

ML Review

Machine Learning for Trading (CS 7641)

- example x's: price, bollinger, momentum; y's: return and future price
- Supervised regression learning: linear regression, KNN, trees, forests
- RL
 - Markov decision problem: set of states (in market), set of actions (buy, sell, nothing), transition function $T(\text{state}, \text{action}, \text{state})$, reward function $R(\text{state}, \text{action})$
 - Q Learning: $Q'[s,a] = (1-\alpha) * Q[s,a] + \alpha * \text{improved_estimate}$
- Induction, deduction, supervised learning, unsupervised learning (news, genes), RL, decision trees
- Definitions: instances (input), concept (function), target concept (answer), hypothesis (set of all possible concepts), sample (training set), candidate (possible target concept), testing set. Tree nodes = attributes, edges = values
- Preprocessing (clean, train/test) -> Learning (model, cross-validate, performance, params optimization) -> Evaluation (against test) -> Prediction
- Target function: type of knowledge to be learned (e.g. each possible checkers board score)
- Representation for target function (e.g. linear function of board artifacts, # of pieces, # of pieces threatened)
- Learning mechanism: gradient descent
- Decision Tree: Robust to errors and missing attributes
- Entropy: $\sum(-p * \log p)$
- Overfit -> Occam's razor
- NN: Well suited for noisy, complex sensor data, such as inputs from cameras and microphones
- Gradient descent derivation
- Sigmoid: $1/(1-e^{-y})$
- Instance based learning (KNN): training data in storage and use it to make a forecast
- Other algorithms reduce data into a function, then make predictions ignoring the data
- Bayesian Learning: $P(h | D) = P(D | h) * P(h) / P(D)$

$$P(\text{disease}|\text{pos}) = 21\% = 98\% * 0.8\% / (98\% * 0.8\% + 3\% * 99.2\%)$$

- Pros/cons: DT, KNN, Boosting, SVM, NN, Bayes, Random Opt/Annealing

- Review
 - Maximum a posteriori MAP = $\text{argmax}_h P(D | h) * P(h)$
 - Maximum likelihood ML = $\text{argmax}_h P(D | h)$
- EM: Will not diverge, may not converge, can get stuck - must random restart
- K-means: randomly select k centers (points), assign each point to cluster (E), recalculate centers (M)
- Feature selection: exponential problem 2^n
- Filtering: selecting features first, then running algo, ignores learning problem, fast. Can use decision tree to select which features give most info. gain, then pass those features to another learner such NN
- Wrapping (optimizing algorithm based on given features and reiterating, slower). forward search (run learner with each feature independently, keep the best, add one more feature in addition to first and iterate as long as error improves)
- Feature transformation: PCA (Maximizes variance, Mutually orthogonal), ICA (Cocktail party problem: extract voice from multiple sources in a party)

Machine Learning (CS 7641)

- PCA: Obtain the Eigenvectors and Eigenvalues from the covariance matrix or correlation matrix. Sort eigenvalues in decreasing order
- Value Iteration, Policy Iteration, and Q-Learning
- Feature selection => curse of dimensionality (amount of data needed is 2^n , where n is the number of features)

Reinforcement Learning (CS 7642)

- RL: model is unknown or difficult to work with directly
- states (S), actions (A), rewards (R)
- methods for solving finite Markov decision problems:
 - dynamic programming: methods are well developed mathematically, but require a complete and accurate model of the environment
 - Monte Carlo methods: methods don't require a model and are conceptually simple, but are not well suited for step-by-step incremental computation
 - temporal-difference learning: methods require no model and are fully incremental, but are more complex to analyze. Monte Carlo methods must wait until the end of the episode to determine the increment, TD methods need wait only until the next time step

- Q-learning. ϵ -greedy guarantees convergence if

$$\sum \alpha = \infty; \sum \alpha^2 < \infty$$

- Sarsa update

$$Q_t = Q_t + \alpha(r + \gamma Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t))$$

- partially observable Markov decision processes: the agent does not simply know its state and must take actions to gain state-related information
- Q-Learning (off-policy greedy)
- SARSA (on-policy)
- Deep Q Network
- Plans: fixed, conditional (if statements), stationary policy/universal plan (mapping from state \rightarrow action, RL focus)
- Summarize policy
 - One sequence: sum of rewards
 - Over many sequences: average expectation
- Evaluate learner: total value, computational complexity (time), sample complexity (time)
- Incremental learning

$$V_T(S_1) = V_{T-1}(S_1) + \alpha_T[R_T(S_1) - V_{T-1}(S_1)]$$

- Where

$$\alpha_T = 1/T$$

- Must satisfy

$$\sum \alpha = \infty; \sum \alpha^2 < \infty$$

- Examples

$$\sum \alpha = 1/T$$

$$\sum \alpha = (1/T)^{2/3}$$

AI (CS 6601)

- AI (pass Turing test): natural language processing, knowledge representation, automated reasoning, machine learning (extrapolate), computer vision, robotics (manipulate objects)
- Minimax time: $O(b^m)$ where b is the number of actions and m number of steps (depth of the tree)
- Search: BFS, DFS, Cheapest first search (explored shortest total length), A*
- - Annealing: use temperature as a proxy for randomness. Start with high temperature (high randomness) and slowly lower it (low randomness)
- Travelling salesman: randomly connect cities, then remove any crossings of paths (within 1% of optimal)
- Genetic algorithms: determine score for each state. Higher scores have higher probability to appear in next generations. Crossover with other state for breed new, more optimal states
- Decision theory = probability theory + utility theory
- Bayes rule: $P(\text{cause} \mid \text{effect}) = P(\text{effect} \mid \text{cause})P(\text{cause}) / P(\text{effect})$
- ML: KNN, Gaussian, Naive Bayes
 - DT: decide each variable to split on based on information gain. Info gain is the expected reduction in entropy
 - Boosting: use weak classifiers and combine then by weighting errors more
 - NN: perceptron and backprop
 - K-means: assigning to clusters and updating means of clusters correspond respectively to the E (expectation) and (maximization) steps of the EM algorithm. $O(k \cdot n)$ where k is the k means and n is number of data
- Learning from Examples
- Cross validation methodology: k-fold training set and test set
- Regularization: process of explicitly penalizing complex hypotheses
- Hidden Markov Models

Data Visualization (CSE 6242)

- 1D data: histogram, strip plot, box plot
- 2D data: scatter plot, line plot
- 3D+: multivariate scatter, facets, contour
- Strip plot: x-axis description, y-axis value
- Histograms: x-axis bar label, y-axis count
- Multivariable scatter: use point type to distinguish 3rd dimension

- Missing Completely At Random (MCAR): probability that data is missing does not depend on observed or unobserved measurements. All solutions possible
- Missing At Random (MAR): probability that data is missing does not depend on unobserved data. May introduce bias
- Solutions:
 - Remove entire row
 - Replace with most likely value
 - Imputation: Build a probability model and sample from the model
- Outliers detection:
 - Below and above certain percentile (robust)
 - More than x standard deviations (requires the computation of mean and median which is not robust given outliers)
- Solutions:
 - Truncate: remove all outliers
 - Winsorization: shrink to the border of the main part of data
 - Robust procedure: keep all data, choose robust procedure (such as median)
- Transformation: Highly skewed distribution -> transformation -> map data to common distribution (Gaussian or Gamma) -> fit model
- power transform: $\frac{x^\lambda - 1}{\lambda}$
 - $\lambda > 1$: convex, removes left skew
 - $\lambda < 1$: concave, removes right skew
 - λ choice: histogram or log-log plot
- Other transforms: binning, binarization (0-1), tall vs wide data (easier to analyze, hard to remove)
- Logistic regression
- If data not linearly separable in original dim (eg 2D): increase dimension $(x_1, x_2) \Rightarrow (1, x_1, x_2, x_1^2, x_2^2, x_1x_2)$

ML Crash Course Google

- Terminology: labels, features, examples, models
- A regression model predicts continuous values
- A classification model predicts discrete values
- Regression:
 - loss is a number indicating how bad the model's prediction was
 - Mean square error (MSE) is the average squared loss per example over the whole dataset
- Gradient descent, convergence, training, loss
- A Machine Learning model is trained by starting with an initial guess for the weights and bias and iteratively adjusting those guesses until

learning the weights and bias with the lowest possible loss.

- gradient always points in the direction of steepest increase in the loss function
- gradient descent algorithm takes a step in the direction of the negative gradient
- Stochastic gradient descent (SGD) uses only a single example (a batch size of 1 per iteration)
- TensorFlow: Tensors are N-dimensional (where N could be very large) data structures, most commonly scalars, vectors, or matrices
- Estimator (tf.estimator) High-level, OOP API.
- tf.layers/tf.losses/tf.metrics Libraries for common model components.
- TensorFlow Lower-level APIs
- TensorFlow consists of the following two components:
 - a graph protocol buffer
 - a runtime that executes the (distributed) graph
- These two components are analogous to Python code and the Python interpreter

CONSOLIDATED:

Supervised Learning

Linear Regression

- Assumptions
 - LINE assumptions for confidence intervals:
 - Linearity: each y is a linear combination of features
 - Independent errors
 - Normal errors
 - Equal error variances
 - (x must be within scope of the model)
 - if all tested is that the slope β_1 is 0, you should be okay even if it appears that the normality condition is violated
 - if you want to use your model to predict a future response y_{new} , then you are likely to get inaccurate results if the error terms are not normally distributed
 - Tests
 - Plot predicted values y (x-axis) vs errors size (y-axis)
 - Plot each INCLUDED predictor (x-axis) vs errors size (y-axis)
 - Histogram of residuals (should be approx normal)

- Scatter of residuals (x-axis) vs percent (log y-axis): should be appx straight
- Plot each EXCLUDED predictor (x-axis) vs errors size (y-axis). Consider including if a useful trend appears
- Anderson-Darling Test: area between a fitted line and a nonparametric step function
- Shapiro-Wilk Test
- Ryan-Joiner Test
- Kolmogorov-Smirnov Test: compares the empirical cumulative distribution function of sample data with the distribution expected if the data were normal
- Variance
 - sample: $\frac{\sum (y_i - \bar{y})^2}{n-2}$
 - costs us 2 degrees of freedom to estimate b0 and b1: therefore, n-2
- R^2
 - quantifies the strength of a linear relationship, R^2 could be 0 but there could be a non-linear relationship
 - value should not be interpreted as meaning that the estimated regression line fits the data well (it might be slightly curved)
 - coefficient of determination R^2 could be greatly affected by just one data point
 - always increases (or stays the same) as more predictors are added to a multiple linear regression model, even if the predictors added are unrelated to the response variable
- Confidence interval
 - $\bar{y} \pm t * sd$
 - $\beta \pm t * \left(\frac{MSE}{\sum_i (y_i - \bar{y})} \right)^{1/2} = t * \left(\frac{\sum_i (y_i - \hat{y})/n}{\sum_i (y_i - \bar{y})} \right)^{1/2}$
- Analysis of Variance (ANOVA)

Source of Variation	DF	SS	MS	F
Regression	1	$SSR = \sum_{i=1}^n (\hat{y}_i - \bar{y})^2$	$MSR = \frac{SSR}{1}$	$F^* = \frac{MSR}{MSE}$
Residual error	n-2	$SSE = \sum_{i=1}^n (y_i - \hat{y}_i)^2$	$MSE = \frac{SSE}{n-2}$	
Total	n-1	$SSTO = \sum_{i=1}^n (y_i - \bar{y})^2$		

- Hypothesis test
 - $t^* = (\text{sample coefficient} - \text{hypothesized value}) / \text{standard error of coefficient}$.
 - testing if $b_1 = 0$
 - $t^* = (b_1 - 0) / SE(b_1)$
- Model evaluation
 - Define a larger full model
 - Define a smaller reduced model. (one with fewer parameters.)

- Use an F-statistic to decide whether or not to reject the smaller reduced model in favor of the larger full model. Low t-statistic > reject smaller model.
- Test if $\text{model_reduced} = \text{model_full}$
- $F^* = (SSE(R) - SSE(F)) / (df_r - df_f) / (SSE(F) / df_f)$
 - df: degrees of freedom, number of observations n - number of parameters
- If $t > 0.05 \Rightarrow$ cannot reject null hypotheses
- **Categorical Predictors**
 - When two predictors do not interact, we say that each predictor has an "additive effect"
 - Leaving out interacting terms may make the entire model insignificant
 - Piecewise model: introduce new variable for subset of data if function is piecewise: $y = b + w_1 * x + w_2 * (x - 70)$
 - Allows for two lines to be fit: < 70 and > 70
- **Model building**
 - model is underspecified
 - biased regression coefficients and biased predictions of the response
 - model is overspecified: contains one or more extraneous variables (unrelated to features or target)
 - unbiased regression coefficients, unbiased predictions of the response, and an unbiased MSE BUT confidence intervals tend to be wider
 - should not be used to describe the effect of a predictor
 - If only the prediction of response is important: multicollinearity is less concerning
 - Stepwise Regression: entering and removing predictors
 - Specify an Alpha-to-Enter: eg 0.15, Specify an Alpha-to-Remove: e.g. 0.15
 - Add the most significant feature first
 - Next, add the second most significant test tge model including the most significant
 - If the first feature becomes not significant by including the most significant second feature, remove the first
 - Continue with the next feature
 - Best Subsets Regression
 - select the subset of features that best meet an objective, such as the largest R2 value or the smallest MSE
 - given n features, we have 2^n possible models

- to cut down on the size to to explore, find few best with 1 feature, few best with 2 features, few best with 3 features ... and then compare
 - R2-adj makes adjustments for model size (no of features) so it's better for comparing across different models than raw R2
 - To select the best model from those suggested by the 2 procedures, check for multicollinearity. No none present, take the simplest
- Information Criteria
 - Bayesian Information Criterion (BIC): $n * \ln(SSE) - n * \ln(n) + p * \ln(n)$
 - places a higher penalty on the number of parameters in the model so will tend to reward more parsimonious (smaller) models. lower BIC is better
- Influential points
 - Outliers: extreme y
 - High leverage points: extreme x
 - MSE is substantially inflated by the presence of the outlier
 - Handling data errors:
 - If the error is just a data entry or data collection error, correct it.
 - If the data point is not representative of the intended study population, delete it.
 - If the data point is a procedural error and invalidates the measurement, delete it.
 - Did you leave out any important predictors?
 - Should you consider adding some interaction terms?
 - Is there any nonlinearity that needs to be modeled?
- Multicollinearity
 - two or more of the predictors in a regression model are moderately or highly correlated
 - Structural multicollinearity is a mathematical artifact caused by creating new predictors from other predictors
 - Data-based multicollinearity is a result of reliance on purely observational data, or the inability to manipulate the system on which the data are collected
 - Perfectly uncorrelated coefficients
 - SE of regression, SE of features, coef of features are the same in case of multiple and single regression
 - Highly correlated features
 - the estimated coefficient of any one variable depends on which other predictor variables are included in the model

- precision of the estimated regression coefficients decreases
- does not prevent good, precise predictions
- detecting multicollinearity using Variance Inflation Factors
quantifies how much the variance is inflated
- to remove structural correlation ($x+x^2$), we need to center the feature x

Logistic Regression

- Precision: $TP / (TP + FP)$
- Recall: $TP / (TP + FN)$
- F1 score: $2 * (\text{precision} * \text{recall}) / (\text{precision} + \text{recall})$
 - [source](#)

Unsupervised Learning

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Reinforcement Learning

- Sarsa: On-Policy TD Control

$$Q(S_t, A_t) = Q(S_t, A_t) + \alpha * [R_{t+1} + \gamma * Q(S_{t+1}, A_{t+1}) - Q(S_t, A_t)]$$

- Q-learning: Off-Policy TD Control

$$Q(S_t, A_t) = Q(S_t, A_t) + \alpha * [R_{t+1} + \gamma * \max_a Q(S_{t+1}, a) - Q(S_t, A_t)]$$

- Solving the Multi-Armed Bandit Problem
 - $Q_k = 1/k * (r_1 + r_2 + r_3 \dots + r_k)$
 - $Q_{k+1} = Q_k + 1/(k+1) * (r_{k+1} - Q_k)$
 - towardsdatascience.com/solving-the-multi-armed-bandit-problem-b72de40db97c

Time series

- Algorithm requirements:
 - extrapolate patterns outside of the domain of training data
 - derive confidence intervals
- Most common algos Linear regression
 - +Handles different time series

- +High interpretability
- -Sensitive to outliers
- -Narrow confidence intervals Exponential smoothing ARIMA
(Autoregressive Integrated Moving Average) Dynamic Linear Model
- Sources
 - datascience.com/blog/time-series-forecasting-machine-learning-differences

Preprocessing

outliers

missing values

duplicates

feature correlation

skew / class distribution

- collect more data
- use a difference metric: precision / recall / F1 score
- over or under sampling (copy infrequent classes, remove frequent)
- generate synthetic samples
- try different algorithms (decision trees often perform well on imbalanced datasets)
- different perspective (anomaly detection and change detection)
 - machinelearningmastery.com/tactics-to-combat-imbalanced-classes-in-your-machine-learning-dataset/
- If important predictor variables are omitted, see whether adding the omitted predictors improves the model.
 - onlinecourses.science.psu.edu/stat501/node/318/
- If the mean of the response is not a linear function of the predictors, try a different function. For example, polynomial regression
- If there are unequal error variances, try transforming the response and/or predictor variables or use weighted least squares regression.

- each observation i is weighted by $1/\sigma_i^2$
- If an outlier exists, try using a "robust estimation procedure."
- If error terms are not independent, try fitting a "time series model."
- transforming the x values is appropriate when non-linearity is the only problem — the independence, normality and equal variance conditions are met
- if the error terms are well-behaved, transforming the y values could change them into badly-behaved error terms
- transforming the response y values should be considered when non-normality and/or unequal variances
- typically try \ln transformation for non-linearity. Others e^{-x} , $1/x$, $\ln(y)$, $\ln(y) + \ln(x)$
- transforming the y -variable changes the variance of the y -variable and the errors
- interaction terms ($x_1 * x_2$): if $X_1 * X_2$ is shown to be a statistically significant predictor of Y , then your model should also include the "main effects" X_1 and X_2

Articles

Data Science for Startups: Data Pipelines

- low latency
- scalability
- interactive querying
- versioning
- monitoring
- testing
- towardsdatascience.com/data-science-for-startups-data-pipelines-786f6746a59a

Estimating Probabilities with Bayesian Modeling in Python

- Bayesian Model: $(p | x, a)$. x are actual samples, a are prior beliefs
- parameter vector for a multinomial is drawn from a Dirichlet Distribution
 - $(p | x, a) = (c_i + a_i) / (N + \sum(a_i))$

- towardsdatascience.com/estimating-probabilities-with-bayesian-modeling-in-python-7144be007815