ASDS Statistics, YSU, Fall 2020 Lecture 01

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15 Sep 2020

Welcome

Welcome to the ASDS Statistics Course

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And Happy New Year Semester ! =

Contents

- Syllabus highlights
- ► Intro to the Course
- ► Glance at a Course Structure
- Some important Notions and Definitions
- Stages of Doing a Statistical Analysis
- Different Types of Variables

► Course name: **Applied Statistics with R**

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- ▶ No late HWs (except some veeery special cases)
- Advice: Always ask your questions during lectures, ask your questions during OHs, solve HWs by yourself!
- Advice: Run over the Probability Topics, especially, about RVs and Distributions

QA Session

Questions?



Business

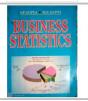










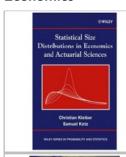


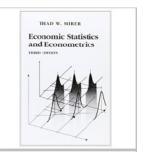


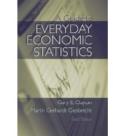


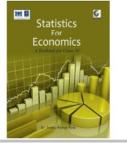


Economics









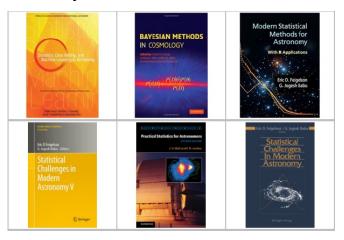
Agriculture



Finance



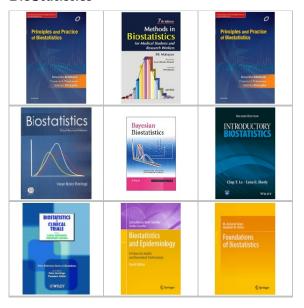
Astronomy



Biology



BioStatistics



Psychology

















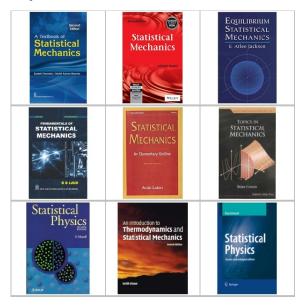


Medicine

MADE EASY
M. Harris and G. Taytor @CK.hes.



Physics and Mechanics



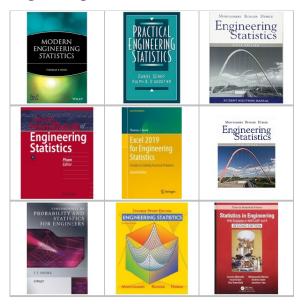
Marketing



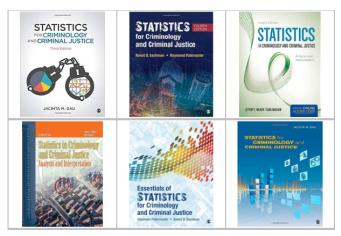
Language Study



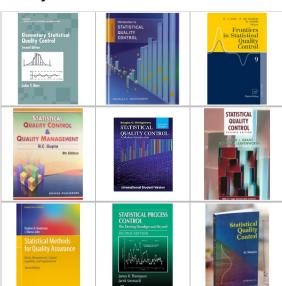
Engineering



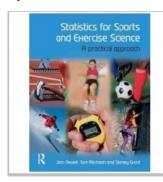
Criminology

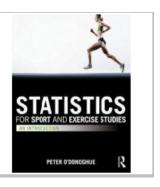


Quality Control

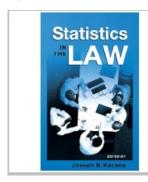


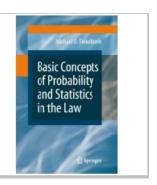
Sport





Law





Food



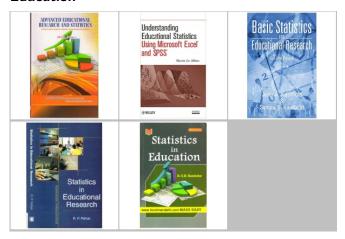
Genetics



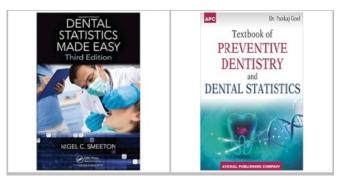
Chemistry



Education



Dentistry



Other...



ML, Statistical Learning



... and so on ...

▶ What is Statistics?

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Statistics is the Art and Science of **Collecting, Describing and Analyzing Data**, getting insight from Data.

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We assume that the daily number of customers who are ordering Pepperoni Pizza at a particular pizzeria is following the *Pois*(15.2) Distribution (the Reality, the Generating Process), and we are interested in the Probability that the daily number will exceed 17 (*Probability of a possible outcome*)

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We have Data about daily number of customers ordering Pepperoni Pizza at that pizzeria for some days:

and we want to find out the Distribution of the r.v.

X = the daily number of customers ordering PP at that pizzeria.

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Simple - to pass this course $\ddot{\ }$

About Statistics

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And finally, to understand the everyday usage of Statistical language, graphs and estimates, say, about polls and salaries —

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- Estimate the number/proportion of defective production in a manufacturing plant;
- Show that there is a strong correlation between education and income;
- ▶ Determine whether it is true that, in average, women earn less than men;

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- Check if the drug is effective against Corona

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Of course, the question/statement was not correct. If, say, half of the data is not correct, then, even if you will check the whole Dataset for correctness, you cannot be sure with 95% that the data is correct.

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- moreover, we can Estimate the number of Observations we need to take in the Sample (Sample Size) to be sure with 95% that the real proportion (of correct data) is within given small neighborhood of our Estimate;
- also we need to suggest how to choose that Sample (we need a Random Sampling)

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- ► Intro + Descriptive Statistics
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► Models, Statistical Inference and Learning:

Here we will talk mainly about the Parametric Statistics.

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Linear Regression

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And at the end of the course we will return back to Testing and cover:

Goodness of fit tests

Stages of the Statistical Analysis, and Data Types

Stages of Doing a Statistical Analysis

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We will mainly talk about the 2nd and 3rd stages. But first I want to give some Notions and Definitions we will use later.

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In Inferential Statistics, roughly, we use the Sample to get information about the Population.

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- ▶ **Statistics** is a numerical characteristic of the *Sample*

Here is one of the standard Datasets in R (the first several rows):

head(cars)

	speed	dist
1	4	2
2	4	10
3	7	4
4	7	22
5	8	16
6	9	10
	2 3 4 5	1 4 2 4 3 7 4 7 5 8

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- Which are the Variables ?
- Give two Observations.

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