5 || dest > 5)
   36 ▼
   37
                       printf("Error src = %d, dest = %d invalid", src, dest);
   38
                  }
                  else
   39
   40
                  {
   41
                       c[src][dest] = wt;
   42
   43
   44
             for (int k = 0; k < n; k++)
   45
   46
   47
                  for (int i = 0; i < n; i++)
   48 1
                       for (int j = 0; j < n; j++)
   49
   50
   51
                           if (i != j)
   52 1
                            {
                                 if (c[i][j] != INT_MAX \&\& d[i] != INT_MAX)
   53
   54
   55
                                     d[j] = min(d[j], d[i] + c[i][j]);
   56
                                 }
   57
   58
                       }
   59
                  }
   60
   61
            printf("A-%d\n", d[0]);
printf("B-%d\n", d[1]);
printf("C-%d\n", d[2]);
printf("D-%d\n", d[3]);
printf("E-%d\n", d[4]);
printf("F-%d\n", d[5]);
   62
   63
   64
   65
   66
   67
   68
   69
             return 0;
   70 }
```

Output:



Question 2:

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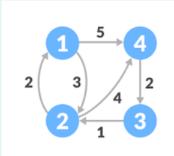
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Question 2

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 $\begin{picture}(20,0)\put(0,0){\line(1,0){10}}\put(0,0){\line(1,0){10}$

Write a program to determine all pair shortest path algorithm using the following graph



Note: Assume infinity as 100

Test	Result	:
1	A0 =	
	0 3 10	0 5
	2 0 10	0 4
	100 1	0 100
	100 10	0 2 0
	A1=	
	0 3 10	0 5
	2 0 10	0 4
	100 1	0 8
	100 10	0 2 0
	A2=	
	0 3 10	0 5
	2 0 10	0 4
	3 1 0	5
	100 10	0 2 0
	A3=	
	0 3 10	0 5
	2 0 10	0 4
	3 1 0	
	5 3 2	0
	A4=	
	0 3 7	5
	2 0 6	
	3 1 0	
	5 3 2	0

```
Answer: (penalty regime: 0 %)
   4
       int min(int a, int b)
   5 🔻
           return a > b ? b : a;
   6
   7
   8
       int main()
   9
  10 •
  11
           int x = 100;
  12
           int n = 4;
  13 •
           int a[4][4] = {
  14
               \{0, 3, x, 5\},\
  15
               \{2, 0, x, 4\},\
                \{x, 1, 0, x\},\
  16
                \{x, x, 2, 0\},\
  17
  18
           };
  19
           printf("A0 =\n");
  20
           for (int i = 0; i < n; i++)
  21
  22 1
               for (int j = 0; j < n; j++)
  23
  24 1
                   printf("%d ", a[i][j]);
  25
  26
               printf("\n");
  27
  28
  29
           printf("\n");
  30
  31
           for (int k = 0; k < n; k++)
  32
               printf("A%d=\n", k + 1);
  33
  34
               for (int i = 0; i < n; i++)
  35 1
  36
                    for (int j = 0; j < n; j++)
  37 1
                        if (a[i][k] != INT MAX && a[k][j] != INT MAX)
  38
  39 1
                            a[i][j] = min(a[i][j], a[i][k] + a[k][j]);
  40
  41
  42
  43
                for (int i = 0; i < n; i++)
  44
  45
  46
                    for (int j = 0; j < n; j++)
  47
                        printf("%d ", a[i][j]);
  48
  49
                    printf("\n");
  50
  51
  52
  53
  54
           return 0;
  55
```

Output:

	Test	Expected	Got	
/	1	A0 =	A0 =	~
		0 3 100 5	0 3 100 5	
		2 0 100 4	2 0 100 4	
		100 1 0 100	100 1 0 100	
		100 100 2 0	100 100 2 0	
		A1=	A1=	
		0 3 100 5	0 3 100 5	
		2 0 100 4	2 0 100 4	
		100 1 0 100	100 1 0 100	
		100 100 2 0	100 100 2 0	
		A2=	A2=	
		0 3 100 5	0 3 100 5	
			2 0 100 4	
		3 1 0 5	3 1 0 5	
			100 100 2 0	
		A3=	A3=	
			0 3 100 5	
			2 0 100 4	
		3 1 0 5	3 1 0 5	
		5 3 2 0	5 3 2 0	
		A4=	A4=	
		0 3 7 5	0 3 7 5	
		2 0 6 4	2 0 6 4	
		3 1 0 5	3 1 0 5	
		5 3 2 0	5 3 2 0	

Question 3:

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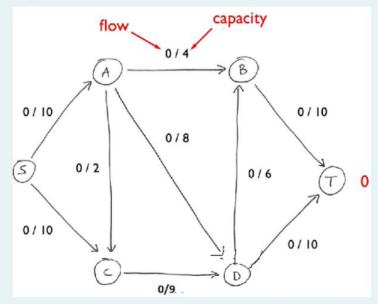
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Question 3 Correct Marked out of 20.00

Flag question

Write a Program to implement the max flow algorithm Ford Fulkerson by using the following graph



note: given the input based on the directed graph

Test	Res	ult						
1	The	maximum	flow	of	the	algorithm	is	19

```
Answer: (penalty regime: 0 %)
   1 #include <stdio.h>
       #include <stdlib.h>
       #include <limits.h>
   4 #include <string.h>
   6 int min(int a, int b)
   7 ▼ {
           return a > b ? b : a;
   8
   9
  10
  11
       struct edge
  12 ▼ {
           int capacity;
  13
           int flow;
  14
           int from;
  15
           int to;
  16
  17
       };
  18
  19
       struct queue
  20 ▼ {
           int v[100];
  21
  22
           int front;
  23
           int back;
  24
      };
  25
  26
       void enqueue(struct queue *Q, int v_no)
  27 ▼ {
           Q->front += 1;
  28
  29
           Q \rightarrow v[Q \rightarrow front] = v_no;
  30
  31
  32
      void dequeue(struct queue *Q)
  33 ₹ {
           Q->back += 1;
   35
      }
```

```
36
37
    struct edge *newE(int cap, int flow, int v1, int v2)
38 •
        struct edge *e = (struct edge *)malloc(sizeof(struct edge));
39
40
        e->capacity = cap;
41
        e->flow = flow;
42
        e \rightarrow from = v1;
43
        e\rightarrow to = v2;
44
        return e;
45
    }
46
47
    int main()
48 •
    {
49
                    // No of vertices
        int n = 6;
50
        int n_e = 18; // No of edges
51
52
        struct edge *E[18]; // For Residual edges as well
53
        int ans = 0;
54
55
        E[0] = newE(10, 0, 0, 1); // Normal Edge
        E[1] = newE(0, 0, 1, 0);
56
                                   // Residual Edge
57
        E[2] = newE(10, 0, 0, 3); // Normal Edge
58
                                    // Residual Edge
        E[3] = newE(0, 0, 3, 0);
59
        E[4] = newE(4, 0, 1, 2);
                                    // Normal Edge
60
                                    // Residual Edge
        E[5] = newE(0, 0, 2, 1);
61
        E[6] = newE(2, 0, 1, 3);
                                    // Normal Edge
62
        E[7] = newE(0, 0, 3, 1);
                                    // Residual Edge
63
        E[8] = newE(8, 0, 1, 4);
                                    // Normal Edge
64
        E[9] = newE(0, 0, 4, 1);
                                    // Residual Edge
65
        E[10] = newE(10, 0, 2, 5); // Normal Edge
66
        E[11] = newE(0, 0, 5, 2); // Residual Edge
67
        E[12] = newE(9, 0, 3, 4);
                                   // Normal Edge
68
        E[13] = newE(0, 0, 4, 3);
                                   // Residual Edge
69
        E[14] = newE(6, 0, 4, 2);
                                   // Normal Edge
70
        E[15] = newE(0, 0, 2, 4); // Residual Edge
71
        E[16] = newE(10, 0, 4, 5); // Normal Edge
72
        E[17] = newE(0, 0, 5, 4); // Residual Edge
```

```
73
 74
          int pathAvailable = 1;
 75
          while (pathAvailable == 1)
 76 🔻
 77
              int visited[6] = {0};
 78
              int parent[n];
 79
              for (int i = 0; i < n; i++)
 80 1
              {
 81
                  parent[i] = -1;
 82
              struct queue *Q = (struct queue *)malloc(sizeof(struct queue))
 83
 84
              Q \rightarrow front = -1;
 85
              Q \rightarrow back = 0;
 86
 87
              enqueue(Q, 0);
 88
              visited[0] = 1;
 89
 90
              while (visited[n - 1] != 1)
 91 •
 92
                  if (Q->front < Q->back)
 93 •
 94
                       pathAvailable = 0;
 95
                       break;
 96
                  for (int i = 0; i < n_e; i++)
97
98 •
99
                       int currentV = Q->v[Q->back];
100
                       if (E[i]->from == currentV)
101 •
                           if (visited[E[i]->to] == 1)
102
103 1
                           {
104
                               continue;
105
106
                           if (E[i]->capacity - E[i]->flow == 0)
107 ▼
108
                               continue;
109
110
```

```
111
                         // printf("Going from vertex %d to %d\n", E[i]->fr
112
                         visited[E[i]->to] = 1;
113
                         enqueue(Q, E[i]->to);
114
                         parent[E[i]->to] = E[i]->from;
115
116
                 dequeue(Q);
117
118
             }
119
             // printf("[");
120
             // for (int i = 0; i < n; i++)
121
122 •
             // {
                    printf("%d ", visited[i]);
             //
123
             // }
124
             // printf("]\n[");
125
             // for (int i = 0; i < n; i++)
126
127 •
             // {
                    printf("%d ", parent[i]);
128
             //
129
             // }
             // printf("]\n");
130
131
             int vert = n - 1;
132
133
             int min_cap = INT_MAX;
             // printf(" Path (reversed):\n");
134
135
             while (vert != 0)
136
137
                 if (parent[vert] == -1)
138 1
                 {
                     pathAvailable = 0;
139
140
                     break;
                 }
141
                 int vert2 = parent[vert];
142
                 // printf(" %d-%d ", vert2, vert);
143
                 for (int i = 0; i < 2 * n_e; i++)
144
145 •
                     if ((E[i]->from == vert2) && (E[i]->to == vert))
146
147 •
                     {
```

```
min_cap = min(min_cap, E[i]->capacity - E[i]->flow
148
149
                          // printf("\n
                                           {%d %d %d %d}\n", min_cap, E[i]->
150
                          break;
151
152
153
                  vert = vert2;
154
155
156
              if (!pathAvailable)
157 1
              {
158
                  break;
159
160
             // printf("\n min cap = %d\n\n", min cap);
161
162
             ans += min_cap;
163
164
              vert = n - 1;
             while (vert != 0)
165
166 •
                  int vert2 = parent[vert];
167
                 // printf("\n(vert2 = %d)\n", vert2);
168
                  for (int i = 0; 2 * i < n_e - 1; i++)
169
170 •
                      // printf("[[2*i = %d]]", 2 * i);
171
                      if ((E[2 * i]->from == vert2) && (E[2 * i]->to == vert
172
173 1
                          // printf("{%d} ", 2 * i);
174
                          E[2 * i] \rightarrow flow += min cap;
                                                           // Forward Edge
175
176
                          E[2 * i + 1]->flow -= min cap; // Residual Edge
                          // printf("\nChanging flow for edge %d,%d\n", E[2
177
178
179
180
                  vert = vert2;
181
              }
182
         }
183
         printf("The maximum flow of the algorithm is %d", ans);
184
185
186
          return 0;
187
188
```

Check

	Test	Expected	Got
~	1	The maximum flow of the algorithm is 19	The maximum flow of the algorit

Question 4:

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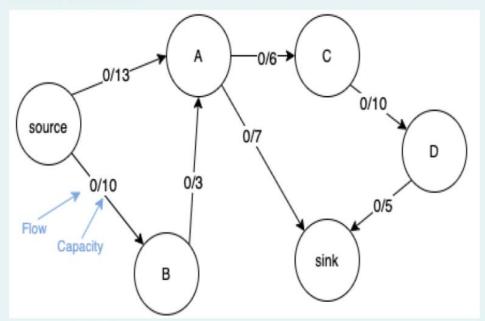
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Question 4

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Flag question

Write a program to implement Push Relabel Algorithm to compute the max flow in the given network at the sink node T



Note: use the directed edges as input to determine the maxflow network

Test	Res	ult							
1	The	max	flow	at	the	Sink	node	is	12

```
Answer: (penalty regime: 0 %)
      #include <stdio.h>
       #include <stdlib.h>
   2
   3
   4
      int min(int a, int b)
   5 ▼ {
           return a > b ? b : a;
   6
   7
   8
   9
      struct edge
  10 ▼ {
           int src;
  11
  12
           int dest;
  13
           int flow;
  14
           int cap;
  15
       };
  16
       struct edge *newEdge(int s, int d, int f, int c)
  17
  18 ▼ {
  19
           struct edge *e = (struct edge *)malloc(sizeof(struct edge));
           e \rightarrow src = s;
  20
           e->dest = d;
  21
  22
           e->flow = f;
           e \rightarrow cap = c;
  23
  24
  25
           return e;
  26
  27
       int main()
  28
  29 ▼ {
  30
           int n_v = 6;
           int n_e = 7;
  31
  32
           struct edge *E[7];
  33
  34
           E[0] = newEdge(0, 1, 0, 13);
  35
```

```
36
        E[1] = newEdge(0, 2, 0, 10);
37
        E[2] = newEdge(1, 3, 0, 6);
        E[3] = newEdge(1, 5, 0, 7);
38
        E[4] = newEdge(2, 1, 0, 3);
39
40
        E[5] = newEdge(3, 4, 0, 10);
        E[6] = newEdge(4, 5, 0, 5);
41
42
        int ht[7] = \{0\};
43
        int ov[7] = \{0\};
44
45
        ht[0] = 6;
46
47
        for (int i = 0; i < n_e; i++)
48
49 1
50
             if (E[i]->src == 0)
51 1
52
                 E[i] - flow = E[i] - cap;
                 ov[E[i]->dest] = E[i]->cap;
53
54
55
        int sum_of_overflows = 1;
56
        while (sum_of_overflows > 0)
57
58 •
            for (int v = 1; v < n_v - 1; v++)
59
60 •
                 if (ov[v] > 0)
61
62 1
                 {
                     // printf("{%d, %d, %d}\n", v, ov[v], ht[v]);
63
                     // Only forward edges
64
                     for (int e = 0; e < n_e; e++)
65
66 1
                         if (E[e]->src == v && E[e]->cap > E[e]->flow && ht[
67
68
                              int f1 = min(ov[v], E[e]->cap - E[e]->flow);
69
                             E[e]->flow += f1;
70
```

```
ov[v] -= f1;
  71
  72
                               ov[E[e]->dest] += f1;
                               // printf("Forward flow of %d to %d increased
  73
  74
  75
  76
 77
                       // Only backward edges
                       for (int e = 0; e < n_e; e++)
  78
  79 •
                           if (E[e]->dest == v && E[e]->flow > 0 && ht[E[e]->
  80
  81 •
                               int f1 = min(ov[v], E[e]->flow);
 82
                               E[e]->flow -= f1;
 83
                               ov[v] -= f1;
 84
                               ov[E[e]->src] += f1;
 85
                               // printf("Forward flow of %d to %d decreased
 86
 87
 88
 89
                       if (ov[v] == 0)
 90 1
                                         Vertex %d has overflow 0\n", v);
                           // printf("
 91
 92
                           continue;
 93
                       }
                       else if (ov[v] > 0)
 94
 95 •
 96
                           ht[v]++;
 97
                           v = 0;
 98
                           continue;
 99
                       }
 100
 101
 102
              sum_of_overflows = 0;
              for (int i = 1; i < n_v - 1; i++)
 103
 104 •
                  sum of overflows += ov[i];
 105
              }
 106
 107
 108
          printf("The max flow at the Sink node is %d", ov[n v-1]);
 109
          return 0;
 110
 111
Check
```

	Test	Expected	Got
~	1	The max flow at the Sink node is 12	The max flow at the Sink node is 12
4			
asse	d all te	ests! 🗸	