

## Binary numbers

| Decimal | Binary |
|---------|--------|
| 0       | 0000   |
| 1       | 0001   |
| 2       | 0010   |
| 3       | 0011   |
| 4       | 0100   |
| 5       | 0101   |
| 6       | 0110   |
| 7       | 0111   |
| 8       | 1000   |
| 9       | 1001   |
| 10      | 1010   |
| 11      | 1011   |
| 12      | 1100   |
| 13      | 1101   |
| 14      | 1110   |
| 15      | 1111   |

1 0 1 1

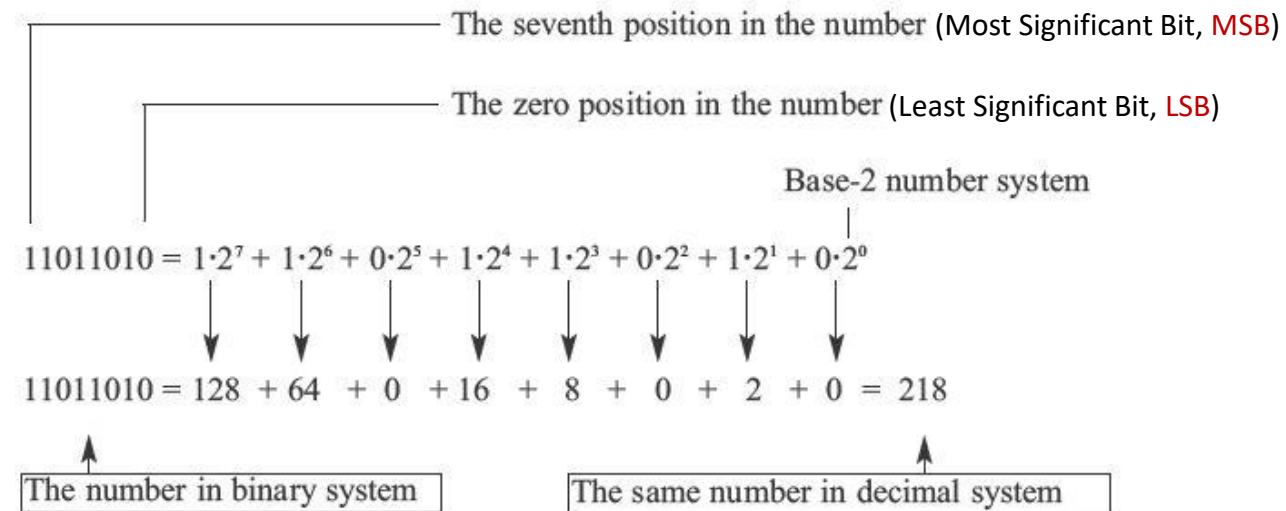
$1 \times 1 = 1$

$1 \times 2 = 2$

$0 \times 4 = 0$

$1 \times 8 = 8$

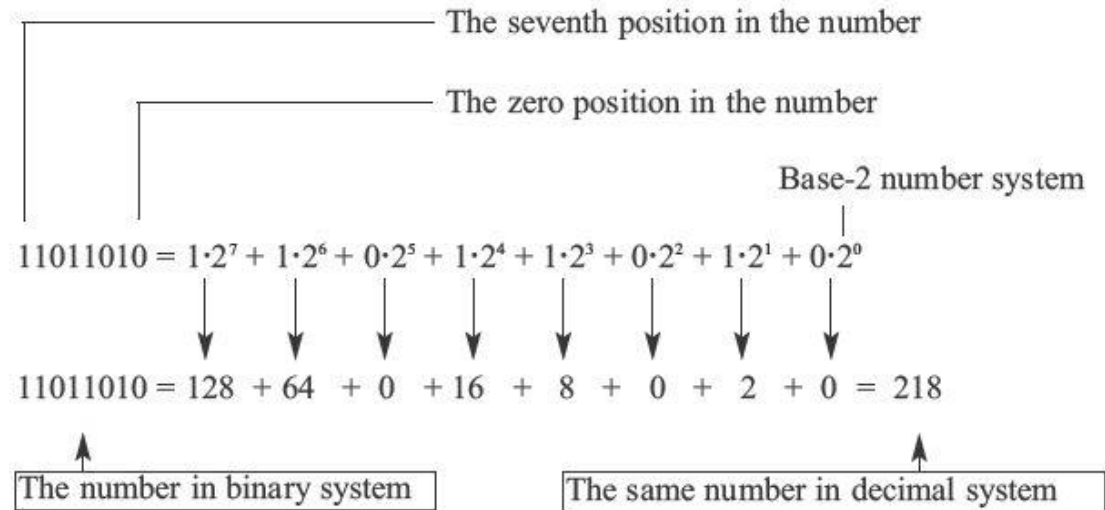
## Binary Weights



## Number of bits in a binary number

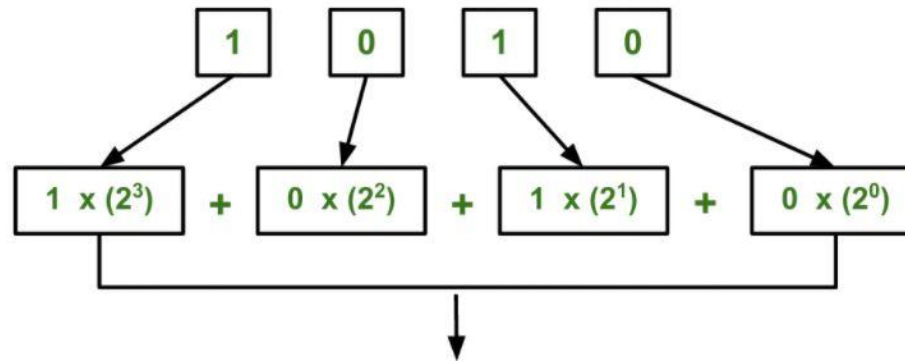
An n-bit number produces  $2^n$  combinations of 0s and 1s in n bits

An 8-bit number produces  $2^8 = 256$  combinations (that is from 0 to 255)



## Binary to decimal conversion

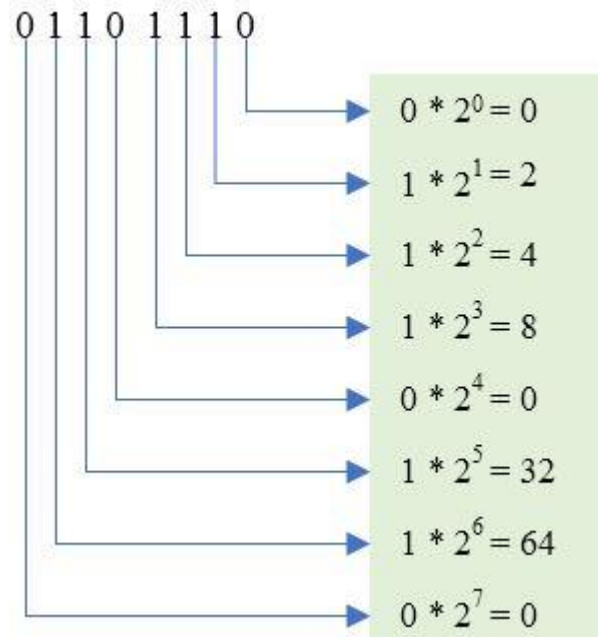
4-bit Binary number: 1010



Decimal number:  $8+0+2+0 = 10$

## Binary to decimal conversion

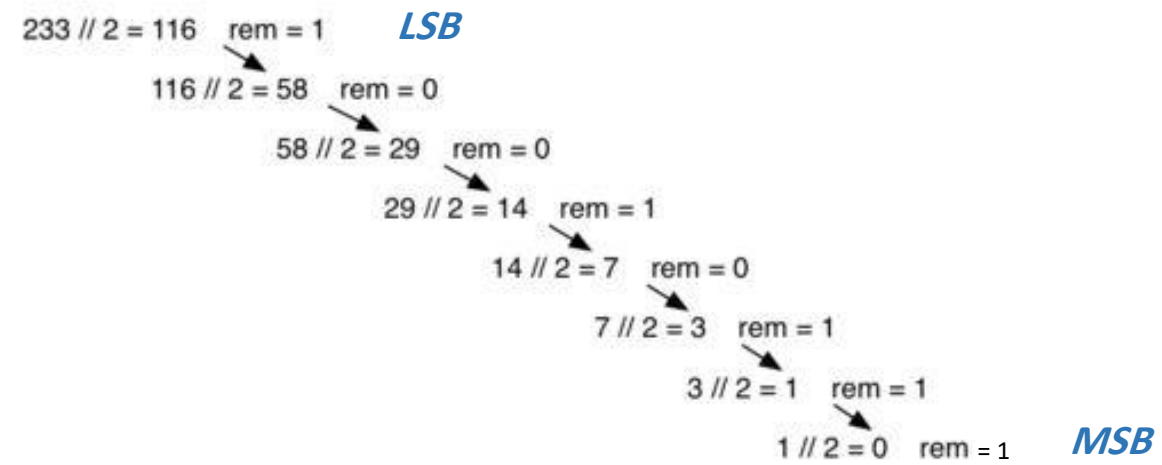
8-bit Binary number: 01101110



Decimal number:  $0+2+4+8+0+32+64+0 = 110$

## Decimal to binary conversion

Decimal number: 233



Binary number: 11101001

Binary addition

Example 1:

|   |     |
|---|-----|
| <div><div>1 1</div><div>00110 +</div></div> | 6 + |
| <div>00011</div>                            | 3   |
| <hr/>                                       |     |
| <div>01001</div>                            | 9   |

Example 2:

|                    |      |
|--------------------|------|
| <div>10000 +</div> | 16 + |
| <div>00111</div>   | 7    |
| <hr/>              |      |
| <div>10111</div>   | 23   |

Example 3:

|   |      |
|---|------|
| <div><div>1 1</div><div>10011 +</div></div> | 19 + |
| <div>10001</div>                            | 17   |
| <hr/>                                       |      |
| <div>1 ← 00100</div>                        | 36   |

} *Overflow*  
*Need more than five bits for the sum*

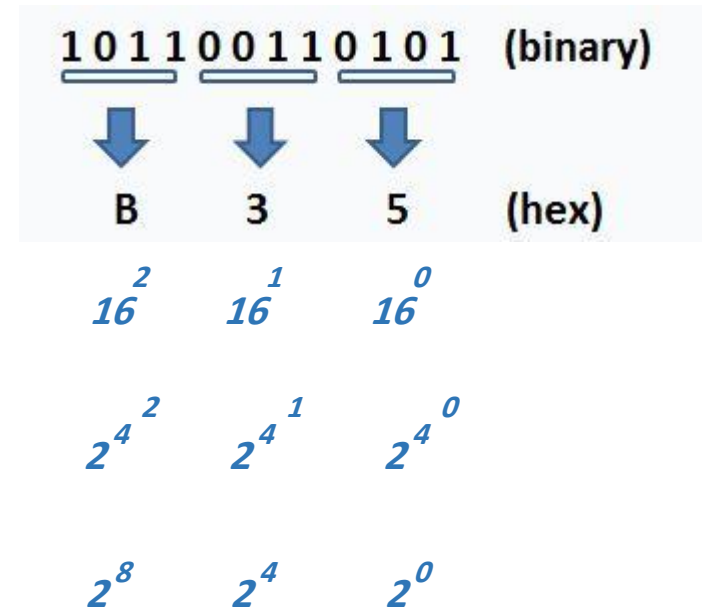
Octal and Hexadecimal numbers are closely related to binary numbers

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |



## Binary to Hexadecimal conversion

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |



## Binary to Hexadecimal conversion

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |

**Find the Hex Equivalent  
for Binary 1011010**

**101**  
group 2

**1010**  
group 1

*Group 2 containing only 3 bits,  
so add 0 to the left*

**0101**  
↓  
**5**

**1010**  
↓  
**A**

## Hexadecimal to binary conversion

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |

### Binary to Hexadecimal Conversion

Convert the binary number  $1111110101110011_2$  to its hexadecimal equivalent.

1. Separate the digits into groups from right to left side; each group contains 4 bits of binary number.

**1111 1101 0111 0011**

2. Find the equivalent hexadecimal number for each group.

**1111 1101 0111 0011**

**F D 7 3**

## Hexadecimal to binary conversion

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |

### Hex to Binary Number Conversion

Convert the hexadecimal  $9DB5_{16}$  to its binary equivalent.

1. Separate the digits of the given hexadecimal, if more than 1 digit.

**9                  D                  B                  5**

2. Find the equivalent binary number for each digit of hex number, add 0's to the left if any of the binary number is shorter than 4 bits.

**9                  D                  B                  5**  
**1001   1110   1011   0101**

## Binary to Octal conversion

|                 | $2^1$         | $2^3$        | $2^4$                |
|-----------------|---------------|--------------|----------------------|
| Decimal Base-10 | Binary Base-2 | Octal Base-8 | Hexa Decimal Base-16 |
| 0               | 0             | 0            | 0                    |
| 1               | 1             | 1            | 1                    |
| 2               | 10            | 2            | 2                    |
| 3               | 11            | 3            | 3                    |
| 4               | 100           | 4            | 4                    |
| 5               | 101           | 5            | 5                    |
| 6               | 110           | 6            | 6                    |
| 7               | 111           | 7            | 7                    |
| 8               | 1000          | 10           | 8                    |
| 9               | 1001          | 11           | 9                    |
| 10              | 1010          | 12           | A                    |
| 11              | 1011          | 13           | B                    |
| 12              | 1100          | 14           | C                    |
| 13              | 1101          | 15           | D                    |
| 14              | 1110          | 16           | E                    |
| 15              | 1111          | 17           | F                    |
| 16              | 10000         | 20           | 10                   |

### Binary to Octal Conversion

Convert the binary number  $111110011001_2$  to its octal equivalent.

1. Separate the digits of a given binary number into groups from right to left side, each containing 4 bits.

**111 110 011 001**

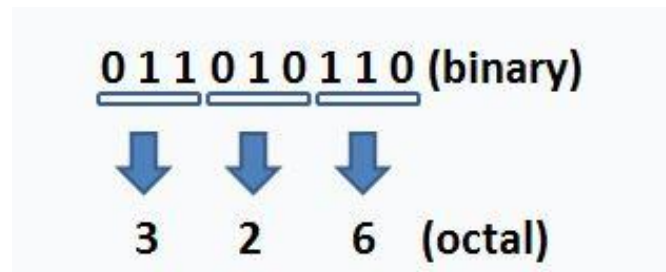
2. Find the equivalent octal number for each group.

**111 110 011 001**

**7 6 3 1**

## Binary to Octal conversion

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |





## Octal to Binary conversion

|                    | $2^1$            | $2^3$           | $2^4$                   |
|--------------------|------------------|-----------------|-------------------------|
| Decimal<br>Base-10 | Binary<br>Base-2 | Octal<br>Base-8 | Hexa Decimal<br>Base-16 |
| 0                  | 0                | 0               | 0                       |
| 1                  | 1                | 1               | 1                       |
| 2                  | 10               | 2               | 2                       |
| 3                  | 11               | 3               | 3                       |
| 4                  | 100              | 4               | 4                       |
| 5                  | 101              | 5               | 5                       |
| 6                  | 110              | 6               | 6                       |
| 7                  | 111              | 7               | 7                       |
| 8                  | 1000             | 10              | 8                       |
| 9                  | 1001             | 11              | 9                       |
| 10                 | 1010             | 12              | A                       |
| 11                 | 1011             | 13              | B                       |
| 12                 | 1100             | 14              | C                       |
| 13                 | 1101             | 15              | D                       |
| 14                 | 1110             | 16              | E                       |
| 15                 | 1111             | 17              | F                       |
| 16                 | 10000            | 20              | 10                      |

### Octal to Binary Conversion

Convert the octal  $7631_8$  to its binary equivalent.

1. Separate the digits of the given octal number, if it contains more than 1 digit.

**7                  6                  3                  1**

2. Find the equivalent binary number for each digit of octal number. Add 0's to the left if any of the binary equivalent is shorter than 3 bits.

**7                  6                  3                  1**

**111    110                  011    001**