MathsStart and MathsTrack: Mathematics Bridging at the University of Adelaide.

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Abstract

In this thesis the University of Adelaide's mathematics bridging courses: MathsStart and MathsTrack are discussed in detail. Their context and purpose is reviewed, their content is aligned to national and state highschool curriculums, as well as appropriate entry-level university courses. The pedagogy and excellence in educational practice demonstrated through the University of Adelaide's maths learning center, which offers these bridging courses, is examined with an eye to learning from their exemplary approach to supporting what can be one of the most vunerable cohorts of students attempting to enter into tertiary education. Ultimately, reccomendations are made both in terms of exemplary practice that can be generalised to other such courses accross Australia, and also in terms of restructuring of the courses to better align them with national and state curriculums, while also tailoring their content to better suit the cohort of students enrolling in these courses.

Declaration

I certify that this work contains no material which has been accepted for the award of any other degree or diploma in my name, in any university or other tertiary institution and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text. In addition, I certify that no part of this work will, in the future, be used in a submission in my name, for any other degree or diploma in any university or other tertiary institution without the prior approval of the University of Adelaide and where applicable, any partner institution responsible for the joint-award of this degree.

I give permission for the digital version of my thesis to be made available on the web, via the University's digital research repository, the Library Search and also through web search engines.

Signed:			
Date:			

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First, my thanks go to David Butler and Nicholas Crouch from the maths learning center at the University of Adelaide. Not only did their exemplary educatational expertise inspire me to try my hand at education in the first place, but they continue to inspire me on a daily basis with the way the help and support students. Even while dealing with a university review Nicholas still found time (somehow) to sit with me and discuss improvements that could be made to their bridging courses.

My thanks also extend to Igusti Darmawan, my supervisor from inside the school of education, for his guidance but mostly support and his willingness to allow me to pursue a somewhat unorthodox project of my own construction, despite it being quite outside of his speciality area of educational research, none-the-less supporting me in my project.

- Lynda
- Linda
- Brendan, for doing his best,
- Ed
- Saman?
- Jason?
- Amanda?
- Trev?
- Students?
- •

Chapter 1

Introduction

This thesis is concerned with the mathematics bridging courses offered at the University of Adelaide (UofA) through the Maths Learning Centre (MLC): MathsStart and MathsTrack. These courses are intended to take students with very little mathematics background and bring them to a state where they can continue their education (which will generally have some mathematics pre-requisites or assumed knowledge) and be successful. The courses are structured to be student-paced, with no deadlines having been set apriori, in a deliberate attempt to both alleiviate test-anxiety, and to aclimitise students to a learning environment in which the primary onus for motivation is on the students. Although the bridging courses are offered through the MLC at the UofA, the cohort of students come from a very diverse set of backgrounds and have a variety of needs. Although the majority of students enrolling in these courses are planning to continue into tertiary education at the UofA, many students do not intend to continue into tertiary education at all, but instead enroll in the bridging courses to meet the requisite assumed knowledge for other pathways — pilot training in the defence forces, for example. The purpose, structure, and context for these courses are discussed in more detail below, but this brief introduction is enough to introduce the "guiding question", or "purpose statement" for this thesis, which is:

How can MathsStart and MathsTrack be improved?

Naturally, this vague statement invites the question "how is improvement measured?", or "improvement in what outcome?". The question is left deliberately vague in this way because part of this work will be dedicated to teasing apart the different possible interpretations, the importance of taking care when interpreting improvement in an educational context, and the consequences of different interpretations. A solution is not proposed, only alternatives and their consequences, with comments on the stakeholders in each case. In the spirit of being vague however, as educators our interest is always centered on the best interests of our students and this is the general position taken in this work. Of course, determining what is in the best interests of our students, is not always clear.

In order to address this guiding question, this thesis will be structured as follows:

• The remainder of this introductory chapter (Chapter 1) is broken into two broad topics. First, in Section 1.1, a broad educational framework is introduced which can be used to give large-scale context for the work that will be done in this thesis, motivating the structure of the work and outlining the key areas of importance. Second, the remainder of this introductory chapter will

be spent exploring in more detail the purpose, structure, and context of mathematics bridging courses in general (Section 1.2) and specifically at the UofA (Section 1.3)

- In Chapter 3 I will provide a indepth discussion of the existing literature, what
 is known, approaches attempted in the past both in Australia and internationally, and some deeper discussion on some of the particularly relevant related
 concepts, such as maths anxiety.
- One of the major contributions of this thesis is the detailed curriculum mapping which is the focus on Chapter 4 in which the top two levels of senior highschool mathematics in the Australian Curriculum (AC) and South Australian Certificate of Education (SACE) are mapped to each other, and to the content currently in MathsStart and MathsTrack. Detailed discussion of this mapping also includes commentary on how the content relates to typical entry-level university mathematics courses, and other relevant curriculums.
- Finally, in Chapter 5 the conclusions from this work are summarisd, and in particular the interactions between the different avenues of research are consolidated. Additional work done outside of this thesis is discussed, and future work is outlined.

1.1 A Framework to Frame this Work

When considering improvements to the bridging courses, one of the key concepts that comes immediately to mind is content — curriculum. The content of the courses is one of the things that can be most readily modified, and niavely one might think that in this way, improvements to the course could be easily implemneted. However, as discussed by (Mohandas, Wei, & Keeves, 2003) and will be explored in much more depth in Chapter 3, content does not live alone, and cannot be considered independantly of the broader environment. Specifically, there are bidirectional relationships between curriculum (content), learning experiences (the experiences students have while learning), and evaluation (an umbrella term containing several meaningfully different concepts that will be discussed below), as shown in the curriculum triangle of Tyler (1949) in Figure 1.1. To give some simplified examples:

- A test is informed by the content as it must not contain content not taught in the course, and might aim to cover all of (or most of) the content taught in the course. But the results of the test, or even the fact that there is a test at all, can (and should) also influence decisions about what content to include in the course in the first place.
- The learning exeriences students have depends on the content, obviously. But in the other direction, student's experiences should also inform decisions about curriculum.
- If students with a specific concept in a test, perhaps the learning experiences
 they have surrounding that concept should be re-examined. On the other hand,
 if the learning experiences students have surrounding a particular concept are
 framed in a particular way, then the way those concepts are tested should take
 that into account.

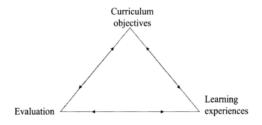


Figure 1.1: The curriculum triangle of Tyler (1949) as visualised in Figure 1 of Mohandas et al. (2003)

Although each of these areas can be considered individually to some degree, it is important that when decisions are made that the bigger picture with all the interactions is taken into account. Mohandas et al. (2003) also make the good point that Evaluation needs to be thought of more granularly, as different forms of evaluation serve very different purposes, and very different roles in both the learning and teaching processes. They expand the curriculum triangle to the "curriculum-evaluation diamond" shown in Figure 1.2, which is of course no diamond at all, but rather an triangular bipyramid with its axis of $\frac{2\pi}{3}$ rotation symmetry representing the fully connected graph of 5 nodes. Mathematical pedantry aside, Mohandas et al. (2003) make the important point that two critical changes should be made to the curriculum triangle model:

- (Student) assessment should be distinguished from evaluation and accountability (Mohandas et al. (2003) also present definitions for each of these terms in order to help distinguish them, of which a concise summary will be included below).
- Standards of performance and how they interact with the other elements play an important role.

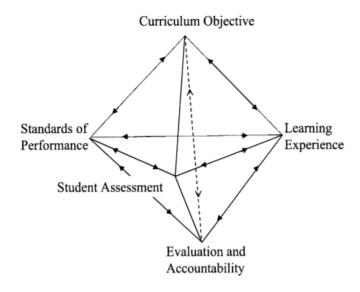


Figure 1.2: The curriculum-assessment diamond as shown in Figure 2 of Mohandas et al. (2003)

The definitions of the terms "assessment", "evaluation", and "accoutability" according to Mohandas et al. (2003) and hence as used in Figure 1.2 are useful in order to distinguish between these concepts, and very concisely can be summarised as:

- Assessment usually refers to indivudual students, and it's goal is generally to understand what/ how much learning has occured. It can be performed by eductors, or importantly by students themselves, and it can be formal (tests, exams, assignments) or informal (discussion, practice questions, etc.)
- Evaluation usually refers to some a decision making process: A university evaluates a student to decide if they should be allowed to enroll in a particular degree, for example.
- Accountability usually refers to a responsibility held by an educator or organisation, and is often associated to reporting to some stakeholders.

All three of these terms are important and hold important but very different roles in the context of improving the bridging courses. Assessment is the most important, and in particular student self-assessment as will be discussed in more detail in Chapter 3, but also in terms of the self-pacing of the assignments in the bridging courses, which act as all three: assessmnet (because of the feedback cycle used to help students through the assignments, they are initially used to assess the learning that has occurred and use this information to inform students about how to proceed through feedback), evaluation because the assignments are used to gate students from completion of the courses, and accountability to ensure students are at the required level of knowledge and satisfy the responsibility of ensuring they are adequately prepared for their future studies.

There are two key concepts in which the standards of performance are important. First, because it is important to establish standards based assessmnet in which students are assessed against fixed standards and not against each other (this is widely accepted in the educational literature). Secondly, these fixed standards should be set in clear objectives in mind. It is in this sense that the standards of performance are quite complicated to nail down in the context of the bridging courses. Typically at a university level, standards of performance will be determined by things such as industry standards (for example studying an engineering degree, the industry standards for engineers will apply). Ultimately, the skills and knowledge required of students completing a degree will be determined by the skills and knowledge that the industry hiring those students needs graduates to have. However, with the students in the bridging courses going in so many different directions this is difficult to determine. In Chapter 4 we discuss some of the most common first year subjects students aim to enroll in (which are common to many different degrees), but ultimately as the bridging courses usually fit into the secondary-tertiary transition, i.e. the evaluation of students for university entry, the primary basis for the standards of performance is the senior highshool curriculum, which is discussed in detail in Chapter 4.

This thesis can be thought of as consisting of two broad avenues of research, focusing on different parts of the curriculum-assessment 'diamond' shown in Figure 1.2:

 Chapter 4 explores the curriculum and standards of performance part of the 'diamond' by mapping the national and state curriculums to the current currliculum of the bridging courses, while discussing the various relevant standards of performance to contextualise the advantages and disadvantages of including or excluding particular sections of these curriculums.

• Chapter 3 explores the existing literature in order to make reccomendations around what learning experiences and assessment methodologies are needed in order to facilitate the learning prescribed my the curriculum discussion.

Naturally, and as supported by the 'diamond' framework of Mohandas et al. (2003), neither of these two approaches to improvement of the bridging courses would be successful in isolation, but rather by taking into account both in unison real improvements could be acheived.

1.2 Bridging Courses

Students will usually enroll in university mathematics bridging courses because they are required to demonstrate a certain level of mathematical knowledge/ competence before commencing study at university, but either do not meet those requirements, or do but feel a lack of confidence in their abilities and feel like they need to refresh/revise/ learn some mathematics prior to commencing their studies.

Reasons why these students do not either meet the entry requirements, or feel a lack of confidence in their abilities can be quite varied:

- A long period of time may have passed since they last studied mathematics (or studied at all). Adult-entry students are over-represented in bridging courses (REFERENCE?).
- They may have performed poorly in mathematics in highschool.
- They may have chosen not to study mathematics at a higher level in highschool.
- They may suffer from maths anxiety (which would make them likely to fit into the above two categories as well).

The role of mathematics bridging courses is to take these students, and:

- Bridge their content knowledge so they are prepared for university entry.
- Support the growth of their confidence and self-efficacy surrounding mathematics.
- Ultimately prepare them to be successful in a university context.

What content should be taught in a university bridging course is actually a question that has dramatically different answers from different perspectives on the role of such a course, even when restricting the question to purely knowledge-based content (and excluding the teaching of self-efficacy etc.):

• If you take the perspective that the role of such a course is to fill in the gaps in student's knowledge left from an incomplete or maths-light highschool education, then the content that should be taught should be up to and including the advanced year 12 australian curriculum. This is particularly appropriate if you do not know the direction of the students, or if they are potentially just doing the bridging course with you and they are planning on studying a degree at a different university say, interstate.

If you take the perspective that the role of such a course is to prepare students
for entry into the particular courses they are about to commence studying, the
content relevant to them will be dramatically different. The senior mathematics
australian curriculum is extremely generalist and contains many topics that
would be completely irrelevant to any particular field of study.

In terms of choosing what content to teach in a university bridging course, the above two competing perspectives will often create tension between each other, making finding a happy compromise a difficult endevour.

Quote from (Johnson & O'Keeffe, 2016):

(Hardin, 2008) highlights that in recent years, the 'face of higher education' has changed, with a more diverse range of leaners now entering third-level education. (Hardin, 2008) notes that in 1987, the number of adult learners 2 in College or University in the U.S. had increased to 4.9 million and the 2010 projections were set at 6.8 million. In the Irish context, the National Adult Learning Organisation (Aontas) identified that in 2012, adult learners accounted for 15% of all third-level full-time students and 96% of all part-time students. According to Aontas (2012), these percentages equate to circa 6000 full-time and 1500 part-time adult learners each year. (Murtaugh, Burns, & Schuster, 1999) point out that increases in the number of adult learners can cause additional retention worries for university policy-makers, as research shows that attrition rates have been found to increase with age. Further to this statistic, studies such as those conducted by (House, 2000) and (Tsui, 2007) indicate that significant numbers of students dropout of STEM degree programmes within the first two years, which highlights the importance of addressing this retention issue as early as possible in a student's career. One approach that has proven effective in addressing this issue is to encourage students to engage with mathematics learner support provisions. (Lee, Harrison, Pell, & Robinson, 2008) advocate that appropriate engagement with mathematics learner support can have a positive impact on student retention and progression.

1.3 MathsStart and MathsTrack

The University of Adelaide offers two mathematics bridging courses, MathsStart and MathsTrack, through their maths learning center. According to the staff at the maths learning center, the vast majority of students enrolling in their bridging courses are aiming to end up in one of three places:

- Studying a tertiary degree at The University of Adelaide (approximately 60–70% of bridging courses at any one time),
- Studying a tertirary degree at James Cook University, or
- In the defence forces.

Only about a single student will not fit into any of the three categories above at any one time, so thinking of this as being the complete cohort of students is fairly close to being accurate. The distribution within these categories can also be broken down and the most common trends considered:

- Of the students aiming to enroll in a tertiary degree at the University of Adelaide, about 50% are aiming to study something in the Faculty of Engineering, Computer and Mathematical Sciences (ECMS) (i.e. Engineering, Mathematics, Computer Science, etc.), and about 10% are aiming to study something in the sciences, often vetenary science or oral health.
- Of the students aiming to enroll at James Cook University, most are aiming to enroll in medical degrees, with some interested in marine biology or vetenary science broadly biological science in large.
- Of the studets aiming to enlist in the defence forces, the majority of those enrolled in the briding courses are doing so to meet their pre-requisite mathematics knowledge criteria for airforce pilot training.

To meet the needs of these cohort of students, it is clear there are two broad areas of content knowledge that different students will need:

- Calculus focused maths, differentiation, integration, and understanding of functions and graphs are fundamental to the students aiming to study in ECMS at the University of Adelaide, as most entry level mathematics and engineering subjects are very calculus-focused, and this calculus-emphasis is carried through both engineering and mathematics degrees.
- Probability/ Statistics are an important focus of the science, with particularly biological science students having been found to struggle with the mathematical (largely statistical) requirements of their degrees (ADD REFERENCE HERE?).

Both of these focus-areas require a base of content knowledge of fundamentals, things like re-arranging equations, fractions, log-laws, etc. So it makes sense to structure the content of the bridging courses in a way aligned with this thinking, in order to best meet the needs of the students enrolled in the programs.

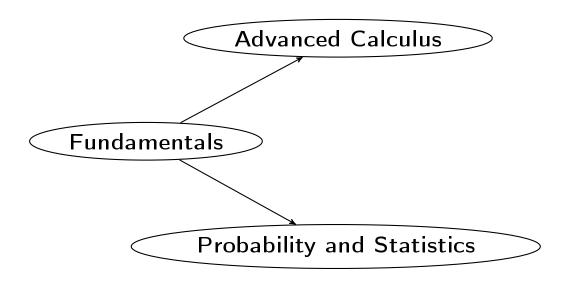


Figure 1.3: Ideal High-Level Content Structure for the University of Adelaide Bridging Courses

Chapter 2

Methodology

In this chapter the methodology imployed when performing the research presented in the remainder of this thesis is described. There are two main bodies of work in this thesis:

- A literature review, presented in Chapter 3, and
- A curriculum mapping, presented in Chapter 4.

Each of these bodies of work was completed employing a non-overlapping methodology, and so the methodology for each will be described seperately.

2.1 Literature Review

The initial phase of the literature review was performed in an iterative process which given a list of references involved reading the list of references and generating a new list repeatedly. In the first iteration, the papers identified where (Nicholas & Rylands, 2015), (Gordon & Nicholas, 2013b), and (Johnson & O'Keeffe, 2016), and these where found by using search engines, including google scholar and the UofA library search with terms such as "mathematics bridging courses" in order to identify several recent, directly relevant, key papers to start with. The iterative process then involved reading the current list of references, taking notes and quotations for later use, and compiling a new list of references by:

- Noting relevant references used in the current list,
- Papers referencing these papers (using "cited by" functionality of search engines),
- Additional papers identified by use of seach engines for newly identified key terms, such as "adult-education" for example.

This iterative process was performed until the same papers kept coming up more and more frequently, which only took approximately three or four iterations. Then, the notes and quotations made while reading these references where reviewed, and synthesised into a coherent discussion, which is presented in Chapter 3.

2.2 Curriculum Mapping

The curriculum mapping was performed by first establishing the levels of detail of interest, and terminology for these levels of detail. Specifically, there are two levels of detail at which the curriculum mapping is performed: the topic level, and the key concept level. These are discussed in more detail in Chapter 4, but very breifly each curriculum is broken up into approximately 12-24 topics, with each of these topics including typlically 6-12 key concepts each.

The first phase of the curriculum mapping methodology was to summarise the key concepts in a concise way such that in the later phases this summary could be used to guide alignment between curriculums. This essentially boils down to the generation of the table presented in Appendix A. This was essentually a 'document analysis', and involved carefully reading the curriculum documents associated to each curriculum, and summarising the key concepts in each topic therin. There are three curriculums analysed in this way, and the details of how this phase was performed for each follow:

- For the AC, the curriculum is presented on their website, and both Senior Mathematical Methods and Senior Specialist Mathematics where considered (accessed between Feburary and May 2019). Each of these subjects is broken down into 4 units, and each unit has three components: a description, learning outcomes, and content descriptions. The content descriptions section for each unit is split into three topics, each of these topics corresponds to a topic in our level of detail terminology. The material under these topics in the content descriptions section of each unit was the focus for this curriculum mapping, and this is the material that was read carefully and summarised to generate the key concept list in Appendix A.
- For SACE, the Subject Outline (for teaching in 2019) document was retreived from the SACE website for each of the three relevant subjects: Stage 1 Mathematics, Stage 2 Mathematical Methods, and Stage 2 Specialist Mathematics. In each of these documents, the "LEARNING SCOPE AND REQUIREMENTS" section contains a summary of the curriculum by topic, and each of these topics correspond to a topic in our level of detail terminology. Within each topic, SACE often has subtopics, but we do not consider this level of detail in this curriculum mapping, instead treating each entire topic as a whole. Within each topic, the left-hand column "Key questions and key concepts" was read carefully and summarised to generate the key concept list in Appendix A. As discussed in Chapter 4, the focus of this curriculum mapping is primarily on the content itself, rather than the surrounding concepts involved in how the content is taught (which is more what the right-hand column, "Considerations for developing teaching and learning strategies" is relevant too).
- For the bridging courses, the content is available on their website in the form
 of a number of booklets for each of the courses: MathsStart and MathsTrack.
 Each of these booklets will constitute a topic in our level of detail terminology,
 and these entire booklets where carefully read and summarised to generate the
 key concept list in Appendix A.

Once the first draft of the key concept summary presented in Appendix A was completed, two mappings where produced: one at the topic level, and one at the

key-concept level. The topic level mapping, shown in Figure 4.1, was produced by comparing the broad concepts covered in the topics, with little concern for the details involved with particular alignment of key concepts. For example an "introductory calculus" topic would be mapped to another "introductory calculus" topic, even if a specific concept such as anti-derivitives is introduced in one but not the other. The purpose of this mapping is to provide a high-level view of the mapping between the curriculums in order to help structure the more detailed discussion of key concept alignment. The key concept alignment was then performed by going topic by topic, and aligning every single key concept listed in Appendix A, then in any mismatching cases, referring back to the original curriculum document to check for mistakes and validate any conclusions made. This mapping is obviously too complex to be able to meaningfully represent it graphically, and so instead the conclusions thereof are presented in the form of discussion in Chapter 4. No major mistakes where discovered in this process, but some small modifications where made to Appendix A all of which had to do simply with harmonising terminology used. For example, "slope of a line" vs "gradient of a line", etc. This key concept level mapping was also used to make adjustments to the topic level mapping shown in Figure 4.1. No major changes where made, but single key-concept links where added as dashed lines as a result of the key concept mapping.

Although it was not part of the initial intent, it became apparent in the process of completing the mappings described above that particularly due to the very different structure of the curriculums it would be useful to add another level of detail in which topics where grouped under broad areas of mathematics, and to reproduce another version of Figure 4.1 in which the tipics where rearranged into these broad areas, so this was done producing Figure 4.2.

Chapter 3

Literature Review

3.1 Introduction

In this chapter the literature surrounding mathematics bridging courses in Australia and internationally is explored. The literature reviewed here is not restricted strictly to these topics, but also extends into some directly relevant areas, specifically areas such as general perceptions of mathematics, the secondary-tertiary transition, relevant frameworks that have been proposed, and some of the key areas that prevent students from being successful such as maths anxiety.

Remembering the purpose statement of this thesis, and the questions it raises, it is interesting to note that these questions are by no means new questions, although they do not neccessarily have any consensus on how to answer them. In particular, Poladian and Nicholas (2013) offer an insightful discussion of two key (unanswered) questions within bridging mathematics posed by Galligan and Taylor (2008):

- How is success defined in bridging mathematics activities?
- Are successful bridging mathematics students successful university students?

which Poladian and Nicholas (2013) address with the following comments:

- "there are inherent difficulties in defining and measuring success in bridging courses. Godden and Pegg (1993) suggest that formal evaluation of bridging mathematics programs may be contrary to the aims of the programs, and undermine their major strengths of flexibility and student-centred approach. They argue that traditional evaluative techniques are 'just not possible' and 'risk losing the essence of the support and assistance so necessary for these students'."
- "internationally, bridging mathematics programs have been shown to be highly effective at resolving skill deficiencies for some students (Kajander & Lovric, 2005; Bahr, 2008). In a large US study, (Bahr, 2008, p.442) found that 'remediation has the capacity to fully resolve the academic disadvantage of math skill deficiency' for the quarter of students who 'remediated successfully', but the likelihood of successful remediation declined sharply as the 'depth of remedial need' increased. The latter finding echoes (Wood, 2001)'s remark that bridging programs do not work for very mathematically weak students."

respectively.

TODO: I should comment more on the quotes above, and update intro to literature review once I've finished the lit review, to better reflect the content of the chapter.

3.2 "The Mathematics Problem"

"The mathematics problem" is a term originally coined by Howson et al. (1995) but that has continued to be relevant to the present day, receiving even greater attention and research in recent times. It refers to the trend of declining interest and participation of final year highschool students in mathematics. It also refers to the carry-over effects this has on the success of students in tertiary education (both in mathematics, but also notably in other areas). "The mathematics problem" is a term now used also to describe the downstream impacts these trends have on the economy: modern industries are dominated by a need for mathematically skilled graduates (engineering, science, technology, ...), but the importance of mathematics in these fields is often overlooked from the general populations perspective (King & Cattlin, 2015; Gordon & Nicholas, 2013b).

Barrington and Evans (2016) shows that in Australia, although the number of both advanced and intermediate mathematics year 12 students was increasing over the ten years from 2006 to 2015 (as the overall population of total year 12 students increased), the percentage participation in these subjects steadily declined. James (2019) updates the figures of Barrington and Evans (2016) with data up to 2017, showing a continuation of the same steady trend. These reports also highlight the significant gender gap that exists in mathematics participation in final year highschool students. The gender gap is more dramatic in advanced level mathematics than in the intermediate level, with 37.8% of advanced mathematics year 12 students identifying as female, especially when considering that 51.8% of year 12 students of that year where female. 2017 saw a significant jump in intermediate level mathematics participation by female students, with there being more female students than males for the first time in recorded history (James, 2019). The gender gap in mathematics education is a significant issue that needs to be taken into account when considering unviersity mathematics entry, particularly as the gap is most pronounced in the advanced level subjects which are targetted at university entry. It is an issue recognised by the Australian Mathematical Sciences Institute (AMSI), who have commited significant resources towards programs intended to address this inequity. Perhaps the uptick in female student participation in intermediate level mathematics in 2017 could be partly attributed to some of these programs, such as the CHOOSEMATHS project. (Brown, 2009) gives a shocking wider-view picture of this overall trend, specifically that the proportion of year 12 students studying intermediate or advanced level mathematics has declined by 22% and 27% respoectively from 1995 to 2007.

Amongt other reasons, this decline in participation in mathematics is a problem in Australia because mathematical skills are essential to just about all the key future industries (Croft, Harrison, & Robinson, 2009), and hence the Australian economy. The key economic importance of mathematics is widely acknowledged amongst the academy and industry, but it's importance is often overlooked and difficult to communicate to the wider community because of it's indirect importance through what

are perceived to be other fields: engineering, science, etc. all of which require a deep level of mathematical skills, but aren't associated to mathematics in the general populations view. Thomas, Muchatuta, and Wood (2009) argues that one of the most influential factors in the declining participation in mathematics is the "community's perception that mathematics is not useful in the marketplace". Gordon and Nicholas (2013b) go on to emphasise the carry-on effects of negative community perceptions of mathematics leading to highscool students choosing not to participate in higher-level mathematics impacting on not only their success in university, but on whether they continue to study mathematics at all. This obviously has implicatons for mathematics bridging courses at universities, as it is to them that these students will turn should they realise the importance of mathematics later on in life.

Observation, concern surrounding, and research of this decline in mathematics participation in senior highschools are not limited to Australia (Hourigan &O'Donoghue, 2007; Hoyles, Newman, & Noss, 2001). Hoyles et al. (2001), as well as Luk (2005) further connect this trend to another: the apparent divergence of content (curriculum) between senior secondary and tertiary education. This divergence of curriculum is a point that will be explored extensively in Chapter 4. In a landmark study, Kajander and Lovric (2005) identified a gap between secondary and tertiary mathematics education in Canada. In the United Kingdom Tariq (2002) noted a decline in numeracy skills among first-year bioscience students. This trend is neither limited to Australia, nor new. Universities around the world have recognised this continuing problem for some time, but oppinions on how to address it vary. Robinson (2003) suggested that the standard for highschool mathematics should be raised, but even if there where consensus amongst the academy that this was appropriate (which there is not), this is beyond the power of universities to control (although, the setting of pre-requisites is a topic that will be explored in more detail below). Within the power of universities to implement are solutions such as to introduce "remedial mathematics" into first-year teaching programmes as highlighted by Kitchen (1999). More recently, as Moses et al. (2011) suggest, universities have been increasing their reliance on "advanced and targeted preparatory programmes" — i.e. briding courses. As an example of this from outside Australia, Faulkner, Hannigan, and Gill (2010) note that at the University of Limerick in Ireland

"there has been a 20–25% reduction in students attending their first service mathematics lecture, a 12–16% reduction in the number of students entering service mathematics modules with higher level mathematics and an 8–12% increase in the number of non-standard students. Such changes place additional pressure on support services like MLCs whose primary function is to provide the necessary and appropriate support to all university students."

(Johnson & O'Keeffe, 2016)

3.3 The Secondary-Tertiary Education Transition

A key step we are interested in from the perspective of bridging courses is university entry, or more broadly: the transition from secondary to tertiary education. It may seem obvious that students engagement and performance in mathematics in secondary education is a strong predictor of their success in tertiary mathematics education, but the exact relationship has some important subtleties. Specifically, it

has been shown that the level of mathematics completed in highschool (advanced, intermediate, etc.) is substantially worse at predicting success in tertiary mathematics education than when combined with the level of acheivement in secondary school (Kajander & Lovric, 2005; Nicholas, Poladian, Mack, & Wilson, 2015). Students having completed a lower level of mathematics in secondary school to a higher degree of acheivement can in some cases have a higher chance of success in tertiary education than students who completed a higher level of mathematics in secondary school but to a lower level of acheivement. Although this might seem intuitive, it is not entirely obvious when looking at it in terms of content — curriculum — alone. It should not be understated that although it has been shown quite clearly that the effect of bridging courses is smaller than the effect of highschool engagement in mathematics education, that bridging courses have been shown to have a substantial effect nonetheless, and even more importantly have been shown to fill a critical gap in addressing student needs (?, ?). It is important to acknowledge the importance This is important to acknowledge, and will come into the discussion surrounding university entry requirements below, but engaging students in mathematics in secondary school is beyond the scope of this work, although it is clearly a very important aspect of "the mathematics problem". For now, we consider that one of the roles of bridging courses is to make tertiary mathematics education accessible to all students, including those that where disengaged with mathematics in highschool and therefore are in particularly high risk in tertiary education.

Rite of Passage Model

Very little has been done in terms of developing educational frameworks for understanding the secondary-tertiary transition more systematically, but Clark and Lovric (2008) suggest using the pre-existing and well-undestood literature surrounding the concept of a 'rite of passage' from anthropology and culture studied (relating concepts such as culture shock) to help structure our thinking about about the difficulties and evaluating strategies to address difficulties with the secondary-tertiary transition. Clark and Lovric (2008) propose using the seminal work of Arnold van Gennep and thinking about a "life crisis" event as consisting of three phrases: separation, liminal, and incorporation. One of key and important implications this perspective has is that this transition does not only involve difficulty for the individuals (students), but the broader community (their family, teachers, etc.). The wider communities negative perceptions of mathematics are widely acknowledged to have a substantial effect on students attitudes, and hence success (King & Cattlin, 2015; Gordon & Nicholas, 2013b), and it is important to take this into account. One of the immediate consequences the "rite-of-passage" model implies is that "It is normal to feel discomfort during a rite of passage but much easier to deal with if this is expected." (Clark & Lovric, 2008). This is a key take-away: setting clear expectations is critical for students to be able to cope with the difficulty of this transition, they need to know that it will be difficult, so they can expect that difficulty and come into it prepared.

NOTE: There are also some suggestions made by Clark and Lovric (2008) that I disagree with. Specifically, that we abandon imprecise language and descriptions of concepts, in favour of rigorous explicit anguage. I should probably add some discussin of this here.

None-the-less, the "rite-of-passage" model of Clark and Lovric (2008) aligns well with the broader literature and research surrounding bridging courses and the

secondary-tertiary education transition. Specifically, the concept of being socially isolated and needing to adapt to a new environment with different expectations and social norms is reflected widely in the academic writing. Gordon and Nicholas (2013b) disuccses how one of the key valuble experiences students got out of the bridging courses at the Unviersity of Sydney was the interactions with peers and teachers. This experience is supported by literature discussing the importance of social and interactive learning as a formative element of early university experience that is highly predictive of retention (Peat, Dalziel, & Grant, 2001; Trotter & Roberts, 2006) particularly for students whose family or friends are for example from a "working class" background (Leese, 2010), or from a cultural background less familiar with the social norms and expectations associated with university education. In particular, self-motivation and independant learning are expectations that consistently come up as being shock factors for students transitioning from secondary to tertiary education (Murtagh, 2010).

Assumed Knowledge and Conditions of Entry

Contributing to the problem of expectations not being set explicitly, in recent years Australia universities have been moving away from prerequisites for entry towards a "assummed knowledge" approach. What this means is that instead of requiring students to have completed certain subjects in highschool in order to allow them to enroll in a course at university, they instead put the content from those subjects under "assumed knowledge", allow students to enrol in the subject even if they have not completed the highschool subject, and put the onus for having that knowledge on the students. That is how the universities see it, anyway. How the students see it is quite different, as demonstrated by the work of Gordon and Nicholas (2015), who show substantial variance in student perceptions of "assumed knowledge" ranging from perceiving it as vague and pointless 'stuff' to a cohesive body of foundational knowledge for tertiary study". One of the consequences of this is the increasing under-preparedness of first year undergraduate students.

The issue of entry requirements into university and prerequisites being moved into "assumed knowledge" is an even more complex issue than it might at first appear. Varsavsky (2010) discuss how in Australia the way university entry is managed may infact be contributing to the problem of low participation in higher level senior highschool mathematics. Specifically, the absence of prerequisite subjects in many universities means the only condition of entry to university is the acheivement of a sufficiently high "tertiary entrance rank", a score calculated based on acheivement in all final highschool year subjects, with some adjustments for the combination of difficulties of the subjects. A substantial amount of effort is gone too by final year highschool students, teachers, and councellors to optimse students performance on this tertiary entrance rank through very careful choice of which subjects to take in their final year of highschool. Often this will result in creating a tension between acheiving a high tertiary entrance rank and hence being accepted into university, and having the required knowledge to be successful in university because the subjects chosen are not those containing the content relevant to the degree the student is enrolling in (Gordon & Nicholas, 2013a; Poladian & Nicholas, 2013). This is of course an issue that generalises far beyond mathematics, but to every area of study. Gordon and Nicholas (2013b) claim that: "the major reasons for students taking lower levels of mathematics in senior year(s), or dropping mathematics, include finding enough time for non-mathematics subjects, confidence in mathematical capability, advice and maximizing potential ranking for university admission". Rylands and Coady (2009) demonstrated that what a student studied in senior highschool predicted their performance at university, whole their tertiary entrance rank did not. The result in the bridging course literature that although bridging courses can help, their effect cannot compare with engagement in highschool is a result that has been reproduced many times in the literature accross many countries (Kajander & Lovric, 2005; Nicholas et al., 2015; Tariq, 2002). This is likely, as suggested by Kajander and Lovric (2005), due to the time-period typically involved. A bridging course is usually a short preparatory course covered in an interim before beggining tertiary study, while highschool engagement is a learning and teaching experience spanning several years. Despite Australia's Chief Scientist reccomending moving back to pre-requisites (Chubb, Findlay, Du, Burmester, & Kusa, 2012), there is no sign of this being on the table: the commercial aspect of universities demands increased enrollment of students, and that means relaxing entry conditions.

NOTE: (King & Cattlin, 2015) has more to say on this topic, I should review that paper and maybe adjust/ add some more discussion here.

3.4 Maths Anxiety

Why is Maths Anxiety Important?

Maths anxiety is hugely prevalent, the 2012 Programme for International Student Assessment (PISA) report states that across Organisation for Economic Co-operation and Development (OECD) countries, over 30% of 15 year old students "get very nervous doing mathematics problems", and over 60% of students "worry about getting poor grades in mathematics" (OECD, 2013). This not only impacts on those students in terms of their academic performance and subject choice, but given this has been an ongoing issue for many decades with literature documenting it dating back to the 1950's (Dreger & Aiken Jr, 1957), it is also a community issue — parents, and teachers also suffering from such anxieties and hence both normalising the behaviour as well as actively passing it down. It has been shown that students with a high level of maths anxiety often literally experience the anticipation of a maths task as visceral pain (Lyons & Beilock, 2012), this is no small issue.

Even if the wellbeing issue was not enough, there is also a clear maths anxiety-performance connection, which is where it holds particular relevance to enrollments in bridging courses. Students enrolling in bridging courses are more likely to have performed poorly in highschool and given the prevalence of maths anxiety and the strength of the maths anxiety-performance link, are more likely to suffer from maths anxiety. This inference is supported by the survey studies of bridging course students by Nicholas, Gordon and Polodian. One example of this is highlighted by Foley et al. (2017) who juxtaposes the internationally rising demand for Science, Technology, Engineering and Mathematics (STEM) professionals with the negative correlation between maths anxiety and performance shown in the 2012 PISA report (OECD, 2013) to highlight the relevance of addressing maths anxiety in filling this demand, aligning with 'the mathematics problem' discussed earlier in this chapter. The relationship between maths anxiety and maths-qualified professionals in the workforce is supported throughout the literature: when a student has low self-concept (correlated

with high maths anxiety), they will tend not to enroll in maths beyond the minimum requirements for graduation (Ashcraft, Krause, & Hopko, 2007), and students affect towards maths can predict their university major (LeFevre, Kulak, & Heymans, 1992). Beyond this example, the list of stakeholders in a students academic success in maths goes on and on: parents; the student's themselves; schools (which are often funded based on the results of standardised testing such as National Assessment Program — Literacy and Numeracy (NAPLAN)), and teachers amongst them. From the perspective of bridging courses, this link is important because A) it motivates supporting these maths anxious students to pursue a tertiary mathematics educations, but also B) because industry is an important stakeholder in tertiary education, inlcuding bridging courses.

Maths Anxiety as Distinct from General Anxiety

The existence of maths anxiety as "emotional disturbances in the presence of mathematics" has been noted as early as the 1950's, Dreger and Aiken Jr (1957) even postulated that what he tentatively designated "Number Anxiety" and later became to be known as Maths Anxiety could be a distinct syndrome from general anxiety. Later the landmark meta-study of Hembree (1990) supported this hypothesis, showing a correlation of only 0.38 between maths anxiety and general anxiety. In more recent times, this hypothesis has also been confirmed by Young, Wu, and Menon (2012) using functional magnetic resonance imaging (fMRI) to show that the brain activity in a person experiencing maths anxiety is measurably distinct from that in a person suffering general anxiety. These later studies, as well as the the work of Kazelskis et al. (2000) and more, have also delineated maths anxiety from test anxiety, and these different anxieties exisiting as meaningfully distinct constructs is now quite well accepted. For more on the history of maths anxiety, Suárez-Pellicioni, Núñez-Peña, and Colomé (2016) offers a more detailed review.

Frameworks for Understanding Maths Anxiety

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Only a few studies focus on maths anxiety itself (primarily fMRI studies such as those of Young et al. (2012) or Lyons and Beilock (2012)). Instead the bulk of the literature is focused on the maths anxiety-performance link. Specifically, there seem to be two distinct theories being pursued and I will adopt the terminology of Ramirez, Shaw, and Maloney (2018) to describe them: the "Disruption Account" and the "Reduced Competency Account". Ramirez et al. (2018) go on to make a convincing argument that although these two theories might seem to compete, they are not actually mutually exclusive and instead quite compatible with each other. Ramirez et al. (2018) suggests a third "Interpretation Account" which encapsulates observations made by both lines of research, see Figure 3.1.

First, a little more detail on the existing theories. The "Disruption Account", spearheaded by the work of Ashcraft et al., is centered around the concept of working memory (Ashcraft & Kirk, 2001; Ashcraft & Krause, 2007). Specifically that anxiety about maths takes up students working memory, which prevents them from using that working memory to complete maths tasks and thereby impacts their performance. The "Reduced Competency Account" on the other hand proposes the opposite causality: that lower ability in maths leads to negative experiences associated

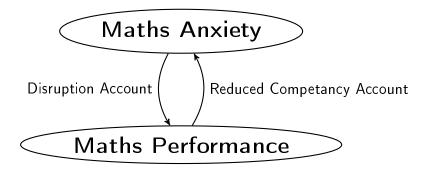


Figure 3.1: The Interpretation Account of Ramirez et al. (2018) for the maths anxiety-performance link showing how the Disruption Account and the Reduced Competency Account can be compatible.

to maths, which in turn cause maths anxiety to develop. There is also a significant body of work to support this hypothesis, including the milestone meta-analysis of Hembree (1990) and the longitudinal study of Ma and Xu (2004) which found that although past maths anxiety was correlated with future maths performance it was a small effect, while past maths performance had a strong effect on future maths anxiety.

Complexities in Finding Effective Interventions

These theoretical views are of course broad oversimplifications of what is an incredibly complex and interconnected topic. They also imply very different approaches for The "Reduced Competency Account" would imply interventions to boost maths performance and hence allow students to experience success in math should also help to reduce maths anxiety. The results of Supekar, luculano, Chen, and Menon (2015) seem to support this hypothesis as when students are given an intensive 8-week tutoring program to boost their maths skills, this is associated to a reduction in maths anxiety. The earlier work by Faust (1996) further supports this by demonstrating an anxiety-complexity effect in which low and high maths anxiety groups performed similarly on low complexity problems, but in high complexity problems the high anxiety groups performance was impacted. On the other hand, Jansen et al. (2013) showed that it is not neccessarily that simple, by showing that when students experience more success they attempt more problems and perform better. However their improved performance is almost completely predicted by the number of problems they attempted, not their experience of success, and their level of maths anxiety was not affected in a significant way which raises a lot of interesting but unanswered questions about this approach.

On the other side of attempted interventions are those in line with the "Disruption Account", in which the maths anxiety itself is addressed in the hopes that will free up extra working memory and hence boost students performance. Park, Ramirez, and Beilock (2014) demonstrate a direct and successful attempt at this in which they used expressive writing exercises to help guide students self-perceived narratives about their maths experiences and thereby reduce their maths anxiety. Notably the approach of Park et al. (2014) is in line with successful treatments for clinical anxiety disorders (see McNally (2007); Becker, Darius, and Schaumberg (2007); Foa

et al. (2005)). Another approach that has shown success in this vein does not attempt to directly reduce the anxiety experienced, but rather reappraise it's symptoms (Jamieson, Peters, Greenwood, & Altose, 2016). This is another technique from clinical psychology in which stress is reconceptualised as a coping tool, an evolutionary method for heightening performance in response to a challenge to be overcome, instead of a symptom of exposure to something to be feared and avoided. This change in the perspective of stress is also very much in line with the "Interpretation Account" of Ramirez et al. (2018).

The work of Wang et al. (2015) showed the role that intrinsic motivation has mediating the relationship between maths anxiety and performance, and suggested the importance of a mindset centred on viewing the process of learning maths as one of "productive struggle". This reconceptualisation to a 'productive struggle' model is supported by other literature as well, Lin-Siegler, Ahn, Chen, Fang, and Luna-Lucero (2016) exposes students in a classroom to struggles experienced by famous scientists in order to help normalise the concept of productive struggle, and Hiebert and Grouws (2007) discuss the importance of this same concept in a maths context.

One of the implications of the "Interpretation Account" is that if an intervention targets only one of these two possible links in the cycle (see Figure 3.1), the cycle may re-establish itself after the intervention is over and negate any potential longterm effects. However there is only a very limited amount of research out there on such longterm effects, and several authors have discussed the need for further research into this (Suárez-Pellicioni et al., 2016; Chang & Beilock, 2016). My hypothesis is that a multi-faceted approach targetting both directions simultaneously could disrupt the cycle shown in Figure 3.1 and result in significant longterm effects.

3.5 The Role of Bridging Courses

(Gordon & Nicholas, 2013b) abstract: "students are aware of the value of the bridging courses not only to ameliorate prior difficulties with mathemat- ics and improve their approaches to learning mathematics but, less trans- parently, as an important opportunity to facilitate their transition into higher education, meet fellow students and help realise their potential." — (Croft et al., 2009; MacGillivray, 2009) could be relevant references for this too.

Quote from (Galligan & Taylor, 2008):

In a quantitative approach, Klinger (2006) investigated attitudes, self-efficacy beliefs, and mathematics anxiety of a diverse group of pre-tertiary adult learners using a self-designed survey and pre- and post-testing. He found that although students initially shared the negative views reported in the wider popUlation, these views changed significantly by the conclusion of the topic(s). He concluded that adults' perceptions of, and capacity to engage with, mathematical content was strongly influenced by early learning experiences, but like authors before, confirmed that these could be changed. In a later study, Klinger (2008) repeated the analysis with commencing arts, humanities, and science students and found the arts/humanities students to have significantly lower mathematical self-efficacy and poorer attitudes than the science students. The results were strongly linked with gender, with females scoring lower than

males. He concluded that these kinds of results indicated that undergraduate support programs would have to address such poor attitudes to enable students to succeed and develop mathematical literacy necessary for their discipline.

In two similar quantitative studies underpinned by Bandura's social cognitive theory (C. S. Carmichael, Dunn, & Taylor, 2006; C. Carmichael & Taylor, 2005), motivation (particularly self-efficacy) and other factors such as prior knowledge were examined as measures of prediction of success in a university preparatory mathematics course. Results suggested that students' assessment of their confidence was based, in part, on their current levels of knowledge and skills, and that this assessment influenced their current performance. Females and those who had been away from study for a long period of time had lower entering levels of confidence and self-efficacy than males and recent school leavers, but final performance in the course was not significantly different.

(Taylor & Galligan, 2006) used conversation theory framework to design a multimedia package to simultaneously develop students' mathematical skills while improving mathematics confidence. The evaluation of this program indicated the effectiveness of this approach. It is apparent through the work discussed above that although attitudes and beliefs about mathematics are important for students enrolled in bridging programs, the programs can change students' attitudes and beliefs about mathematics as well as their achievement. An alternative to the above is to design programs that can assist in self-selection. Egea (2004) has designed and evaluated an online self assessment tool that assists students to choose the appropriate level of bridging mathematics program. It has been speci fically designed with mathematics anxious students in mind, and participating students indicated that the test was 'enjoyable', 'fun', 'easy', and even 'relaxing', confirming that its design had addressed both the cognitive and affective domains.

Quotes from (Johnson & O'Keeffe, 2016):

 Focusing on adult learners, who constitute the largest cohort of non-standard stu- dents at the University of Limerick, (Burton, 1987) and Klinger (2006) as well as (Klinger, 2011) indicate that negative preconceptions are of major concern, both preconceptions of mathematics, in general, and also of their own abilities. (Bandura, 1997, pg391) defines self-efficacy as 'people's judgement of their capabilities to organize and execute courses of action required to attain designated types of performance'. Self-efficacy is vital among all students but particularly among adult learners as an individual's beliefs of self-capability has been shown to affect motivation, performance, achieve- ment, effort, willingness to persist with a task, as well as the anxiety they experience (Bandura, 1997: Pajares & Miller, 1994: Pajares, 1996: Pajares & Miller, 1997: Pajares & Graham, 1999). Woodley (1987) (cited in (McGivney, 1996)) noted that the main personal factors that contribute to dropout are: self-perception, being disorganised, not having sufficient study skills and lacking in self-confidence. This suggests that an indi- vidual's self-efficacy plays a role in their decision with regard to dropping out.

• (Hackett & Betz, 1989) and (Pajares & Miller, 1994) and Pajares and Miller (1995) also found that self- efficacy can have an impact on career choice. In these studies, it was found that math- ematical self-efficacy is a stronger predictor of students' mathematical interest and choice of degree programmes than either prior mathematical achievement or math- ematical outcome expectations. Self-efficacy also influences how often mathematics is used, as well as an individual'swillingness to pursue advancedwork in mathematics, and even the choice of prospective occupations (Dutton and Dutton 1991). Engineers Ireland (2010) highlight that this avoidance of mathematics, and mathematics-related courses, at university will eventually prove detrimental when attempting to build a knowledge economy. This point was also stressed decades before by (Hembree, 1990, pg34) when he stated that 'when otherwise capable students avoid the study of mathematics, their options regarding careers are reduced, eroding the country's resource base in science and technology'.

3.6 Conclusions/ Take-Away Messages

• Setting clear expectations is critical. Although addressing the misconceptions arond mathematics not being critical for other diciplines of study such as science and engineering is beyond the scope of what can be acheived in a bridging course context, students should be explicitly told that the first semester will be hard. It will be stressful. But that it will be worth it. To expect difficulty, but to embrace it. Several frameworks suggest this, including the rite-of-passage model of Clark and Lovric (2008) and the re-evaluation model for maths anxiety from clinical psychology. An emphasis should be placed on not setting expectations that the difficult period will pass quickly, but rather that it is a natural, expected transitionary period. That it will continue to be difficult, but that that is ok. Each of these frameworks suggest that if students are aware of the difficulty ahead of time, they will be more prepared to deal with it when it occurs, and are more likely to be able to do so in a productive manner and be successful despite the challenges.

(Carlson, 1999) shows that establishing a mindset of persistence tackling complex problems puts students in good stead in ongoing mathematical study. Supporting that establishing this 'productive struggle' mindset is effective in acheiving success later on.

• TODO: Condense this point.

Various factors have been identified that ease the transition of students into university and appear to contribute to improved rates of retention. These include activities that help students find their feet, make friends and get to know other students on their pro- gramme (Trotter & Roberts, 2006); learning-to-learn programmes (Zeegers & Martin, 2001) and workshops facilitating the early formation of social networks and peer groups (Peat et al., 2001).

(Gordon & Nicholas, 2013b) shows the value students place on interaction with peers and teachers during the bridging courses. As reported in our introduction, social and interactive aspects of learning in early university education are formative in students' adjustment to and retention in higher education (Peat

et al., 2001; Trotter & Roberts, 2006). This could be particularly critical for students where family or friends are unfamiliar with the discourse and ways of learning in the university context (Leese, 2010).

TODO List (Papers to read in more detail, and incorporate into discussion):

•

- (Irwin, Baker, & Carter, 2018) Talks about the importance of alternate avenues to access education. read and summarise again.
- Some of the books I found would be good to read more thoroughly too, (Volmink, 1994) for example, and/or (McGivney, 1996) for example.
- Quote from (Galligan & Taylor, 2008):

Miller-Reilly (2006), in a significant long term analysis of two large bridging courses and one individual bridging program in New Zealand, used quantitative and qualitative measures to compare students' reactions. These multiple strands of evidence provided a complex overall picture of three largely successful teaching approaches. A one-to-one supervised course focused on understanding fear of mathematics and early mathematics experiences. The course empowered the student who came to believe that mathematics was a creative and enjoyable process. A second course (100 students) focused on the mathematization of realistic situations. Here, students came to regard mathematics as useful, interesting, and relevant to real life. The third course (100 students) was a carefully structured reintroduction of mathematics. The students appreciated the course and were pleased that they could now do mathematics that they could not do in school. Students in all programs were highly motivated, mature, and had not seen formal mathematics for some years. One surprising result from the study was that if students were unsuccessful they were, in fact, worse otT than before, and often confused. A significant component of the study was the focus placed on dealing with students' mathematics anxiety or fear. Quantitative measures and qualitative descriptors indicated a decrease in mathematics anxiety throughout the duration of the three programs, and in the larger courses this correlated with achievement. Beliefs about mathematics in general, however, did not necessarily change, although students in the larger courses did see the practical nature of mathematics.

 Student wellbeing is a research interest, with high strain in the first semester at uni (Bewick, Koutsopoulou, Miles, Slaa, & Barkham, 2010)

Chapter 4

Curriculum Mapping

One of the important roles of university mathematics bridging courses (such as MathsStart and MathsTrack) is to fill the content knowledge gap for students who did not complete mathematics to a sufficiently high level in highschool, or completed it long enough ago that they need to re-learn the material, but wish to commence study at a university level in subjects that have a high level of required knowledge in mathematics.

There are two angles from which this required knowledge can be seen: the knowledge required for the university study intended, and knowledge expected from high-school graduates. As we will come to see, these two angles or perspectives can be quite dramatically different. From the perspective of knowledge expected from highschool graduates, the AC serves as a good guide, but even so the exact content knowledge expected of students having completed highschool in Australia varies for a number of reasons:

- To begin with, the AC specifies four levels of mathematics: essential mathematics, general mathematics, mathematical methods, and specialist mathematics. Our focus will be on the higher two of these: mathematical methods and specialist mathematics, as these are the ones often associated to university entry into mathematics-intensive courses.
- Different states within Australia teach different curriculums, with varying degrees of alignment to the AC. In South Australia the primary curriculum taught in senior secondary school is SACE, and so we will focus on that.

The other perspective is of course the knowledge required for entry level university mathematics courses. This will vary hugely from course to course: a entry level calculus course will require very different knowledge than an entry level statistics course, for example. Even within one discipline of mathematics, different universities will have very different expectations of entry level students: in particular, South Australian universities will often structure their entry level mathematics courses to align with SACE even though not all their students have completed SACE, because of the majority who have it is still useful for them to do so. For example, the University of Adeliade re-structured it's first year mathematics courses in 2018 to match changes in SACE. Similarly, universities interstate will often structure their entry level courses to align with their local senior highschool curriculum.

This places a difficult tension on mathematics bridging courses as to what content to teach. Although many of the students enrolling in the mathematics bridging

courses at the university of adelaide do so with the intention to begin study at the University of Adelaide (and hence might benefit from SACE structured content), many do not. Even amongst those that do, some may end up going to a different university interstate or even overseas — plans change. So it is important to try and maintain some connection to a broader set of knowledge expected in general and not neccessarily remain laser focussed on the requirements of the particular university courses most students are going to be attempting. This is one of the reasons why the AC is a useful construct as even though some states do not align to the AC as well as others, it still forms a guiding structure at a national level and individually considering the curriculum taught in each state is... beyond the scope of this work. Tailoring the content of the bridging courses more narrowly to target entry into particular disciplines (say calculus/ matrix alebra/ statistics for example) could potentially still be of interest down the line, but is likely to be unrealistic with the current resources available to the maths learning center.

This chapter will examine the alignment of the content of MathsStart and MathsTrack (the mathematics bridging courses offered at the university of adelaide) with the AC and SACE. First, in Section 4.1, some notation will be introduced and the content of each of the three curriculums will be reviewed:

- The AC senior mathematics subjects mathematical methods and specialist mathematics,
- The SACE curriculum stage 1 mathematics, stage 2 mathematical methods, and stage 2 specialist mathematics,
- The University of Adelaide's bridging courses: MathsStart, and MathsTrack.

Then, these will be mapped to each other in Section 4.2 (see Figure 4.1), and alignments/misalignments discussed. Finally, the discussion throughout around alignment and gaps between the content of these curriculums and courses will be summarised, explanations and reasons for these discrepancies discussed, and potential modifications to content suggested.

Beyond that, this chapter will also briefly discuss the alignment of these bridging courses to first year university mathematics courses and bridging courses offered by other universities in Australia, and discuss the relationship between the gaps in alignment between the AC/SACE and the bridging courses and the requirements of these first year university courses.

4.1 Content

4.1.1 Notation

Each of the senior highschool curriculums, as well as the university bridging courses, being considered here is broken down into topics, with each topic containing a number of key concepts. In Section 4.2, the alignment between these curriculums and bridging courses will be considered thoroughly at both a topic-level, and to the finer detail of particular key concepts. In order to abstract away some of the complexity of considering the topic-level alignment, and be able to present the topic-level alignment in a meaningful way abbreviated codes will be used to identify each topic. These abbreviated codes are presented in Table 4.1 and will be used for the remainder of this chapter.

Table 4.1: Abbreviated codes for topics within the AC and SACE senior mathematics subjects: Mathematical Methods nd Specialist Mathematics, as well as the Unviersity of Adelaides bridging courses: MathsStart and MathsTrack. Square brackets ([]) are used to indicate numeric values that can vary.

Code	Meaning
MMu[#1]t[#2] MMu[#1]t[#2]	AC Senior Mathematical Methods Unit [#1], Topic [#2] AC Senior Specialist Mathematics Unit [#1], Topic [#2]
S1M[#] S2MM[#] S2SM[#]	SACE Stage 1 Mathematics, Topic [#] SACE Stage 2 Mathematical Methods, Topic [#] SACE Stage 2 Specialist Mathematics, Topic [#]
MS[#] MT[#]	Maths Start, Topic (Booklet) [#] Maths Track, Topic (Booklet) [#]

4.1.2 Within-Topic Key Concepts

Description of each topic in the AC Mathematical Methods and Specialist Mathematics Topics, SACE stage 1 mathematics, stage 2 mathematical methods and stage 2 specialist mathematics, and the University of Adelaides MathsStart and MathsTrack programs. For brevity a code is used to identify each topic, see Table 4.1, and then for each topic it's name is given in bold followed by a list of the key concepts covered in that topic. These are discussed at length below, and this table is intended to be used as reference material for that discussion.

Some notes on the way the key concepts are summarised:

- This key concept summary is intended for a reader deeply familiar with the content, and as such it is heavily condensed and uses notation and terminology without the usually appropriate rigorous definitions.
- Concepts relating to "interpretation" and application in a general sense are ommited. The assumption is that to the intended readers, these should go without saying. For example, in S1M2 the key concept "Quadratic Equations in Vertex and Factorised Form" is included, but this implies a variety of auxillary knowledge which is not explicitly included in the key concept summary: the interpretation of roots and vertices, deducing vertices and roots from the equation of a quadratic, or deducing the equation of a quadratic given these bits of information, etc. It is intended that an experienced maths educator should be able to deduce such surrounding concepts from the key concepts that are listed.

Producing this curriculum mapping was a delicate balance between being broad and vague in order to be able to present the entire curriculum mapping within a single frame of view, and yet still be granular enough so that specific content is clear and explicity and useful actionable reccomendations can be made. This balance was acheived by presenting these curriculums are two levels of detail:

• At a topic level (see Figure 4.1). This is intended to give the broad strokes, and show the entire mapping in a single frame of view (a page, in this case).

It is also intended to be reference material for the following more detailed discussion, to aid the reader in structuring the information contained in the more detialed discussion and place each peice of information into where it belongs in the bigger picture.

 At a key concept level, this is what will be presented for the remainder of this section, and intended to be the grandular level at which content is presented specifically enough that reccomended actions can be understood explicitly and implemented easily. Note that although the key concept level is much more granular than the topic level discussion, it is still intended as a summary and does not include every single detail of the content, as discussed above.

4.1.3 AC Mathematical Methods and Specialist Mathematics

AC has four levels of mathmatics, including also essential and general mathematics. Mathematical Methods and Specialist Mathematics are the two highest level mathematics, intended (partly) for preparation to university entry. Broadly speaking, the content of these two subjects can be grouped into several areas:

- Functions and Graphs, which is broken up primarily into families of functions, with some extra concepts thown into some generalist topics:
 - Polynomials and Rational Functions (MMu1t1, SMu3t2),
 - Exponentials and Logarithms (MMu2t1, MMu2t2, MMu4t1)
 - Trigonometric Functions (MMu1t2, SMu2t1)
- Calculus, which is largely structured similarly to the Functions and Graphs: breaking it up by the type of function you are doing calculus on, splitting up differentiation from integration, and throwing in rules of differentiation and approaches to integration with a few extra concepts along the way (MMu2t3, MMu3t1, MMu3t2, SMu4t1, SM4t2).
- Geometry and Linear Algebra: Mostly vectors, with some matrices, systems of
 equations, and even circle theorems. This is the topic in which the concept
 of proof is primarily attempted to be introduced, and perhaps that is the reason why it is entirely contained within the Specialist Mathematics curriculum
 (SMu1t2, SMu1t3, SMu2t2, SMu3t3),
- Complex Numbers, as well as rational/irrational numbers, etc. (SMu2t3, SMu3t1), and finally
- Probability and Statistics, with some combinatorics thrown in for good measure (MMu1t3, MMu3t3, MMu4t2, MMu4t3, SMu1t1, SMu4t3)

Although there are a couple of topics (MMu2t2 for example) which although they relate to these broader areas, also contain a substantial amount of other content.

More detailed discussion of the specific key concepts of interest will follow in Section 4.2 as a natural part of comparisons between curriculums, as that is where the specifics will be important. These sections are intended to give a broader overview of the structure of the content in these curriculums

4.1.4 SACE Stage 1 Mathematics, Stage 2 Mathematical Methods and Specialist Mathematics

SACE follows the AC fairly well at a broad level (although there are differences in the details, which will be discussed in Section 4.2. Broadly though the topics in the three SACE subjects here, although split into three subjects instead of two, can be broadly grouped into areas much the same as the AC:

- Functions and Graphs, which is broken roughy as:
 - General Concepts (S1M1, S2SM3),
 - Polynomials and Rational Functions (S1M2, S2SM3),
 - Exponentials and Logarithms (S1M5, S2MM4, S1M7)
 - Trigonometric Functions (S1M3, S1M10)
- Calculus, which similarly split up by the type of function you are doing calculus on, differentiation vs integration, and throwing in rules of differentiation and approaches to integration with a few extra concepts along the way (S1M6, S2MM1, S2MM3, S2MM4, S2SM5, S2SM6).
- Geometry and Linear Algebra: Mostly vectors, with some matrices, systems of equations, and even circle theorems. This is the topic in which the concept of proof is primarily attempted to be introduced, and perhaps that is the reason why it is entirely contained within the Specialist Mathematics curriculum (S1M8, S1M9, S1M11, S2SM4),
- Complex Numbers, as well as rational/irrational numbers, etc. (S1M12, S2SM2), and finally
- Probability and Statistics, with some combinatorics thrown in for good measure is included almost exclusively in Stage 2 Mathematical Methods (S1M4, S2MM2, S2MM5, S2MM6)

Although there are a couple of topics (S1M7,for example — very similarly to MMu2t2) which although they relate to these broader areas, also contain a substantial amount of other content. This grouping also leaves one topic out in the SACE context: S2SM1 which is essentially just the concept of mathematical induction.

4.1.5 MathsStart and MathsTrack

MathsStart can be seen as essentially an introduction to functions, MathsTrack then takes this, and extends it primarily to calculus, taking a little detour along the way to cover some vector and matrix geometry/ systems of linear equations concepts. So broadly grouping the topics in a way analogous to above:

- Functions and Graphs, roughly broken up into:
 - General Concepts (MS1, MS2),
 - Polynomials and Rational Functions (MS3, MS4, MT1),
 - Exponentials and Logarithms (MS7, MS8), and

- Trigonometry (MS5, MS6)
- Calculus, similarly first introducing differentiation on polynomials with various other general concepts (MT6, MT7) and then exponentials and logarithms (MT8) and finally also integration (MT9).
- Geometry and Linear Algebra (MT2, MT3, MT4).

Note the missing topic 5 in MathsTrack, this used to be part of the course some time ago but is currently no longer included in the content of the course, and so is not included here.

4.2 Curriculum Mapping

Figure 4.1 shows the topic-level alignment between the AC (senior mathematical methods and specialist mathematics), SACE (stage 1 mathematics, stage 2 mathematical methods and stage 2 specialist mathematics), MathsStart and MathsTrack. This is the broad, eagle-eye, view of the alignment between the content in these topics.

Although key concept level alignment between topics connected with lines in Figure 4.1 is not always perfect, it is fairly strong in most cases. Individual cases with any misalignment will be discussed in the remainder of this chapter.

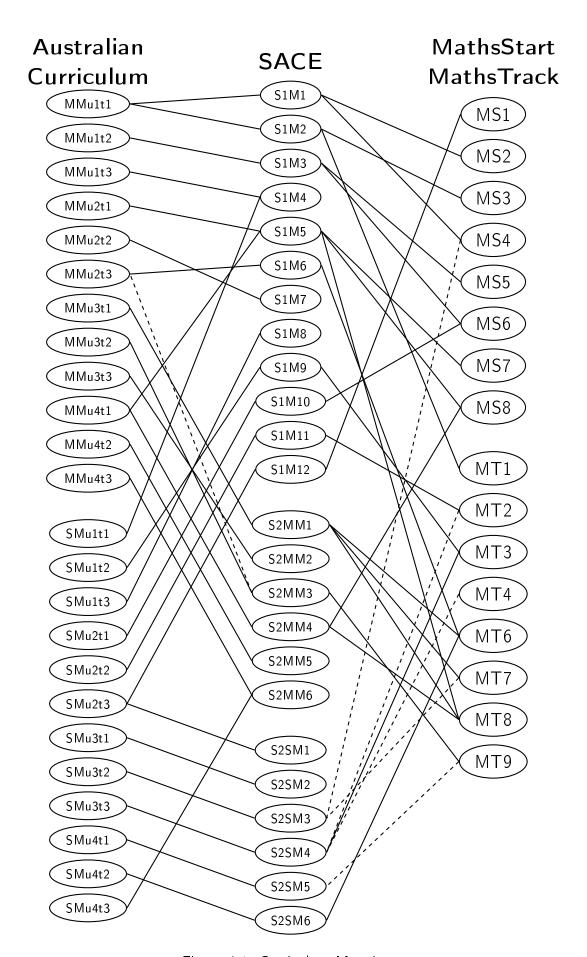


Figure 4.1: Curriculum Mapping

4.2.1 AC to SACE

At a glance, there appears to be a very good one-to-one alignment at the topic level between the AC and SACE. Broadly speaking the biggest difference between these two curriculums is their structure. The AC content is structured into two subjects (mathematical methods and specialist mathematics) which span "senior highschool", which most commonly would equate to both years 11 and 12 in Australia. Each of these two subjects contains 12 topics. The SACE content on the other hand is split into stage 1 (commonly year 11 in Australia) and stage 2 (commonly year 12), stage 1 consists of a single subject "mathematics" with 12 topics, and stage 2 is split into two (mathematical methods and specialist mathematics) each with 6 topics. So the total number of topics is actually the same accross the board between the AC and SACE, and they seem to match almost exactly with a pattern in which the first 6 topics of both the AC mathematical methods and specialist mathematics constitute SACE stage 1 mathematics and the remaining 6 topics in each of the AC subjects align to the corresponding SACE stage 2 subject.

Note: The content is almost identical between these, the structure is simply different. Given how we don't really care about the structure, but rather care about the content maybe it would be more useful to structure this discussion into content areas rather than base it on the curriculum structure.

As usual however, the devil is in the details:

- In terms of Functions and Graphs:
 - Gerneral Concepts, Polynomials and Rational Functions: In both the AC and SACE this area is split into two: basic introduction and advanced concepts. The basic introduction topics align well (MMu1t1 to S1M1 and S1M2), with only slight differences in terminology (AC refers to inverse proportion while SACE refers to reciprocal for example) and focus (SACE puts much more of an emphasis on polynomials, seperating it into it's own topic (S1M2) and breaking it down into much more granular concepts). The advanced concepts are covered in SMu3t2 and S2SM3 are essentially identical.
 - Exponentials and Logarithims: There is essentially perfect alignment between the concepts for logarithms between MMu4t1 and S2MM4. Concepts around exponentials however are a little less straightforward. Similarly, MMu2t2 is almost exactly the same as S1M7, they are both centered on the introduction of recurrance relations, partial sums, and linking this back to exponential functions. I include these topics under exponentials as they link to those concepts, but really they focus on concepts around sequences and series, it's just they don't connect to anything else better than they connect with exponentials, so here they go, really they are a fairly distinct set of concepts though. However it is in the alignment between MMu2t1 and S15 that there is a difference: S15 includes Log-Laws, while MM2t1 does not, focusing only on Index Laws. This is not actually a difference in content between the AC and SACE as the log laws are covered in the AC in MMu4t1. They are actually repeated in the SACE curriculum, covered both in S1M5 and then again in S2MM4.
 - Trigonometry: MMu1t2 matches almost identically to S1M3, with the biggest difference being that in the AC the unit circle interpretations/

definitions of $\sin(x)$, $\cos(x)$, and in particular $\tan(x)$ are emphasised, where in SACE $\tan(x)$ in particular is introduced instead as $\frac{\sin(x)}{\cos(x)}$. That being the biggest difference between the two should emphasise how similar they are in terms of content. Similarly, SMu2t1 and S1M10 align just about perfectly.

Calculus:

- SMu4t1 aligns perfectly with S2SM5, both covering integration by parts, by substitution, inverse trig substitutions in integration problems, volume of solids of revolution, partial fractions and area between two curves.
- SMu4t2 aligns well to S2SM6, both covering implicit differentiation, solving first-order seperable differential equations, and the logistic equation.
 However there are some differences in that the AC goes on to focus on rates of change, while SACE instead decides to focus on parameterised curves, trigonometric parameterisations, etc.
- MMu2t3 and S1M6 both introduce differentiation by leading in with the concept of average rate of change, first principles and lead into linearity of differentiation, derivitives of polynomials, slope of the tangent and optimisation but in SACE S1M6 introduces the terms "increasing" and "decreasing" and sign diagrams, which are not mentioned in MMu2t3 (or AC?), while MMu2t3 introduces the concept of an antiderivative.
- MMu3t1 and S2MM1 align perfectly introducing the chain, product, and quotient rule. Introducing $e=2.718\ldots$ in the same way (using first principles to explore $\frac{d}{dx}a^x$ for different a, derivitives of $\sin(x)$ and $\cos(x)$, and second derivatives.
- MMu3t2 and S2MM3 are very closely aligned, both introducing both definite and indefinite integrals of polynomials, exponentials, and trigonometric functions, linearity of integration and the fundamental theorem of calculus, they have diverge slightly in their approach to definite integrals. In particular, SACE S2MM3 introduces the concepts of upper and lower sums and the definite integral as the unique number between the two as the size of the rectangles approaches zero, while in the AC MMu3t2 this is not discussed. Also, S2MM3 introduces anti-differentiation, a concept introduced in the AC MMu2t3 but not introduced in SACE S1M6, instead being covered here in S2MM3.

Note how although most derivatives are introduced in differentiation specific topics, $\frac{d}{dx} \ln(x)$ is introduced in a seperate topic entirely about logarithm functions in both the AC (MMu4t1) and SACE (S2MM4), and I categorise these topics under 'Functions and Graphs' above because I see these topics as an introduction to logarithms, but they do also contain concepts around calculus (of logarithm functions).

• Geometry and Linear Algebra

Vectors in the Plane are covered in SMu1t2 and S1M9, with the content being very well aligned and the only really notable difference being the inclusion of geometric vector proofs in SACE S1M9 which is not included in SMu1t2, instead being introduced but restricted to other topics... i.e.

- Proof and Circle Theorems which are covered in SMu1t3 to S1M8. Both these cover the same "content" in the sense of theorems: circle theorems, but they also both attempt to broach the difficult topic of proof, methods of proof, and some of the language around proof, and they take quite different approaches to this. The AC SMu1t2 is quite explicit specifing the introduction of language around formal logic: imlication, equivalence, converse, negative, contrapositive, contradiction, 'for all' and 'there exists', counter-examples. On the other hand, SACE S1M8 simply specifies proof to be investigated as "justification of properties of circles", and only breifly mentions specifics of language and methods as suggestions not specificying them as being required components of the curriculum and instead leaving the approach and specific content chosen to be used to introduce the concept of proof much more open to interpretation by the teacher.
- Matrices, covered in SMu2t2 and S1M11 are essentially identical in content covering matrix notation, linear combinations of matrices, matrix multiplication, matrix indentity and inverses (and determinants), and the perspective of matrices as linear transformations.
- Vectors in 3D in SMu3t3 and S2SM4 are also introduced very similarly in terms of content: cross product, equations for lines and planes, systems of equations and geometric interpretation of their solutions. One of the main differences however is in how they apply these concepts, the AC SMu3t3 includes a focus on parameterised vector equations, the equation for a sphere, and in particular kinematics: projectile and circular motion in 3D, which are not coverted in SACE S2SM4, which instead remains more abstract with these concepts, and on the other hand the examples required are less complex to interpret.
- Complex Numbers are introduced in two topics, a basic an advanced topic, in both curriculums. The basic topics, SMu2t3 in the AC and S1M12 in SACE are quite similar in their base content: rational/irrational numbers, i, complex arithmetic, conjugates, and complex roots of polynomials. However there are a couple of key differences between the two: first, induction is introduced in the AC SMu2t3 while in SACE it is seperated into it's own seperate topic: S2SM1. The second key difference is that interval notation is explicitly introduced in SACE S1M12, while in the AC interval notation seems to be neglected. The advanced topics SMu3t1 and S2SM2 on the other hand align almost perfectly in content.
- Probability and Statistics is the topic area in which the alignment between the AC and SACE is at it's loosest, and the most substantial differences in content exist between the two.
 - Combinatorics: MMu1t3, SMu1t1, and S1M4. The overlap between the AC and SACE for these topics is essentially concepts around permutations, factorial (and the 'multiplication principle'), combinations. Although it is notable that the AC MMu1t3 extends the concept of combinations to binomial coefficients and Pascal's triangle while SACE does not. Beyond

these common concepts, both curriculums have some introductory probability content, but they take very different approaches to this. The AC does this via set thoeretic concepts, union intersection and complement of sets, the pidgeonhole principle, and then probability notation (P(A)) for set complement, intersection and union and introduces basic probability concepts from this angle (for example, $0 \le P(A) \le 1$), including conditional probabilities (P(A|B)). On the other hand, SACE S1M4 has introductory statistics concepts (as opposed to introductory probability concepts). Specifically, S1M4 reviews mean median ad mode, interquartile range, standard deviation, and introduces the basic concepts around the normal distribution. S1M4 also introduces the distinction between discrete and continuous random data/ variables, not quite introducing the concept of a 'random' variable yet, but still. Very big difference in approach between these topics.

- Introduction to Distributions/ Random Variables: Discrete (MMu3t3 and S2MM2), ad Continuous (MMu4t2 and S2MM5). There is quite good alignment between these topics actually. For both discrete and continuous general definitions of expected value and variance are given. For discrete the uniform, examples of arbitrary non-uniform, the bernoulli, and binomial distributions are introduced. For continuous the uniform, restricted domain polynomial, and normal distributions are considered, and transformations of normal distributions (in particular to get the standard normal) are considered. The one key difference is that in SACE the central limit theorem is explicitly explored, while it's significance is much less explicit in the AC.
- Confidence Intervals: The confidence intervals introduced are the same accross both curricula, specifically the normal approximation to the binomial confidence interval for a proportion (Wald interval, MMu4t3) and the standard normal distribution confidence interval for the mean of a continuous variable (SMu4t3) are both introduced in SACE S2MM6. However the approach taken to justifying these confidence intervals is a little difference, in SACE the justification is very central limit theorem centric, relying on the introduction to that concept in S2MM5, while in the AC instead many of these concepts (including the central limit theorem itself) are simply stated and students are encouraged to test them by simulation. Althogh SACE also takes this simulation approach to justification it is emphasised less, and the introduction of the concepts around the central limit theorem are much more explicit.

Note: Cumulative Distribution Function not mentioned in SACE

The only substantial difference in content is the concept of proof by induction, which is in the SACE curriculum but not the AC. This is represented in Figure 4.1 by S2SM1 which is an entire topic on induction with no link to the AC, although induction is also briefly introduced earlier in SACE in S1M12.

TODO: Review above dot points, trim/edit down, condense, and write a paragraph here begginng "In summary, ..." or "To summarise, ..."

If we rearrange the topics in Figure 4.1 into their five broad topic areas: Functions and Graphs, Calculus, Geometry and Linear Algebra, Complex Numbers, and Probability and Statistics, we get a much clearer picture, as shown in Figure 4.2.

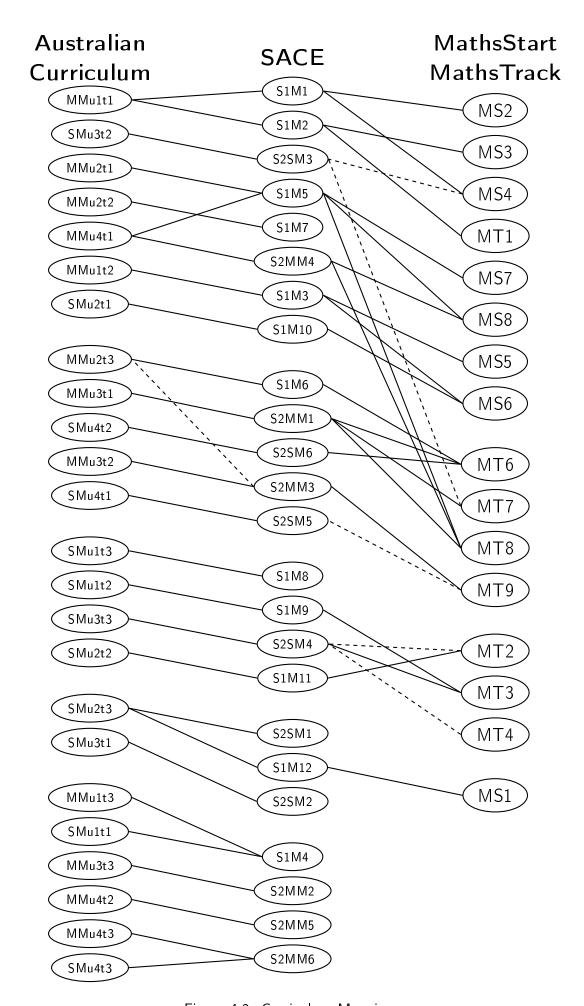


Figure 4.2: Curriculum Mapping

4.2.2 AC and SACE to MathsStart and MathsTrack

In the broad sense of areas of mathematics the topcs can be grouped into naturally, as discussed above in Section 4.1, the topics that are covered in the AC and SACE but not in MathsStart or MathsTrack are complex numbers, and Probability/ Statistics/ Combinatorics. Note that the 'missing' MT5 is a topic on complex numbers that is currently being ommitted from the bridging course. So given that those areas are not covered in MathsStart or MathsTrack currently, lets take a look in more detail (at a key concept level) at the alignment of the topics that are covered in MathsStart and MathsTrack.

- Functions and Graphs. This topic essentially covers the entire of MathsStart, and the first topic of MathsTrack MT1, and it make sense to split it into the usual three sub-topics:
 - General Concepts, Polynomials and Rational Functions.
 - * Polynomials and Rational Functions have an interesting binary tree structure, with MMu1t1 splitting into both S1M1 and S1M2 in SACE, which each split into MS2, MS4 and MS3, MT1 respectively in the bridging courses. S1M1 covers mainly linear equations, but also reciprical functions and asymptotes, while in MathsStart these are split into MS2 and MS4 respectively. Similarly S1M2 covers polynomials, including quadratics and related concepts as well as higher order polynomials, while in the bridging course these are separated into an entire topic just on quadratics (MS3) in MathsStart which is still less indepth than the introduction to quadrtics in S1M2, which introduces rearrangments of quadratics into vertex and factorised form, and then later a more indepth topic on polynomials in MathsTrack (MT1), which covers some of the more details concepts on quadratics missed in MS3 (such as the quadratic formula), and goes on to higher order polynomials.
 - * S2SM3 introduces advanced general concepts on functions: domain and range, function composition, one-to-one, inverse functions, graphing more general rational functions (not just reciprocal functions), and the absolute value function. This concepts are not covered in the bridging courses, and could be useful, but on the other hand, are part of the specialist mathematics curriculum, so aren't the highest priority to include.
 - Exponentials and Logarithms. Both the AC and SACE introduce the concept of exponential functions via recurrance relations describing geometric sequences. Although this is certainly not the only (or even neccessarily the best) way to introduce and understand exponential functions, it is the way prescribed by the AC and SACE curriculums, so it might be valuable. On the other hand, the way the number e is introduced is actually identical accross AC, SACE, and the bridging course which is remarkable given how many different ways this could be done. Interestingly, exponent laws and logarithm laws (as well as basic properties of exponential and logarithmic functions) are introduced in S1M5 of SACE, and are split into

the two topics MS7 and MS8, it seems that the granularity of the MathsStart program is roughly a factor of two more granular than the SACE curriculum, which is pretty interesting. Could be a direction for future research on some measure of "degree of granularity" of a course/program. It is also interesting to note the location of S2MM4 in Figure 4.2 in the Functions and Graphs section, rather than the differentiation section. This is a choice because of how concepts of exponents and logarithms are very distinctly seperated in the AC into MMu2t1 and MMu4t1, while in SACE introductory concepts for both are introduced in S1M5 and S1M7, but while advanced concepts around logarithms (including calculus) have their own topic in SACE — S2MM4, advanced concepts (such as calculus) around exponential functions do not, and are instead lumped into more general calculus topics (S2MM1 in SACE and MMu3t1 in AC). I'll include a more indepth discussion of this under calculus, as this section ought to focus on the function and graph properties, but there is significant overlap between the two in the way the content is arranged (perhaps rightfully so).

- Trigonometry There is actually fairly good alignment in the trigonometry sections, although they are organised differently (S1M5 and S1M10 in SACE and MS5 and MS6 in MathsStart), the content is fairly well aligned. SACE covers some graphing slightly more comprehensively, talking about translations and dilations for example (a concept from MS3 that could be "translated" here effectively, linking the concepts and chaining them from topic to topic a little more strongly.
- Calculus, it makes sense to organise this under the MathsTrack topics (maybe I should do that for functions and graphs above as well actually).
 - MT6: Differential calculus is introduced very similarly, through first principles etc. in both MT6 and S1M6, MT6 actually goes beyond the content of S1M6, introducing also the product, chain and quotient rules (which are covered in S2MM1) and implicit differentiation (which is covered in S2SM6). On the other hand, MT6 does not cover increasing and decreasing (which is in S1M6), which is instead covered in MT7. Also, the concept of a normal to a curve is introduced in MT6, but it is not really covered anywhere in SACE (apart from sort of in S2SM4 using cross products).
 - MT7: Covers a few concepts from S1M6 that where skimmed over in MT6, as well as some of the more advanced function and graph concepts such as sketching rational functions which is only covered in S2CM3.
 - MT8: Similarly, taking the more advanced concepts from the functions and graphs topics of SACE, and combining them with the introductory calculus concepts MT8 introduced differentiation of exponents (from S2MM1) and logarithms (S2MM4), at the same time as re-hashing concepts from MS7 and MS8 and revising them (such as introducing exponential and logarithm functions/ sketching them, etc.). Notably, surge models and logistic models are introduced as well. Surge models are not covered anywhere in the AC or SACE as far as I cna tell, and logistic models are only introduced in S2SM6.

- MT9: All the integration is fit into this single topic in MathsTrack, which students inevitably find challenging. This covers essentially all of S2MM3, and then goes a little further with the notable addition being integration by substitution, which in SACE is only covered in S2SM5. Notably summation notation is also introudced (in an appendix) in MT9, an important bit of notation that students often struggle with in first year university, but that isn't anywhere in the SACE curriculum as far as I can tell.
- Geometry and Linear Algebra is where SACE and the briding courses begin to really diverge in earnest.
 - MT2 aligns well to S1M11, although it goes a little further and also introduced row operations, a concept not introduced in S1M11 although it is introduced in S2SM4 in a quite different context, not so much to do with matrices in the pure sense, but instead focussing on the connection to solving 3×3 systems of linear equations. This aspect, of solving systems of equations, in introduced in MT4 and actually gone into in great depth, while the concept seems tacked on and is not gone into in detail at all in S2SM4.
 - MT3 Introduces vectors and vector concepts in both \mathbb{R}^2 (concepts covered in S1M9) and \mathbb{R}^3 (concepts covered in S2SM4). The overlap between S1M9 and MT3 is substantial, with MT3 covering most of the concepts in S1M9, although S1M9 goes into a little more detail on scalar dot products (a concept covered in both), and also introduces the concept of orthogonal projection, and even throws in a dash of geometric styled proof. S2SM4 also goes significantly further, most notably introducing the concept of the vector cross product which is not covered in MT3, although both introduce equations for planes in \mathbb{R}^3 .
 - MT4 focuses on systems of linear equations, and although this concept is introduced in S2SM4, it is covered in MT4 in a much more detailed, granular way. Also, MT4 introduces Gauss-Jordan Elimination, an algorithm not explicitly introduced in SACE as far as I can tell (although it is implied).

MS4: Note the link to S2SM3

• MS1: Maybe Introduce Interval Notation along with Intervals?

4.3 Notes on interpreting

Figure 4.2, the dashed lines represent tenous connections, usually a single concept shared:

- the one between and AC and SACE essentially represents the concept of antidifferentition,
- the one between S2SM3 and MT7, as well as the one between S2SM3 and MS4 essentially represents sketching rational functions, although in MS4 only recipricol functions and transformations thereof are considered, this concept of

sketching these graphs and the properties of these graphs is heavily emphasised as a way to explore the concepts connected to these functions.

- the one between S2SM5 and MT9 essentially represents integration by substitution.
- the one between S2SM4 and MT2 essentially represents row operations, in MT2 introduced on matrices, but in S2SM4 it is introduced explicitly in the context of solving 3 × 3 systems of linear equations. Similarly the dashed line between S2SM4 and MT4 represents essentially the same concept in S2SM4, but in MT4 the system of equations perspective is explored, which is not really done as much in MT2.

4.4 Conclusions/Summary

Broadly the content for functions and graphs, as well as calculus is well aligned between the bridging courses and the AC/ SACE, although the bridging courses tend to mix the two more, merging the more advanced concepts from functions and graphs into the calculus topics. This makes perfect sense to do, especially considering how inter-connected the areas are in the first place. Bigger differences between the content of the bridging courses and the AC and SACE exist in the other area though, with big differences in linear algebra and geometry, complex numbers almost not being covered in the bridging courses (although they used to be covered more, see the discussion relating to MT5), and the biggest difference being that statistics and probability are not covered in the bridging courses at all.

Broadly, a big difference in emphasis between the bridging courses and SACE is the emphasis the bridging courses place on sketching graphs, and explicitly exploring the connection between transformation (translations and dilations primarily) of a graph relate to algebraic changes to functions. Although this is covered in SACE to some degree, it is largely implicit and left to reading between the lines, while it is quite explicit in the bridging courses.

My reccomendations for MathsStart would be to include some work on fractions, index laws, and more emphasise on re-arranging equations as in my experience these are the topics and concepts that students need the most from middle school mathematics (up to year 10) and form foundations for building other concepts with in senior highschool. This is already the implicit purpose of MathsStart in a sense, and this is good. Aside from that, concepts that could be added to the bridging courses to bring them more in alignment with the AC and SACE are:

- I'm not sure if I missed it somewhere, but a formal introduction of the definition
 of a function (and hence the alternative a relation) would be good as the
 concept of a relation is in the AC and SACE, although it is not used much. It
 is a little useful later when doing implicit differentiation, for example.
- S2SM3 introduces advanced general concepts on functions: domain and range, function composition, one-to-one, inverse functions, graphing more general rational functions (not just reciprocal functions), and the absolute value function. This concepts are not covered in the bridging courses, and could be useful, but on the other hand, are part of the specialist mathematics curriculum, so aren't the highest priority to include.

- I like the way quadratics are introduced in MS3, particularly as the concepts used to introduce them (dilations, translation) are very applicable in the AC and SACE in many places. On the other hand there are a couple of concepts here that are missed in the gap betwen MS3 and MT1, specifically rearranging quadratics algebraically to get them in vertex form and factored form, although these forms are introduced implicitly in MS3 and interpreted, algebraic rearrangment of them could be emphasised more, especially given how this is one of the key concepts we want students to be picking up as they go through MathsStart.
- Both the AC and SACE introduce the concept of exponential functions via recurrance relations describing geometric sequences. Although this is certainly not the only (or even neccessarily the best) way to introduce and understand exponential functions, it is the way prescribed by the AC and SACE curriculums, so it might be valuable.
- Overall having the concepts link from topic to topic more, for example in MS3 dilations and translations of quadratic functions are considered. It would be useful if these concepts where re-visited in MS6 for example when looking at graphing/ sketching trigonometric functions, as this is covered in SACE explicitly but also because it connects the concept to multiple different topics and applications (different kinds of functions).
- Scalar dot product of vectors is introduced in MT3, but SACE goes a little further, also introducing the concept of orthogonal projection in \mathbb{R}^2 in S1M9.
- I think it would be a good idea to introduce interval notation along with the concept of intervals when that concept is introduced in MS1.

while concepts currently in the briding courses that could be removed as they are not part of the AC or SACE include:

- Implicit differentiation is technically only in Stage 2 Specialist Mathematics, so could potentially be removed from MT6.
- Normal to a curve is a concept introduced in MT6 but not used anywhere in the SACE curriculum (as far as I can tell), apart from breifly in S2SM4 when it is used in the contect of vector cross products and equations for a plane a very different context.
- Surge models are not anywhere in the AC or SACE, so could potentially be removed from MT8 entirely.
- Logistic models are only included in Stage 2 Specialist Mathematics, so could potentially be removed from MT8. Alternatively if it was kept, it could be introduced with concepts around differential equations, which is how it is introduced in Stage 2 Specialist Mathematics. At the moment, it is introduced as a model (an equation), not a solution to a differential equation, so even as it is it is very different content.
- Integration by Substitution is only covered in Stage 2 Specialist Mathematics, so could potentially be removed but is also very useful in first year university

calculus-based courses (such as Maths IA etc.) so I'm not sure. Depends, as most of these do, on the mindset: it would be useful content for the students to be exposed too early, or you could look at it from the perspective of they are not expected to know it going into a course like Maths IM.

- Concepts covered in S2SM4 on geometry in \mathbb{R}^3 are technically only covered in Specialist Mathematics, so could be cut in principal if we are operating under the assumption bridging course students will be doing Maths IM. So concepts like vector cross product, and the equation for a plane, to be specific.
- Technically, the Gauss-Jordan Elimination method introduced in MT4 is not anywhere in SACE, but that said it is somewhat implied a little in the topic that discusses the other concepts in MT4 (around systems of linear equations) S2SM4. That said, this entire topic and broad concept of systems of linear equations is entirely contained in Stage 2 Specialist Mathematics, so it could be argued to not be included for that reasoning.

Other reccomendations:

 Maybe spread out the introduction of integration? Potentially introduce both differentiation and integration, and then introduce them together on each individual type of function? Not sure.

Chapter 5

Moving Forward: Improvements

5.1 Current Strengths of MathsStart and MathsTrack

Moving foward is a two-part process:

- Recognise what is being done well, encourage and recognise it, and continue to support its ongoing excellence.
- Recognise what can be improved on, gaps that may exist, and address them with specific actionable changes.

5.1.1 SQWIGLES

SQWIGLES is an abbreviation (see Figure ??) developed at the University of Adelaide maths learning centre with several purposes in mind:

- As a way to guide tutors working at the maths learning center on how to best help the students.
- To scaffold self-reflection in teaching and education when working one-on-one with students by providing specific actions one can focus on paying attention to and reflecting on.
- As a tool to focus efforts on self-improvement, by choosing one action to improve on at a time it can provide an avenue towards improvement that feels acheivable, and can provide concrete progression.

SQWIGLES also had some ancillary and unintended benefits, as once an educator is engaged actively in self-reflection, even if it is prompted by paying attention to one specific action, they notice other things perhaps even things unrelated to SQWIGLES itself. David Butler, the current maths learning center coordinator at the University of Adelaide, wrote a blog post about SQWIGLES which is quite informative and has more detail, but here I will provide a breif overview as it is a very beneficial tool that generalises well beyond mathematics education.

As teachers we are constantly encouraged to reflect on our practice and continually aim to improve and develop our skills, and rightfully so. Teaching is a process of continual improvement. Often however, we can reflect on our practice and either be

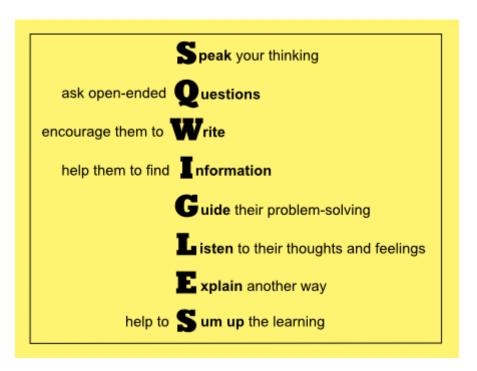


Figure 5.1: SQWIGLES

overwhelmed by the amount of observations we make and not know where to start, or be unsure what to reflect on, exactly — what aspects of our practice to spend the time to critically analyse. Teaching is an incredibly broad and diverse profession with many aspects, and improvement is always possible in every aspect of it. However pursuing improvement takes time (a resource we as teachers are very low on), and attention and energy, and so it is completely untenable to pursue improvement in all aspects of teaching simultaneously. In the face of this, we often suffer from either decision paralysis, or choosing relatively insignificant aspects of our teaching to focus on. SQWIGLES can serve as a guide for both where to focus our self-reflective attention, and as a list of suggestions for individual aspects of our teaching practice to focus on improving one at a time.

Speak Your Thinking

- Mathematics as language, speaking to translate.
- Mathematics as the process of reasoning, speaking to illustrate that process.

Ask Open-Ended Questions

Encourage Them to Write

Help Them Find Information

Guide Their Problem-Solving

Listen to Their Thoughts and Feelings

Explain Another Way

Help to Sum Up the Learning

5.1.2 Staff Culture at the Maths Learning Center

5.1.3 Self-Paced Assessment and Content Speed (!!!)

Link to Maths Anxiety literature review.



Conclusions and Reccomendations

With respect to the bridging courses run through the university of adelaide's maths learning centre: MathsStart and MathsTrack,

- The self-paced and feedback focused approach to assessment is certainly the highlight of the programs, should be continued, encouraged, potentially further resourced, expanded, and reccomended to other bridging course facilitators.
- The role of bridging courses as what is often student's first experience at university implies that potentially students wellbeing and retention could be improved by structuring the programs to provide more opportunities for students to meet each other and work together: either in the maths learning center drop-in area, or a seperate area, but potentially assigning a certain time on a certain day perhaps weekly or fortnightly during which students are encouraged to come and work together, could allow them to make freinds, build social networks, and better aclimitise them to the university environment in order to better prepare them for success in their studies.
- The smallest but perhaps easiest to implement improvement could be to better align the course content with curriculum, both the highschool curriculum (AC/SACE) in the case of students doing the bridging course to then comence study interstate or overseas, or with specific first year entry level courses, to better match the potential gaps in knowledge students may encounter.

5.2 Further Research

- Review of Australian Universities, Bridging courses they offer, and placing the UofA courses into that context.
- Generation of Resources for a Probability and Statistics Topic booklet



Appendices



Appendix A

Key-Concept Level Description of Topics in the AC, SACE, MathsStart and MathsTrack

Note, topics are identified using the code notation introduced in Table 4.1. The full topic name is given in bold where applicable, and then key concepts covered in that topic are listed.

Code	Name and Key Concepts
MMu1t1	Functions and graphs: Midpoint of a Line, $y=mx+c$, Quadratic
	Equations in Vertex and Factorised Forms, Inverse Proportions, Polyno-
	mials, Relations, Translations and Dilations
MMu1t2	Trigonometric functions: Unit Circle, Radians, SOH CAH TOA, Sine
	Rule, Cosine Rule, Exact Values, Amplitude/Period/Phase, Length of
	Arc, Area of Sector
MMu1t3	Counting and probability: Binomial Coefficients, Set Complement
	Intersection and Union, Probability, $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
	B), Conditional Probability, Independance
MMu2t1	Exponential functions : Index Laws, Fractional Indices, Functions,
	Asymptotes, Graphs
MMu2t2	Arithmetic and geometric sequences and series: Arithmetic and
	Geometric Sequences as Recurrence Relations, Limiting Behaviour, and
	Partial Sum Formulae, Growth and Decay
MMu2t3	Introduction to differential calculus Average Rate of Change, First
	Principles, Leibniz Notation, Instantaneous Rate of Change, Slope of
	Tangent, Derivitive of Polynomials, Linearity of Differentiation, Sta-
	tionary Points, Optimisation, Anti-Derivitives, Interpret Position-Time
	Graphs
MMu3t1	Further differentiation and applications: Define e as a s.t.
	$\lim_{h\to 0} \frac{a^h-1}{h} = 1$, Derivitives of $e^x \sin(x)$ and $\cos(x)$, Chain Product
	and Quotient Rules, Second Derivitives
MMu3t2	Integrals: Integrate Polynomial Exponential and Trigonometric Func-
	tions, Linearity of Integration, Determine Displacement given Velocity,
	Definite Integrals, Fundamental Theorem of Calculus, (signed) Area Un-
	der a Curve

- MMu3t3 **Discrete random variables**: Frequencies, General Properties, Expected Value, Variance, Standard Deviation, Bernoulli and Binomial Distribtions
- MMu4t1 The logarithmic function: Logs as Inverse of Exponentials, Log-Scales, Log Laws, Log Function Graphs, Natural Log, $\frac{d}{dx}\ln(x)=\frac{1}{x}$, $\int \frac{1}{x}dx=\ln(x)+c$ for x>0
- MMu4t2 Continuous random variables and the normal distribution: Probability Density Function, Cumulative Distribution Function, Probabilites Expected Value, Variance and Standard Deviation as Integrals, Linear Transformation of Random Variables, Normal Distribution using Technology
- MMu4t3 Interval estimates for proportions Simple Random Sampling, Bias, Sample Proportion, Normal Approximation to the Binomial Proportion, Wald Confidence Interval, Trade-Off Between Width and Level of Confidence
- SMu1t1 Combinatorics Multiplication of Possibilities, Factorial Notation, Permutations with and without Repeated Objects, Union of Three Sets, Pigeon-Hole Principle, Combinations, Pascals Triangle
- SMu1t2 Vectors in the plane: Magnetude and Direction, Scalar Multiplication, Addition and Substraction as a Triangle, Vector Notation, $a\mathbf{i} + b\mathbf{j}$ Notation, Scalar Dot Product, Projection, Parallel and Perpendicular Vectors
- SMu1t3 **Geometry**: Notation for Implication (\Rightarrow) and Equivalence (\Leftrightarrow), Converse ($B\Rightarrow A$) Negation ($\neg A\Rightarrow \neg B$) and Contrapositive ($\neg B\Rightarrow \neg A$), Proof by Contradiction, \forall and \exists Notation, Counter-Examples, Circle Theorems, Quadrilateral Proofs in \mathbb{R}^2
- SMu2t1 Trigonometry: Graph and Solve Trig Functions, Prove Various Trig Indentities, Reciprocal Trig Functions
- SMu2t2 Matrices: Notation, Addition and Scalar Multiplication of Matrices, Multiplicative Identity and Inverse, Determinant, Matrices as Transformations
- SMu2t3 Real and complex numbers: Rationality and Irrationality, Induction, $i=\sqrt{-1}$, Complex Numbers a+bi and Arithmetic $(+,-,\times,\div)$, Complex Conjugates, Complex Plane, Complex Conjugate Roots of Polynomials
- SMu3t1 Complex numbers: Modulus and Argument, Arithmetic $(\times, \div, \text{ and } z^n)$ in Polar Form, Convert between Polar and Cartesian Form, De Moivre's Theorem, Roots of Complex Numbers, Factorising Polynomials
- SMu3t2 Functions and sketching graphs: Composition of Functions, Oneto-One, Inverse Functions, Absolute Value Function, Rational Functions
- SMu3t3 **Vectors in three dimensions**: $a\mathbf{i} + b\mathbf{j} + c\mathbf{k}$ Notation, Equation for Spheres, Parameterised Vector Equations, Equations of Lines, the Cross Product, Equation for a Plane, Systems of Linear Equation (Elimination Method) and Geometric Interpretation of Solutions, Kinematics via Differentiation of Vector Equations, Projectile and Circular Motion

- SMu4t1 Integration and applications of integration Substitution, $\int \frac{1}{x} dx = \ln |x| + c$ for $x \neq 0$, Inverse Trig Functions and their Derivitives, Integrate $\frac{\pm 1}{\sqrt{a^2 x^2}}$ and $\frac{a}{a^2 + x^2}$, Partial Fractions, Integration by Parts, Area Between Two Curves, Volume of Solids of Revolution, Numerical Integration using Technology
- SMu4t2 Rates of change and differential equations: Implicit Differentiation, First-Order Seperable Differential Equations, The Logistic Equation, Kinematics (Rates of Change)
- SMu4t3 Statistical inference: Central Limit Theorem and the Resulting Confidence Interval for a Mean
- S1M1 Functions and graphs: Equations for a Line, Slope, y-intercept, Intersection of Lines, Reciprocal Function, Asymptotes, Functions vs Relations, Domain, Range, Function Notation
- S1M2 Polynomials: Quadratic Equations in Vertex and Factorised Forms, Quadratic Formula, Completing the Square, The Leading Coefficient and Degree of a Polynomials, Cubics, Quartics
- S1M3 Trigonometry: Pythagoras, SOH CAH TOA, Cosine Rule, Sine Rule, Unit Circle, Exact Values, Sine and Cosine Functions, Radians, Length of Arc, Area of Sector, Amplitude, Period, Phase, $\tan(x) = \frac{\sin(x)}{\cos(x)}$
- Counting and statistics: Factorial, Permutations, Multiplication Principle, Combinations, Discrete vs Continuous Random Variables, Mean, Median, Mode, Range, Interquartile Range, Standard Deviation, Normal Distribution,
- S1M5 **Growth and decay**: Index and Logarithm Laws, Exponential Functions and their Graphs
- S1M6 Introduction to differential calculus: Average Rate of Change, First Principles, Notation $f'(x) = \frac{df}{dx}$, $\frac{d}{dx}x^n = nx^{n-1}$, Linearity of Differentiation, Slope of Tangent, Increasing vs Decreasing, Local and Global Maxima and Minima, Stationary Points, Sign Diagram
- S1M7 Arithmetic and geometric sequences and series: Arithmetic and Geometric Series as Recurrance Relations and Explicit Expressions, Partial Sums, Limiting Behaviour
- S1M8 **Geometry**: Circle Properties, Proofs (Direct, Contradiction, and Contrapositive)
- Vectors in the plane: Component (column) vs ai+bj Notation, Length and Direction, Linear Combinations of Vectors, Scalar Dot Product, Projection, Angle Between Two Vectors and Parallel/Perpendicular, Geometric Proof
- S1M10 Further Trigonometry: Sketch Trigonometric Functions with Translations and Dilations, Solve for Angles, Trigonometric Identities, Reciprocal Trigonometric Functions
- S1M11 Matrices: Linear Combinations of Matrices, Matrix Multiplication, The Identity, Inverse Matrices, The 2×2 Inverse, The 2×2 Determinant, Linear Transformations (including rotations, reflections and composition)

- S1M12 Real and complex numbers: Rationals, Irrationals, Interval Notation, Induction, $i=\sqrt{-1}$, Real and Imaginary Components, Complex Conjugates and Arithmetic, Argand Diagram, Modulus, Complex Roots of Polynomals
- S2MM1 Further differentiation and applications: S1M6, Chain Product and Quotient Rules, $e=2.718\ldots$, $\frac{d}{dx}e^x=e^x$, $\frac{d}{dx}\sin(x)=\cos(x)$, $\frac{d}{dx}\cos(x)=-\sin(x)$, Second Derivatives, Concavity and Points of Inflection
- S2MM2 **Discrete random variables**: Random Variables, Discrete vs Continuous, Probability Functions and Distributions, Properties of Probabilities, Frequency, Expected Value $E[X] = \sum xp(x) = \mu_X$, Standard Deviation $\sigma_X = \sqrt{\sum (x \mu_X)^2 p(x)}$, Uniform Bernoulli and Binomial Distributions
- S2MM3 Integral calculus: Anti-differentiation, Reversing Chain Rule for $\int f(ax+b)dx$, Linearity of Integration, Finding the Constant of Integration, Area Under the Curve as Upper and Lower Sum Approximations, Definite Integral, Area Between Two Functions and Between a Negative Function and the x-axis, Fundamental Theorem of Calculus,
- S2MM4 Logarithmic functions: Logs as Inverse of Exponentials, Log-Scales, Log Laws, Sketching $y=a\ln(b(x-c))$, $\frac{d}{dx}\ln(x)=\frac{1}{x}$, For x>0 $\int \frac{1}{x}dx=\ln(x)+c$
- S2MM5 Continuous random variables and the normal distribution: $P(X=x)=0, \text{ Probability Density Function, } \mu_X=\int_{-\infty}^{\infty}xf(x)dx,$ $\sigma_X=\int_{-\infty}^{\infty}(x-\mu_X)^2f(x)dx, \ f(x)=\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}, \text{ Standard Normal } Z=\frac{X-\mu}{\sigma}, \text{ Simple Random Sampling, For } X\sim(\mu,\sigma) \text{ and } X_i\sim iidX \text{ Sampling Distributions of } S_n=\sum_{i=1}^nX_i \ (n\mu,\sigma\sqrt{n}) \text{ and } \bar{X}_n=\frac{S_n}{n} \ (\mu,\frac{\sigma}{\sqrt{n}}), \text{ If } X \text{ is Normally Distributed, then so are } S_n \text{ and } \bar{X}_n, \text{ Central Limit Theorem (CLT)}$
- S2MM6 Sampling and confidence intervals: Confidence Interval for a Mean using CLT $\left(\bar{x}-z^*\frac{s}{\sqrt{n}}\right) \leq \mu \leq \left(\bar{x}+z^*\frac{s}{\sqrt{n}}\right)$, Wald Interval for a Proportion
- S2SM1 Mathematical induction: Initial Case and Induction Step
- S2SM2 **Complex numbers**: Cartesian vs Polar Form, Real and Imaginary Components, Modulus and Argument, Arithmetic in both Cartesian and Polar Forms, de Moivre's Theorem including Negative and Fractional Powers, Geometric Properties of the Argand Plane, Complex Arithmetic as Transformations, $n^{\rm th}$ Roots of a Complex Number, Factorising Polynomials with Complex Roots
- S2SM3 Functions and sketching graphs: Function Composition, Informal Intro to Domain and Range, One-to-One, Inverse Functions, Absolute Value Function, Graphing Rational Functions

- **Vectors in three dimensions**: Notation, Equations of a Line in \mathbb{R}^3 , S2SM4 Scalar Dot Product, Vector Cross Product, $|\mathbf{a} \times \mathbf{b}|$ is the Area of their Parallelogram, Equation for a Plane in \mathbb{R}^3 , Systems of Linear Equations, Geometric Interpretation of No/Unique/Infinite Solutions to a System of Linear Equations in \mathbb{R}^3
- S2SM5 Integration techniques and applications: Integration by Substitution, Using Trigonometric Identities for Integration, Derivatives of Inverse Trigonometric Functions (so $\int \frac{\pm 1}{\sqrt{a^2-x^2}} dx$ and $\int \frac{a}{a^2+x^2} dx$, Integration by Parts, Partial Fractions for Integrating Rational Functions, Area Between two Curves, Volume of Solids of Revolution
- S2SM6 Rates of change and differential equations: Implicit Differentiation, First-Order Seperable Differential Equations, The Logistic Differential Equation, Parameterised Curves, Example: if $\mathbf{v} = \frac{d}{dt}(x(t),y(t))$ is Velocity, $|\mathbf{v}|$ is Speed, and so the Arc Length along the Parameterised Curve is $\int_a^b \sqrt{\mathbf{v} \cdot \mathbf{v}} dt$, Trigonometric Parameterisations (unit circle, and non-circular parameterisations)
- MS1 Numbers & Functions: Natural Numbers, Integers, Rational Numbers, Real Numbers, Functions, Intervals
- Linear Functions: Equation for Linear Functions, Simultaneous Linear MS2 Equations, Sketching Linear Inequalities
- MS3 Quadratic Functions: Sketching a Parabola, General Form of a Quadratic, Translations and Dilations
- MS4 Rational Functions: Sketching Reciprocal Functions (Hyperbola), Lines of Symmetry, Limits and Asymptotes
- MS5 Trigonometry I: Pythagoras, Similar Triangles, SOH CAH TOA, Trigonometric and Inverse Trigonometric Functions using Technology, **Exact Values**
- MS₆ Trigonometry II: Unit Circle, Sketching Trigonometric Functions, Finding all Solutions to Trigonometric Equations, The Sine Rule, The Cosine Rule, Introductory Trigonometric Identities, Radians
- MS7 Exponential Functions: Index Laws, Sketching Exponential Functions, e = 2.718... Growth and Decay
- MS8 Logarithms: Natural Logarithm, Logarithm Laws, Using Logarithm to Fit Growth/Decay Functions, Half-Life/ Doubling Time
- Polynomials: Polynomial Division and "Remainder Theorem", Factor MT1 Theorem Linking Zeros to Factors, Continuous vs Discontinuous Functions, Smoothness, Sketching Factorised Form of Polynomials, Factorising Polynomials, The Quadratic Formula
- MT2 Matrices: Order, Notation, Linear Combinations of Matrices, Matrix Multiplication (Associative but not Commutative, Distributes across Linear Combinations), The Identity Matrix, Powers of Square Matrices, Matrix Transpose, Systems of Linear Equations, Matrix Inverse, 2×2 determinant, The 2×2 Inverse, $n \times n$ Inverses, Elementary Row Operations,

Code Inallie and INCy Concepts	Code	Name and Key Concepts
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- Vectors and Applications: Directed Line Segment Notation for Vectors, Magnetude/ Length and Direction, Linear Combinations of Vectors, Component and $a\mathbf{i} + b\mathbf{j}$ Notation, Vectors in \mathbb{R}^2 and \mathbb{R}^3 , Scalar Dot Product, Equation for a Plane in \mathbb{R}^3
- MT4 Systems of Linear Equations: Augmented Matrix for Systems of Linear Equations, Elementary Row Operations, Row-Echelon Form, Solutions to Systems of Linear Equations and Geometric Interpretations in \mathbb{R}^2 and \mathbb{R}^3 , Matrix Inverses by Gauss-Jordan Elimination
- MT6 **Differentiation**: Rates of Change, Gradient, First Principles, Limit Notation, Derivative Notation, $\frac{d}{dx}x^n = nx^{n-1}$ (including n=0 and n=1), Linearity of Differentiation, Product Rule, Quotient Rule, Chain Rule, Implicit Differentiation, Normal to a Curve
- MT7 Applications of Differentiation: Sketching Polynomials and Rational Functions (Intercepts and Asymptotes), Continuity, Sign Diagrams, Increasing and Decreasing, Stationary Points, Points of Inflection, Concavity, Optimisation,
- MT8 Exponential and Logarithm Functions: Sketching Exponential Functions, $e=2.718\ldots, \frac{d}{dx}e^x=e^x$, Natural Logarithm, $\frac{d}{dx}\ln(x)=\frac{1}{x}$, Growth and Decay, Surge Models, Logistic Models
- Integration: Area Under a Curve, Lower and Upper Sums, Definite Integrals, Definite Integrals of Negative Functions, Linearity of Integration, Properties of Definite Integrals, Fundamental Theorem of Calculus, Antiderivatives, Indefinite Integrals, Integrating by Reversing the Chain Rule, Integration by Substitution, Area Between two Curves, Summation Notation (Appendix)

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