Reinforcement learning in quantitative wealth and investment management $\mathbb{QWIM}$

Cristian Homescu

December 2022

Abstract

This document provides details for this QWIM project, and it incorporates the following sections

- Motivation
- Relevant references
- Suggested project tasks and timelines
- Practical info
  - ◇ Recommended software tools
  - ◇ Recommended datasets
- Design and implementation for the project codes
- Potentially useful Python and R packages, codes and frameworks
- Appendices

Appendices include

- Overviews of investment processes and models in QWIM
- Comparison of investment portfolios using portfolios metrics and benchmark portfolios

Contents

1 Motivation for the project

1.1 Reinforcement learning

Reinforcement learning $\mathbb{RL}$ considers the problem of the automatic learning of optimal decisions over time. It differs from other types of learning (such as unsupervized or supervised) since the learning follows from feedback and experience (and not from some fixed training sample of data).

$\mathbb{RL}$ is learning what to do (how to map situations to actions), to maximize a numerical reward signal. The learner is not told which actions to take, but instead must discover which actions yield the most reward by trying them. Actions may affect not only the immediate reward but also the next situation and, through that, all subsequent rewards. These two characteristics (trial-and-error search and delayed reward) are the two most important distinguishing features of reinforcement learning.

Thus $\mathbb{RL}$ algorithms describe how an agent can learn an optimal action policy in a sequential decision process, through repeated experience, with primary purpose of finding an optimal policy (a mapping from the states of the world to the set of actions), in order to maximize cumulative reward (a long term strategy), although exploring might be sub-optimal on a short-term horizon.

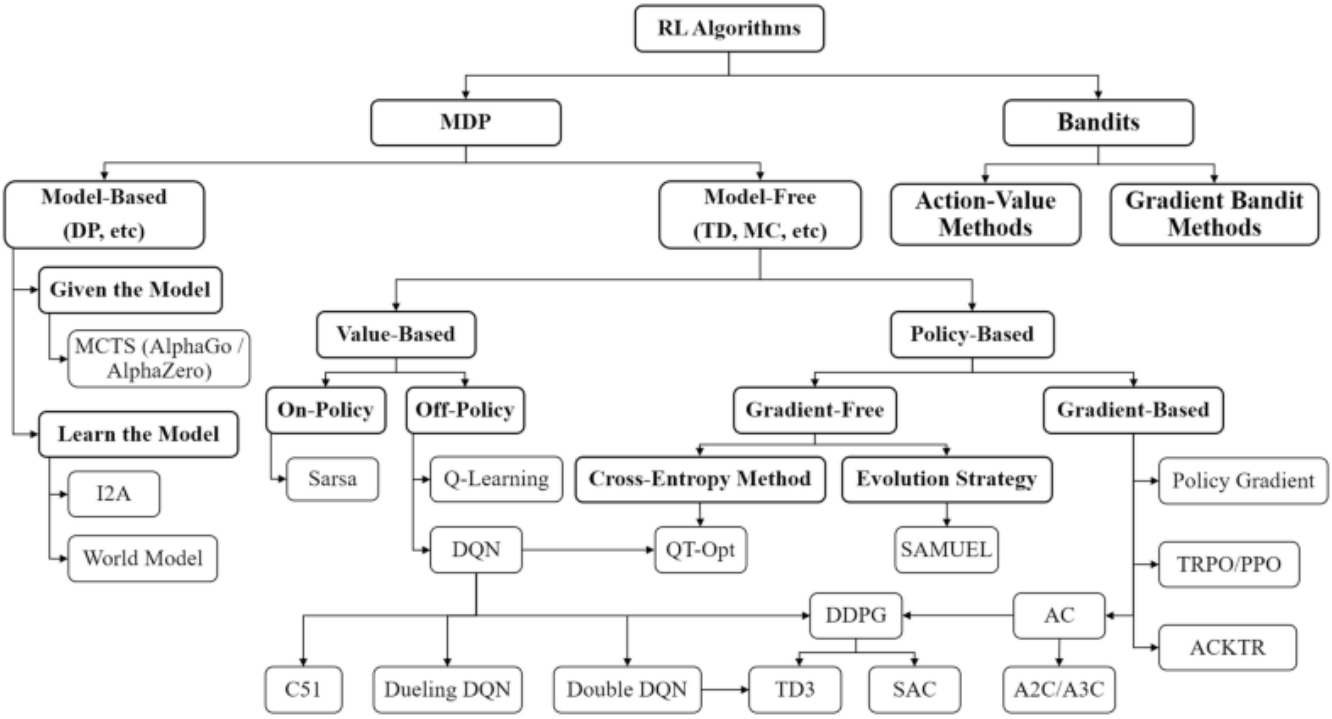
In a given environment, the agent policy provides some intermediate and terminal rewards, while the agent learns sequentially. When an agent picks an action, she can not infer ex-post the rewards induced by other action choices. Agent's actions have consequences, influencing not only rewards, but also future states of the world.

$\mathbb{RL}$ combines the following:

- major entities
  - ◇ agent: somebody or something who/that interacts with the environment by executing certain actions, making observations, and receiving eventual rewards for this. It is the learner and decision maker
  - ◇ environment: everything outside of an agent's direct control
  - ◇ policy: mapping from perceived states of the environment to actions to be taken when in those states, which defines how an agent selects actions
  - ◇ (optional) model of environment: mimics the behavior of the environment, or more generally, that allows inferences to be made about how the environment will behave
- communication channels:
  - ◇ actions: executed by the agent and given to the environment
  - ◇ reward: describes the goal of a $\mathbb{RL}$ problem, and it is a scalar value (obtained from environment) whose main purpose is to tell our agent how well it has behaved
  - ◇ value function: value of a state is the total amount of reward an agent can expect to accumulate over the future, starting from that state. Whereas the reward signal indicates what is good in an immediate sense, a value function specifies what is good in the long run
  - ◇ observations: information besides the reward that the agent receives from the environment, indicating what's going on around the agent

A taxonomy of reinforcement learning algorithms is shown next. Boxes with thick lines denote different categories, others denote specific algorithms.

Figure 1: Taxonomy of einforcement learning algorithms



Source: Zhang and Yu ("Taxonomy of Reinforcement Learning Algorithms," 2020)

1.2 Using $\mathbb{RL}$ in $\mathbb{QWIM}$

$\mathbb{RL}$ allows to combine "prediction" and "portfolio construction" tasks in one integrated step, thereby closely aligning $\mathbb{ML}$ problem with investor objectives. $\mathbb{RL}$ is capable of handling real-world complexity of financial planning, including effects of income taxes, mean-reverting asset classes, time-varying bond yield curves, and uncertain life expectancies. $\mathbb{RL}$ allows robo-advisor to "learn" investor risk preference over time by observing her portfolio choices under different markets.

- Das and Varma ("Dynamic Goals-Based Wealth Management using Reinforcement Learning," 2020): use $\mathbb{RL}$ to solve for Goal Based Investing $\mathbb{GBI}$, with the solution converging to the solution obtained using dynamic programming
- Dixon and Halperin ("Goal-based wealth management with generative reinforcement learning," 2021), Dixon and Halperin ("G-Learner and GIRL: Goal Based Wealth Management with Reinforcement Learning," 2020), Dixon and Halperin ("G-Learner and GIRL: Goal Based Wealth Management with Reinforcement Learning," 2020): $\mathbb{GBI}$ approach using $\mathbb{RL}$:
  - ◇ G-Learner, which operates with explicitly defined one-step rewards, does not assume a data generation process and is suitable for noisy data
  - ◇ GIRL extends G-Learner within context of Inverse Reinforcement Learning $\mathbb{IRL}$, where rewards collected by agent are not observed, and should instead be inferred
- Fischer (*Reinforcement learning in financial markets - a survey*, 2018): $\mathbb{RL}$ combines "prediction" and "portfolio construction"
- Noguer i Alonso and Srivastava ("Deep Reinforcement Learning for Asset Allocation in US Equities," 2020): $\mathbb{DRL}$ for model-free asset allocation
- Sato ("Model-Free Reinforcement Learning for Financial Portfolios: A Brief Survey," 2019): model-free $\mathbb{RL}$ for financial portfolios

- Irlam ("Machine learning for retirement planning," 2020): $\mathbb{RL}$ is capable of handling real-world complexity of financial planning; taxes, inflation, longevity, etc.
- Irlam ("Machine learning for retirement planning," 2020): financial and retirement planning via $\mathbb{DRL}$ outperforms traditional approaches
- Benhamou et al. ("Adaptive learning for financial markets mixing model-based and model-free RL for volatility targeting," 2021): bridges the gap between $\mathbb{DRL}$ and Modern Portfolio Theory, with $\mathbb{DRL}$ mapping directly market conditions to actions by design
- Benhamou et al. ("Adaptive learning for financial markets mixing model-based and model-free RL for volatility targeting," 2021): augmented asset management via $\mathbb{DRL}$
- Hu and Lin ("Deep reinforcement learning for optimizing finance portfolio management," 2019), Cong et al. ("AlphaPortfolio: Direct Construction Through Deep Reinforcement Learning and Interpretable AI," 2022): $\mathbb{DRL}$-based portfolio management
- Cong et al. ("Deep Sequence Modeling: Development and Applications in Asset Pricing," 2021), Cong et al. ("AlphaPortfolio: Direct Construction Through Deep Reinforcement Learning and Interpretable AI," 2022): $\mathbb{DRL}$ plus deep sequence modeling delivers AlphaPortfolio with impressive out-of-sample performance.
- Alsabah et al. ("Robo-Advising: Learning Investors Risk Preferences via Portfolio Choices," 2021): using $\mathbb{RL}$, roboadvisor "learns" over time investor risk preference by observing her portfolio choices under different markets.
- Cao et al. ("Deep Hedging of Derivatives Using Reinforcement Learning," 2020): $\mathbb{DRL}$ for optimal hedging under transaction costs
- Carbonneau ("Deep Hedging of Long-Term Financial Derivatives," 2020), Carbonneau and Godin ("Equal risk pricing of derivatives with deep hedging," 2021), Cao et al. ("Deep Hedging of Derivatives Using Reinforcement Learning," 2021), Benhamou et al. ("Time your hedge with Deep Reinforcement Learning," 2020): $\mathbb{DRL}$ for hedging of financial derivatives (including long term)

Dixon and Halperin ("Goal-based wealth management with generative reinforcement learning," 2021): $\mathbb{RL}$ does not require a specific parametric model for the asset price dynamics, offering instead a data-driven extension of dynamic programming. However, practical applications of $\mathbb{RL}$ to problems of portfolio optimization amount to a high-dimensional control in a continuous space of allocations (actions, in the language of $\mathbb{RL}$). However, methods based on deep $\mathbb{RL}$ are very data-hungry, slow to train, very sensitive to both the inputs and hyperparameters, and usually rely heavily on various heuristics.

1.3 Using $\mathbb{RL}$ in $\mathbb{QWIM}$: Goals-based investing

Goal Based Investing $\mathbb{GBI}$ is an investment approach where performance is measured by the success of investments in meeting the investor financial goals. For an individual investor such goals may be retirement, education for children, or vacation home, while for insitutional investors such as pension funds the goals may be aligned to the pension liabilities. The objective is to invest systematically in a consistent manner with investor's risk profile and time horizon of the goals, and performance is measured by probabilities of success in achieving investor financial goals (at given time horizons and for specified priority levels)

Portfolio optimization for GBI can be viewed as an optimal control problem performed within a data-driven world. $\mathbb{GBI}$ can be solved via reinforcement learning $\mathbb{RL}$, a paradigm of learning by trial-and-error, solely from rewards or punishments. It was shown that $\mathbb{RL}$ can solve financial applications of intertemporal choice.

Given current state-of-the-art for $\mathbb{RL}$, incorporating multiple goals with their corresponding priority levels within a $\mathbb{RL}$-based solution for $\mathbb{GBI}$ appears to be a significant modeling challenge. One possible solution may leverage hierarchical $\mathbb{RL}$ and curiosity-driven exploration.

1.4 Using $\mathbb{RL}$ in $\mathbb{QWIM}$: Asset allocation and portfolio construction

Benhamou ("Next Generation Robo Advisors," 2021)

Benhamou et al. ("AAMDRL: Augmented Asset Management With Deep Reinforcement Learning," 2021)

Benhamou et al. ("Bridging the Gap Between Markowitz Planning and Deep Reinforcement Learning," 2021)

Benhamou et al. ("Deep Reinforcement Learning (DRL) for Portfolio Allocation," 2021)

Benhamou et al. ("DRLPS: Deep Reinforcement Learning for Portfolio Selection (Presentation Slides ECML PKDD)," 2021)

Benhamou et al. ("Deep Reinforcement Learning (DRL) for Portfolio Allocation," 2021)

Benhamou et al. ("Bridging the gap between Markowitz planning and deep reinforcement learning (ICAPS PRL Presentation Slides 2020)," 2021)

Ungari and Benhamou ("Deep Reinforcement Learning for Portfolio Allocation," 2021)

2 Relevant references

2.1 Main references

List of references:

Aliaga-Diaz et al. (*Vanguard's Life-Cycle Investing Model (VLCM): A general portfolio framework for goals-based investing*, 2021)

Alsabah et al. ("Robo-Advising: Learning Investors Risk Preferences via Portfolio Choices," 2021)

Bartram et al. ("Machine Learning for Active Portfolio Management," 2021)

Benhamou et al. ("AAMDRL: Augmented Asset Management With Deep Reinforcement Learning," 2021)

Benhamou et al. ("Bridging the Gap Between Markowitz Planning and Deep Reinforcement Learning," 2021)

Benhamou et al. ("Deep Reinforcement Learning (DRL) for Portfolio Allocation," 2021)

Benhamou et al. ("Detecting and Adapting to Crisis Pattern with Context Based Deep Reinforcement Learning," 2021)

Benhamou et al. ("Adaptive learning for financial markets mixing model-based and model-free RL for volatility targeting," 2021)

Benhamou et al. ("Bridging the gap between Markowitz planning and deep reinforcement learning (ICAPS PRL Presentation Slides 2020)," 2021)

Cong et al. ("AlphaPortfolio: Direct Construction Through Deep Reinforcement Learning and Interpretable AI," 2022)

Cuschieri et al. ("TD3-Based Ensemble Reinforcement Learning for Financial Portfolio Optimisation," 2021)

Das et al. ("Dynamic portfolio allocation in goals-based wealth management," 2020)

Das and Varma ("Dynamic Goals-Based Wealth Management using Reinforcement Learning," 2020)

Das et al. ("Optimal Goals-Based Investment Strategies For Switching Between Bull and Bear Markets," 2021)

Das et al. ("Dynamic portfolio allocation in goals-based wealth management," 2020)

Das et al. ("Optimal Goals-Based Investment Strategies For Switching Between Bull and Bear Markets," 2022)

Das et al. ("Dynamic optimization for multi-goals wealth management," 2022)

Dempster et al. ("Lifecycle Goal Achievement or Portfolio Volatility Reduction?" 2016)

Dixon and Halperin ("G-Learner and GIRL: Goal Based Wealth Management with Reinforcement Learning," 2020)

Dixon and Halperin ("Goal-based wealth management with generative reinforcement learning," 2021)

Dixon et al. (*Machine Learning in Finance: from theory to practice*, 2020)

Dong et al. ("Baconian: A Unified Open source Framework for Model-Based Reinforcement Learning," 2021)

Fleiss et al. ("Deep Reinforcement Learning and Feature Extraction For Constructing Alpha Generating Equity Portfolios," 2021)

Guan and Liu ("Explainable Deep Reinforcement Learning for Portfolio Management: An Empirical Approach," 2021)

Halperin et al. ("Combining Reinforcement Learning and Inverse Reinforcement Learning for Asset Allocation Recommendations," 2022)

Hambly et al. ("Recent Advances in Reinforcement Learning in Finance," 2021)

Honchar (*AI for portfolio management: from Markowitz to Reinforcement Learning*, 2019)

Irlam ("Machine learning for retirement planning," 2020)

Irlam ("Multi Scenario Financial Planning via Deep Reinforcement Learning AI," 2020)

Ivanov and D'yakonov ("Modern Deep Reinforcement Learning Algorithms," 2019)

Jaimungal et al. ("Robust Risk-Aware Reinforcement Learning," 2021)

Kim et al. ("Personalized goal-based investing via multi-stage stochastic goal programming," 2020)

Kolm and Ritter ("Modern Perspectives on Reinforcement Learning in Finance," 2020)

Liu et al. ("FinRL: Deep Reinforcement Learning Framework to Automate Trading in Quantitative Finance," 2021)

Jaisson ("Deep differentiable reinforcement learning and optimal trading," 2022)

Martellini et al. ("Securing Replacement Income with Goal-Based Retirement Investing Strategies," 2020)

Marzban et al. ("WaveCorr: Correlation-savvy Deep Reinforcement Learning for Portfolio Management," 2021)

Mohammed et al. ("Embracing advanced AI/ML to help investors achieve success: Vanguard Reinforcement Learning for Financial Goal Planning," 2021)

Mulvey et al. ("A Factor- and Goal-Driven Model for Defined Benefit Pensions: Setting Realistic Benefits," 2019)
Noguer i Alonso and Srivastava ("Deep Reinforcement Learning for Asset Allocation in US Equities," 2020)
Nguyen et al. ("Review, Analyze, and Design a Comprehensive Deep Reinforcement Learning Framework," 2021)
Odermatt et al. ("Deep Reinforcement Learning for Finance and the Efficient Market Hypothesis," 2021)
Parker ("Goal-Based Portfolio Optimization," 2016)
Parker ("Portfolio Selection in a Goal-Based Setting," 2016)
Parker ("Allocation of wealth both within and across goals: a practitioner guide," 2020)
Parker ("Multi-Period Goals-Based Portfolio Optimization," 2021)
Parker ("Achieving Goals While Making an Impact: Balancing Financial Goals with Impact Investing," 2021)
Parker ("A Goals-Based Theory of Utility," 2021)
Plaat et al. ("High-Accuracy Model-Based Reinforcement Learning, a Survey," 2021)
Schwarzer et al. ("Pretraining Representations for Data-Efficient Reinforcement Learning," 2021)
Sun et al. ("Reinforcement Learning for Quantitative Trading," 2021)
Ungari and Benhamou ("Deep Reinforcement Learning for Portfolio Allocation," 2021)
Wang et al. ("Portfolio Selection in Goals-Based Wealth Management," 2011)
Yekelchik et al. ("Deep Q-Network Interpertability: Applications to ETF Trading," 2021)
Zhang et al. ("On the Importance of Hyperparameter Optimization for Model-based Reinforcement Learning," 2021)

2.2 Comprehensive list of references

2.2.1 Goals-based investing

List of references:

Brunel ("Extending the Goals-Based Framework to Comprise Both Investment and Financial Planning," 2020)
Chhabra (*The Aspirational Investor: Taming the Markets to Achieve Your Life's Goals*, 2015)
Cvitanic et al. ("Pi portfolio management: reaching goals while avoiding drawdowns," 2020)
Das et al. ("Dynamic portfolio allocation in goals-based wealth management," 2020)
Das and Varma ("Dynamic Goals-Based Wealth Management using Reinforcement Learning," 2020)
Das and Ross ("The Role of Options in Goals-Based Wealth Management," 2021)
Das et al. ("Dynamic portfolio allocation in goals-based wealth management," 2020)
Das et al. ("Optimal Goals-Based Investment Strategies For Switching Between Bull and Bear Markets," 2022)
Das et al. ("Dynamic optimization for multi-goals wealth management," 2022)
Deguest et al. (*Introducing a Comprehensive Investment Framework for Goals-Based Wealth Management*, 2015)
Dempster et al. ("Lifecycle Goal Achievement or Portfolio Volatility Reduction?" 2016)
Denault and Simonato ("A note on a dynamic goal-based wealth management problem," 2022)
Dixon et al. (*Machine Learning in Finance: from theory to practice*, 2020)
Dixon and Halperin ("G-Learner and GIRL: Goal Based Wealth Management with Reinforcement Learning," 2020)
Guo et al. ("Portfolio optimization with a prescribed terminal wealth distribution," 2022)
Janssen et al. ("Life Cycle Investing: From Target-Date to Goal-Based Investing," 2013)
Kim et al. ("Personalized goal-based investing via multi-stage stochastic goal programming," 2020)
Liu et al. ("FinRL: Deep Reinforcement Learning Framework to Automate Trading in Quantitative Finance," 2021)
Martellini et al. ("Securing Replacement Income with Goal-Based Retirement Investing Strategies," 2020)
Mohammed et al. ("Embracing advanced AI/ML to help investors achieve success: Vanguard Reinforcement Learning for Financial Goal Planning," 2021)
Mulvey et al. ("A Factor- and Goal-Driven Model for Defined Benefit Pensions: Setting Realistic Benefits," 2019)
Muralidhar ("Asset Pricing, Asset Allocation and Risk-Adjusted Performance with Multiple Goals and Agency: The Goals and Risk-based Asset Pricing Model," 2020)
Parker ("Goal-Based Portfolio Optimization," 2016)
Parker ("Portfolio Selection in a Goal-Based Setting," 2016)
Parker ("Achieving Goals While Making an Impact: Balancing Financial Goals with Impact Investing," 2021)

Parker ("Multi-Period Goals-Based Portfolio Optimization," 2021)
Parker ("Allocation of wealth both within and across goals: a practitioner guide," 2020)
Parker ("A Goals-Based Theory of Utility," 2021)
Roncalli ("How Machine Learning Can Improve Portfolio Allocation of Robo-Advisors," 2019)
Roncalli ("Advanced Course in Asset Management," 2021)
Shalett (*An Outcomes-Oriented Approach to Alternatives*, 2015)
Wang et al. ("Portfolio Selection in Goals-Based Wealth Management," 2011)

2.2.2 Reinforcement learning within context of QWIM

List of references:
Aboussalah ("Topological Phase Space Reconstruction For Augmented Real-World Reinforcement Learning," 2021)
Aboussalah et al. ("What is the value of the cross-sectional approach to deep reinforcement learning?" 2022)
Alsabah et al. ("Robo-Advising: Learning Investors Risk Preferences via Portfolio Choices," 2021)
Andre and Coqueret ("Dirichlet policies for reinforced factor portfolios," 2021)
Ardon et al. ("Towards a fully RL-based Market Simulator," 2021)
Bartram et al. ("Machine Learning for Active Portfolio Management," 2021)
Benhamou et al. ("AAMDRL: Augmented Asset Management With Deep Reinforcement Learning," 2021)
Benhamou et al. ("Bridging the Gap Between Markowitz Planning and Deep Reinforcement Learning," 2021)
Benhamou et al. ("Deep Reinforcement Learning (DRL) for Portfolio Allocation," 2021)
Benhamou et al. ("Detecting and Adapting to Crisis Pattern with Context Based Deep Reinforcement Learning," 2021)
Benhamou et al. ("Adaptive learning for financial markets mixing model-based and model-free RL for volatility targeting," 2021)
Benhamou et al. ("Bridging the gap between Markowitz planning and deep reinforcement learning (ICAPS PRL Presentation Slides 2020)," 2021)
Borrageiro et al. ("Reinforcement Learning for Systematic FX Trading," 2021)
Borrageiro et al. ("The Recurrent Reinforcement Learning Crypto Agent," 2022)
Brini and Tantari ("Deep Reinforcement Trading with Predictable Returns," 2022)
Buehler et al. ("Deep hedging," 2019)
Carbonneau ("Deep Hedging of Long-Term Financial Derivatives," 2020)
Carbonneau and Godin ("Equal risk pricing of derivatives with deep hedging," 2021)
Cartea et al. ("Deep Reinforcement Learning for Algorithmic Trading," 2022)
Charpentier et al. ("Reinforcement Learning in Economics and Finance," 2020)
Coache and Jaimungal ("Reinforcement Learning with Dynamic Convex Risk Measures," 2022)
Cong et al. ("AlphaPortfolio: Direct Construction Through Deep Reinforcement Learning and Interpretable AI," 2022)
Das et al. ("Dynamic portfolio allocation in goals-based wealth management," 2020)
Das and Varma ("Dynamic Goals-Based Wealth Management using Reinforcement Learning," 2020)
Das et al. ("Optimal Goals-Based Investment Strategies For Switching Between Bull and Bear Markets," 2021)
Das et al. ("Dynamic optimization for multi-goals wealth management," 2022)
Dixon and Halperin ("G-Learner and GIRL: Goal Based Wealth Management with Reinforcement Learning," 2020)
Dixon and Halperin ("Goal-based wealth management with generative reinforcement learning," 2021)
Dixon et al. (*Machine Learning in Finance: from theory to practice*, 2020)
Dong et al. ("Factor Representation and Decision Making in Stock Markets Using Deep Reinforcement Learning," 2021)
Du et al. ("Deep Reinforcement Learning for Option Replication and Hedging," 2020)
Fleiss et al. ("Deep Reinforcement Learning and Feature Extraction For Constructing Alpha Generating Equity Portfolios," 2021)
Forsyth et al. ("Optimal control of the decumulation of a retirement portfolio with variable spending and dynamic asset allocation," 2021)

Gasperov et al. ("Adaptive rolling window selection for minimum variance portfolio estimation based on reinforcement learning," 2020)

Gašperov et al. ("Reinforcement Learning Approaches to Optimal Market Making," 2021)

Gu ("Deep Reinforcement Learning with Function Properties in Mean Reversion Strategies," 2021)

Guan and Liu ("Explainable Deep Reinforcement Learning for Portfolio Management: An Empirical Approach," 2021)

Hambly et al. ("Recent Advances in Reinforcement Learning in Finance," 2021)

Hieu ("Deep Reinforcement Learning for Stock Portfolio Optimization," 2020)

Hirsa et al. ("Deep reinforcement learning on a multi-asset environment for trading," 2021)

Honchar (*AI for portfolio management: from Markowitz to Reinforcement Learning*, 2019)

Huang and Tanaka ("A Modularized and Scalable Multi-Agent Reinforcement Learning-based System for Financial Portfolio Management," 2021)

Huang et al. ("Deep reinforcement learning for portfolio management," 2022)

Irlam ("Machine learning for retirement planning," 2020)

Irlam ("Multi Scenario Financial Planning via Deep Reinforcement Learning AI," 2020)

Ivanov and D'yakonov ("Modern Deep Reinforcement Learning Algorithms," 2019)

Jaimungal et al. ("Robust Risk-Aware Reinforcement Learning," 2021)

Jaimungal ("Reinforcement learning and stochastic optimisation," 2022)

Jaisson ("Deep differentiable reinforcement learning and optimal trading," 2022)

Janner et al. ("Reinforcement Learning as One Big Sequence Modeling Problem," 2021)

Katongo and Bhattacharyya ("The Use of Deep Reinforcement Learning in Tactical Asset Allocation," 2021)

Liu et al. ("MTV: Visual Analytics for Detecting, Investigating, and Annotating Anomalies in Multivariate Time Series," 2021)

Li et al. ("FinRL-Podracer: High Performance and Scalable Deep Reinforcement Learning for Quantitative Finance," 2021)

Li ("An Automated Portfolio Trading System with Feature Preprocessing and Recurrent Reinforcement Learning," 2021)

Li ("Financial Trading with Feature Preprocessing and Recurrent Reinforcement Learning," 2021)

Li et al. ("FinRL-Podracer: High Performance and Scalable Deep Reinforcement Learning for Quantitative Finance," 2021)

Liao et al. ("Portfolio Allocation with Dynamic Risk Preference Via Reinforcement Learning: Evidence from the Taiwan 50 Index," 2022)

Liu et al. ("FinRL: Deep Reinforcement Learning Framework to Automate Trading in Quantitative Finance," 2021)

Liu et al. ("Goal-Conditioned Reinforcement Learning: Problems and Solutions," 2022)

Ma et al. ("Deep Q-Learning for Trading Cryptocurrency," 2021)

Marzban et al. ("WaveCorr: Correlation-savvy Deep Reinforcement Learning for Portfolio Management," 2021)

Mohammed et al. ("Embracing advanced AI/ML to help investors achieve success: Vanguard Reinforcement Learning for Financial Goal Planning," 2021)

Mosavi et al. ("Comprehensive Review of Deep Reinforcement Learning Methods and Applications in Economics," 2020)

Noguer i Alonso and Srivastava ("Deep Reinforcement Learning for Asset Allocation in US Equities," 2020)

Odermatt et al. ("Deep Reinforcement Learning for Finance and the Efficient Market Hypothesis," 2021)

Pricope ("Deep Reinforcement Learning in Quantitative Algorithmic Trading: A Review," 2021)

Soleymani and Paquet ("Deep Graph Convolutional Reinforcement Learning for Financial Portfolio Management - DeepPocket," 2021)

Sun et al. ("Reinforcement Learning for Quantitative Trading," 2021)

Suri et al. ("TradeR: Practical Deep Hierarchical Reinforcement Learning for Trade Execution," 2021)

Ungari and Benhamou ("Deep Reinforcement Learning for Portfolio Allocation," 2021)

Wang and Yu ("Robo-Advising: Enhancing Investment with Inverse Optimization and Deep Reinforcement Learning," 2021)

Wells and Bednarz ("Explainable AI and Reinforcement Learning—A Systematic Review of Current Approaches and Trends," 2021)

Yang et al. ("Deep Reinforcement Learning for Automated Stock Trading: An Ensemble Strategy," 2020)

Yashaswi ("Deep Reinforcement Learning for Portfolio Optimization using Latent Feature State Space (LFSS) Module," 2021)

2.2.3 Reinforcement learning

List of references:

Amin et al. ("A Survey of Exploration Methods in Reinforcement Learning," 2021)

Bareinboim (*Causal Reinforcement Learning*, 2020)

Chan et al. ("ESG in Factors," 2020)

Cruz Barsce et al. ("Automatic tuning of hyper-parameters of reinforcement learning algorithms using Bayesian optimization with behavioral cloning," 2021)

Dong et al. ("Baconian: A Unified Open source Framework for Model-Based Reinforcement Learning," 2021),

Dulac-Arnold et al. ("An empirical investigation of the challenges of real-world reinforcement learning," 2021)

Fedus et al. ("Hyperbolic Discounting and Learning over Multiple Horizons," 2019)

Francois-Lavet et al. ("An introduction to deep reinforcement learning," 2018)

Garau-Luis et al. ("Evaluating the progress of Deep Reinforcement Learning in the real world: aligning domain-agnostic and domain-specific research," 2021)

Glanois et al. ("A Survey on Interpretable Reinforcement Learning," 2022)

Hamadanian et al. ("Reinforcement Learning in Time-Varying Systems: an Empirical Study," 2022)

Hayes et al. ("A Practical Guide to Multi-Objective Reinforcement Learning and Planning," 2021)

Hoang et al. ("Successor Feature Landmarks for Long-Horizon Goal-Conditioned Reinforcement Learning," 2021)

Ivanov and D'yakonov ("Modern Deep Reinforcement Learning Algorithms," 2019)

Jordan et al. ("Evaluating the Performance of Reinforcement Learning Algorithms," 2020)

Khetarpal et al. ("Towards Continual Reinforcement Learning: A Review and Perspectives," 2021)

Lambert et al. ("Learning Accurate Long-term Dynamics for Model-based Reinforcement Learning," 2021)

Lapan (*Deep Reinforcement Learning Hands-On*, 2020)

Laskin et al. ("Reinforcement Learning with Augmented Data," 2020)

Laskin et al. ("URLB: Unsupervised Reinforcement Learning Benchmark," 2021)

Lazaridis et al. ("Deep Reinforcement Learning: A State-of-the-Art Walkthrough," 2020)

Lehnert and Littman ("Successor Features Combine Elements of Model-Free and Model-based Reinforcement Learning," 2020)

Li et al. ("Anchor: The achieved goal to replace the subgoal for hierarchical reinforcement learning," 2021)

Li et al. ("GenURL: A General Framework for Unsupervised Representation Learning," 2021)

Llorente et al. ("A survey of Monte Carlo methods for noisy and costly densities with application to reinforcement learning," 2021)

Moerland et al. ("Model-based Reinforcement Learning: A Survey," 2021)

Nachum et al. ("Why Does Hierarchy (Sometimes) Work So Well in Reinforcement Learning?" 2019)

Naeem et al. ("A Gentle Introduction to Reinforcement Learning and its Application in Different Fields," 2020)

Nguyen et al. ("Review, Analyze, and Design a Comprehensive Deep Reinforcement Learning Framework," 2021)

Parker-Holder et al. ("Automated Reinforcement Learning (AutoRL): A Survey and Open Problems," 2022)

Plaat ("Deep Reinforcement Learning," 2022)

Plaat et al. ("High-Accuracy Model-Based Reinforcement Learning, a Survey," 2021)

Qian and Yu ("Derivative-Free Reinforcement Learning: A Review," 2021)

Ren et al. ("A Free Lunch from the Noise: Provable and Practical Exploration for Representation Learning," 2021)

Schwarzer et al. ("Pretraining Representations for Data-Efficient Reinforcement Learning," 2021)

Shi et al. ("Self-Supervised Discovering of Causal Features: Towards Interpretable Reinforcement Learning," 2020)

Stapelberg and Malan ("A survey of benchmarking frameworks for reinforcement learning," 2021)

Sutton and Barto (*Reinforcement Learning: An Introduction (Second Edition)*, 2018)

Tarbouriech et al. ("Adaptive Multi-Goal Exploration," 2021)

Wang et al. ("Benchmarking Model-Based Reinforcement Learning," 2019)

Xing ("Learning and Exploiting Multiple Subgoals for Fast Exploration in Hierarchical Reinforcement Learning," 2019)
Yaghmaie and Ljung ("A Crash Course on Reinforcement Learning," 2021)
Zhang and Yu ("Taxonomy of Reinforcement Learning Algorithms," 2020)
Zhang et al. ("On the Importance of Hyperparameter Optimization for Model-based Reinforcement Learning," 2021)
Zhao et al. ("Deep Hierarchical Reinforcement Learning Based Recommendations via Multi-goals Abstraction," 2019)

2.2.4 Deep reinforcement learning

List of references:
Arulkumaran et al. ("Deep reinforcement learning: A brief survey," 2017)
Bertsekas ("Feature-Based Aggregation and Deep Reinforcement Learning: A Survey and Some New Implementations," 2018)
Cai et al. ("A Survey on Deep Reinforcement Learning for Data Processing and Analytics," 2022)
Chakraborty ("Deep Reinforcement Learning in Financial Markets," 2019)
Francois-Lavet et al. ("An introduction to deep reinforcement learning," 2018)
Fujita et al. ("ChainerRL: A Deep Reinforcement Learning Library," 2021)
Heuillet et al. ("Explainability in deep reinforcement learning," 2021)
Ivanov and D'yakonov ("Modern Deep Reinforcement Learning Algorithms," 2019)
Kirk et al. ("A Survey of Generalisation in Deep Reinforcement Learning," 2022)
Liu et al. ("Goal-Conditioned Reinforcement Learning: Problems and Solutions," 2022)
Majid et al. ("Deep Reinforcement Learning Versus Evolution Strategies: A Comparative Survey," 2021)
Pardo ("Tonic: A Deep Reinforcement Learning Library for Fast Prototyping and Benchmarking," 2021)
Rafati and Marcia ("Deep Reinforcement Learning via L-BFGS Optimization," 2018)
Raileanu et al. ("Automatic Data Augmentation for Generalization in Deep Reinforcement Learning," 2021)
Stooke and Abbeel ("Accelerated Methods for Deep Reinforcement Learning," 2018)
Stooke and Abbeel ("rlpyt: A Research Code Base for Deep Reinforcement Learning in PyTorch," 2019)
Sun et al. ("TimeTraveler: Reinforcement Learning for Temporal Knowledge Graph Forecasting," 2021)
Weng et al. ("Tianshou: a Highly Modularized Deep Reinforcement Learning Library," 2022)
Xiong et al. ("Practical Deep Reinforcement Learning Approach for Stock Trading," 2018)
Yang et al. ("Exploration in Deep Reinforcement Learning: A Comprehensive Survey," 2022)
Zhang et al. ("A Study on Overfitting in Deep Reinforcement Learning," 2018)
Zhu et al. ("Transfer Learning in Deep Reinforcement Learning: A Survey," 2021)

2.2.5 Inverse reinforcement learning

List of references:
Abbeel and Ng ("Inverse Reinforcement Learning," 2017)
Arora and Doshi ("A Survey of Inverse Reinforcement Learning: Challenges, Methods and Progress," 2018)
Brown et al. ("Risk-Aware Active Inverse Reinforcement Learning," 2019)
Brown and Niekum ("Machine teaching for inverse reinforcement learning: algorithms and applications," 2019)
Castro et al. ("Inverse Reinforcement Learning with Multiple Ranked Experts," 2019)
Freymuth et al. ("Versatile Inverse Reinforcement Learning via Cumulative Rewards," 2021)
Fu et al. ("Evaluating Strategic Structures in Multi-Agent Inverse Reinforcement Learning," 2021)
Halperin ("The QLBS Q-Learner goes NuQLear: fitted Q iteration, inverse RL, and option portfolios," 2019)
Halperin and Feldshteyn ("Market Self-Learning of Signals, Impact and Optimal Trading: Invisible Hand Inference with Free Energy (Or, How We Learned to Stop Worrying and Love Bounded Rationality)," 2018)
Krishnan et al. ("HIRL: Hierarchical Inverse Reinforcement Learning for Long-Horizon Tasks with Delayed Rewards," 2016)

2.2.6 Testing and comparison procedures for investment portfolios

References:

Adcock et al. ("Portfolio Performance Measurement: Monotonicity with Respect to the Sharpe Ratio and Multivariate Tests of Correlation," 2017)

Arnott et al. ("A backtesting protocol in the era of machine learning," 2019)

Bailey et al. ("Stock Portfolio Design and Backtest Overfitting," 2017)

Bessler and Wolff ("Portfolio Optimization with Industry Return Prediction Models," 2017)

Bessler et al. ("Multi-asset portfolio optimization and out-of-sample performance: an evaluation of Black Litterman, mean-variance, and naive diversification approaches," 2017)

Bjerring et al. ("Feature selection for portfolio optimization," 2017)

Bruni et al. ("On exact and approximate stochastic dominance strategies for portfolio selection," 2017)

Bruni et al. ("Real-world datasets for portfolio selection and solutions of some stochastic dominance portfolio models," 2016)

Bryzgalova et al. ("Bayesian solutions for the factor zoo: we just ran two quadrillion models," 2021)

Cesarone et al. ("On the stability of portfolio selection models," 2019)

Cesarone et al. ("Why Small Portfolios Are Preferable and How to Choose Them," 2018)

Chaudhuri and Lo ("Dynamic Alpha: A Spectral Decomposition of Investment Performance Across Time Horizons," 2019)

Diris et al. ("Long-Term Strategic Asset Allocation: An Out-of-Sample Evaluation," 2015)

Fabozzi and Lopez de Prado ("Being Honest in Backtest Reporting: A Template for Disclosing Multiple Tests," 2018)

Greiner and Stoyanov ("Portfolio scoring by expected risk premium," 2019)

Guidolin et al. ("Portfolio performance of linear SDF models: an out-of-sample assessment," 2018)

Guo ("A Statistical Response to Challenges in Vast Portfolio Selection," 2019)

Guo et al. ("When Does The 1/N Rule Work?" 2019)

Haley ("K-fold cross validation performance comparisons of six naive portfolio selection rules: how naive can you be and still have successful out-of-sample portfolio performance?" 2017)

Harvey et al. ("An Evaluation of Alternative Multiple Testing Methods for Finance Applications," 2020)

Hens et al. ("Escaping the backtesting illusion," 2020)

Hsu et al. (*Do Cross-Sectional Stock Return Predictors Pass the Test without Data-Snooping Bias?* 2017)

Hsu et al. ("Asset allocation strategies, data snooping, and the 1 / N rule," 2018)

Huang and Yu ("A new procedure for resampled portfolio with shrinkaged covariance matrix," 2020)

Hwang et al. ("Naive versus optimal diversification: Tail risk and performance," 2018)

Ielpo et al. (*Engineering Investment Process: Making Value Creation Repeatable*, 2017)

Jaeger et al. ("Understanding machine learning for diversified portfolio construction by explainable AI," 2020)

Kazak and Pohlmeier ("Testing out-of-sample portfolio performance," 2019)

Kazak and Pohlmeier (*Portfolio Pretesting with Machine Learning*, 2020)

Kuntz ("Portfolio Strategies with Classical and Alternative Benchmarks," 2018)

Lohre et al. ("Hierarchical Risk Parity: Accounting for Tail Dependencies in Multi-asset Multi-factor Allocations," 2020)

Lopez de Prado ("A Data Science Solution to the Multiple-Testing Crisis in Financial Research," 2019)

Lopez de Prado and Lewis ("Detection of false investment strategies using unsupervised learning methods," 2019)

Malavasi et al. ("Second order of stochastic dominance efficiency vs mean variance efficiency," 2021)

Mooney et al. ("Dynamic Regime Strategy for Stress Testing and Optimizing Institutional Investor Portfolios," 2020)

Platanakis et al. ("Horses for Courses: Mean-Variance for Asset Allocation and 1/N for Stock Selection," 2021)

Radovanov and Marcikic ("Testing The Performance Of The Investment Portfolio Using Block Bootstrap Method," 2014)

Rebonato ("A financially justifiable and practically implementable approach to coherent stress testing," 2019)

Schumann ("Backtesting," 2019)

Seymour et al. ("Dynamic portfolio management strategies: A framework for historical analysis," 2018)

Suhonen et al. ("Quantifying Backtest Overfitting in Alternative Beta Strategies," 2017)

Taljaard and Maré ("Why has the equal weight portfolio underperformed and what can we do about it?" 2021)

Tayali ("A novel backtesting methodology for clustering in mean–variance portfolio optimization," 2020)
Traccucci et al. ("A Triptych Approach for Reverse Stress Testing of Complex Portfolios," 2019)
Valentine et al. ("Beyond p values: utilizing multiple methods to evaluate evidence," 2019)
Vincent et al. ("Analyzing the Performance of Multifactor Investment Strategies under a Multiple Testing Framework," 2018)
Vovk and Wang ("True and false discoveries with e-values," 2020)
Vovk and Wang ("E-values: Calibration, combination, and applications," 2021)
Wiecki et al. ("All That Glitters Is Not Gold: Comparing Backtest and Out-of-Sample Performance on a Large Cohort of Trading Algorithms," 2016)
Yu ("Comparing Classical Portfolio Optimization and Robust Portfolio Optimization on Black Swan Events," 2021)
Yuan and Zhou ("Why Naive 1/N Diversification Is Not So Naive, and How to Beat It?" 2022)
Zhang et al. ("DoubleEnsemble: A New Ensemble Method Based on Sample Reweighting and Feature Selection for Financial Data Analysis," 2020)
Zhang et al. ("Information Coefficient as a Performance Measure of Stock Selection Models," 2020)
Zhang et al. ("Deep Learning for Portfolio Optimization," 2020)

2.2.7 Software implementations and frameworks

List of references:
Bargiacchi et al. ("AI-Toolbox: A C++ library for Reinforcement Learning and Planning (with Python Bindings)," 2020)
Beysolow II (*Applied Reinforcement Learning with Python: With OpenAI Gym, Tensorflow, and Keras*, 2019)
Brockman et al. ("OpenAI Gym," 2016)
Bou and De Fabritiis ("PyTorchRL: Modular and Distributed Reinforcement Learning in PyTorch," 2021)
Castro et al. ("Dopamine: A Research Framework for Deep Reinforcement Learning," 2018)
Dong et al. ("Baconian: A Unified Open source Framework for Model-Based Reinforcement Learning," 2021)
D'Eramo et al. ("MushroomRL: Simplifying Reinforcement Learning Research," 2021)
Fujita et al. ("ChainerRL: A Deep Reinforcement Learning Library," 2021)
Hoffman et al. ("Acme: A Research Framework for Distributed Reinforcement Learning," 2020)
Hulbert et al. ("EasyRL: A Simple and Extensible Reinforcement Learning Framework," 2020)
Kolesnikov and Hrinchuk ("Catalyst.RL: A Distributed Framework for Reproducible RL Research," 2019)
Kuttler et al. ("TorchBeast: A PyTorch Platform for Distributed RL," 2019)
Li et al. ("RL: Generic reinforcement learning codebase in TensorFlow," 2019)
Liu et al. ("FinRL: Deep Reinforcement Learning Framework to Automate Trading in Quantitative Finance," 2021)
Liu et al. ("Goal-Conditioned Reinforcement Learning: Problems and Solutions," 2022)
Loon et al. ("SLM Lab: A Comprehensive Benchmark and Modular Software Framework for Reproducible Deep Reinforcement Learning," 2019)
Nguyen et al. ("Review, Analyze, and Design a Comprehensive Deep Reinforcement Learning Framework," 2021)
Pardo ("Tonic: A Deep Reinforcement Learning Library for Fast Prototyping and Benchmarking," 2021)
Pineda et al. ("MBRL-Lib: A Modular Library for Model-based Reinforcement Learning," 2021)
Pretorius et al. ("Mava: a research framework for distributed multi-agent reinforcement learning," 2021)
Prollochs and Feuerriegel ("ReinforcementLearning: A Package to Perform Model-Free Reinforcement Learning in R," 2019)
Staley et al. ("The AI Arena: A Framework for Distributed Multi-Agent Reinforcement Learning," 2021)
Terry et al. ("PettingZoo: Gym for Multi-Agent Reinforcement Learning," 2021)
Weng et al. ("Tianshou: a Highly Modularized Deep Reinforcement Learning Library," 2022)
Xu and Chen ("A Validation Tool for Designing Reinforcement Learning Environments," 2021)

3 Practical details for the project

The main purpose of the project described in this document is to provide exposure to students on important (and interesting) practical topics in quantitative wealth and investment management QWIM.

The level of complexity depends on the number of hours designated for the project. For example, 50-60 hours for a regular project, and 100-120 hours for a thesis/capstone project. Upon request, the scope (and the corresponding number if hours) of any given project can be extended.

The students would work on the project as part of a team (usually with 2-3 students).

All QWIM projects were selected such that the students' efforts have a good chance of producing results relevant to the industry, and at least as good as the results presented in the QWIM literature. Thus for each project we may consider (on an optional basis, based primarily on students' preference) to submit a corresponding article to journals widely followed by practitioners and academics in investment and wealth management, with participating students included as the leading coauthors of the submitted article.

The main challenge for each project is to identify the criteria for what would be considered **"good enough"**. Similar to projects in the industry, the meaning of "good enough" is based on a combination of comprehensive literature review, discussions within team and with me (and/or my colleagues) and analysis of results. Emphasis is placed on creating a narrative (with the aid of an interactive visualizer) for convincing the intended audience that what was done in the project delivers **"good enough"** outcome.

3.1 Interaction with students

For each project I would make myself available for meetings on a weekly basis (for discussions and guidance). Some of my colleagues have also expressed interest to participate in such meetings. Due to our work schedule and deliverables, most of the discussions will have to be scheduled outisde working hours (in weekends or evenings). The meetings will take place through video conferencing such as WebEx, Zoom, Google Meet, Microsoft Teams, etc., based on the team's preference. If the meetings are through WebEx, I would provide a link, while the student team will provide a link for any other video conferencing tool.

The students working on a given project can also send questions by email (my recommendation is to aggregate the questions from team members into an email sent once a day). We aim to provide answers within 1-2 days, either by email or through a phone discussion.

3.2 Data

Due to compliance reasons all projects would be based on publicly available, non-proprietary and non-confidential data (indices, ETFs, mutual funds, etc.). Since neither I nor my team are allowed to provide these datasets, I can only provide a list of suggested datasets. This list is included in a later section named Practical Info.

The datasets were selected to have the following features:

- be good proxies for most representative asset and subasset classes
- to be widely available
- to be as liquid as possible
- to have daily granularity
- to encompass periods with as many market regimes as possibles (most proposed daily datasets are from 1990 or 1991)
- time series have "nicer" statistical properties compared to time series of, say, individual stocks or bonds

3.3 Private GitHub repository for the QWIM project

The team will create a private GitHub repository, which will store relevant project materials, including codes. The team will use Git Desktop application as source control repository linked to the GitHub repository.

3.4 Deliverables

The project deliverables include literature survey, numerical results, analysis and visualization. For each project references will be provided for a comprehensive literature survey, and students are encouraged to identify additional relevant literature. Regarding the implementation, the project will primarily use existing codes:

- Python and R packages from official repositories (PyPi for Python and CRAN for R)
- machine learning platforms such as TensorFlow, PyTorch, CNTK, Chainer, mlr3, H20, PlaidML, mlpack, etc.
- implementations of articles through codes available in repositories such as GitHub, BitBucket, GitLab, etc.

Visualization of data and results visualization will be interactive and it will be based on Shiny R framework; to reduce programming effort, a template for such a Shiny visualizer will be provided in the team private GitHub repository.

The deliverables are:

- written report including literature survey and numerical results
- interactive visualizer (most likely Shiny-based visualizer using R and Python packages)
- (optional) presentation slides, and/or RMarkdown presentation, and/or Jupyter Notebook(s)

3.5 (Optional) Article submission to leading journals

On an optional basis (based primarily on students' preference), a version of the report can be prepared for submision to leading journals such as Journal of Financial Data Science, Journal of Portfolio Management, Journal of Asset Management, Journal of Investment Strategies, Quantitative Finance, Journal of Wealth Management, Journal of Investing, Journal of Machine Learning in Finance, etc.

4 Project tasks and timelines

For each project the main tasks are:

1) literature review

2) decide on the appropriate metrics and quantitative methods within context of "good enough" for the project

3) write-up summary of literature review: methods, metrics, testing procedures

4) identification of Python and/or R packages which are most appropriate for the selected methods and metrics

5) code design to decide on main code components

6) implementation of code components

7) interactive visualization of numerical results

8) project report containing description of methods, metrics, and tests, and analysis of results.

4.1 Suggested timelines for project tasks

The table below suggests a timeline for the project tasks and the corresponding percentages of project time:

Table 1: Suggested timeline for project tasks

Task ID	Task Name	Percentage of project time
1	Literature review	15%
2	Identification of "good enough" metrics and quantitative methods	5%
3	Write-up of summary of literature review	5%
4	Identification of appropriate packages in Python and/or R	10%
5	Code design for main components of project coding framework	5%
6	Implementation of coding framework and components	40%
7	Interactive visualizer using the provided Shiny template	10%
8	Project report and presentation	10%

4.2 Literature review

The first task is based on a comprehensive literature survey, included in the preliminary document of the project. Students are encouraged to identify additional relevant literature.

This task may be the most important of the project, since it provides an overview of what was done, what works well and less well, and what appear to be the most promising avenues to complete the project.

Emphasis is placed on information contained in the Main References; the other References would be considered only if time permits and the team is interested in exploring other avenues.

When reading the literature, there are 4 main directions to consider:

1) methods

2) metrics to assess the performance/robustness of the methods

3) testing procedures

4) numerical results

The primary focus would be on the the references included in "Main References" subsection of the document for your QWIM project. Then, to the extent there is time, to consider the other references included in the project document. In the same time, you are encouraged to identify other references that might be considered "Main references", and to share those references with me for discussion.

For the articles in Main References category, the suggested approach would be the following:

- For each article focus primarily on Abstract, Conclusion, and Numerical Results
- Do this for all articles considered to be Main References, such that you gain a high-level understanding of what is currently done in the literature
- Select the metrics that you may want to use in order to quantify the meaning of "good enough" for the project.
- Select the quantitative methods which appear to be most likely to be "good enough" for the project.
- Perform a "deeper dive" into the articles containing the approaches you consider the most promising,

For the articles which are not in "Main References" category, read Abstract, Conclusion, and Numerical Results, to see whether any of those articles might need to be considered for inclusion in your summary.

4.3 Write-up summary of literature review

The write-up summary summarizes the methods, metrics, testing procedures, and numerical results identified during the literature review. The write-up could also be incorporated within reports and/or presentations for the QWIM project.

4.4 Identification of appropriate Python and/or R packages

Based on the literature review and on diiscussions, we identify the most potentially useful methods, metrics and testing procedures. Then wee identify the most appropriate implementations of the selected methods and metrics.

The primary sources of implementatins are existing codes from:

- Python and R packages from official repositories (PyPi for Python and CRAN for R)
- machine learning platforms such as TensorFlow, PyTorch, CNTK, Chainer, mlr3, H20, PlaidML, mlpack, etc.
- Codes available in repositories such as GitHub, BitBucket, GitLab, etc.

4.5 Code design

An important task is to have a code design session to decide in advance on the main code components, which are meant to be modular and encapsulated, such that the entire team can work on the codes.

Examples of such main components include extracting data, calculate metrics for the considered procedures, portfolio metrics, performing tests, construct interactive visualizer, etc.

The code design procedure consists of:

1) visual display of major components of the coding framework
2) UML diagrams for each of the components.

The Appendix contains an illustrative example within context of a QWIM project on forecasting of financial time series. The first figure shows the major components, while the second figure shows UML diagrams of those components (the names of data members and methods are currently generic, and one would need to change them to appropriate names)

While these figures were obtained through Microsoft Visio using a code design file (.vsd file), there are other software tools (either online or installed locally) which can be used to create such code design diagrams. NOTE: if you have access to Microsoft Visio and you want to use it for code design diagrams, you can ask me for the .vsd file which was exported into the PDF from which I have extracted the snapshots.

List of software tools for code design diagrams, which are either free (open source) or have a free type of account

- Modelio (either desktop version or online version)
- LucidChart (online)
- draw.io (either desktop version or online version, now called app.diagrams.net)

- Visual Paradigm (online)
- UMLet (either desktop or online version)
- Curated list of UML tools – 2019 edition
- Top online UML modeling tools in 2019

4.6 Implementation of coding framework and components

The implementation is done using identified packages or codes, in Python and/or R. The project will primarily use existing codes:

- Python and R packages from official repositories (PyPi for Python and CRAN for R)
- machine learning platforms such as TensorFlow, PyTorch, CNTK, Chainer, mlr3, H20, PlaidML, mlpack, etc.
- implementations of articles through codes available in repositories such as GitHub, BitBucket, GitLab, etc.

4.7 Interactive visualizer

While visualization of data and numerical results can be done through various tools (including Jupyter notebooks or Dash in Python), my recommendation is to consider an interactive visualizer based on Shiny framework in R. A template for the Shiny visualizer will be provided in the private GitHub repository set up by the team for the project.

Some information about Shiny:

- Shiny from RStudio: tutorials and gallery
- Why R Shiny Trumps UI and JavaScript Based Visualization Tools
- Shiny's Holy Grail: Interactivity with reproducibility

4.8 Project report and presentation

The report containing description of methods, metrics, and tests, and analysis of results.

While the report can be written using various tools (including Microsoft Word), my recommendation is to use LyX to write both the project report and the project presentation. Two LyX templates for creating reports and, respectively, presentations will be provided in the private GitHub repository set up by the team for the project.

Some information about Shiny:

- LyX features
- LyX tutorial with PDF here
- LyX Tutorial video Part One and Part Two
- LyX tutorial video Part One and Part Two and Part Three and Part Four
- Introduction to LyX
- Insert figures in LyX
- Essentials of LyX

5 Design and implementation for the project codes

This section describes a possible approach for the design process and for the implementation (folder structure) of the project. This approach is presented only to exemplify how it could be done. Each student team has freedom to consider their own design process.

Design and implementation would be based on following principles:

- coding framework is Python based, with calls to functions available in existing Python and R packages
- leverage common components (such as data input/output, numerical methods, time series, testing, interactive visualization and reporting, etc.)
- reusability
- incorporate best practices in coding and numerical implementations
- use, augment and enhance (to largest extent possible) existing Python and R packages and codes

5.1 Visualize project workflow and coding framework

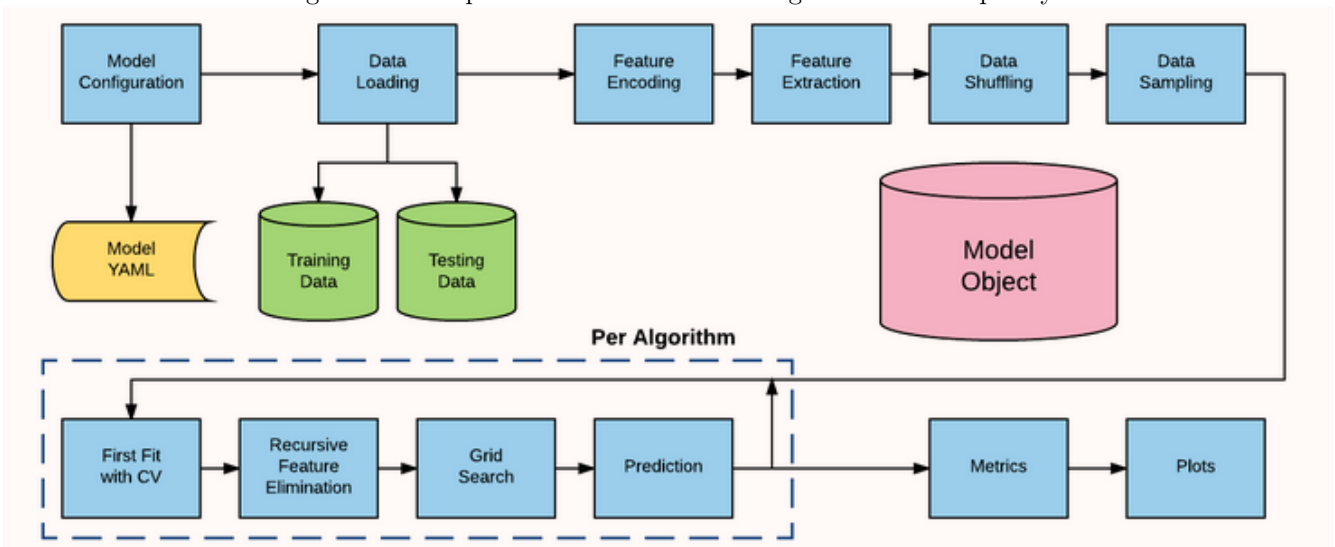
The starting point is to visualize the project workflow in terms of major components, and then to design the code framework.

The code design procedure consists of:

1) visual display of major components of the coding framework
2) UML diagrams for each of the components.

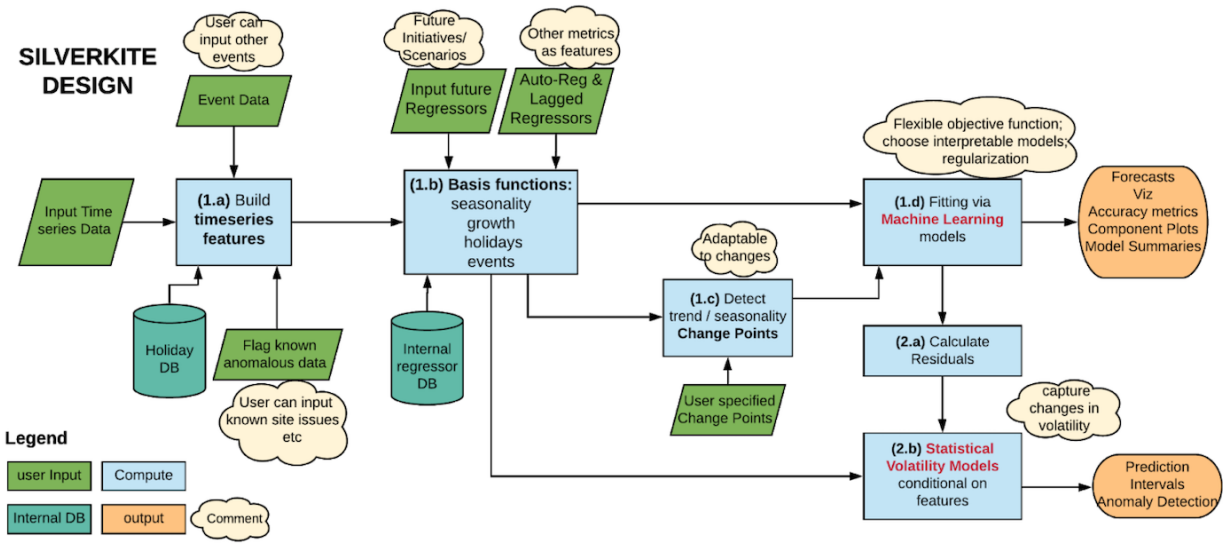
We present examples below for projects including time series forecasting and analysis, machine learning for portfolio construction, etc.

Figure 2: Examples of architecture of coding framework: AlphaPy



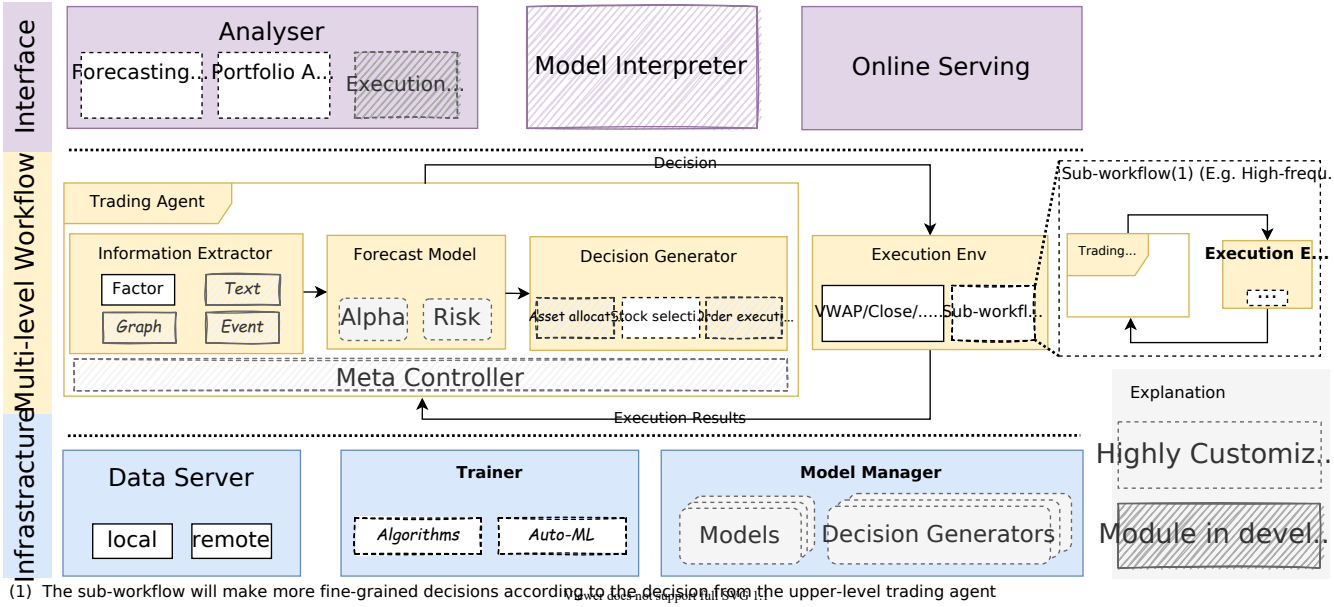
Source: AlphaPy

Figure 3: Examples of architecture of coding framework: Greykite



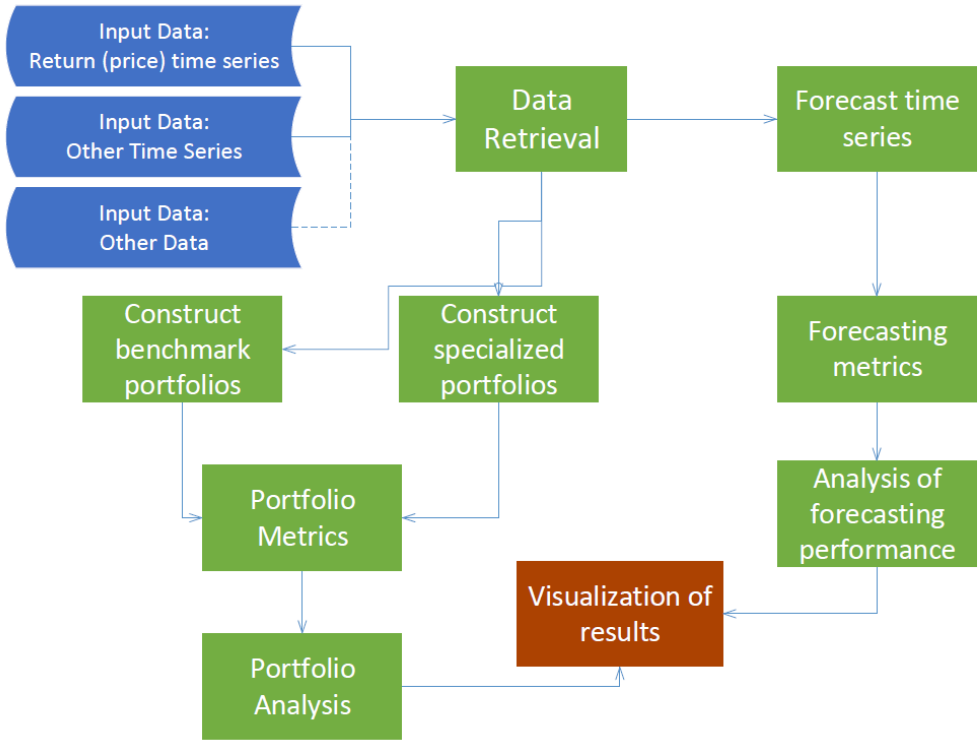
Source: Geykite

Figure 4: QLib Framework



(1) The sub-workflow will make more fine-grained decisions according to the decision from the upper-level trading agent

Figure 5: Examples of major components of coding framework (top) and UML diagrams (bottom)



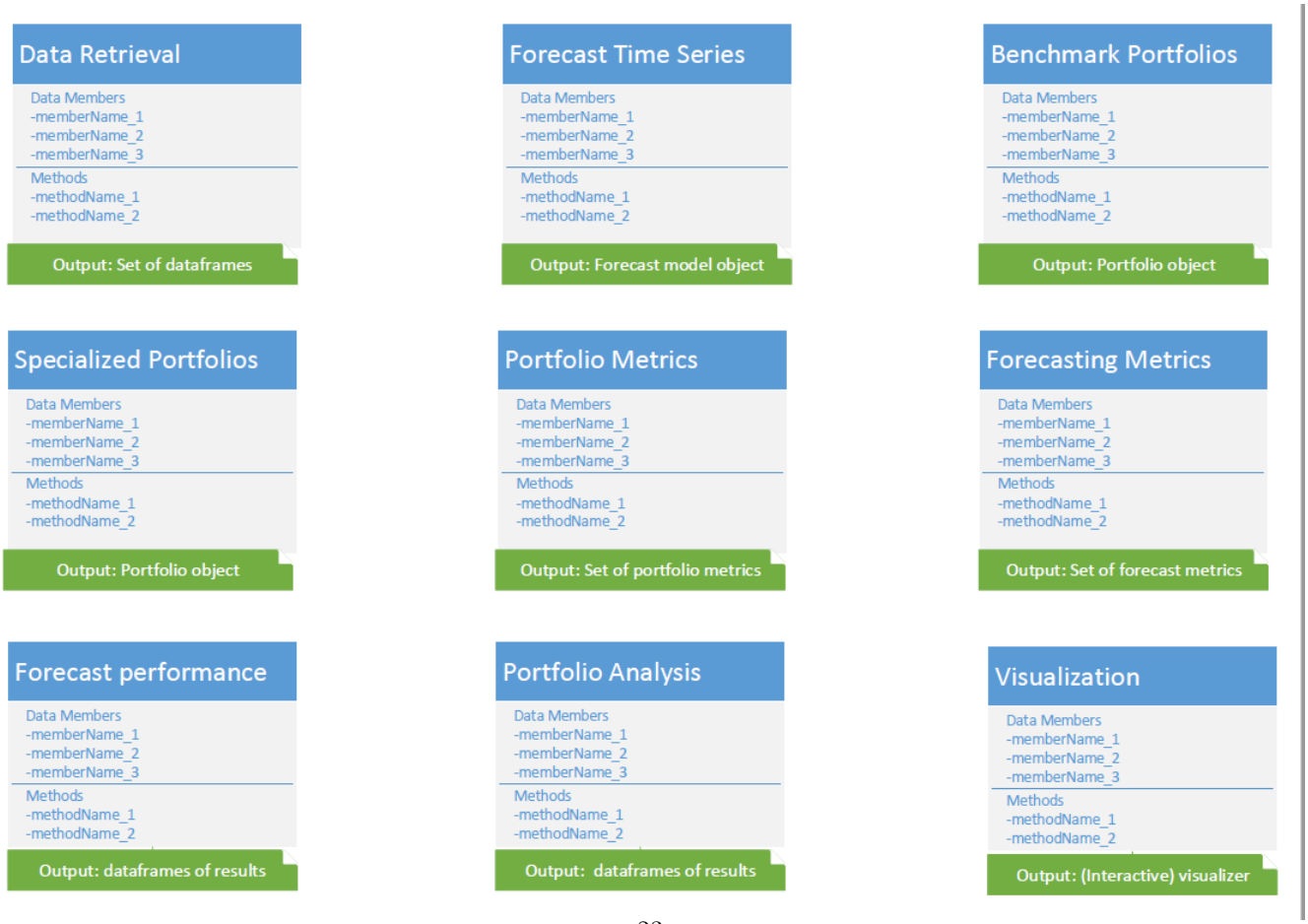
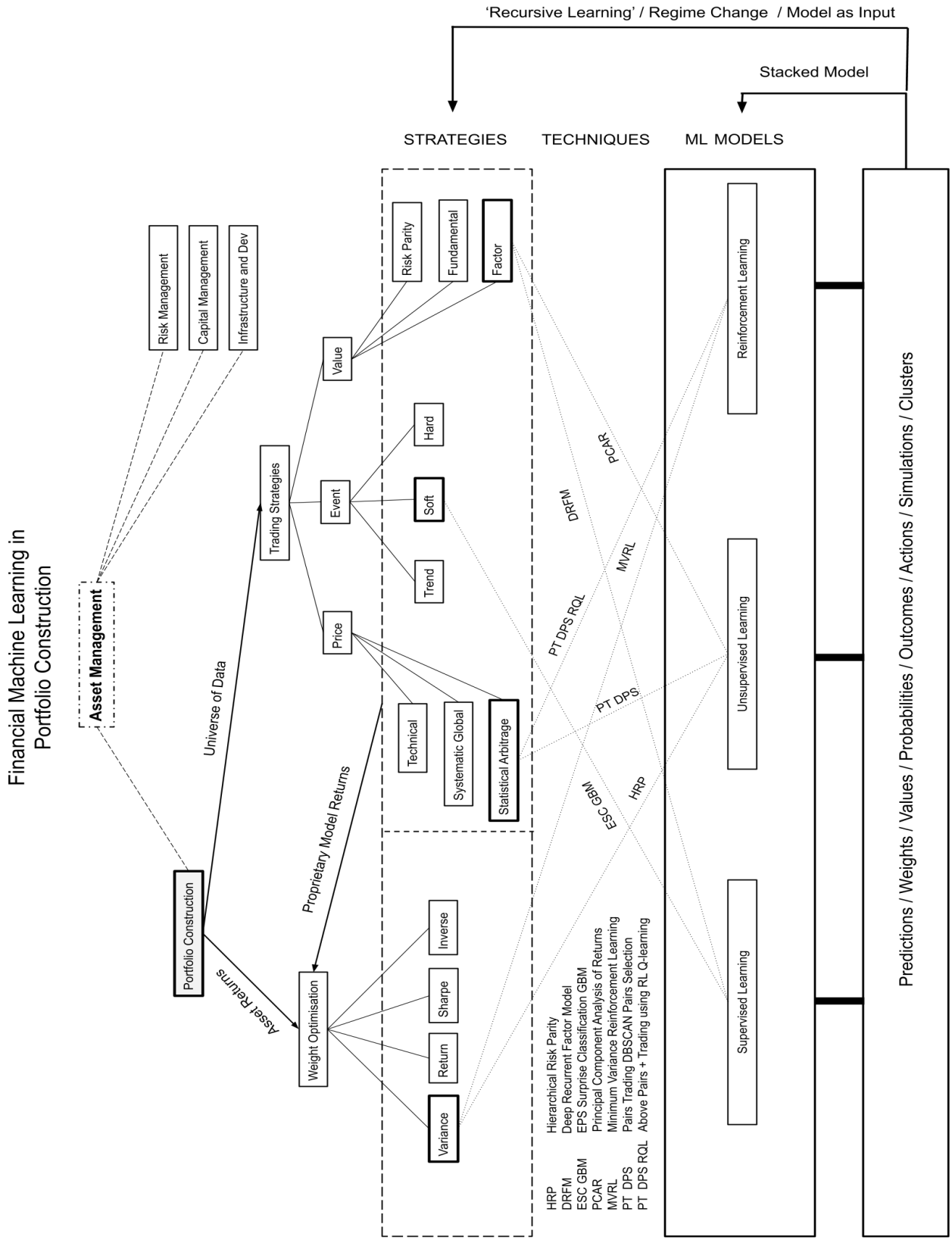


Figure 6: Financial Machine Learning in Portfolio Construction



Source: Machine Learning in Asset Management

5.2 Representative examples of Python libraries with well designed folder structure

List of Python libraries

- QLib is a AI-oriented quantitative investment platform in Python developed by Microsoft researchers
- GluonTS is a Python library deveoped by Amazon researchers for probabilistic time series modeling
- sktime is a unified framework for machine learning with time series, developed by researchers at Alan Turing Institute for data science and artificial intelligence.
- darts is a Python library for easy manipulation and forecasting of time series, developed by researchers at Unit8 AI and data analytics company.
- Kats is a Python library developed by Facebook researchers to analyze time series data.
- Kats is a Python library developed by Tinkoff AI researchers to analyze time series data.
- MLFinLab (Machine Learning Financial Laboratory) is a Python library developed by researchers at Hudson & Thames.

6 Practical Info

6.1 Recommended software tools

The sections below describe the recommended software tools, including corresponding versions/subversions, tutorials and details

6.1.1 Python

The recommended versions are:

- Python version 3.8 (subversion Python 3.8.10 or 3.8.15)
- Python version 3.9 (subversion Python 3.9.10 or 3.9.15)
- Python version 3.10 (latest subversion, currently Python 3.10.8)

There are also relevant Python packages, identified while you are working the project. As a starting point you can consider the packages included in section on Potentially useful Python and R packages.

6.1.2 R

The recommended versions are:

- R version 4.2 (recommended is latest subversion, currently R 4.2.2)
- R version 3.6 (subversion R 3.6.3)

On Windows computers you also need to install Rtools to build R packages from source through compilation, since not all packages have associated Windows binaries.

There are also relevant R packages, identified while you are working the project. As a starting point you can consider the packages included in section on Potentially useful Python and R packages.

6.1.3 R IDE

The recommended R IDE is RStudio Desktop Open Source

- latest version, currently 2022.07.2+576

6.1.4 Python IDE

The recommended Python IDE is Visual Studio Code VSC

- latest version, currently VSC 1.73

Then add Python extension and other Visual Studio Code extensions from Visual Studio MarketPlace.

Note: Upon request I can provide a list of potentially useful VSC extensions, which can be installed on your computer (see for example link)

6.1.5 Bibliography Manager

The recomemnded bibliography manager is JabRef

- latest version: version 5.7, or
- latest development version from link

I can provide you with a bibliography file which contains all refeernces mentioned in the project description, This file (of extension bib) can be viewed and edited with JabRef, and used together with LyX to write your project related documents (report, presentation, etc.).

You can easily add/delete/edit this bib file using JabRef.

There are video tutorials on using JabRef: link 1, link 2, link 3.

In addition to these video tutorials, I can also have a video online session, to provide an overview and answer your questions on using LyX and JabRef. This online session (through Google Meet Google Meet) can be recorded and shared with you afterwards.

6.1.6 Document processor

The recommended document processor is LyX, which is a document processor that encourages an approach to writing based on the structure of your documents (WYSIWYM) and not simply their appearance (WYSIWYG).

LyX combines the power and flexibility of TeX/LaTeX with the ease of use of a graphical interface. It shoudl be emohasized that you do not need to know/learn LaTeX in order to tuse LyX.

To install LyX, you need to download and install first TeXLive (see link), which is a packaged distribution of LaTeX and associated packages

Then install LyX using installers, making sure that you are pointing to location of installed TeXLive when asked for a LaTeX distribution during the run of LyX installer.

Recommended versions:

- TexLive (recommended is latest version, currently TeXLive 2022)
- LyX (recommended is latest subversion, currently LyX 2.3.6.1)

There are video tutorials (link 1 and link 2).

In addition to these video tutorials, I can also have a video online session, to provide an overview and answer your questions on using LyX and JabRef. This online session (through Google Meet Google Meet) can be recorded and shared with you afterwards.

6.1.7 Source control manager

The recommended source control manager is GitHub desktop, which can be used in conjunction with thr private GitHub repository that each student team will create for their project

- latest subversion, currently GitHub Desktop 3.1.2

6.1.8 File editor

The recommended file editor is Notepad++

- latest subversion (currently Notepad++ 8.4.7) with various plugins (see list of available plugins at link 1 and link 2)

6.1.9 Runtime libraries

Many Python and R packages require runtime libraries such as Microsoft Visual C++ Redistributable

- latest version, currently Microsoft Visual C++ Redistributable 64-bit for Visual Studio 2015, 2017, 2019, and 2022

6.2 Recommended datasets

The datasets below were selected to have the following features:

- to be representative proxies for most relevant asset and subasset classes
- to be widely available

- to be as liquid as possible
- to have daily granularity
- to encompass time periods containing as many market regimes as possibles (under this consideration, the recommended daily datasets start from early 1990s)
- to have "nicer" statistical properties, which will make modeling easier (under this consideration, time series of recommended financial indices have "nicer" statistical properties compared to time series of individual stocks or bonds)

The following datasets are suggested

Table 2: Daily data sets

Name	Description	Name	Description
BCOMTR	Bloomberg Commodity Index Total Return	RU20VATR	iShares Russell 2000 Value ETF
HFRIFWI	HFRI Fund Weighted Composite Index	RUMCINTR	iShares Russell Mid-Cap ETF
LBUSTRUU	Bloomberg Barclays US Aggregate Bond Index	RUMRINTR	iShares Micro-Cap ETF
LG30TRUU	Bloomberg Barclays Global High Yield Total Return Index Value Unhedge	RUTPINTR	iShares Russell Top 200 ETF
LMBITR	Bloomberg Barclays Municipal Bond Index Total Return Index Value Unhedged USD	S5COND	S&P 500 Consumer Discretionary Index
NDDUE15X	Amundi MSCI Europe Ex UK Ucits ETF Dr	S5CONS	S&P 500 Consumer Staples Index
NDDUJN	MSCI Japan Index	S5ENRS	S&P 500 Energy Index
NDDUNA	iShares MSCI North America UCITS ETF	S5FINL	S&P 500 Financials Sector GICS Level 1 Index
NDDUPXJ	MSCI Pacific ex Japan UCITS ETF	S5HLTH	S&P 500 Health Care Index
NDDUUK	iShares MSCI UK ETF	S5INDU	S&P 500 Industrials Index
NDDUWXUS	MSCI World ex USA total net return	S5INFT	S&P 500 Information Technology Index
NDUEEGF	SPDR MSCI Emerging Markets UCITS ETF	S5MATR	S&P 500 Materials Index
RU10GRTR	iShares Russell 1000 Growth ETF	S5RLST	S&P 500 Real Estate Index
RU10VATR	iShares Russell 1000 Value ETF	S5TELS	S&P 500 Communication Services Index
RU20GRTR	iShares Russell 2000 Growth ETF	S5UTIL	S&P 500 Utilities Index
RU20INTR	Russell 2000 Total Return	SPXT	Proshares S&P 500 EX Technology ETF

Table 3: Monthly data sets

Name	Description	Name	Description
IBXXSHY1	iShares 0-5 Year High Yield Corporate Bond ETF	M2USEV	MSCI USA Enhanced Value Index
IDCT20RT	ICE U.S. Treasury 20+ Year Bond Total Return Index	M2USRWGT	MSCI USA Risk Weighted Index
LBUSTRUU	Bloomberg Barclays US Agg Total Return Value Unhedged USD	M2USSNQ	MSCI USA Sector Neutral Quality Index
LC07TRUU	Bloomberg Barclays U.S. Universal Total Return Index Value Unhedged	MID	S&P 400 Mid Cap Index index
LD01TRUU	Bloomberg Barclays 1-3 Yr Credit Total Return Index Value Unhedged US	MXEA	MSCI EAFE Index
LT01TRUU	Bloomberg Barclays US Treasury 1-3 Year Index	MXEF	MSCI Emerging Markets Index
LUICTRUU	Bloomberg Barclays U.S. Intermediate Credit Total Return Index	MXUSMVOL	MSCI USA Minimum Volatility Index
LULCTRUU	Bloomberg Barclays U.S. Long Credit Index	MXWD	MSCI All Countries World Index
M1CXBRU	iShares Core MSCI International Developed Markets ETF	MXWOUIM	MSCI All Countries World Index
M1USMVOL	MSCI USA Minimum Volatility (USD) Index	NDDUUS	MSCI Daily Total Return Net USA USD Index
M2US000$	iShares Edge MSCI USA Momentum Factor ETF	SPX	S&P 500 Index

7 Potentially useful Python and R software implementations: packages, codes and frameworks

7.1 Collections and repositories of resources

For Data Science, Numerical Methods/ Algorithms, Programming

List of links:

- Data Science CheatSheet
- professional-programming: collection of full-stack resources for programmers.

For Python

List of links:

- Awesome Python
- Awesome Python frameworks, libraries, software and resources
- Best of Python
- Curated list of Python frameworks, libraries, software and resources
- Pythonidae: Curated decibans of scientific programming resources in Python
- Ranked list of Python open-source Machine Learning libraries and tools
- Ranked list of Python open-source libraries and tools
- Ranked list of Python developer tools and libraries
- Time series: analytics, statistics, machine learning, frameworks and databases
- Time series Python packages

For R

List of links:

- Available CRAN Packages By Date of Publication
- CRAN Task Views

7.2 Connection between Python and R codes

List of links:

- arrow: R interface to 'Apache' 'Arrow', a cross-language for accelerated data interchange in-memory data
- pyarrow: Python library for Apache Arrow
- reticulate: R Interface to 'Python' modules, classes, and functions
- rpy2: Python interface to the R language
- rpy2-arrow: Share Apache Arrow datasets between Python and R
- R Extension for Visual Studio Code

7.3 Anomaly detection and data outliers

Collections of resources

List of links:

- Anomaly detection related books, papers, videos, and toolboxes

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- adtk: Python toolkit for rule-based/unsupervised anomaly detection in time series
- Anomaly Detection Learning Resources
- Awesome anomaly detection resources
- Curve: time series data anomaly detection by Baidu
- kats: kit to analyze time series data by Facebook
- luminaire: ML driven package by Zillow for monitoring time series data
- Merlion: A Machine Learning Framework for Time Series Intelligence by SalesForce
- PyGOD: Graph Outlier Detection (Anomaly Detection)
- PyOD: Python Toolbox for Scalable Outlier Detection (Anomaly Detection)
- PyODDS: An End-to-end Outlier Detection System
- ruptures: change point detection in Python
- seriesdistancematrix: implements the Series Distance Matrix framework, a flexible component-based framework that bundles various Matrix Profile related techniques
- Software tools and datasets for anomaly detection on time series data
- Tools and datasets for anomaly detection on time-series data.
- tsad: Time Series Forecasting and Anomaly Detection
- TODS: An Automated Time-series Outlier Detection System
- tsmoothie: time-series smoothing and outlier detection

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- amelie: Anomaly Detection with Normal Probability Functions
- ANN2: Artificial Neural Networks for Anomaly Detection
- anomaly: Detecting Anomalies in Data
- AnomalyDetection: package by Twitter to detect anomalies
- anomalize: Tidy Anomaly Detection
- composits: Compositional, Multivariate and Univariate Time Series Outlier Ensemble
- dobin: Dimension Reduction for Outlier Detection

- dsos: Dataset Shift with Outlier Scores
- HDoutliers: Leland Wilkinson's Algorithm for Detecting Multidimensional Outliers
- isotree: Isolation-Based Outlier Detection
- kssa: automatically identify and validate the best method for missing data imputation in a time series
- lookout: Leave One Out Kernel Density Estimates for Outlier Detection
- mvoutlier: Multivariate Outlier Detection Based on Robust Methods
- odetector: Outlier Detection Using Partitioning Clustering Algorithms
- otsad: Online Time Series Anomaly Detectors
- outForest: Multivariate Outlier Detection and Replacement
- outliers: Tests for Outliers
- outliertree: Explainable Outlier Detection Through Decision Tree Conditioning
- stray: Anomaly Detection in High Dimensional and Temporal Data
- TagAnomaly: Anomaly detection analysis and labeling tool by Microsoft
- trendsegmentR: Linear Trend Segmentation and Point Anomaly Detection
- tsoutliers: Detection of Outliers in Time Series
- univOutl: Detection of Univariate Outliers

7.4 Bayesian analysis and modeling

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- ArviZ: Exploratory analysis of Bayesian models with Python
- baal: enable Bayesian active learning in your research or labeling work
- bambi: BAyesian Model-Building Interface (Bambi)
- bilby: Bayesian inference library
- BayesianOptimization: implementation of global optimization with gaussian processes
- BayesTSA: ayesian methods for solving estimation and forecasting problems in time series analysis
- BoTorch: Bayesian optimization in PyTorch
- Bumps: data fitting and uncertainty estimation
- nutpie: A fast sampler for bayesian posteriors
- Orbit: Bayesian forecasting package by Uber
- PyApprox: high-dimensional approximation and uncertainty quantification
- pyMC: Bayesian Modeling and Probabilistic Machine Learning with Aesara
- PyStan: Python interface to Stan, a platform for statistical modeling
- zeus: Lightning Fast MCMC

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ashr: Methods for Adaptive Shrinkage, using Empirical Bayes
- bain: Bayes Factors for Informative Hypotheses (equality, inequality, and about equality constrained hypotheses)
- bamp: Bayesian Age-Period-Cohort Modeling and Prediction
- bsamGP: Bayesian Spectral Analysis Models using Gaussian Process Priors
- bayesdfa: Bayesian Dynamic Factor Analysis (DFA) with 'Stan'
- bayefdr: Bayesian Estimation and Optimisation of Expected False Discovery Rate
- BayesFM: Bayesian Inference for Factor Modeling
- bayesforecast: Bayesian Time Series Modeling with Stan
- BayesHMM: Full Bayesian Inference for Hidden Markov Models
- bayesian: Bindings for Bayesian TidyModels
- bayesmodels: The 'Tidymodels' Extension for Bayesian Models
- bayesplot: Plotting for Bayesian Models
- BayesPostEst: Generate Postestimation Quantities for Bayesian MCMC Estimation
- bayestestR: Understand and Describe Bayesian Models and Posterior Distributions
- BayesTools: Tools for Bayesian Analyses
- BayesVarSel: Bayes Factors, Model Choice and Variable Selection in Linear Models
- BEST: Bayesian Estimation Supersedes the t-Test
- beyondWhittle: Bayesian Spectral Inference for Stationary Time Series
- BFpack: Flexible Bayes Factor Testing of Scientific Expectations
- BMAmevt: Multivariate Extremes: Bayesian Estimation of the Spectral Measure
- bmixture: Bayesian Estimation for Finite Mixture of Distributions
- bnmonitor: An Implementation of Sensitivity Analysis in Bayesian Networks
- BNPmix: Bayesian Nonparametric Mixture Models
- bpcs: Bayesian Paired Comparison Analysis with Stan
- bpgmm: Bayesian Model Selection Approach for Parsimonious Gaussian Mixture Models
- brms: Bayesian Regression Models using 'Stan'
- BSL: Bayesian Synthetic Likelihood
- bspec: Bayesian Spectral Inference
- bsvars: Bayesian Estimation of Structural Vector Autoregressive Models
- dalmatian: Automating the Fitting of Double Linear Mixed Models in 'JAGS' and 'nimble'
- dbnR: Dynamic Bayesian Network Learning and Inference

- DEBBI: Differential Evolution-Based Bayesian Inference
- ensembleBMA: Probabilistic Forecasting using Ensembles and Bayesian Model Averaging
- fbst: The Full Bayesian Evidence Test, Full Bayesian Significance Test and the e-Value
- greta: scalable statistical modelling in R
- LaplacesDemon: Complete Environment for Bayesian Inference
- mBvs: Bayesian Variable Selection Methods for Multivariate Data
- mlr3mbo: Flexible Bayesian Optimization
- mombf: Bayesian Model Selection and Averaging for Non-Local and Local Priors
- networkABC: Network Reverse Engineering with Approximate Bayesian Computation
- nimble: MCMC, Particle Filtering, and Programmable Hierarchical Modeling
- Nmix: Bayesian Inference on Univariate Normal Mixtures
- posterior: Tools for Working with Posterior Distributions
- rBayesianOptimization: Bayesian Optimization of Hyperparameters
- Rbeast: Bayesian Change-Point Detection and Time Series Decomposition
- REBayes: Empirical Bayes Estimation and Inference
- Revticulate: Interaction with "RevBayes" in R
- rstan: R Interface to Stan
- rstanarm: Bayesian Applied Regression Modeling via Stan
- SequenceSpikeSlab: Exact Bayesian Model Selection Methods for the Sparse Normal Sequence Model
- shrinkTVP: Efficient Bayesian Inference for Time-Varying Parameter Models with Shrinkage
- tidybayes: Tidy Data and 'Geoms' for Bayesian Models

7.5 Causality, inference and dependencies

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- bilby: Bayesian inference library
- CausalDiscoveryToolbox: causal inference in graphs and in the pairwise settings
- causality: Tools for causal analysis
- causalml: package by Uber for Uplift modeling and causal inference with machine learning algorithms
- copulae: Multivariate data modelling with Copulas
- DoWhy: library by Microsoft for causal inference that supports explicit modeling and testing of causal assumptions
- HiDimStat: High-dimensional statistical inference tool
- tigramite: time series analysis python module for causal discovery

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- causal.decomp: Causal Decomposition Analysis
- CausalImpact: toolkit by Google to infer Causal Effects using Bayesian Structural Time-Series Models
- causaloptim: An Interface to Specify Causal Graphs and Compute Bounds on Causal Effects
- copula: Multivariate Dependence with Copulas
- dCovTS: Distance Covariance and Correlation for Time Series Analysis
- estimatr: Fast Estimators for Design-Based Inference
- flipr: Flexible Inference via Permutations in R
- generalCorr: Generalized Correlations, Causal Paths and Portfolio Selection
- HellCor: The Hellinger Correlation
- infer: Tidy Statistical Inference
- jackstraw: Statistical Inference for Unsupervised Learning
- konfound: Quantify the Robustness of Causal Inferences
- mashr: Multivariate Adaptive Shrinkage
- multivariance: Measuring Multivariate Dependence Using Distance Multivariance
- NlinTS: Models for Non Linear Causality Detection in Time Series
- NNS: Nonlinear nonparametric statistics using partial moments
- pcalg: Methods for Graphical Models and Causal Inference
- qmd: Quantification of Multivariate Dependence
- rmcfs: The MCFS-ID Algorithm for Feature Selection and Interdependency Discovery
- sherlock: package by Netflix for causal machine learning for segment discovery and analysis
- SIHR: Statistical Inference in High Dimensional Regression
- tlverse: One Stop to Targeted Learning in R
- tscopula: Time Series Copula Models
- VLTimeCausality: Variable-Lag Time Series Causality Inference Framework

7.6 Classification, Motifs, Neighbors, Wavelets, Transforms

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best-Subset Selection Library
- catboost: Gradient Boosting on Decision Trees by Yandex
- HiClass: hierarchical classification compatible with scikit-learn

- LightGBM: fast, distributed, high performance gradient boosting (GBT, GBDT, GBRT, GBM or MART) framework by Microsoft
- Local Cascade Ensemble (LCE) is a high-performing, scalable and user-friendly machine learning method for the general tasks of Classification and Regression
- matrixprofile: time series data mining tasks, utilizing matrix profile algorithms
- pyts: time series classification
- scikit-learn: machine learning in Python
- seriesdistancematrix: implements the Series Distance Matrix framework, a flexible component-based framework that bundles various Matrix Profile related techniques
- sktime: unified framework for machine learning with time series
- stumpy: modern time series analysis
- tslearn: machine learning toolkit dedicated to time-series data

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best-Subset Selection Library
- AUC: Threshold Independent Performance Measures for Probabilistic Classifiers
- bcTSNE: Projected t-SNE for Batch Correction
- biwavelet: Conduct Univariate and Bivariate Wavelet Analyses
- caret: Classification and Regression Training
- classmap: Visualizing Classification Results
- classifly: Explore Classification Models in High Dimensions
- ContaminatedMixt: Clustering and Classification with the Contaminated Normal
- CORElearn: Classification, Regression and Feature Evaluation
- cvms: Cross-Validation for Model Selection
- ddalpha: Depth-Based Classification and Calculation of Data Depth
- dtw: Dynamic Time Warping Algorithms
- greed: Clustering and Model Selection with the Integrated Classification Likelihood
- ipred: Improved Predictors
- klaR: Classification and Visualization
- matrixProfile: Matrix Profile
- matrixprofiler: Matrix Profile for R
- mclust: Gaussian Mixture Modelling for Model-Based Clustering, Classification, and Density Estimation
- MixGHD: Model Based Clustering, Classification and Discriminant Analysis Using the Mixture of Generalized Hyperbolic Distributions
- MixMatrix: Classification with Matrix Variate Normal and t Distributions

- mixSPE: Mixtures of Power Exponential and Skew Power Exponential Distributions for Use in Model-Based Clustering and Classification
- mixture: Mixture Models for Clustering and Classification
- randomUniformForest: Random Uniform Forests for Classification, Regression and Unsupervised Learning
- rbooster: AdaBoost Framework for Any Classifier
- rebmix: Finite Mixture Modeling, Clustering & Classification
- regtools: Regression and Classification Tools
- Rmixmod: Classification with Mixture Modelling
- RSSL: Implementations of Semi-Supervised Learning Approaches for Classification
- Rtsne: T-Distributed Stochastic Neighbor Embedding using a Barnes-Hut Implementation
- sbfc: Selective Bayesian Forest Classifier
- SKNN: A Super K-Nearest Neighbor (SKNN) Classification Algorithm
- stacks: Tidy Model Stacking
- TSMining: Mining Univariate and Multivariate Motifs in Time-Series Data
- tsmp: Time Series with Matrix Profile
- yardstick: Tidy Characterizations of Model Performance

7.7 Clustering

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- cclust: Convex Clustering Methods and Clustering Indexes
- ChronoClust: perform clustering on each of a time-series of discrete datasets, and explicitly track the evolution of clusters over time
- classix: Fast and explainable clustering based on sorting
- ClusterEnsembles: package for cluster ensembles
- clustergram: Visualization and diagnostics for cluster analysis in Python
- Clusteval: methods for unsupervised cluster validation
- deeptime: analysis of time series data including dimensionality reduction, clustering, and Markov model estimation
- dtaidistance: Time series distances: Dynamic Time Warping
- DTCR: Learning Representations for Time Series Clustering
- DTW_kmedoids: Multivariate time series clustering using Dynamic Time Warping (DTW) and k-mediods
- ETNA Time Series Library by Tinkoff AI
- faiss: efficient similarity search and clustering of dense vectors
- fastcluster: Fast hierarchical clustering routines

- genieclust: Fast and Robust Hierarchical Clustering with Noise Point Detection
- hcluster: Hierarchical Clustering Algorithms
- hdbscan: high performance implementation of HDBSCAN clustering
- scikit-learn: machine learning in Python
- TimeSeriesDeepClustering: End-to-end deep representation learning for time series clustering
- tslearn: machine learning toolkit dedicated to time-series data
- validclust: Validate clustering results

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- apcluster: Affinity Propagation Clustering
- bahc: bahc: Filter Covariance and Correlation Matrices with Bootstrapped-Averaged Hierarchical Ansatz
- bootcluster: Bootstrapping Estimates of Clustering Stability
- cclust: Convex Clustering Methods and Clustering Indexes
- clue: Cluster Ensembles
- clusrank: Wilcoxon Rank Tests for Clustered Data
- clustAnalytics: Cluster Evaluation on Graphs
- ClustAssess: Tools for Assessing Clustering
- ClustBlock: Hierarchical and partitioning algorithms of blocks of variables
- cluster: "Finding Groups in Data": Cluster Analysis Extended Rousseeuw et al.
- clusterability: Performs Tests for Cluster Tendency of a Data Set
- ClusterBootstrap: Analyze Clustered Data with Generalized Linear Models using the Cluster Bootstrap
- Clustering: Techniques for Evaluating Clustering
- clusterSEs: Calculate Cluster-Robust p-Values and Confidence Intervals
- ClusterR: Gaussian Mixture Models, K-Means, Mini-Batch-Kmeans, K-Medoids and Affinity Propagation Clustering
- clusterSim: Searching for Optimal Clustering Procedure for a Data Set
- clustrd: Methods for Joint Dimension Reduction and Clustering
- clustree: Visualise Clusterings at Different Resolutions
- clValid: Validation of Clustering Results
- cmbClust: Conditional Mixture Modeling and Model-Based Clustering
- Ckmeans.1d.dp: Optimal, Fast, and Reproducible Univariate Clustering
- diceR: Diverse Cluster Ensemble in R
- dtwclust: Time Series Clustering Along with Optimizations for the Dynamic Time Warping Distance

- evclust: Evidential Clustering
- fastcluster: Fast Hierarchical Clustering Routines for R and 'Python'
- fastkmedoids: Faster K-Medoids Clustering Algorithms: FastPAM, FastCLARA, FastCLARANS
- FCPS: Fundamental Clustering Problems Suite
- flexclust: Flexible Cluster Algorithms
- fpc: Flexible Procedures for Clustering
- genie: Fast, Robust, and Outlier Resistant Hierarchical Clustering
- genieclust: The Genie++ Hierarchical Clustering Algorithm with Noise Points Detection
- heatmaply: Interactive Cluster Heat Maps Using 'plotly' and 'ggplot2'
- HierPortfolios: Hierarchical Clustering-Based Portfolio Allocation Strategies
- htestClust: Reweighted Marginal Hypothesis Tests for Clustered Data
- kselection: Selection of K in K-Means Clustering
- l1spectral: An L1-Version of the Spectral Clustering
- leaderCluster: Leader Clustering Algorithm
- LearnClust: Learning Hierarchical Clustering Algorithms
- MatTransMix: Clustering with Matrix Gaussian and Matrix Transformation Mixture Models
- mclust: Gaussian Mixture Modelling for Model-Based Clustering, Classification, and Density Estimation
- mclustcomp: Measures for Comparing Clusters
- mdendro: Extended Agglomerative Hierarchical Clustering
- Mercator: Clustering and Visualizing Distance Matrices
- MixGHD: Model Based Clustering, Classification and Discriminant Analysis Using the Mixture of Generalized Hyperbolic Distributions
- MixSim: Simulating Data to Study Performance of Clustering Algorithms
- mixSPE: Mixtures of Power Exponential and Skew Power Exponential Distributions for Use in Model-Based Clustering and Classification
- mixture: Mixture Models for Clustering and Classification
- MKMeans: A Modern K-Means (MKMeans) Clustering Algorithm
- mlr3cluster: Cluster Extension for 'mlr3'
- motifcluster: Motif-Based Spectral Clustering of Weighted Directed Networks
- MSclust: Multiple-Scaled Clustering
- mstknnclust: MST-kNN Clustering Algorithm
- NNS: Nonlinear nonparametric statistics using partial moments
- ProjectionBasedClustering: Projection Based Clustering
- protoclust: Hierarchical Clustering with Prototypes

- pytorch_cluster: PyTorch Extension Library of Optimized Graph Cluster Algorithms
- QuClu: Quantile-Based Clustering Algorithms
- rebmix: Finite Mixture Modeling, Clustering & Classification
- RCTS: Clustering Time Series While Resisting Outliers
- RMBC: Robust Model Based Clustering
- sClust: R Toolbox for Unsupervised Spectral Clustering
- sigclust: Statistical Significance of Clustering
- SLBDD: Statistical Learning for Big Dependent Data
- Spectrum: Fast Adaptive Spectral Clustering for Single and Multi-View Data
- T4cluster: Tools for Cluster Analysis
- tclust: Robust Trimmed Clustering
- tglkmeans: Efficient Implementation of K-Means++ Algorithm
- TSclust: Time Series Clustering Utilities
- vimpclust: Variable Importance in Clustering

7.8 Coding utilities and frameworks

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Algviz is an algorithm visualization tool for your Python code
- asteval: minimalistic evaluator of python expression using ast module
- autoflake: Removes unused imports and unused variables as reported by pyflakes
- autopep8: automatically formats Python code to conform to the PEP 8 style guide
- autoray: Write numeric code that automatically works with any numpy-ish libraries
- bandit: find common security issues in Python code
- birdseye: Graphical debugger to view the values of all evaluated expressions
- black: uncompromising Python code formatter
- BLUE: The slightly less uncompromising Python code formatter
- Bowler: Safe code refactoring by Facebook for modern Python
- Comprehensive Python Cheatsheet
- conda-deps: Generate conda environment files from Python and R source code
- Crashtest is a Python library that makes exceptions handling and inspection easier.
- darker: Apply black reformatting to Python files only in regions changed since a given commit
- enum_tools: Tools to expand Python's enum module.
- erdantic: tool for drawing entity relationship diagrams (ERDs) for Python data model classes.

- flake8: glues together pycodestyle, pyflakes, mccabe, and third-party plugins to check the style and quality of code
- flake8-black: flake8 plugin to run black for checking Python coding style
- friendly: replaces standard tracebacks by something easier to understand
- Hatch is a modern, extensible Python project manager.
- icecream: Never use print() to debug again
- ipdb: exports functions to access the IPython debugger
- isort: utility / library to sort imports
- jedi: autocompletion, static analysis and refactoring library
- jsonschema: implementation of the JSON Schema specification for Python
- kedro: framework for creating reproducible, maintainable and modular data science code
- kedro-viz: Visualise your Kedro data and machine-learning pipelines and track your experiments.
- libfyaml: Fully feature complete YAML parser and emitter
- luddite: Checks for out-of-date package versions
- makepackage: easy packaging of Python code
- mamba: Fast Cross-Platform Package Manager (reimplementation of the conda package manager in C++)
- memray: memory profiler for Python
- metaflow: build and manage real-life data science projects
- mkdocs: Project documentation with Markdown
- mkdocs-material: Technical documentation that just works
- MonkeyType: toolkit by Instagram to generate static type annotations by collecting runtime types
- Monty: supplementary useful functions for Python that are not part of the standard library
- mypy: Optional static typing for Python
- nptyping: Type hints for Numpy
- numpydoc: Numpy's Sphinx extensions
- pdbpp: a drop-in replacement for pdb (the Python debugger)
- PlantUML: Generate UML diagram from textual description
- poetry: dependency management and packaging made easy
- Pretty_Errors: Prettify Python exception output to make it legible
- prospector: Inspects source files and provides information about type and location of classes, methods
- ptvsd: debugger package by Microsoft for use with Visual Studio and Visual Studio Code
- pudb: Full-screen console debugger for Python
- pyan: Static call graph generator
- pycodestyle: Simple Python style checker

- pydantic: Data parsing and validation using Python type hints
- pyDeprecate: tooling for marking deprecated functions or classes and re-routing to the new successors' instance.
- pyflakes: checks Python source files for errors
- pylint: static code analysis tool
- pyquickhelper: automation of many things
- pyre: framework for building scientific applications in Python
- pyre-check: Performant type-checking toolkit by Facebook
- pyright: Static type checker by Microsoft
- PyScaffold: Python project template generator with batteries included
- PySnooper: Never use print for debugging again
- py-spy: Sampling profiler for Python programs
- pytools: a big bag of things that are "missing" from the Python standard library
- pytype: static type analyzer by Google
- radon: tool that computes various metrics from the source code
- rope: refactoring library
- scalene: high-performance, high-precision CPU, GPU, and memory profiler for Python
- sphinx: Sphinx documentation builder
- StrictYAML is a type-safe YAML parser that parses and validates a restricted subset of the YAML specification
- tryceratops: linter to prevent exception handling antipatterns in Python
- typeguard: Run-time type checker for Python
- TypePigeon: type converter focused on converting values between various Python data types.
- varname:Dark magics about variable names in python
- vulture: Find dead Python code
- xlwings: ibrary that makes it easy to call Python from Excel and vice versa
- yapf: formatter by Google for Python files
- yappi: Yet Another Python Profiler, but this time multithreading, asyncio and gevent aware.

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- adaptalint: Check Code Style Painlessly
- baguette: Efficient Model Functions for Bagging
- box: Write Reusable, Composable and Modular R Code
- butcher: Model Butcher: axe components of fitted model objects and help reduce the size of model objects saved to disk
- cartbonate: Create beautiful images of source code using 'carbon.js
- checkmate: Fast and Versatile Argument Checks
- checkpoint: Install Packages from Snapshots on the Checkpoint Server for Reproducibility
- cleanr: Helps You to Code Cleaner
- delayed: A Framework for Parallelizing Dependent Tasks
- goodpractice: Advice on R Package Building
- hardhat: Construct Modeling Packages
- IRdisplay: 'Jupyter' Display Machinery
- IRkernel: Native R Kernel for the 'Jupyter Notebook'
- jetpack: A Friendly Package Manager
- leprechaun: Create Simple 'Shiny' Applications as Packages
- lintr: A 'Linter' for R Code
- lvec: Out of Memory Vectors
- memuse: Memory Estimation Utilities
- metaflow: build and manage real-life data science projects
- miniCRAN: Create a Mini Version of CRAN Containing Only Selected Packages
- mongolite: Fast and Simple 'MongoDB' Client for R
- packager: Create, Build and Maintain Packages
- parsnip: A Common API to Modeling and Analysis Functions
- prettifyAddins: 'RStudio' Addins to Prettify 'JavaScript', 'C++', 'Python', and More
- R6: Encapsulated Classes with Reference Semantics
- R6P: Design Patterns in R
- recipes: Preprocessing and Feature Engineering Steps for Modeling
- renv: Project Environments
- rhino: A Framework for Enterprise Shiny Applications
- roxut: Document Unit Tests Roxygen-Style
- roxygen2: In-Line Documentation for R

- rstudio.prefs: Set 'RStudio' Preferences
- tidymodules: obust framework for developing 'Shiny' modules based on R6 classes which should facilitates inter-modules communication.
- waldo: Find Differences Between R Objects
- vetiver: Version, Share, Deploy, and Monitor Models
- workflows: Modeling Workflows
- workflowsets: Create a Collection of 'tidymodels' Workflows

7.9 Computational performance

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Aesara: definie, optimize, and efficiently evaluate mathematical expressions involving multi-dimensional arrays.
- arctic: High performance datastore by Man Group for time series and tick data
- bottleneck: Fast NumPy array functions written in C
- Dask: Parallel computing with task scheduling
- Dask-ML provides scalable machine learning in Python using Dask alongside popular machine learning libraries
- datatable: library for fast multi-threaded data manipulation and munging
- fairscale: PyTorch extensions for high performance and large scale training.
- fastcore: Python supercharged for the fastai library
- hypre: high performance preconditioners
- jax: automatically differentiate native Python and NumPy functions
- modin: ake your pandas code run faster by changing one line of code
- multiprocess: better multiprocessing and multithreading in python
- numexpr: Fast numerical expression evaluator for NumPy
- PandaPy: speed of NumPy and the usability of Pandas but much faster
- pandarallel: parallelize Pandas operations on all available CPUs
- pandasvault:Advanced Pandas Vault - Utilities, Functions and Snippets
- polars: Fast multi-threaded DataFrame library
- ppft: distributed and parallel python
- PyArma: Linear algebra library for Python
- PyArmadillo: an alternative approach to linear algebra in Python
- pyperf: Toolkit to run Python benchmarks
- pyperformance: Python Performance Benchmark Suite
- py-spy: Sampling profiler for Python programs

- scalene: high-performance, high-precision CPU, GPU, and memory profiler for Python
- swifter: efficiently applies any function to a pandas dataframe or series in the fastest available manner
- tempeh is a framework to TEst Machine learning PErformance exHaustively which includes tracking memory usage and run time.

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- collapse: Advanced and Fast Data Transformation
- dataPreparation: Automated Data Preparation
- delayed: A Framework for Parallelizing Dependent Tasks
- dplyr: A Grammar of Data Manipulation
- MatrixStats: Methods that Apply to Rows and Columns of Matrices (and to Vectors)
- mirai: Minimalist Async Evaluation Framework for R
- purrr: Functional Programming Tools
- tidyverse: set of packages that work in harmony because they share common data representations and 'API' design
- timetk: A Tool Kit for Working with Time Series in R
- tibble: Simple Data Frames
- tidytidbits: A Collection of Tools and Helpers Extending the Tidyverse
- tsibble: Tidy Temporal Data Frames and Tools

7.10 Containers, projects, pipelines and deployment

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Driblet - Google Cloud based ML pipeline by Google
- MLflow: A Machine Learning Lifecycle Platform
- metaflow: Python/R library by Netflix to build and manage real-life data science projects
- mlflow: Interface to 'MLflow'
- mlxtend: extension and helper modules for data analysis and machine learning libraries
- NNI: toolkit by Microsoft to help users automate Feature Engineering, Neural Architecture Search, Hyperparameter Tuning and Model Compression
- petastorm: toolkit by Uber for single machine or distributed training and evaluation of deep learning models (Tensorflow, Pytorch, and PySpark) from datasets in Apache Parquet format
- pipelines: Machine Learning Pipelines for Kubeflow
- Prefect: second-generation dataflow coordination and orchestration platform
- PyTorch Lightning: The lightweight PyTorch wrapper for high performance AI research
- Tango: toolkit by Allen Institute of Articial Intelligence for choreographing machine learning research

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- DriveML: Self-Drive Machine Learning Projects
- metaflow: Python/R library by Netflix to build and manage real-life data science projects
- mlflow: Interface to 'MLflow'

7.11 Covariances, correlations and volatilities

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- numpy: scientific computing
- precise: online covariance and precision forecasting, portfolios, and model ensembles
- PyPortfolioOpt: Financial portfolio optimization
- sklearn.covariance: covariance estimation in scikit-learn
- statsmodels: statistical modeling and econometrics

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- bahc: Filter Covariance and Correlation Matrices with Bootstrapped-Averaged Hierarchical Ansatz
- BBcor: Bayesian Bootstrapping Correlations
- BEKKs: Multivariate Conditional Volatility Modelling and Forecasting
- BSCOV: Detection of Multiple Structural Breaks in Large Covariance Matrices
- clubSandwich: Cluster-Robust (Sandwich) Variance Estimators with Small-Sample Corrections
- cocor: Comparing Correlations
- corpcor: Efficient Estimation of Covariance and (Partial) Correlation
- correlation: Methods for Correlation Analysis
- corx: Create and Format Correlation Matrices
- CovTools: Statistical Tools for Covariance Analysis
- cvCovEst: Cross-Validated Covariance Matrix Estimation
- dcortools: Providing Fast and Flexible Functions for Distance Correlation Analysis
- dCovTS: Distance Covariance and Correlation for Time Series Analysis
- fitHeavyTail: Mean and Covariance Matrix Estimation under Heavy Tails
- FRCC: Fast Regularized Canonical Correlation Analysis
- gencor: Generate Customized Correlation Matrices
- generalCorr: Generalized Correlations, Causal Paths and Portfolio Selection
- mashr: Multivariate Adaptive Shrinkage

- MatrixCorrelation: Matrix Correlation Coefficients
- MTS: All-Purpose Toolkit for Analyzing Multivariate Time Series (MTS) and Estimating Multivariate Volatility Models
- NonParRolCor: a Non-Parametric Statistical Significance Test for Rolling Window Correlation
- NNS: Nonlinear nonparametric statistics using partial moments
- rags2ridges: Ridge Estimation of Precision Matrices from High-Dimensional Data
- rmcorr: Repeated Measures Correlation
- robcor: Robust Correlations
- robustcov: Collection of Robust Covariance and (Sparse) Precision Matrix Estimators
- RSC: Robust and Sparse Correlation Matrix
- sandwich: Robust Covariance Matrix Estimators
- WGCNA: Weighted Correlation Network Analysis

7.12 Data analysis and exploration

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- AutoViz: Automatically Visualize any dataset, any size with a single line of code.
- daal4py: simplified API to Intel oneAPI Data Analytics Library
- DeepGraph: scalable, general-purpose data analysis with Pandas-based Networks
- D-tale:Visualizer by Man Group for pandas data structures
- dython: Data analysis tools
- empiricaldist: empirical distribution functions
- hyperspy: Multidimensional data analysis
- Lux: automate the visualization and data analysis process
- mlxtend: extension and helper modules for Python's data analysis and machine learning libraries.
- numericalunits: Units and dimensional analysis compatible with everything
- Orange: Interactive data analysis
- pandas-profiling: Create HTML profiling reports from pandas DataFrame objects
- PyApprox: high-dimensional approximation and uncertainty quantification
- sweetviz: Visualize and compare datasets, target values and associations

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- checkmate: Fast and Versatile Argument Checks
- collapse: Advanced and Fast Data Transformation
- datacleanr: Interactive and Reproducible Data Cleaning
- DataEditR: An Interactive Editor for Viewing, Entering, Filtering & Editing Data
- DataExplorer: Automate Data Exploration and Treatment
- datamods: Modules to Import and Manipulate Data in 'Shiny'
- dataprep: Efficient and Flexible Data Preprocessing Tools
- DataVisualizations: Visualizations of High-Dimensional Data
- datawizard: Easy Data Wrangling
- DescTools: Tools for Descriptive Statistics
- dimensio: Multivariate Data Analysis
- discoveR: Exploratory Data Analysis System
- dlookr: Tools for Data Diagnosis, Exploration, Transformation
- EasyDescribe: A Convenient Way of Descriptive Statistics
- esquisse: Explore and Visualize Your Data Interactively
- explor: Interactive Interfaces for Results Exploration
- exploratory: A Tool for Large-Scale Exploratory Analyses
- explore: Simplifies Exploratory Data Analysis
- factoextra: extract and visualize the output of multivariate data analyses, including 'PCA' (Principal Component Analysis), 'CA' (Correspondence Analysis), 'MCA' (Multiple Correspondence Analysis), 'FAMD' (Factor Analysis of Mixed Data), 'MFA' (Multiple Factor Analysis) and 'HMFA' (Hierarchical Multiple Factor Analysis)
- FactoInvestigate: Automatic Description of Factorial Analysis
- FactoMineR: Multivariate Exploratory Data Analysis and Data Mining
- ggESDA: Exploratory Symbolic Data Analysis with 'ggplot2'
- HDTSA: High Dimensional Time Series Analysis Tools
- infotheo: Information-Theoretic Measures
- kfa: K-Fold Cross Validation for Factor Analysis
- MazamaRollUtils: Efficient Rolling Functions
- mmpca: Integrative Analysis of Several Related Data Matrices
- praznik: Tools for Information-Based Feature Selection and Scoring
- predictoR: Predictive Data Analysis System

- rigr: Regression, Inference, and General Data Analysis Tools in R
- robCompositions: Compositional Data Analysis
- rrcov: Scalable Robust Estimators with High Breakdown Point
- SmartEDA: Summarize and Explore the Data
- statsExpressions: Tidy Dataframes and Expressions with Statistical Details
- Statsomat: Shiny Apps for Automated Data Analysis and Automated Interpretation
- thinkr: Tools for Cleaning Up Messy Files
- tswge: Time Series for Data Science.Accompanies the texts Time Series for Data Science and Applied Time Series Analysis with R,
- validata: Validate Data Frames
- validate: Data Validation Infrastructure
- validatetools: Checking and Simplifying Validation Rule Sets
- wrangle: A Systematic Data Wrangling Idiom

7.13 Data augmentation, scenario generation and synthetic time series

Collections of resources

List of links:

- Synthetic data generation by Van Der Schaar Lab
- Useful data augmentation resources

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- agots: Anomaly Generator on Time Series
- benchmark_VAE: Unifying Generative Autoencoder implementations in Python
- Copulas: model multivariate data using copulas
- CTGAN: Conditional GAN for Tabular Data
- COMET Flows: Towards Generative Modeling of Multivariate Extremes and Tail Dependence
- DataGeneration: Synthetic financial correlation matrix and time series generation
- DECAF: Generating Fair Synthetic Data Using Causally-Aware Generative Networks
- DeepEcho: Synthetic Data Generation for mixed-type, multivariate time series
- deltapy: Tabular Data Augmentation
- extremeIndex: Forecast Verification for Extreme Events
- ixmp: platform for integrated and cross-cutting scenario analysis
- MLlforHealthLab: Machine Learning and Artificial Intelligence for Medicine
- pydantic-factories: Pydantic based mock data generation

- pythae: Unifying Generative Autoencoder implementations in Python
- RDT: Reversible Data Transforms to reproduce realistic data
- scattering_covariance: analysis and generation of time series
- SDMetrics: Metrics for Synthetic Data Generation Projects
- SDGym: Benchmarking synthetic data generation methods
- SDV: Synthetic Data Generation for tabular, relational and time series data
- SignalFilters: Signal Filtering and Generation of Synthetic Time-Series
- snorkel: system for quickly generating training data with weak supervision
- synthia: Multidimensional synthetic data generation in Python
- TGAN: Generative adversarial training for generating synthetic tabular data
- TimeGAN: Time-series Generative Adversarial Networks
- time-series-generator: Time Series Generator
- TimeSynth: Synthetic Time Series Generation
- tsaug: time series augmentation
- tsBNgen: Generate Time Series Data Based on an Arbitrary Bayesian Network Structure
- tsGAN: Time-series Generative Adversarial Networks
- ydata-synthetic: Synthetic structured data generators

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- anySim: Simulation of Non-Gaussian Correlated Random Variables, Stochastic Processes and Random Fields
- bootComb: Combine Parameter Estimates via Parametric Bootstrap
- conjurer: A Parametric Method for Generating Synthetic Data
- covsim: VITA, IG and PLSIM Simulation for Given Covariance and Marginals
- fabricatr: Imagine Your Data Before You Collect It
- fwb: Fractional Weighted Bootstrap
- gencor: Generate Customized Correlation Matrices
- gratis: Generating Time Series with Diverse and Controllable Characteristics
- meboot: Maximum Entropy Bootstrap for Time Series
- metamer: Create Data with Identical Statistics
- missMethods: Methods for Missing Data
- MixSim: Simulating Data to Study Performance of Clustering Algorithms
- modeltime.resample: Resampling Tools for Time Series Forecasting
- MonteCarlo: Automatic Parallelized Monte Carlo Simulations

- MSCMT: Multivariate Synthetic Control Method Using Time Series
- mvlognCorrEst: Sampling from Multivariate Lognormal Distributions and Estimating Correlations from Uncomplete Correlation Matrix
- naive: Empirical Extrapolation of Time Feature Patterns
- RMT4DS: Computation of Random Matrix Models
- rsample: General Resampling Infrastructure
- segen: Sequence Generalization Through Similarity Network
- SimJoint: Simulate Joint Distribution
- simmer: Discrete-Event Simulation for R
- simts: Time Series Analysis Tools
- spooky: Time Feature Extrapolation Using Spectral Analysis and Jack-Knife Resampling
- Synth: Synthetic Control Group Method for Comparative Case Studies
- synthesis: Generate Synthetic Data from Statistical Models
- tetragon: Automatic Sequence Prediction by Expansion of the Distance Matrix
- TidyDensity: Functions for Tidy Analysis and Generation of Random Data
- tscopula: Time Series Copula Models

7.14 Data cleaning, preparation and validation

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- cerberus: Lightweight, extensible data validation library
- datatest: Tools for test driven data-wrangling and data validation
- doubtlab: Doubt your data, find bad labels
- framework: Data management framework for Python that provides functionality to describe, extract, validate, and transform tabular data
- formencode: validation and form generation
- pandera: perform data validation on dataframes
- pydantic: Data parsing and validation using Python type hints
- pyjanitor: Clean APIs for data cleaning. Python implementation of R package Janitor
- PyOptimus: framework for cleaning and pre-processing data in a distributed fashion
- scikit-learn: machine learning in Python
- schema: library for validating Python data structures
- serde: framework for defining, serializing, deserializing, and validating data structures
- typical: Fast, simple, & correct data-validation using Python 3 typing.
- validators: Python data validation for Humans

- Voluptuous: data validation library.
- validr: simple, fast, extensible python library for data validation
- wtforms: flexible forms validation and rendering library

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- cleanTS: Testbench for Univariate Time Series Cleaning
- dataPreparation: Automated Data Preparation
- data.validator: Automatic Data Validation and Reporting
- datawizard: Easy Data Wrangling
- errorlocate: Locate Errors with Validation Rules
- pointblank: Data Validation and Organization of Metadata for Local and Remote Tables
- testdat: Data Unit Testing for R
- tsrobprep: Robust Preprocessing of Time Series Data
- validate: Data Validation Infrastructure
- validatetools: Checking and Simplifying Validation Rule Sets
- wrangle: A Systematic Data Wrangling Idiom

7.15 Data Imputation

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- AutoImpute: Imputation Methods
- Clairvoyance: a Unified, End-to-End AutoML Pipeline for Medical Time Series
- fancyimpute: Multivariate imputation and matrix completion algorithms
- HyperImpute: framework for prototyping and benchmarking imputation methods
- imputena: automated and customized treatment of missing values in datasets
- miceforest: Fast, Memory Efficient Imputation with LightGBM
- MissForestExtra: nonparametric imputation on missing values
- scikit-learn: machine learning in Python
- statsmodels: statistical modeling and econometrics
- tsai: time series tasks like classification, regression, forecasting, imputation

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- Amelia: A Program for Missing Data
- CoImp: Copula Based Imputation Method
- deductive: Data Correction and Imputation Using Deductive Methods
- ggmice: Visualizations for 'mice' with 'ggplot2'
- howManyImputations: Calculate How many Imputations are Needed for Multiple Imputation
- imputeFin: Imputation of Financial Time Series with Missing Values and/or Outliers
- imputeGeneric: Ease the Implementation of Imputation Methods
- imputeTestbench: Test Bench for the Comparison of Imputation Methods
- imputeTS: Time Series Missing Value Imputation
- Iscores: Proper Scoring Rules for Missing Value Imputation
- mdgc: Missing Data Imputation Using Gaussian Copulas
- mice: Multivariate Imputation by Chained Equations
- miceadds: Some Additional Multiple Imputation Functions, Especially for 'mice'
- miceafter: Data and Statistical Analyses after Multiple Imputation
- miceFast: Fast Imputations Using 'Rcpp' and 'Armadillo'
- micemd: Multiple Imputation by Chained Equations with Multilevel Data
- misPRIME: Partial Replacement Imputation Estimation for Missing Covariates
- missMDA: Handling Missing Values with Multivariate Data Analysis
- missMethods: Methods for Missing Data
- missRanger: Fast Imputation of Missing Values
- mlim: Multiple Imputation with Automated Machine Learning
- NADIA: NA Data Imputation Algorithms
- naniar: Data Structures, Summaries, and Visualisations for Missing Data
- rego: Automatic Time Series Forecasting and Missing Value Imputation
- Rforestry: Random Forests, Linear Trees, and Gradient Boosting for Inference and Interpretability
- simputation: Simple Imputation
- SLBDD: Statistical Learning for Big Dependent Data
- smcfcs: Multiple Imputation of Covariates by Substantive Model Compatible Fully Conditional Specification
- univOutl: Detection of Univariate Outliers
- VIM: Visualization and Imputation of Missing Values
- yaImpute: Nearest Neighbor Observation Imputation and Evaluation Tools

7.16 Data regimes, states and changepoints: analysis and modeling

Collections of resources

List of links:

- Classifying market regimes
- TCPD: toolkit by UK national institute for data science and artificial intelligence for Turing Change Point Dataset - A collection of time series for the evaluation and development of change point detection algorithms
- TCPDBench: toolkit by UK national institute for data science and artificial intelligence for Turing Change Point Detection Benchmark: An Extensive Benchmark Evaluation of Change Point Detection Algorithms on real-world data

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- changeforest: Random Forests for Change Point Detection
- deeptime: analysis of time series data including dimensionality reduction, clustering, and Markov model estimation
- greykite: flexible, intuitive and fast forecasting library
- HMMLearn: Hidden Markov Models in Python with scikit-learn like API
- kalmanfilter: Kalman Filter
- kats: tookit by Facebook for time series analysis and forecasting
- kimfilter: Rcpp' implementation of the multivariate Kim filter, which combines the Kalman and Hamilton filters for state probability inference
- Merlion: A Machine Learning Framework for Time Series Intelligence by SalesForce
- msmtools: estimation and analysis of discrete state space Markov chains via Markov state models (MSM)
- PyEMMA: Emma's Markov Model Algorithms
- pyGPCCA: Generalized Perron Cluster Cluster Analysis to coarse-grain reversible and non-reversible Markov state models.
- pyhsmm: Bayesian inference in HSMMs and HMMs
- pymc3-hmm: Hidden Markov models in PyMC3
- ruptures: change point detection
- SST: fast implementation of Singular Spectrum Transformation
- Stone-Soup: framework for the development and testing of tracking algorithms
- statsmodels: Markov switching models in statsmodels
- transitionMatrix: Statistical analysis and visualization of state transition phenomena
- tsmoothie: time-series smoothing and outlier detection

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- BayesHMM: Full Bayesian Inference for Hidden Markov Models
- breakfast: Methods for Fast Multiple Change-Point Detection and Estimation
- BSCOV: Detection of Multiple Structural Breaks in Large Covariance Matrices
- ChangepointInference: Tools to test for a change in mean after changepoint detection
- changepoints: A Collection of Change-Point Detection Methods
- ChangePointTaylor: Identify Changes in Mean
- chngpt: Estimation and Hypothesis Testing for Threshold Regression
- cpss: Change-Point Detection by Sample-Splitting Methods
- crossvalidationCP: Cross-Validation for Change-Point Regression
- depmixS4: Dependent Mixture Models - Hidden Markov Models of GLMs and Other Distributions in S4
- dynr: Dynamic Models with Regime-Switching
- earlywarnings: Early Warning Signals Toolbox for Detecting Critical Transitions in Timeseries
- fabisearch: Change Point Detection in High-Dimensional Time Series Networks
- fHMM: Fitting Hidden Markov Models to Financial Data
- inflection: Finds the Inflection Point of a Curve
- InspectChangepoint: High-Dimensional Changepoint Estimation via Sparse Projection
- jcp: Joint Change Point Detection
- HMM: Hidden Markov Models
- hmm.discnp: Hidden Markov Models with Discrete Non-Parametric Observation Distributions
- hmmr: "Mixture and Hidden Markov Models with R" Datasets and Example Code
- KFAS: Kalman Filter and Smoother for Exponential Family State Space Models
- ldhmm: Hidden Markov Model for Financial Time-Series Based on Lambda Distribution
- mHMMbayes: Multilevel Hidden Markov Models Using Bayesian Estimation
- MSGARCH: Markov-Switching GARCH Models
- MSTest: Hypothesis Testing for Markov Switching Models
- NHMSAR: Non-Homogeneous Markov Switching Autoregressive Models
- onlineBcp: Online Bayesian Methods for Change Point Analysis
- plotHMM: Plot Hidden Markov Models
- pomp: Statistical Inference for Partially Observed Markov Processes
- Rbeast: Bayesian Change-Point Detection and Time Series Decomposition
- RChest: Locating Distributional Changes in Highly Dependent Time Series

- robcp: Robust Change-Point Tests
- segmented: Regression Models with Break-Points / Change-Points Estimation
- seqHMM: Mixture Hidden Markov Models for Social Sequence Data and Other Multivariate, Multichannel Categorical Time Series
- trendchange: Innovative Trend Analysis and Time-Series Change Point Analysis
- tsDyn: Nonlinear Time Series Models with Regime Switching
- wbsts: Multiple Change-Point Detection for Nonstationary Time Series

7.17 Data structures, storage and serialization

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- addict: Python Dict
- anndata: package for handling annotated data matrices in memory and on disk
- arctic: High performance datastore by Man Group for time series and tick data
- cloudpickle: serialize Python constructs not supported by the default pickle module
- dataclassy is a reimplementation of data classes in Python
- datatable: fast multi-threaded data manipulation and munging
- dill: extends Python's pickle module for serializing and deserializing python objects to the majority of the built-in python types.
- extendedjson: Easily extend JSON to encode and decode arbitrary Python objects
- framework: Data management framework for Python that provides functionality to describe, extract, validate, and transform tabular data
- MarketStore: DataFrame Server for Financial Timeseries Data
- marshmallow: lightweight library for converting complex objects to and from simple Python datatypes
- modin.pandas DataFrame is a parallel and distributed drop-in replacement for panda
- Mongita is to MongoDB as SQLite is to SQL
- mongo-arrow: Tools for using Apache Arrow with MongoDB
- multidict: multidict implementation
- Odo provides a uniform API for moving data between different formats
- pandas: data structures for data analysis, time series, and statistics
- pandasvault: Advanced Pandas Vault - Utilities, Functions and Snippets
- pickle: Python object serialization
- polars: Fast multi-threaded DataFrame library
- pyarrow: Python API for Apache Arrow, a language independent columnar memory format for flat and hierarchical data

- PyMongo - the Python driver for MongoDB
- PyStore: Fast data store for Pandas time-series data
- PyTables: package for managing hierarchical datasets
- rpy2-arrow: Share Apache Arrow datasets between Python and R
- serde: framework for defining, serializing, deserializing, and validating data structures
- sklearn-pandas: bridge between Scikit-Learn's machine learning methods and pandas-style Data Frames
- sortedcontainers: Sorted Containers – Sorted List, Sorted Dict, Sorted Set
- sqlite: Persistent dict, backed by sqlite3 and pickle, multithread-safe.
- sparse: Sparse Multidimensional Arrays
- srsly: Modern high performance serialization utilities
- tablib: Module for Tabular Datasets in XLS, CSV, JSON, YAML,
- tabmat: Efficient matrix representations for working with tabular data
- TileDB: powerful engine for storing and accessing dense and sparse multi-dimensional arrays
- tidypandas: grammar of data manipulation for pandas inspired by tidyverse
- tinyarray: Tinyarrays are similar to NumPy arrays, but optimized to be much faster for small sizes
- TinyDB is a lightweight document oriented database optimized for your happiness
- tinyflux: iny time series database optimized for your happiness
- torcharrow: torch.Tensor-like DataFrame library by Facebook using Arrow as a common memory format
- ubermagtable: package for manipulating tabular data
- ultrajson: Ultra fast JSON decoder and encoder written in C with Python bindings
- Vector: arrays of 2D, 3D, and Lorentz vectors
- Woodwork is a Python library that provides robust methods for managing and communicating data typing information
- xarray: multidimensional labeled arrays and datasets
- xpandas: Universal 1d/2d data containers with Transformers functionality for data analysis

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- arrow: Integration to Apache Arrow
- dibble: Dimensional Data Frames
- fst: Lightning Fast Serialization of Data Frames
- gluedown: Wrap Vectors in Markdown Formatting
- listdown: Create R Markdown from Lists
- motifcluster: Motif-Based Spectral Clustering of Weighted Directed Networks

- qs: Quick Serialization of R Objects
- RcppSimdJson: 'Rcpp' Bindings for the 'simdjson' Header-Only Library for 'JSON' Parsing
- tibble: stricter checking and better formatting than the traditional data frame
- tibblify: Rectangle Nested Lists
- tidytable: Tidy Interface to 'data.table'
- tiledb: Universal Storage Engine for Sparse and Dense Multidimensional Arrays
- tsibble: Tidy Temporal Data Frames and Tools
- tsbox: Class-Agnostic Time Series
- vtreat: A Statistically Sound data.frame Processor/Conditioner

7.18 Dates and times

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- arrow: Better dates and times for Python
- dateparser: parser for human readable dates
- dateutil: Useful extensions to the standard Python datetime features
- orjson: Fast, correct Python JSON library supporting dataclasses, datetimes, and numpy
- parsedatetime: human-readable date/time strings
- pendulum: datatimes made easy
- Pyrsistent: Persistent/Functional/Immutable data structures
- python-dateutil: Useful extensions to the standard Python datetime features
- PyTime: operate datetime by string

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- clock: Date-Time Types and Tools
- lubridate: Make Dealing with Dates a Little Easier
- qlcal: R Bindings to the Calendaring Functionality of 'QuantLib'
- tidyquant: Tidy Quantitative Financial Analysis
- timechange: Efficient Manipulation of Date-Times
- timetk: A Tool Kit for Working with Time Series in R
- tsbox: Class-Agnostic Time Series
- TSrepr: Time Series Representations
- xts: eXtensible Time Series
- zoo: S3 Infrastructure for Regular and Irregular Time Series

7.19 Dimensionality reduction

Python

List of packages/codes/frameworks/links:

- abess: Fast Best-Subset Selection Library
- deeptime: analysis of time series data including dimensionality reduction, clustering, and Markov model estimation
- direpack: State-of-the-Art Statistical Dimension Reduction Methods
- EZyRB: Easy Reduced Basis method ; performs a data-driven model order reduction for parametrized problems exploiting the recent approaches.
- humap: Hierarchical Manifold Approximation and Projection (HUMAP) is a technique based on UMAP for hierarchical non-linear dimensionality reduction.
- pyFIt-SNE: FFT-accelerated Interpolation-based t-SNE (FIt-SNE)
- scikit-dimension: intrinsic dimension estimation
- scikit-learn: machine learning in Python
- (t-SNE: t-Distributed Stochastic Neighbor Embedding (t-SNE) for dimensionality reduction
- UMAP: Uniform Manifold Approximation and Projection

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best-Subset Selection Library
- abundant: High-Dimensional Principal Fitted Components and Abundant Regression
- bayesdfa: Bayesian Dynamic Factor Analysis (DFA) with 'Stan'
- clustrd: Methods for Joint Dimension Reduction and Clustering
- dimRed: A Framework for Dimensionality Reduction
- DLPCA: The Distributed Local PCA Algorithm
- dobin: Dimension Reduction for Outlier Detection
- dyndimred: Dimensionality Reduction Methods in a Common Format
- EMD: Empirical Mode Decomposition and Hilbert Spectral Analysis
- ForeCA: Forecastable Component Analysis
- freqdom: Frequency Domain Based Analysis: Dynamic PCA
- ica: Independent Component Analysis
- ICtest: Estimating and Testing the Number of Interesting Components in Linear Dimension Reduction
- prinvars: Principal Variables (methods for reducing the number of features within a data set)
- quantdr: Dimension Reduction Techniques for Conditional Quantiles
- rrpack: Reduced-Rank Regression

- Rdimtools: Dimension Reduction and Estimation Methods
- RSpectra: Solvers for Large-Scale Eigenvalue and SVD Problems
- shrinkTVP: Efficient Bayesian Inference for Time-Varying Parameter Models with Shrinkage
- spcr: Sparse Principal Component Regression
- SuperPCA: Supervised Principal Component Analysis
- svd: Interfaces to Various State-of-Art SVD and Eigensolvers
- tapkee: tapkee: Wrapper for 'tapkee' Dimension Reduction Library
- tidydr: Unify Dimensionality Reduction Results
- TSrepr: Time Series Representations (dimensionality reduction, preprocessing, feature extraction)
- umap: Uniform Manifold Approximation and Projection

7.20 Distances and Similarity

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- DataGene: Identify How Similar TS Datasets Are to One Another
- dcor: Distance correlation and related E-statistics
- dtaidistance: Distance measures for time series
- dtw-python: comprehensive implementation of dynamic time warping (DTW) algorithms
- faiss: efficient similarity search and clustering of dense vectors
- FLANN: Fast Library for Approximate Nearest Neighbors
- GraKeL: scikit-learn compatible library for graph kernels
- khiva-python: Python binding for Khiva library for time series analytics
- mass-ts: MASS (Mueen's Algorithm for Similarity Search)
- MatrixProfile: ime series data mining tasks utilizing matrix profile
- matrixprofile-ts: detect patterns and anomalies in massive datasets using Matrix Profile
- netrd: library for network {reconstruction, distances, dynamics}
- POT : Python Optimal Transport
- PyMD: imple but general framework for embedding, called Minimum-Distortion Embedding (MDE), for finite sets of items, such as images, biological cells, nodes in a network, or any other abstract object
- PySCAMP: SCAlable Matrix Profile
- seriesdistancematrix: implements the Series Distance Matrix framework, a flexible component-based framework that bundles various Matrix Profile related techniques
- sktime: unified framework for machine learning with time series by UK national institute for data science and artificial intelligence
- Stone-Soup: framework for the development and testing of tracking algorithms

- stumpy: variety of time series data mining tasks
- tidydr: Unify Dimensionality Reduction Results
- timesmash: Quantifier of universal similarity amongst arbitrary data streams without a priori knowledge, features, or training
- wildboar: Time series learning

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- dispRity: Measuring Disparity (multidimensional space occupancy)
- Distance: Distance Sampling Detection Function and Abundance Estimation
- distantia: Assessing Dissimilarity Between Multivariate Time Series
- dtw: Dynamic Time Warping Algorithms
- dtwclust: Time Series Clustering Along with Optimizations for the Dynamic Time Warping Distance
- fICA: Classical, Reloaded and Adaptive FastICA Algorithms
- gdm: Generalized Dissimilarity Modeling
- IncDTW: Incremental Calculation of Dynamic Time Warping
- KernelKnn: Extends the simple k-nearest neighbors algorithm by incorporating numerous kernel functions and a variety of distance metrics
- MatrixCorrelation: Matrix Correlation Coefficients
- mclustcomp: Measures for Comparing Clusters
- Mercator: Clustering and Visualizing Distance Matrices
- philentropy: Similarity and Distance Quantification Between Probability Functions
- proxy: Distance and Similarity Measures
- segen: Sequence Generalization Through Similarity Network
- tetragon: Automatic Sequence Prediction by Expansion of the Distance Matrix
- TSclust: set of measures of dissimilarity between time series to perform time series clustering
- TSdist: Distance Measures for Time Series Data
- tsmp: UCR Matrix Profile Algorithm
- VPdtw: Variable Penalty Dynamic Time Warping

7.21 ESG and Impact Investing

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- ESG AI: ESG scoring as an automatic, data-driven process
- ESG-BERT: Domain Specific BERT Model for Text Mining in Sustainable Investing

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- EnvStats: Package for Environmental Statistics, Including US EPA Guidance
- ESGBoost: ESG and ECHO-based model for smart investing
- gfer: Green Finance and Environmental Risk
- text2sdg: Detecting UN Sustainable Development Goals in Text

7.22 Explainability, Interpretability, Fairness, Data Privacy

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- AIF360: comprehensive set of fairness metrics for datasets and machine learning models, explanations for these metrics, and algorithms to mitigate bias in datasets and models
- captum: Model interpretability and understanding for PyTorch
- CrypTen: framework for Privacy Preserving Machine Learning
- Dice-ML: Generate Diverse Counterfactual Explanations for any machine learning model
- DoWhy: toolkit by Microsoft for causal inference that supports explicit modeling and testing of causal assumptions
- Interpret: Fit interpretable models by Microsoft. Explain blackbox machine learning
- Interpretability dashboard, for understanding model predictions
- Lime: Local Interpretable Model-Agnostic Explanations for machine learning classifiers
- Lucid: neural network interpretability
- PyExplainer: A Local Rule-Based Model-Agnostic Technique
- Skater: Model Interpretation/Explanations
- transformers-interpret: Model explainability that works seamlessly with transformers
- XAI: eXplainability toolbox for machine learning
- Xplique: toolkit dedicated to explainability, currently based on Tensorflow

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- DALEX: moDel Agnostic Language for Exploration and eXplanation
- distillML: Model Distillation and Interpretability Methods for Machine Learning Models
- fairml: Fair Models in Machine Learning
- iml: Interpretable Machine Learning
- interpret: Fit Interpretable Machine Learning Models
- modelDown: Make Static HTML Website for Predictive Models
- modelStudio: Interactive Studio for Explanatory Model Analysis

- pdp: Partial Dependence Plots
- pre: Prediction Rule Ensembles
- Rforestry: Random Forests, Linear Trees, and Gradient Boosting for Inference and Interpretability
- rSAFE: Surrogate-Assisted Feature Extraction
- sensitivity: Global Sensitivity Analysis of Model Outputs
- triplot: Explaining Correlated Features in Machine Learning Models
- yhat: Interpreting Regression Effects

7.23 Features for time series

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- cesium: Platform for Time Series Inference
- Clairvoyance: a Unified, End-to-End AutoML Pipeline for Medical Time Series
- FeatureTools: automated feature engineering
- Featurewiz: advanced feature engineering strategies
- khiva-python: Python binding for Khiva library for time series analytics
- mne-features: MNE-Features software for extracting features from multivariate time series
- scikit-learn: machine learning in Python
- seglearn: integrated pipeline for segmentation, feature extraction, feature processing, and final estimator
- tsfeatures: Calculates various features from time series data
- tsfel: extract features from time series
- tsflex: Flexible time series feature extraction & processing
- tsfresh: extract features from time series

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- autostsm: Automatic Structural Time Series Models
- bfast: Breaks for Additive Season and Trend
- entropy: Estimation of Entropy, Mutual Information and Related Quantities
- feasts: Feature Extraction and Statistics for Time Series
- fsMTS: Feature Selection for Multivariate Time Series
- naive: Empirical Extrapolation of Time Feature Patterns
- plsVarSel: Variable Selection in Partial Least Squares
- MDFS: MultiDimensional Feature Selection
- Rcatch22: Calculation of 22 CAnonical Time-Series CHaracteristics

- theft: Tools for Handling Extraction of Features from Time Series
- tsfeatures: Time Series Feature Extraction
- TSrepr: Time Series Representations (dimensionality reduction, preprocessing, feature extraction)

7.24 Filtering and spectral analysis for time series

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- FilterPy: Kalman filtering and optimal estimation library
- mkl_fft: NumPy-based Python interface to Intel (R) MKL FFT functionality
- pyfilter: Particle filtering and sequential parameter inference
- PyWavelets: Wavelet Transforms in Python
- simdkalman: Kalman filters vectorized as Single Instruction, Multiple Data
- Stone-Soup: framework for the development and testing of tracking algorithms

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ASSA: Applied Singular Spectrum Analysis (ASSA)
- beyondWhittle: Bayesian Spectral Inference for Stationary Time Series
- BMAmevt: Multivariate Extremes: Bayesian Estimation of the Spectral Measure
- bsamGP: Bayesian Spectral Analysis Models using Gaussian Process Priors
- bspec: Bayesian Spectral Inference
- cohortBuilder: Data Source Agnostic Filtering Tools
- EMD: Empirical Mode Decomposition and Hilbert Spectral Analysis
- FKF: Fast Kalman Filter
- FKF.SP: Fast Kalman Filtering Through Sequential Processing
- frequencyConnectedness: Spectral Decomposition of Connectedness Measures
- kalmanfilter: Kalman Filter
- KFAS: Kalman Filter and Smoother for Exponential Family State Space Models
- kimfilter: Rcpp' implementation of the multivariate Kim filter, which combines the Kalman and Hamilton filters for state probability inference
- LMfilteR: Filter Methods for Parameter Estimation in Linear and Non Linear Regression Models
- mlr3filters: Filter Based Feature Selection for 'mlr3'
- multitaper: Spectral Analysis Tools using the Multitaper Method
- neverhpfilter: An Alternative to the Hodrick-Prescott Filter
- praznik: Tools for Information-Based Feature Selection and Scoring

- psd: Adaptive, Sine-Multitaper Power Spectral Density and Cross Spectrum Estimation
- psdr: Use Time Series to Generate and Compare Power Spectral Density
- quantspec: Quantile-Based Spectral Analysis of Time Series
- Rfssa: Functional Singular Spectrum Analysis
- rhosa: Higher-Order Spectral Analysis
- robfilter: Robust Time Series Filters
- RobKF: Innovative and/or Additive Outlier Robust Kalman Filtering
- RSpectra: Solvers for Large-Scale Eigenvalue and SVD Problems
- Rssa: A Collection of Methods for Singular Spectrum Analysis
- Rwave: Time-Frequency Analysis of 1-D Signals
- SLBDD: Statistical Learning for Big Dependent Data
- spectral: Common Methods of Spectral Data Analysis
- Spectrum: Fast Adaptive Spectral Clustering for Single and Multi-View Data
- spooky: Time Feature Extrapolation Using Spectral Analysis and Jack-Knife Resampling
- wavethresh: Wavelets Statistics and Transforms

7.25 Forecasting time series

Collections of resources

List of links:

- Popular Python Time Series Packages
- State of the art research (with codes) on time series forecasting

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- anticipy: time series forecasting
- atspy: Automated Time Series Models in Python
- Autoformer: Decomposition Transformers with Auto-Correlation for Long-Term Series Forecasting
- AutoTS: Automated Time Series Forecasting
- Auto_TS: Automatically build multiple Time Series models using a Single Line of Code
- Clairvoyance: Unified, End-to-End AutoML Pipeline for Medical Time Series
- darts: toolkit by Unit8 for easy manipulation and forecasting of time series
- ETNA Time Series Library by Tinkoff AI
- fbprophet: forecasting toolkit by Facebook
- fireTS: multi-variate time series prediction library working with sklearn
- Flow Forecast: Deep learning PyTorch library for time series forecasting, classification, and anomaly detection

- glum: Generalized linear models
- GluonTS: toolkit by Amazon for Probabilistic time series modeling in Python
- greykite: flexible, intuitive and fast forecasting library by LinkedIn
- hcrystallball: unifies the API for most commonly used libraries and modeling techniques for time-series forecasting in the Python ecosystem
- HierarchicalForecast: Hierarchical forecasting with statistical and econometric methods
- kats: tookit by Facebook for time series analysis and forecasting
- lazypredict: build models without much code
- Local Cascade Ensemble (LCE) is a high-performing, scalable and user-friendly machine learning method for the general tasks of Classification and Regression
- MAPIE: scikit-learn-compatible module for estimating prediction intervals.
- Merlion: A Machine Learning Framework for Time Series Intelligence by SalesForce
- MLForecast: Scalable machine learning based time series forecasting
- NGBoost: Natural Gradient Boosting for Probabilistic Prediction
- N-HiTS: Neural Hierarchical Interpolation for Time Series Forecasting
- NeuralForecast: time series forecasting with deep learning models
- nixtla: Automated time series processing and forecasting
- Orbit: Bayesian forecasting package by Uber
- piecewise-regression: For fitting straight line models to data with one or more breakpoints where the gradient changes
- pmdarima: tatistical library designed to fill the void in Python's time series analysis capabilities
- predictionrevisited: implements the core statistical concepts from the book "Prediction Revisited: The Importance of Observation"
- Prophet: Automatic Forecasting Procedure by Facebook
- PyAF: Automatic Time Series Forecasting
- PyFlux: modern time series models, nference options (frequentist and Bayesian) that can be applied to these models
- pyFTS: Fuzzy Time Series for Python
- pysf: Supervised forecasting of sequential data by UK national institute for data science and artificial intelligence
- PyTorch Forecasting: Forecasting timeseries with PyTorch - dataloaders, normalizers, metrics and models
- pyts: time series classification
- pytsal: Time Series analysis, visualization, forecasting along with AutoTS
- scikit-hts: Hierarchical Time Series Forecasting
- scikit-learn: machine learning in Python

- sktime: unified framework for machine learning with time series by UK national institute for data science and artificial intelligence
- slearn: package linking symbolic representation with scikit-learn machine learning
- statsforecast: Lightning fast forecasting with statistical and econometric models
- Statsmodels: statistical modeling and econometrics in Python
- tbats: BATS and TBATS time series forecasting methods
- timemachines: Autonomous, univariate, k-step ahead time-series forecasting functions assigned Elo ratings
- TIMEX: time series forecasting as a service
- TSCV: Time Series CrossValidation
- ts-eval: Time Series analysis and evaluation tools
- tslearn: machine learning toolkit dedicated to time series data

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ACV: Optimal Out-of-Sample Forecast Evaluation and Testing under Stationarity
- AIafter: Forecast Combination Using the AI-AFTER Algorithm
- arfima: Fractional ARIMA (and Other Long Memory) Time Series Modeling
- ATAforecasting: Automatic Time Series Analysis and Forecasting Using the Ata Method
- autoTS: Automatic Model Selection and Prediction for Univariate Time Series
- baguette: Efficient Model Functions for Bagging
- bigtime: Sparse Estimation of Large Time Series Models
- BINtools: Bayesian BIN (Bias, Information, Noise) Model of Forecasting
- boot.pval: Bootstrap p-Values
- caretForecast: Time Series Forecasting Using Caret Infrastructure
- cvms: Cross-Validation for Model Selection
- dsos: Dataset Shift with Outlier Scores
- ensembleBMA: Probabilistic Forecasting using Ensembles and Bayesian Model Averaging
- fable: Forecasting Models for Tidy Time Series
- fable.ata: ATAforecasting Modelling Interface for fable Framework
- fable.prophet: Prophet Modelling Interface for 'fable'
- fabletools: Core Tools for Packages in the 'fable' Framework
- FinnTS: Microsoft Finance Time Series Forecasting Framework
- flexmix: Flexible Mixture Modeling
- ForeCA: Forecastable Component Analysis

- ForecastComb: Forecast Combination Methods
- forecastHybrid: Convenient Functions for Ensemble Time Series Forecasts
- forecastML: Time Series Forecasting with Machine Learning Methods
- forecastSNSTS: Forecasting for Stationary and Non-Stationary Time Series
- ForecastTB: Test Bench for the Comparison of Forecast Methods
- FoReco: Point Forecast Reconciliation
- forecTheta: Forecasting Time Series by Theta Models
- fpp3: Data for "Forecasting: Principles and Practice" (3rd Edition)
- fracdiff: Fractionally Differenced ARIMA aka ARFIMA(P,d,q) Models
- fwildclusterboot: Fast Wild Cluster Bootstrap Inference for Linear Models
- greybox: Toolbox for Model Building and Forecasting
- Greymodels: Shiny App for Grey Forecasting Model
- hts: Hierarchical and Grouped Time Series
- ipred: Improved Predictors
- legion: Forecasting Using Multivariate Models
- MAPA: Multiple Aggregation Prediction Algorithm
- mFLICA: Leadership-Inference Framework for Multivariate Time Series
- modeltime: The Tidymodels Extension for Time Series Modeling
- modeltime.ensemble: Ensemble Algorithms for Time Series Forecasting with Modeltime
- modeltime.gluonts: 'GluonTS' Deep Learning
- modeltime.resample: Resampling Tools for Time Series Forecasting
- ngboostForecast: Probabilistic Time Series Forecasting
- OOS: Out-of-Sample Time Series Forecasting
- origami: Generalized Framework for Cross-Validation
- pre: Prediction Rule Ensembles
- predtoolsTS: Time Series Prediction Tools
- profoc: Probabilistic Forecast Combination Using CRPS Learning
- prophet: Automatic Forecasting Procedure
- PSF: Forecasting of Univariate Time Series Using the Pattern Sequence-Based Forecasting (PSF) Algorithm
- PTSR: Positive Time Series Regression
- RFpredInterval: Prediction Intervals with Random Forests and Boosted Forests
- rigr: Regression, Inference, and General Data Analysis Tools in R
- Rlgt: Bayesian Exponential Smoothing Models with Trend Modifications

- robets: Forecasting Time Series with Robust Exponential Smoothing
- robustarima: Robust ARIMA Modeling
- scoringfunctions: A Collection of Scoring Functions for Assessing Point Forecasts
- scoringRules: Scoring Rules for Parametric and Simulated Distribution Forecasts
- scoringutils: Utilities for Scoring and Assessing Predictions
- s2dverification: Set of Common Tools for Forecast Verification
- see: Visualisation Toolbox for 'easystats' and Extra Geoms, Themes and Color Palettes for 'ggplot2'
- seer: Feature-Based Forecast Model Selection
- segmented: Regression Models with Break-Points / Change-Points Estimation
- sense: Automatic Stacked Ensemble for Regression Tasks
- shrink: Global, Parameterwise and Joint Shrinkage Factor Estimation
- SLBDD: Statistical Learning for Big Dependent Data
- smooth: Forecasting Using State Space Models
- spcr: Sparse Principal Component Regression
- SPlit: Split a Dataset for Training and Testing
- StabilizedRegression: Stabilizing Regression and Variable Selection
- stacks: Tidy Model Stacking
- subsemble: An Ensemble Method for Combining Subset-Specific Algorithm Fits
- tensorTS: Factor and Autoregressive Models for Tensor Time Series
- tfarima: Transfer Function and ARIMA Models
- thief: Temporal Hierarchical Forecasting
- tidymv: Tidy Model Visualisation for Generalised Additive Models
- traineR: Predictive Models Homologator
- TSdeeplearning: Deep Learning Model for Time Series Forecasting
- tsDyn: Nonlinear Time Series Models with Regime Switching
- tsensembler: Dynamic Ensembles for Time Series Forecasting
- TSPred: Functions for Benchmarking Time Series Prediction
- TSstudio: Functions for Time Series Analysis and Forecasting
- tsutils: Time Series Exploration, Modelling and Forecasting
- tswge: Time Series for Data Science.Accompanies the texts Time Series for Data Science and Applied Time Series Analysis with R,
- vars: VAR Modelling
- yardstick: Tidy Characterizations of Model Performance
- yhat: Interpreting Regression Effects

7.26 Graphs and graphical modeling

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- ogb: Benchmark datasets, data loaders, and evaluators for graph machine learning
- pathpy: analysis of time series data on networks using higher-order and multi-order graphical models
- PGM: Probabilistic Graphical Models
- pgmpy: Probabilistic Graphical Models
- PGM_PyLib: Inference and Learning of Probabilistic Graphical Models
- pyaGrUM: Bayesian networks and other Probabilistic Graphical Models
- scikit-network: nalysis of large graphs
- skggm: Scikit-learn compatible estimation of general graphical models
- vishwakarma: visualization library for Probabilistic Graphical Models, Discrete & Continuous Distributions, and a lot more

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- backbone: Extracts the Backbone from Graphs
- deepgp: Deep Gaussian Processes using MCMC
- gmgm: Gaussian Mixture Graphical Model Learning and Inference
- pcalg: Methods for Graphical Models and Causal Inference
- Revticulate: Interaction with "RevBayes" in R
- tgp: Bayesian Treed Gaussian Process Models
- tidygraph: A Tidy API for Graph Manipulation

7.27 Linear algebra

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- arctic: High performance datastore by Man Group for time series and tick data
- PyArma: Linear algebra library for Python
- PyArmadillo: an alternative approach to linear algebra in Python
- PyPardiso: Python interface to the Intel MKL Pardiso library to solve large sparse linear systems of equations
- Scipy: mathematics, science, and engineering

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- EigenR: Complex Matrix Algebra with 'Eigen'
- fastmatrix: Fast Computation of some Matrices Useful in Statistics
- freqdom: Frequency Domain Based Analysis: Dynamic PCA
- ica: Independent Component Analysis
- Matrix: Sparse and Dense Matrix Classes and Methods
- MatrixExtra: Extra Methods for Sparse Matrices
- matsbyname: An Implementation of Matrix Mathematics
- proxyC: Computes Proximity in Large Sparse Matrices
- rARPACK: Solvers for Large Scale Eigenvalue and SVD Problems
- RcppArmadillo: 'Rcpp' Integration for the 'Armadillo' Templated Linear Algebra Library
- RcppEigen: 'Rcpp' Integration for the 'Eigen' Templated Linear Algebra Library
- Rlinsolve: Iterative Solvers for (Sparse) Linear System of Equations
- RSpectra: Solvers for Large-Scale Eigenvalue and SVD Problems
- sanic: Solving Ax = b Nimbly in C++
- SparseChol: Sparse Cholesky LDL Decomposition of Symmetric Matrices
- SparseM: Sparse Linear Algebra
- svd: Interfaces to Various State-of-Art SVD and Eigensolvers

7.28 Machine Learning

Collections of resources

List of links:

- Curated list of open source libraries to deploy, monitor, version and scale machine learning
- Dive into Machine Learning
- Artificial Intelligence and Machine Learning For Quantum Technologies

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best Subset Selection
- AIF360: comprehensive set of fairness metrics for datasets and machine learning models, explanations for these metrics, and algorithms to mitigate bias in datasets and models
- benchmark_VAE: Unifying Generative Autoencoder implementations in Python
- bindsnet: Simulation of spiking neural networks (SNNs) using PyTorch
- biosphere: Simple, fast random forests

- Catalyst: PyTorch framework for Deep Learning Research and Development
- catboost: Gradient Boosting on Decision Trees by Yandex
- Chainer: flexible framework of neural networks for deep learning
- combo: A Python Toolbox for Machine Learning Model Combination
- compose: machine learning tool for automated prediction engineering
- coremltools: convert machine learning models from third-party libraries to the Core ML format (by Apple)
- CrypTen: framework for Privacy Preserving Machine Learning
- DeepChecks: Testing and Validating ML Models and Data
- DoubleML: Double Machine Learning in Python
- Driblet - Google Cloud based ML pipeline by Google
- geotorch: Constrained optimization toolkit for PyTorch
- GPyTorch: Gaussian processes for modern machine learning systems.
- Hub for Tensorflow: library for transfer learning by reusing parts of TensorFlow models
- Hummingbird: library by Microsoft for compiling trained traditional ML models into tensor computations
- InvarianceUnitTests: Linear unit-tests for invariance discovery
- JAX: toolkit by Google for composable transformations of Python+NumPy programs: differentiate, vectorize, JIT to GPU/TPU, and more
- jraph: Graph Neural Network Library in Jax
- karateclub: Framework for Unsupervised Learning on Graphs
- keras: deep learning API written in Python, running on top of the machine learning platform TensorFlow
- Local Cascade Ensemble (LCE) is a high-performing, scalable and user-friendly machine learning method for the general tasks of Classification and Regression
- LightGBM: fast, distributed, high performance gradient boosting (GBT, GBDT, GBRT, GBM or MART) framework by Microsoft
- Merlion: A Machine Learning Framework for Time Series Intelligence by SalesForce
- mlflow: Interface to 'MLflow'
- MLForecast: Scalable machine learning based time series forecasting
- mlinsights: Extends scikit-learn with new models, transformers, metrics, plotting.
- MLJAR Automated Machine Learning for Humans
- mlxtend: extension and helper modules for Python's data analysis and machine learning libraries.
- MMdnn: toolkit by Microsoft to convert models between Caffe, Keras, MXNet, Tensorflow, CNTK, PyTorch Onnx and CoreML.
- Model Garden for TensorFlow
- mvlearn is an open-source Python software package for multiview learning tools.

- NannyM: estimate post-deployment model performance (without access to targets), detect data drift, and intelligently link data drift alerts back to changes in model performance
- NeuralForecast: time series forecasting with deep learning models
- NGBoost: Natural Gradient Boosting for Probabilistic Prediction
- nimbusml: toolkit by Microsoft that provides Python bindings for ML.NET
- nolearn: Combines the ease of use of scikit-learn with the power of Theano/Lasagne
- norse: Deep learning with spiking neural networks (SNNs) in PyTorch.
- OPACUS: Training PyTorch models with differential privacy
- ptgnn: PyTorch Graph Neural Network Library
- PyCaret : machine learning library
- PyTorch: Tensors and Dynamic neural networks in Python with strong GPU acceleration
- PyTorch Lightning: lightweight PyTorch wrapper for ML researchers
- Ray: packaged with RLlib, a scalable reinforcement learning library, and Tune, a scalable hyperparameter tuning librar
- scikit-learn: machine learning in Python
- scikit-learn-intelex: Intel Extension for Scikit-learn
- sklearn-onnx converts scikit-learn models to ONNX
- skorch: scikit-learn compatible neural network library that wraps PyTorch
- SNNTORCH: Deep and online learning with spiking neural networks
- tensorflow: end-to-end open source platform for machine learning
- tf2onnx: Convert TensorFlow, Keras, Tensorflow.js and Tflite models to ONNX
- Transfer Learning Library for Domain Adaptation, Task Adaptation, and Domain Generalization
- transformers: State-of-the-art Machine Learning for Pytorch, TensorFlow, and JAX
- Trax: Deep Learning by Google with Clear Code and Speed
- tslearn: machine learning toolkit dedicated to time-series data
- xformers: Hackable and optimized Transformers building blocks, supporting a composable construction
- yellowbrick: Visual analysis and diagnostic tools to facilitate machine learning model selection

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best Subset Selection
- agua: 'tidymodels' Integration with 'h2o'
- APML: An Approach for Machine-Learning Modelling
- arenar: Arena for the Exploration and Comparison of any ML Models
- brulee: High-Level Modeling Functions with 'torch'

- distillML: Model Distillation and Interpretability Methods for Machine Learning Models
- elmNNRcpp: The Extreme Learning Machine Algorithm
- fairmodels: Flexible Tool for Bias Detection, Visualization, and Mitigation
- familiar: End-to-End Automated Machine Learning and Model Evaluation
- KernelKnn: Extends the simple k-nearest neighbors algorithm by incorporating numerous kernel functions and a variety of distance metrics
- lightgbm: Light Gradient Boosting Machine by Microsoft
- MachineShop: Machine Learning Models and Tools
- mcboost: Multi-Calibration Boosting
- MetricsWeighted: Weighted Metrics, Scoring Functions and Performance Measures for Machine Learning
- mikropml: User-Friendly R Package for Supervised Machine Learning Pipelines
- mlflow: Interface to 'MLflow'
- mlquantify: Algorithms for Class Distribution Estimation
- mlr3: Machine Learning in R - Next Generation
- mlr3cluster: Cluster Extension for 'mlr3'
- mlr3learners: Recommended Learners for 'mlr3'
- mlr3tuning: hyperparameter tuning with 'mlr3'
- mlr3verse: package family is a set of packages for machine-learning purposes built in a modular fashion
- mlr3viz: Visualizations for'mlr3
- mlrintermbo: Model-Based Optimization for 'mlr3' Through 'mlrMBO'
- mlrMBO: Bayesian Optimization and Model-Based Optimization of Expensive Black-Box Functions
- multiview: Cooperative Learning for Multi-View Analysis
- rTorch: R Bindings to 'PyTorch'
- SPlit: Split a Dataset for Training and Testing
- tensorflow: R Interface to 'TensorFlow'
- tfdatasets: Interface to 'TensorFlow' Datasets
- tfprobability: Interface to 'TensorFlow Probability'
- TSdeeplearning: Deep Learning Model for Time Series Forecasting
- xgboost: Extreme Gradient Boosting

7.29 Machine Learning frameworks (includes Automated ML and hyperparameters tuning)

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- AI2 Tango: library for choreographing machine learning research
- AutoGluon: toolkit by Amazon on AutoML for Text, Image, and Tabular Data
- AutoKeras: An AutoML system based on Keras
- AutoPyTorch: Automatic architecture search and hyperparameter optimization for PyTorch
- auto-sklearn: Automated Machine Learning with scikit-learn
- BayesianOptimization: global optimization with gaussian processes.
- cesium: Machine Learning Time-Series Platform
- Clairvoyance: Unified, End-to-End AutoML Pipeline for Medical Time Series
- Colossal-AI: A Unified Deep Learning System for Big Model Era
- EvalML is an AutoML library which builds, optimizes, and evaluates machine learning pipelines using domain-specific objective functions.
- FLAML: accurate machine learning models automatically, efficiently and economically (by Microsoft)
- flax: neural network library for JAX that is designed for flexibility
- H2O is an Open Source, Distributed, Fast & Scalable Machine Learning Platform
- Hypernets: General Automated Machine Learning framework
- HyperOpt: Distributed Asynchronous Hyperparameter Optimization
- hyperopt-sklearn: Hyper-parameter optimization for sklearn
- kedro: framework for creating reproducible, maintainable and modular data science code
- kedro-viz: Visualise your Kedro data and machine-learning pipelines and track your experiments.
- keras-tuner: hyperparameter optimization framework
- MLBox: Automated Machine Learning library
- mlpack: 'Rcpp' Integration for the 'mlpack' Library
- mlr3tuning: Tuning for 'mlr3'
- model_search: framework (by Google) that implements AutoML algorithms for model architecture search at scale
- NannyM: estimate post-deployment model performance (without access to targets), detect data drift, and intelligently link data drift alerts back to changes in model performance
- NNI: toolkit by Microsoft to help users automate Feature Engineering, Neural Architecture Search, Hyperparameter Tuning and Model Compression
- oneflow: OneFlow is a deep learning framework designed to be user-friendly, scalable and efficient.
- ONNX: Open Neural Network Exchange is an Open standard for machine learning interoperability

- Optuna: hyperparameter optimization framework
- PyCaret : machine learning library
- squirrel-core: library that enables ML teams to share, load, and transform data in a collaborative, flexible, and efficient way.
- Relevance AI - The ML Platform for Unstructured Data Analysis
- Talos: Hyperparameter Optimization for TensorFlow, Keras and PyTorch
- trax: end-to-end library (by Google Brain) for deep learning that focuses on clear code and speed.
- tune-sklearn: drop-in replacement for Scikit-Learn's GridSearchCV / RandomizedSearchCV – but with cutting edge hyperparameter tuning techniques
- vowpal_wabbit: machine learning system which pushes the frontier of machine learning with techniques such as online, hashing, allreduce, reductions, learning2search, active, and interactive learning

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- autokeras: R Interface to 'AutoKeras'
- automl: Deep Learning with Metaheuristic
- DriveML: Self-Drive Machine Learning Projects
- familiar: End-to-End Automated Machine Learning and Model Evaluation
- mlpack: 'Rcpp' Integration for the 'mlpack' Library
- mlr3tuningspaces: Search Spaces for Hyperparameter Tuning
- ParBayesianOptimization: Parallel Bayesian Optimization of Hyperparameters
- rBayesianOptimization: Bayesian Optimization of Hyperparameters
- RemixAutoML: automation of machine learning, forecasting, feature engineering, model evaluation, model interpretation, recommenders, and EDA.

7.30 Network and graph analysis

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- dantro: handle, transform, and visualize hierarchically structured data
- deeptime: nalysis of time series data including dimensionality reduction, clustering, and Markov model estimation
- ETNA Time Series Library by Tinkoff AI
- fastpath: find the path through a network of nodes
- GraKeL: scikit-learn compatible library for graph kernels
- grapharray: handle network link/node attributes as Numpy arrays
- GraphVite: A General and High-performance Graph Embedding System
- karateclub: Framework for Unsupervised Learning on Graphs

- netrd: etwork {reconstruction, distances, dynamics}
- networkit: toolkit for large-scale network analysis
- NetworkX: Network Analysis in Python
- pandana: Pandas Network Analysis: fast accessibility metrics and shortest paths, using contraction hierarchies
- pyvis: visualizing interactive network graphs
- rustworkx: high performance Python graph library implemented in Rust
- scikit-learn: machine learning in Python
- tslearn: machine learning toolkit dedicated to time-series data

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- backbone: identify the most 'important' or 'significant' edges in a network
- bnmonitor: An Implementation of Sensitivity Analysis in Bayesian Networks
- bootnet: Bootstrap Methods for Various Network Estimation Routines
- CINNA: Deciphering Central Informative Nodes in Network Analysis
- dbnR: Dynamic Bayesian Network Learning and Inference
- diceR: Diverse Cluster Ensemble in R
- dtwclust: Time Series Clustering Along with Optimizations for the Dynamic Time Warping Distance
- fabisearch: Change Point Detection in High-Dimensional Time Series Networks
- fastkmedoids: Faster K-Medoids Clustering Algorithms: FastPAM, FastCLARA, FastCLARANS
- gRain: Graphical Independence Networks
- heatmaply: Interactive Cluster Heat Maps Using 'plotly' and 'ggplot2'
- influential: Identification and Classification of the Most Influential Nodes
- MatTransMix: Clustering with Matrix Gaussian and Matrix Transformation Mixture Models
- Mercator: Clustering and Visualizing Distance Matrices
- MixSim: Simulating Data to Study Performance of Clustering Algorithms
- mixture: Mixture Models for Clustering and Classification
- MKMeans: A Modern K-Means (MKMeans) Clustering Algorithm
- ndtv: Network Dynamic Temporal Visualizations
- network: Classes for Relational Data
- networkABC: Network Reverse Engineering with Approximate Bayesian Computation
- networkDynamic: Dynamic Extensions for Network Objects
- NetworKit: tool suite for high-performance network analysis
- networktools: Tools for Identifying Important Nodes in Networks

- statnet: Software Tools for the Statistical Analysis of Network Data
- visNetwork: Network Visualization using 'vis.js' Library
- wdnet: Weighted and Directed Networks
- WGCNA: Weighted Correlation Network Analysis

7.31 Numerical methods (includes numerical optimization)

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- ADE: Asynchronous Differential Evolution, with efficient multiprocessing
- autoray: Write numeric code that automatically works with any numpy-ish libraries
- BayesianOptimization: global optimization with gaussian processes
- CasADi is a symbolic framework for numeric optimization implementing automatic differentiation in forward and reverse modes on sparse matrix-valued computational graphs
- cmaes: Covariance Matrix Adaptation Evolution Strategy (CMA-ES)
- coco: Numerical Black-Box Optimization Benchmarking Framework
- cp_solver: CP-SAT Solver by Google
- cvxopt: convex optimization
- cvxpy: convex optimization
- DEAP: Distributed Evolutionary Algorithms in Python
- derivative: Numerical differentiation of noisy time series data
- Differential Evolution expensiveopt
- eigenpy: Efficient Python bindings between Numpy/Eigen
- ELA drframework: Dimensionality Reduction Framework for Exploratory Landscape Analysis
- evol: grammar for evolutionary algorithms and heuristics
- fcmaes complements scipy optimize by providing additional optimization methods, faster C++/Eigen based implementations and a coordinated parallel retry mechanism.
- gemseo: Generic Engine for Multi-disciplinary Scenarios, Exploration and Optimization
- General Purpose Optimization Library GPOL
- HiGHS: Linear optimization
- hyperactive: optimization and data collection toolbox for convenient and fast prototyping of computationally expensive models
- ipopt: Cython interface for the interior point optimzer IPOPT
- ipyopt: interface for the interior point optimizer COIN-OR IPOpt
- mystic: highly-constrained non-convex optimization and uncertainty quantification
- nevergrad: Python toolbox for performing gradient-free optimization by Facebook

- nlopt: nonlinear optimization
- Open MDAO: optimization framework
- optima: library for numerical optimization calculations
- OR-Tools: optimization toolkit by Google
- osqp: Operator Splitting QP Solver
- pybobyqa: Derivative-Free Optimization with Bound Constraints
- pycma: Covariance Matrix Adaptation Evolution Strategy (CMA-ES)
- pymoo: Multi-objective Optimization
- pyomo: supports a diverse set of optimization capabilities for formulating and analyzing optimization models.
- PyOptSparse: object-oriented framework for formulating and solving nonlinear constrained optimization problems
- PyPDE: solve partial differential equations using finite differences.
- qpsolvers: Quadratic programming solvers in Python with a unified API
- root_numpy: interface between ROOT and NumPy
- scikit-opt: Swarm Optimization methods
- scikit-optimize: Sequential model-based optimization with a ‘scipy.optimize‘ interface
- Scipy: Fundamental algorithms for scientific computing
- SHADE: Success-History Based Parameter Adaptation for Differential Evolution
- stgaircase: data analysis package based on mathematical step functions
- theseus: differentiable nonlinear optimization
- torchquad: High-performance numerical integration on the GPU with PyTorch, JAX and Tensorflow
- torchsde: Differentiable SDE solvers with GPU support and efficient sensitivity analysis
- trust-region:trust-region subproblem solvers for nonlinear optimization

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ao: Alternating Optimization
- bbotk: Black-Box Optimization Toolkit
- CGNM: Cluster Gauss-Newton Method: Find multiple solutions of a nonlinear least squares problem
- CVXR: Disciplined Convex Optimization
- DEoptim: Global Optimization by Differential Evolution
- DEoptimR: Differential Evolution Optimization in Pure R
- ECOSolveR: Embedded Conic Solver in R
- ggblanket: Simplify ’ggplot2’ Visualisation

- graDiEnt: derivative-free, optim-style Stochastic Quasi-Gradient Differential Evolution optimization
- itp: The Interpolate, Truncate, Project (ITP) Root-Finding Algorithm
- LowRankQP: Low Rank Quadratic Programming
- miesmuschel: Mixed Integer Evolution Strategies
- minqa: Derivative-Free Optimization Algorithms by Quadratic Approximation
- mlr3mbo: Flexible Bayesian Optimization
- NMOF: Numerical Methods and Optimization in Finance
- osqp: Quadratic Programming Solver using the 'OSQP' Library
- RcppEnsmallen: Header-Only C++ Mathematical Optimization Library for 'Armadillo'
- rvinecopulib: High Performance Algorithms for Vine Copula Modeling
- rgenoud: R Version of GENetic Optimization Using Derivatives
- rmoo: Multi-Objective Optimization in R
- scs: Splitting Conic Solver for linear programs ('LPs'), second-order cone programs ('SOCPs'), semidefinite programs ('SDPs'), exponential cone programs ('ECPs'), and power cone programs ('PCPs'), or problems with any combination of those cone
- SimEngine: A Modular Framework for Statistical Simulations in R
- trustOptim: Trust Region Optimization for Nonlinear Functions with Sparse Hessians

7.32 Probabilistic modeling (includes mixture models and Gaussian Processes)

Links to resources

- Professionally curated list of awesome Conformal Prediction videos, tutorials, books, papers, PhD and MSc theses, articles and open-source libraries

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- beanmachine: inference on probabilistic models
- celerite2: fast and scalable Gaussian Process (GP) Regression
- conformal-rnn: code for "Conformal time-series forecasting", NeurIPS 2021
- crepes: Conformal Regressors and Conformal Predictive Systems
- EnbPI: Ensemble batch prediction intervals
- EnCQR: ensemble conformalized quantile regression (EnCQR)
- GluonTS: toolkit by Amazon for Probabilistic time series modeling in Python
- gptools: Gaussian processes with arbitrary derivative constraints and predictions.
- GPy: Gaussian processes framework
- GPyTorch: Gaussian processes for modern machine learning systems.
- MAPIE: scikit-learn-compatible module for estimating prediction intervals

- NGBoost: Natural Gradient Boosting for Probabilistic Prediction
- orbit-ml: Bayesian forecasting package by Uber
- pgmpy: Probabilistic Graphical Models – learning (Structure and Parameter), inference (Probabilistic and Causal), and simulations in Bayesian Networks
- pplbench: Evaluation Framework for Probabilistic Programming Languages
- PyMC: Bayesian Modeling and Probabilistic Machine Learning with Aesara
- pyro: Deep universal probabilistic programming with Python and PyTorch
- PySloth: Probabilistic Prediction
- skpro: toolkit by UK national institute for data science and artificial intelligence for Supervised domain-agnostic prediction framework for probabilistic modelling
- tinyGP: The tiniest of Gaussian Process libraries
- zhusuan: probabilistic programming library for Bayesian deep learning, generative models, based on Tensorflow

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- AdequacyModel: Adequacy of Probabilistic Models and General Purpose Optimization
- AdMit: Adaptive Mixture of Student-t Distributions
- aldvmm: Adjusted Limited Dependent Variable Mixture Models
- bgmm: Gaussian Mixture Modeling Algorithms and the Belief-Based Mixture Modeling
- bmixture: Bayesian Estimation for Finite Mixture of Distributions
- BNPmix: Bayesian Nonparametric Mixture Models
- bpgmm: Bayesian Model Selection Approach for Parsimonious Gaussian Mixture Models
- ClusterR: Gaussian Mixture Models, K-Means, Mini-Batch-Kmeans, K-Medoids and Affinity Propagation Clustering
- conformalInference.multi: Conformal Inference Tools for Regression with Multivariate Response
- DistributionOptimization: Distribution Optimization
- distributionsrd: Distribution Fitting and Evaluation
- EMCluster: EM Algorithm for Model-Based Clustering of Finite Mixture Gaussian Distribution
- evmix: Extreme Value Mixture Modelling, Threshold Estimation and Boundary Corrected Kernel Density Estimation
- flexmix: Flexible Mixture Modeling
- flexmixNL: Finite Mixture Modeling of Generalized Nonlinear Models
- GauPro: Gaussian Process Fitting
- gmgm: Gaussian Mixture Graphical Model Learning and Inference
- greta.gp: Gaussian Process Modelling in 'greta'

- hmmr: "Mixture and Hidden Markov Models with R" Datasets and Example Code
- ltmix: Left-Truncated Mixtures of Gamma, Weibull, and Lognormal Distributions
- MatrixMixtures: Model-Based Clustering via Matrix-Variate Mixture Models
- MGMM: Missingness Aware Gaussian Mixture Models
- mistr: Mixture and Composite Distributions
- mixComp: Estimation of Order of Mixture Distributions
- MixMatrix: Classification with Matrix Variate Normal and t Distributions
- MixSim: Simulating Data to Study Performance of Clustering Algorithms
- mixsmsn: Fitting Finite Mixture of Scale Mixture of Skew-Normal Distributions
- mixreg: Functions to Fit Mixtures of Regressions
- mixSPE: Mixtures of Power Exponential and Skew Power Exponential Distributions for Use in Model-Based Clustering and Classification
- mixsqp: Sequential Quadratic Programming for Fast Maximum-Likelihood Estimation of Mixture Proportions
- mixtools: Tools for Analyzing Finite Mixture Models
- mixture: Mixture Models for Clustering and Classification
- mclust: Gaussian Mixture Modelling for Model-Based Clustering, Classification, and Density Estimation
- mlr3proba: Probabilistic Supervised Learning for 'mlr3'
- MoMPCA: Inference and Clustering for Mixture of Multinomial Principal Component Analysis
- mvgb: Multivariate Probabilities of Scale Mixtures of Multivariate Normal Distributions via the Genz and Bretz (2002) QRSVN Method
- ngboostForecast: Probabilistic Time Series Forecasting
- nlsmsn: Fitting Nonlinear Models with Scale Mixture of Skew-Normal Distributions
- Nmix: Bayesian Inference on Univariate Normal Mixtures
- nvmix: Multivariate Normal Variance Mixtures
- opGMMassessment: Optimized Automated Gaussian Mixture Assessment
- pgmm: Parsimonious Gaussian Mixture Models
- pGPx: Pseudo-Realizations for Gaussian Process Excursions
- pks: Probabilistic Knowledge Structures
- plgp: Particle Learning of Gaussian Processes
- plotmm: Tidy Tools for Visualizing Mixture Models
- QuantileGH: Quantile Least Mahalanobis Distance Estimator for Tukey g-&-h Mixture
- rebmix: Finite Mixture Modeling, Clustering & Classification
- Revticulate: Interaction with "RevBayes" in R
- RGMM: Robust Mixture Model

- RMixtComp: Mixture Models with Heterogeneous and (Partially) Missing Data
- robmixglm: Robust Generalized Linear Models (GLM) using Mixtures
- Rmixmod: Classification with Mixture Modelling
- RobMixReg: Robust Mixture Regression
- rrMixture: Reduced-Rank Mixture Models
- seqHMM: Mixture Hidden Markov Models for Social Sequence Data and Other Multivariate, Multichannel Categorical Time Series
- skewlmm: Scale Mixture of Skew-Normal Linear Mixed Models
- skewMLRM: Estimation for Scale-Shape Mixtures of Skew-Normal Distributions
- uGMAR: Estimate Univariate Gaussian and Student's t Mixture Autoregressive Models

7.33 Reinforcement learning

Collections of resources

List of links:

- Awesome Reinforcement Learning: Reinforcement learning resources curated
- Awesome Deep RL: curated list of awesome Deep Reinforcement Learning resources

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Acme: a research framework by DeepMind for reinforcement learning
- Baconian: Model-based Reinforcement Learning Framework
- Open AI Baselines: high-quality implementations by OpenAI of reinforcement learning algorithms
- Catalyst.RL: Distributed Framework for Reproducible RL Research
- ChainerRL: deep reinforcement learning library built on top of Chainer
- Coach: Reinforcement Learning by Intel AI Lab
- d3rlpy: offline deep reinforcement learning library
- Decision Transformer: Reinforcement Learning via Sequence Modeling
- DRL with PyTorch: PyTorch implementations of deep reinforcement learning algorithms and environments
- Deep Reinforcement Learning Hands-On
- deer: DEEp Reinforcement learning framework
- Dopamine: research framework by Google for fast prototyping of reinforcement learning algorithms
- ElegantRL: Lightweight and scalable deep reinforcement learning using PyTorch
- FinRL: Deep Reinforcement Learning for Quantitative Finance
- FinRL-Meta: Universe of Near-Real Market Environments for Data-Driven Financial Reinforcement Learning
- garage: toolkit for reproducible reinforcement learning research

- Gym: ttolkit by openAI for toolkit for developing and comparing reinforcement learning algorithms
- HRAC: Generating Adjacency-Constrained Subgoals in Hierarchical Reinforcement Learning
- keras-rl: Deep Reinforcement Learning for Keras
- Mava: library of multi-agent reinforcement learning components and systems
- Multi-Agent Resource Optimization (MARO) platform is an instance of Reinforcement Learning as a Service (RaaS) for real-world resource optimization problems.
- MBRL-Lib: toolbox by Facebook for facilitating development of Model-Based Reinforcement Learning algorithms
- Mushroom RL: modular toolkit able to use modularity allows to use libraries for tensor computation (e.g. PyTorch, Tensorflow) and RL benchmarks (e.g. OpenAI Gym, PyBullet, Deepmind Control Suite)
- PettingZoo: Gym for multi-agent reinforcement learning
- PFRL: PyTorch-based deep reinforcement learning library
- PGPortfolio: Policy Gradient Portfolio
- PyTorchRL: reinforcement learning library focused on modularity and simplicity
- Rainbow: Combining Improvements in Deep Reinforcement Learning
- ReAgent: platform by Facebook for Reasoning systems (Reinforcement Learning, Contextual Bandits, etc.)
- rl: modular, primitive-first, python-first PyTorch library for Reinforcement Learning.
- RLkit: Collection of reinforcement learning algorithms
- RLlib: Ray is packaged with RLlib, a scalable reinforcement learning library, and Tune, a scalable hyperparameter tuning librar
- RLMeta is a light-weight flexible framework for Distributed Reinforcement Learning Research
- rlpyt: Reinforcement Learning in PyTorch
- rlstructures: Facebook library to facilitate the implementation of new reinforcement learning algorithms
- skrl: Modular reinforcement learning
- Stable Baselines3: PyTorch version of Stable Baselines, reliable implementations of reinforcement learning algorithms
- Tensorforce: TensorFlow library for applied reinforcement learning
- TensorLayer: Deep Learning and Reinforcement Learning Library for Scientists and Engineers
- TF-Agents: TensorFlow library for Contextual Bandits and Reinforcement Learning
- Tianshou: PyTorch deep reinforcement learning library
- Tonic RL: Tonic RL library
- TorchBeast: A PyTorch Platform by Facebook for Distributed RL
- TRFL: TensorFlow Reinforcement Learning by DeepMind
- vowpal_wabbit: machine learning system which pushes the frontier of machine learning with techniques such as online, hashing, allreduce, reductions, learning2search, active, and interactive learning

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- Hands-On Reinforcement Learning
- QLearning: Reinforcement Learning using the Q Learning Algorithm
- reinforcelearn: reinforcement learning, including Q-Learning algorithm
- ReinforcementLearning: Model-Free Reinforcement Learning
- RLT: Reinforcement Learning Trees

7.34 Robust numerical methods

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- derivative: Numerical differentiation of noisy time series data
- hypothesize: hypothesis testing using robust statistics
- robusta: interface to many common statistical analyses, performed using through R and RPY2.
- Robustats is a Python library for high-performance computation of robust statistical estimators
- robustbase: Statistical Estimators (Sn, Qn, MAD, IQR)

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- clubSandwich: Cluster-Robust (Sandwich) Variance Estimators with Small-Sample Corrections
- l1spectral: An L1-Version of the Spectral Clustering
- L2E: Robust Structured Regression via the L2 Criterion
- pcaPP: Robust PCA by Projection Pursuit
- RCTS: Clustering Time Series While Resisting Outliers
- RDnp: Robust Test for Complete Independence in High-Dimensions
- revss: Robust Estimation in Very Small Samples
- RGMM: Robust Mixture Model
- rigr: Regression, Inference, and General Data Analysis Tools in R
- robcp: Robust Change-Point Tests
- robcor: Robust Correlations
- robfilter: Robust Time Series Filters
- robmixglm: Robust Generalized Linear Models (GLM) using Mixtures
- RobMixReg: Robust Mixture Regression
- RobStatTM: Robust Statistics: Theory and Methods
- robust: Port of the S+ "Robust Library"

- RobustANOVA: Robust One-Way ANOVA Tests under Heteroscedasticity and Nonnormality
- robustbase: Basic Robust Statistics
- RobustCalibration: Robust Calibration of Imperfect Mathematical Models
- robustcov: Collection of Robust Covariance and (Sparse) Precision Matrix Estimators
- robustHD: Robust Methods for High-Dimensional Data
- rrcov: Scalable Robust Estimators with High Breakdown Point
- RSC: Robust and Sparse Correlation Matrix
- sandwich: Robust Covariance Matrix Estimators
- StabilizedRegression: Stabilizing Regression and Variable Selection
- tsrobprep: Robust Preprocessing of Time Series Data
- walrus: Robust Statistical Methods

7.35 Selection of features, variables, models, data splits

Collections of resources

List of links:

- Data Science Feature Engineering and Selection Tutorials
- Feature Engineering and Selection: A Practical Approach for Predictive Models
- Guide for Feature Engineering and Feature Selection

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best-Subset Selection Library
- boruta_py: Boruta all-relevant feature selection method
- dython: Data analysis tools
- featureclass: Feature engineering library to keep track of feature dependencies, documentation and schema
- feature_engine: library with multiple transformers to engineer and select features for use in machine learning models
- FeatureTools: automated feature engineering
- Featurewiz: advanced feature engineering strategies
- ITMO_FS: Feature selection library
- KnockPy: Knockoffs for controlled variable selection
- kydavra: feature selection
- Py_FS: Feature Selection
- pyHSICLasso: Versatile Nonlinear Feature Selection Algorithm for High-dimensional Data
- python_stepwiseSelection: Automated Backward and Forward Selection

- scikit-learn: machine learning in Python
- scikit-rebate: scikit-learn-compatible Python implementation of ReBATE, a suite of Relief-based feature selection algorithms
- Sklearn-genetic-opt: Hyperparameters tuning and feature selection, using evolutionary algorithms
- sktime: unified framework for machine learning with time series by UK national institute for data science and artificial intelligence
- tsfeatures: Calculates various features from time series data. Python implementation of the R package tsfeatures
- UltraNest: Fit and compare complex models reliably and rapidly. Advanced nested sampling
- zoofs: feature selection using a variety of nature-inspired wrapper algorithms

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- abess: Fast Best-Subset Selection Library
- BAS: Bayesian Variable Selection and Model Averaging using Bayesian Adaptive Sampling
- basad: Bayesian Variable Selection with Shrinking and Diffusing Priors
- BayesVarSel: Bayes Factors, Model Choice and Variable Selection in Linear Models
- bpgmm: Bayesian Model Selection Approach for Parsimonious Gaussian Mixture Models
- bravo: Bayesian Screening and Variable Selection
- care: High-Dimensional Regression and CAR Score Variable Selection
- dials: Tools for Creating Tuning Parameter Values
- EMVS: The Expectation-Maximization Approach to Bayesian Variable Selection
- FeatureTerminatoR: Feature Selection Engine to Remove Features with Minimal Predictive Power
- FSinR: Feature Selection
- fsMTS: Feature Selection for Multivariate Time Series
- gausscov: The Gaussian Covariate Method for Variable Selection
- greybox: Toolbox for Model Building and Forecasting
- hrqglas: Group Variable Selection for Quantile and Robust Mean Regression
- knockoff: The Knockoff Filter for Controlled Variable Selection
- mBvs: Bayesian Variable Selection Methods for Multivariate Data
- MDFS: MultiDimensional Feature Selection
- mlr3fselect: Feature Selection for 'mlr3'
- mplot: Graphical Model Stability and Variable Selection Procedures
- MXM: Feature Selection (Including Multiple Solutions) and Bayesian Networks
- nestfs: Cross-Validated (Nested) Forward Selection

- NonpModelCheck: Model Checking and Variable Selection in Nonparametric Regression
- pcaPP: Robust PCA by Projection Pursuit
- picR: Predictive Information Criteria for Model Selection
- plsVarSel: Variable Selection in Partial Least Squares
- praznik: Tools for Information-Based Feature Selection and Scoring
- prinvars: Principal Variables (methods for reducing the number of features within a data set)
- projpred: Projection Predictive Feature Selection
- Rforestry: Random Forests, Linear Trees, and Gradient Boosting for Inference and Interpretability
- rmcfs: The MCFS-ID Algorithm for Feature Selection and Interdependency Discovery
- rSAFE: Surrogate-Assisted Feature Extraction
- rstanarm: Bayesian Applied Regression Modeling via Stan
- SelectBoost: A General Algorithm to Enhance the Performance of Variable Selection Methods in Correlated Datasets
- SignifReg: Consistent Significance Controlled Variable Selection in Generalized Linear Regression
- sivs: Stable Iterative Variable Selection
- smoothic: Variable Selection Using a Smooth Information Criterion
- SPlit: Split a Dataset for Training and Testing
- splitTools: Tools for Data Splitting
- stabiliser: Stabilising Variable Selection
- stabm: Stability Measures for Feature Selection
- stacks: Tidy Model Stacking
- stepgbm: Stepwise Variable Selection for Generalized Boosted Regression Modeling
- SWIM: Scenario Weights for Importance Measurement
- theft: Tools for Handling Extraction of Features from Time Series
- tornado: Plots for Model Sensitivity and Variable Importance
- valse: Variable Selection with Mixture of Models
- WLasso: Variable Selection for Highly Correlated Predictors

7.36 Sensitivity analysis and numerical derivatives

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- derivative: Numerical differentiation of noisy time series data
- higher: obtain higher order gradients
- jacobi: Numerical derivatives for Python
- JAX: toolkit by Google for composable transformations of Python+NumPy programs: differentiate, vectorize, JIT to GPU/TPU, and more
- OMSens: OpenModelica sensitivity analysis and optimization module
- PyApprox: high-dimensional approximation and uncertainty quantification by Sandia Labs
- SALib: Sensitivity Analysis Library (Contains Sobol, Morris, FAST, and other methods)
- sensitivity: Sensitivity Analysis
- tangent: library (by Google) for automatic differentiation providing Source-to-Source Debuggable Derivatives in Pure Python
- torchsde: Differentiable SDE solvers with GPU support and efficient sensitivity analysis

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- bnmonitor: An Implementation of Sensitivity Analysis in Bayesian Networks
- GSA.UN: Global Sensitivity Analysis Tool
- reval: Argument Table Generation for Sensitivity Analysis
- samon: Sensitivity Analysis for Missing Data
- sensemakr: Sensitivity Analysis Tools for Regression Models
- sensitivity: Global Sensitivity Analysis of Model Outputs
- sensobol: Computation of Variance-Based Sensitivity Indices
- SWIM: Scenario Weights for Importance Measurement
- tornado: Plots for Model Sensitivity and Variable Importance

7.37 Statistics and Probability

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- distfit: probability density function fitting and hypothesis testing
- empiricaldist: empirical distribution functions
- momentum: Running mean, variance, skew, and kurtosis
- pingouin: Statistical package in Python based on Pandas
- probs: Probability library

- PyProbables: Probabilistic data structures in python
- PyStats: statistical analysis and distributions
- RunStats: Computing Statistics and Regression in One Pass
- statsmodels: statistical modeling and econometrics
- tensorflow-probability: Probabilistic reasoning and statistical analysis in TensorFlow
- wquantiles: Weighted quantiles

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- arsenal: An Arsenal of 'R' Functions for Large-Scale Statistical Summaries
- ashr: Methods for Adaptive Shrinkage, using Empirical Bayes
- confintr: Confidence Intervals
- DEM: The Distributed EM Algorithms in Multivariate Gaussian Mixture Models
- DescTools: Tools for Descriptive Statistics
- distr6: The Complete R6 Probability Distributions Interface
- distr: Object Oriented Implementation of Distributions
- distrEx: Extensions of Package 'distr'
- distributionsrd: Distribution Fitting and Evaluation
- DPQ: Density, Probability, Quantile ('DPQ') Computations
- EasyDescribe: A Convenient Way of Descriptive Statistics
- entropy: Estimation of Entropy, Mutual Information and Related Quantities
- estimatr: Fast Estimators for Design-Based Inference
- evd: Functions for Extreme Value Distributions
- expectreg: Expectile and Quantile Regression
- fitur: Fit Univariate Distributions
- fromo: Fast Robust Moments
- Gmedian: Geometric Median, k-Medians Clustering and Robust Median PCA
- HSAUR3: A Handbook of Statistical Analyses Using R (3rd Edition)
- lmom: L-Moments
- lmomco: L-Moments, Censored L-Moments, Trimmed L-Moments, L-Comoments, and Many Distributions
- matrixdist: Statistics for Matrix Distributions
- MatrixModels: Modelling with Sparse and Dense Matrices
- matrixStats: Functions that Apply to Rows and Columns of Matrices (and to Vectors)
- minsample2: The Minimum Sample Size

- mlquantify: Algorithms for Class Distribution Estimation
- mvtnorm: Multivariate Normal and t Distributions
- NNS: Nonlinear nonparametric statistics using partial moments
- overlapping: Estimation of Overlapping in Empirical Distributions
- PCDimension: Finding the Number of Significant Principal Components
- philentropy: Similarity and Distance Quantification Between Probability Functions
- pls: Partial Least Squares and Principal Component Regression
- psre: Presenting Statistical Results Effectively
- Qest: Quantile-Based Estimator
- qp: Quantile parametrization for probability distribution functions
- RcppRoll: Efficient Rolling / Windowed Operations
- revss: Robust Estimation in Very Small Samples
- RobStatTM: Robust Statistics: Theory and Methods
- robustbase: Basic Robust Statistics
- roll: Rolling and Expanding Statistics
- statsExpressions: Tidy Dataframes and Expressions with Statistical Details
- walrus: Robust Statistical Methods
- weights: Weighting and Weighted Statistics

7.38 Stress testing, rare events, extreme values and scenarios, survival analysis

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- pyextremes: Extreme Value Analysis
- pycox is a python package for survival analysis and time-to-event prediction with PyTorch
- scikit-extremes: univariate extreme value calculations

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- BMAmevt: Multivariate Extremes: Bayesian Estimation of the Spectral Measure
- climextRemes: Tools for Analyzing Climate Extremes
- extRemes: Extreme Value Analysis
- extremeStat: Extreme Value Statistics and Quantile Estimation
- evd: Functions for Extreme Value Distributions
- evmix: Extreme Value Mixture Modelling, Threshold Estimation and Boundary Corrected Kernel Density Estimation

- ExtremalDep: Extremal Dependence Models
- ExtremeRisks: Extreme Risk Measures
- lax: Loglikelihood Adjustment for Extreme Value Models
- lite: Likelihood-Based Inference for Time Series Extremes
- mev: Modelling of Extreme Values
- survivalmodels: Models for Survival Analysis

7.39 Symbolic regression & data-driven model discovery and machine learning

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- 2SEGP: Simple Simultaneous Ensemble Learning in Genetic Programming
- AIFeynman: Physics-Inspired Method for Symbolic Regression
- BindingGP: Symbolic Regression with Dimension Calculation
- Data Driven Symbolic Regression
- DEAP: Distributed Evolutionary Algorithms
- DeepSymReg: Neural Network-Based Symbolic Regression in Deep Learning for Scientific Discovery
- DeepSymRegTorch: PyTorch implementation of the EQL network, a neural network for symbolic regression
- Deep symbolic optimization
- diffeqpy: Solving differential equations in Python using DifferentialEquations.jl and the SciML Scientific Machine Learning organization
- ellyn: python-wrapped version of ellen, a linear genetic programming system for symbolic regression and classification
- EQLearner: A Seq2Seq approach to Symbolic Regression
- ffx: Fast Function Extraction for symbolic regressio
- geppy: framework for gene expression programming
- gplearn: Genetic Programming in Python, with a scikit-learn inspired API
- hal-cgp: Cartesian genetic programming
- Neural Symbolic Regression That Scales
- pyglyph: library based on deap providing abstraction layers for symbolic regression problems
- pymbolic: Easy Expression Trees and Term Rewriting
- PySR: High-Performance Symbolic Regression in Python
- PySINDy: sparse identification of nonlinear dynamical systems from data
- pySRURGS: Symbolic regression by uniform random global search
- salmon-lm: symbolic algebra of linear regression and modeling
- slearn: package linking symbolic representation with scikit-learn machine learning

- SR Bench: benchmark framework for symbolic regression
- SymEngine is a fast symbolic manipulation library
- symfit: Symbolic Fitting; fitting as it should be.
- symbolic experiments: Repository for symbolic regression/classification experiments
- Symbolic Regression Boosting
- Simpy: symbolic mathematics
- symreg: A Symbolic Regression engine

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- DiffEqR: Solving differential equations in R using DifferentialEquations.jl and the SciML Scientific Machine Learning ecosystem
- gramEvol: Grammatical Evolution for R
- symbolicDA: Analysis of Symbolic Data
- symengine: Interface to the 'SymEngine' Library

7.40 Testing (numerical, statistical, etc.), comparison and ranking

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- AutoTS: Automated Time Series Forecasting
- darts: toolkit by Unit8 for easy manipulation and forecasting of time series
- goftests: Generic goodness of fit tests for random plain old data
- hypothesize: hypothesis testing using robust statistics
- hypothetical: Hypothesis and statistical testing
- hyppo: multivariate hypothesis testing
- InvarianceUnitTests: Linear unit-tests for invariance discovery
- MAPIE: scikit-learn-compatible module for estimating prediction intervals.
- Merlion: A Machine Learning Framework for Time Series Intelligence by SalesForce
- permute: permutation tests and confidence sets
- PhiK: practical correlation constant that works consistently between categorical, ordinal and interval variables
- pingouin: Statistical package in Python based on Pandas
- responsible-ai-toolbox: Error Analysis dashboard, for identifying model errors and discovering cohorts of data for which the model underperforms.
- RunStats: Computing Statistics and Regression in One Pass
- scikit-learn: machine learning in Python
- statsmodels: statistical modeling and econometrics
- UltraNest: Fit and compare complex models reliably and rapidly. Advanced nested sampling.
- xskillscore: Metrics for verifying forecasts

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ACV: Optimal Out-of-Sample Forecast Evaluation and Testing under Stationarity
- amp: Statistical Test for the Multivariate Point Null Hypotheses
- ashr: Methods for Adaptive Shrinkage, using Empirical Bayes
- bayefdr: Bayesian Estimation and Optimisation of Expected False Discovery Rate
- BEST: Bayesian Estimation Supersedes the t-Test
- BFpack: Flexible Bayes Factor Testing of Scientific Expectations
- blocklength: Select an Optimal Block-Length to Bootstrap Dependent Data (Block Bootstrap)
- boot: Bootstrap Functions
- boot.pval: Bootstrap p-Values
- bootUR: Bootstrap Unit Root Tests
- CADFtest: A Package to Perform Covariate Augmented Dickey-Fuller Unit Root Tests
- ChangepointTesting: Change Point Estimation for Clustered Signals
- clusrank: Wilcoxon Rank Tests for Clustered Data
- cocor: Comparing Correlations
- corTESTsrd: Significance Testing of Rank Cross-Correlations under SRD
- CovTools: Statistical Tools for Covariance Analysis
- crossvalidationCP: Cross-Validation for Change-Point Regression
- crseEventStudy: A Robust and Powerful Test of Abnormal Stock Returns in Long-Horizon Event Studies
- cvCovEst: Cross-Validated Covariance Matrix Estimation
- cvms: Cross-Validation for Model Selection
- CVST: Fast Cross-Validation via Sequential Testing
- dgof: Discrete Goodness-of-Fit Tests
- digitTests: Tests for Detecting Irregular Digit Patterns
- DiscreteFDR: Multiple Testing Procedures with Adaptation for Discrete Tests
- dsos: Dataset Shift with Outlier Scores
- elo: Ranking Teams by Elo Rating and Comparable Methods
- energy: E-Statistics: Multivariate Inference via the Energy of Data
- exactRankTests: Exact Distributions for Rank and Permutation Tests
- FactorAssumptions: Set of Assumptions for Factor and Principal Component Analysis
- FAMT: Factor Analysis for Multiple Testing (FAMT) : Simultaneous Tests under Dependence in High-Dimensional Data
- fbst: The Full Bayesian Evidence Test, Full Bayesian Significance Test and the e-Value

- fdrci: Permutation-Based FDR Point and Confidence Interval Estimation
- FDRestimation: Estimate, Plot, and Summarize False Discovery Rates
- funtimes: Nonparametric estimators and tests for time series analysis
- fwb: Fractional Weighted Bootstrap
- fwildclusterboot: Fast Wild Cluster Bootstrap Inference for Linear Models
- gvlma: Global Validation of Linear Models Assumptions
- gt: Easily Create Presentation-Ready Display Tables
- gtExtras: Extending 'gt' for Beautiful HTML Tables
- heplots: Visualizing Hypothesis Tests in Multivariate Linear Models
- HSAUR3: A Handbook of Statistical Analyses Using R (3rd Edition)
- htestClust: Reweighted Marginal Hypothesis Tests for Clustered Data
- ICtest: Estimating and Testing the Number of Interesting Components in Linear Dimension Reduction
- inferr: Inferential Statistics (parametric and non-parametric statistical tests)
- L2DensityGoFtest: Density Goodness-of-Fit Test
- locits: Test of Stationarity and Localized Autocovariance
- mashr: Multivariate Adaptive Shrinkage
- mcStats: Visualize Results of Statistical Hypothesis Tests
- melt: Multiple Empirical Likelihood Tests
- metrica: evaluate prediction performance of point-forecast models
- MixedIndTests: Tests of Randomness and Tests of Independence
- modeltime.resample: Resampling Tools for Time Series Forecasting
- MSTest: Hypothesis Testing for Markov Switching Models
- multDM: Multivariate Version of the Diebold-Mariano Test
- MultiFit: Multiscale Fisher's Independence Test for Multivariate Dependence
- MultiHorizonSPA: Multi Horizon Superior Predictive Ability
- multiverse: 'Explorable Multiverse' Data Analysis and Reports to show the robustness of statistical inference
- MVTests: Multivariate Hypothesis Tests and the confidence intervals
- nestedcv: Nested Cross-Validation with 'glmnet' and 'caret'
- NonParRolCor: a Non-Parametric Statistical Significance Test for Rolling Window Correlation
- OOS: Out-of-Sample Time Series Forecasting
- origami: Generalized Framework for Cross-Validation
- OptSig: Optimal Level of Significance for Regression and Other Statistical Tests
- OPTtesting: Optimal Testing

- OutliersO3: Draws Overview of Outliers (O3) Plots
- pbo: Probability of Backtest Overfitting
- performance: Assessment of Regression Models Performance
- permutes: Permutation Tests for Time Series Data
- poolr: Methods for Pooling P-Values from (Dependent) Tests
- portes: Portmanteau Tests for Univariate and Multivariate Time Series Models
- randtoolbox: Toolbox for Pseudo and Quasi Random Number Generation and Random Generator Tests
- RDieHarder: R Interface to the 'DieHarder' RNG Test Suite
- RDnp: Robust Test for Complete Independence in High-Dimensions
- rigr: Regression, Inference, and General Data Analysis Tools in R
- Rita: Automated Transformations, Normality Testing, and Reporting
- rmcorr: Repeated Measures Correlation
- RobustANOVA: Robust One-Way ANOVA Tests under Heteroscedasticity and Nonnormality
- robusTest: Calibrated Correlation, Two-Sample Tests
- rsample: General Resampling Infrastructure
- rstatix: Pipe-Friendly Framework for Basic Statistical Tests
- s2dverification: Set of Common Tools for Forecast Verification
- scoringfunctions: A Collection of Scoring Functions for Assessing Point Forecasts
- scoringRules: Scoring Rules for Parametric and Simulated Distribution Forecasts
- scoringutils: Utilities for Scoring and Assessing Predictions
- sdafilter: distribution free multiple testing rules for false discovery rate (FDR) control under general dependence
- sgof: Multiple Hypothesis Testing
- SHT: Statistical Hypothesis Testing Toolbox
- slider: Sliding Window Functions
- SlidingWindows: Methods for Time Series Analysis
- SPlit: Split a Dataset for Training and Testing
- splitTools: Tools for Data Splitting
- statsExpressions: Tidy Dataframes and tests (parametric, nonparametric, robust, etc)
- tidyposterior: Bayesian Analysis to Compare Models using Resampling Statistics
- tidystats: Save Output of Statistical Tests
- UnitStat: Performs Unit Root Test Statistics
- urca: Unit Root and Cointegration Tests for Time Series Data
- USP: U-Statistic Permutation Tests of Independence for all Data Types
- walrus: Robust Statistical Methods
- yardstick: Tidy Characterizations of Model Performance

7.41 Testing software codes

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- benchmark: microbenchmark support library
- bugsnag error monitoring and error reporting
- case: Python unittest Utilities
- cxxtest: CxxTest Unit Testing Framework
- dirty-equals: make python code (generally unit tests) more declarative and therefore easier to read and write.
- expectest: implements expect tests (also known as "golden" tests)
- formencode: validation and form generation
- freezegun: allows your Python tests to travel through time by mocking the datetime module
- green: clean, colorful, fast python test runner
- Hypothesis: family of testing libraries which let you write tests parametrized by a source of examples
- Mamba Test Runner: definitive testing tool for Python
- mutattest: Safely run mutation trials without source code modifications and see what will get past your test suite.
- nose2: unittest with plugins.
- nox: Flexible test automation for Python
- partialtesting: toolkit by Man Group to run only the tests relevant for code changes
- playwright-python: Python version of the Playwright testing and automation library
- Pynguin: PYthoN General UnIt Test geNerator
- pyperformance: intended to be an authoritative source of benchmarks for all Python implementations
- pytest: easy to write small tests, yet scales to support complex functional testing
- pytest-benchmark: py.test fixture for benchmarking code
- pytest-check: pytest plugin that allows multiple failures per test.
- pytest-html: Plugin for generating HTML reports for pytest results
- pytest-parallel: pytest plugin for parallel and concurrent testing
- pytest-regressions: Pytest plugin for regression testing
- stestr: parallel Python test runner built around subunit
- TestSlide: test framework by Facebook
- testtools: extensions to the Python standard library's unit testing framework.
- tox: Command line driven CI frontend and development task automation tool
- ward: modern test framework for Python with a focus on productivity and readability.

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- exampletestr: Help for Writing Unit Tests Based on Function Examples
- melt: Multiple Empirical Likelihood Tests
- mockthat: Function Mocking for Unit Testing
- patrick: Parameterized Unit Testing by Google
- realtest: When Expectations Meet Reality: Realistic Unit Testing
- shinytest2: Testing for Shiny Applications
- testdat: Data Unit Testing for R
- testthat: Unit Testing for R
- testthis: Utils and 'RStudio' Addins to Make Testing Even More Fun
- ttdo: Extend 'tinytest' with 'diffobj'
- unitizer: Interactive R Unit Tests
- unittest: TAP-Compliant Unit Testing
- xpectr: Generates Expectations for 'testthat' Unit Testing

7.42 Time series analysis and modeling

Collections of resources

List of links:

- Curated list with python packages for time series analysis
- Popular Python Time Series Packages
- Resources for working with time series and sequence data

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Clairvoyance: Unified, End-to-End AutoML Pipeline for Medical Time Series
- darts: toolkit by Unit8 for easy manipulation and forecasting of time series
- DataGene: Identify How Similar TS Datasets Are to One Another
- deeptime: analysis of time series data including dimensionality reduction, clustering, and Markov model estimation
- EntropyHub: open-source toolkit for entropic time-series analysis.
- ETNA Time Series Library by Tinkoff AI
- fastreg: Fast sparse regressions with advanced formula syntax. OLS, GLM, Poisson, Maxlike, and more. High-dimensional fixed effects
- Featuretools: automated feature engineering
- glum: Generalized linear models

- hcrystalball: unifies the API for most commonly used libraries and modeling techniques for time-series forecasting in the Python ecosystem
- HyperTools: toolbox for gaining geometric insights into high-dimensional data
- HyperTS: Full-Pipeline Automated Time Series (AutoTS) Analysis Toolkit
- kats: tookit by Facebook for time series analysis and forecasting
- KFAS: Kalman Filter and Smoother for Exponential Family State Space Models
- khiva-python: Python binding for Khiva library for time series analytics
- Loud ML: inference engine for metrics and events
- luminaire: ML driven solutions for monitoring time series data
- matrixprofile-ts: detect patterns and anomalies in massive datasets using Matrix Profile
- MatrixStats: Methods that Apply to Rows and Columns of Matrices (and to Vectors)
- mkl_fft: NumPy-based Python interface to Intel (R) MKL FFT functionality
- nixtla: Automated time series processing and forecasting
- pandas: data structures for data analysis, time series, and statistics
- pyFFTW is a pythonic wrapper around FFTW 3, the speedy FFT library
- pyFIt-SNE: FFT-accelerated Interpolation-based t-SNE (FIt-SNE)
- pyts: time series classification
- pytsal: Time Series analysis, visualization, forecasting along with AutoTS
- seglearn: machine learning for time series
- sktime: unified framework for machine learning with time series by UK national institute for data science and artificial intelligence
- slearn: package linking symbolic representation with scikit-learn machine learning
- statsmodels: statistical modeling and econometrics
- stumpy: variety of time series data mining tasks
- theft: Tools for Handling Extraction of Features from Time Series
- timemachines: Evaluation and standardization of popular time series packages
- timetk: A Tool Kit for Working with Time Series in R
- Traces: library for unevenly-spaced time series analysis
- tsai: time series tasks like classification, regression, forecasting, imputation
- tsam: time series aggregation module (tsam)
- ts-eval: Time Series analysis and evaluation tools
- tsfresh: extracts relevant characteristics from time series
- tslearn: machine learning toolkit dedicated to time-series data
- tspreprocess: package to preprocess time series
- tsmoothie: time-series smoothing and outlier detection in a vectorized way
- vectorbt: library for backtesting and analyzing trading strategies at scale

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ASSA: Applied Singular Spectrum Analysis
- astsa: Applied Statistical Time Series Analysis
- autostsm: Automatic Structural Time Series Models
- bdots: Bootstrapped Differences of Time Series
- bfast: Breaks for Additive Season and Trend
- bimets: Time Series and Econometric Modeling
- bootUR: Bootstrap Unit Root Tests
- ctbi: A Procedure to Clean, Decompose and Aggregate Timeseries
- energy: E-Statistics: Multivariate Inference via the Energy of Data
- entropy: Estimation of Entropy, Mutual Information and Related Quantities
- freqdom: Frequency Domain Based Analysis: Dynamic PCA
- funtimes: Functions for Time Series Analysis
- garchx: Flexible and Robust GARCH-X Modelling
- LMD: A Self-Adaptive Approach for Demodulating Multi-Component Signal
- LSTS: Locally Stationary Time Series
- lubridate: Make Dealing with Dates a Little Easier
- mcvis: Multi-Collinearity Visualization
- MixedIndTests: Tests of Randomness and Tests of Independence
- MTS: All-Purpose Toolkit for Analyzing Multivariate Time Series (MTS) and Estimating Multivariate Volatility Models
- NonlinearTSA: Nonlinear Time Series Analysis
- nonlinearTseries: Nonlinear Time Series Analysis
- nortsTest: Assessing Normality of Stationary Process
- NTS: Nonlinear Time Series Analysis
- Rfssa: Functional Singular Spectrum Analysis
- rhosa: Higher-Order Spectral Analysis
- rrcov: Scalable Robust Estimators with High Breakdown Point
- rrMixture: Reduced-Rank Mixture Models
- Rssa: A Collection of Methods for Singular Spectrum Analysis
- rtrend: Trend Estimating Tools
- Rwave: Time-Frequency Analysis of 1-D Signals
- seastests: Seasonality Tests

- shrink: Global, Parameterwise and Joint Shrinkage Factor Estimation
- simts: Time Series Analysis Tools
- SLBDD: Statistical Learning for Big Dependent Data
- svars: Data-Driven Identification of SVAR Models
- tempdisagg: Temporal Disaggregation and Interpolation of Time Series
- theft: Tools for Handling Extraction of Features from Time Series
- TidyDensity: Functions for Tidy Analysis and Generation of Random Data
- timetk: A Tool Kit for Working with Time Series in R
- TSA: Time Series Analysis
- tsbox: Class-Agnostic Time Series
- tscopula: Time Series Copula Models
- tseries: Time Series Analysis and Computational Finance
- TSrepr: Time Series Representations
- tsrobprep: Robust Preprocessing of Time Series Data
- TSstudio: Functions for Time Series Analysis and Forecasting
- tsutils: Time Series Exploration, Modelling and Forecasting
- tsviz: Easy and Interactive Time Series Visualization
- vars: VAR Modelling
- xts: eXtensible Time Series

7.43 Text, sentiment and topic analytics (including NLP)

Python software implementations

- AllenNLP: toolkit by Allen Institute of Articial Intelligence for NLP research
- EmTract: Extracting Emotions from Social Media Text Tailored for Financial Contexts
- EvoMSA: Sentiment Analysis System based on B4MSA and EvoDAG
- fairseq: Facebook AI Research Sequence-to-Sequence Toolkit
- FastFormers: toolkit by Microsoft to achieve inference of Transformer models for Natural Language Understanding
- gensim: topic modelling, document indexing and similarity retrieval with large corpora
- GPT-3: Language Models are Few-Shot Learners
- LIT: Language Interpretability Tool: Interactively analyze NLP models for model understanding
- LangTech Text Library (LTTL) is an open-source python package for text processing and analysis.
- Natural Language Processing Best Practices and Examples by Microsoft
- netts: toolkit by UK national institute for data science and artificial intelligence for creating networks capturing semantic content of speech transcripts

- nlpaug: Data augmentation for NLP
- nltk: Natural Language Toolkit
- pytext: A natural language modeling framework based on PyTorch
- PyTorch-NLP: Basic Utilities for PyTorch Natural Language Processing (NLP)
- Senta: Baidu's open-source Sentiment Analysis System.
- spaCy: Industrial-strength Natural Language Processing (NLP) in Python
- stocksight: Stock market analyzer and predictor using Elasticsearch, Twitter, News headlines, NLP and sentiment analysis
- sumy: automatic summarization of text documents and HTML pages
- textacy: NLP, before and after spaCy
- vaderSentiment: VADER (Valence Aware Dictionary and sEntiment Reasoner) is a lexicon and rule-based sentiment analysis tool
- wordfreq: Access a database of word frequencies, in various natural languages.

R software implementations

- cleanNLP: Tidy Data Model for Natural Language Processing
- doc2concrete: Measuring Concreteness in Natural Language
- fastTextR: An Interface to the 'fastText' Library
- globaltrends: Google Trends portal.
- lsa: Latent Semantic Analysis
- LSX: Model for Semisupervised Text Analysis Based on Word Embeddings
- meanr: Sentiment Analysis Scorer
- NLP: Natural Language Processing Infrastructure
- opitools: Analyzing the Opinions in a Big Text Document
- quanteda: Quantitative Analysis of Textual Data
- saotd: Sentiment Analysis of Twitter Data
- sentiment.ai: Simple Sentiment Analysis Using Deep Learning
- SentimentAnalysis: Dictionary-Based Sentiment Analysis
- sentimentr: Calculate Text Polarity Sentiment
- sentometrics: Integrated Framework for Textual Sentiment Time Series Aggregation and Prediction
- spacyr: Wrapper to the 'spaCy' 'NLP' Library
- sweater: Speedy Word Embedding Association Test and Extras Using R
- syuzhet: Extracts Sentiment and Sentiment-Derived Plot Arcs from Text
- tau: Text Analysis Utilities
- text2map: R Tools for Text Matrices, Embeddings, and Networks

- text2sdg: Detecting UN Sustainable Development Goals in Text
- text2vec: Modern Text Mining Framework for R
- texter: An Easy Text and Sentiment Analysis Library
- TextForecast: Regression Analysis and Forecasting Using Textual Data from a Time-Varying Dictionary
- textTinyR: Text Processing for Small or Big Data Files
- tidytext: Text Mining using 'dplyr', 'ggplot2', and Other Tidy Tools
- transforEmotion: Sentiment Analysis for Text and Qualitative Data
- tsentiment: Fetching Tweet Data for Sentiment Analysis
- Xplortext: Statistical Analysis of Textual Data

7.44 Uncertainty: analysis and modeling

Links to resources

- Professionally curated list of awesome Conformal Prediction videos, tutorials, books, papers, PhD and MSc theses, articles and open-source libraries

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Bumps: data fitting and uncertainty estimation
- conformal-rnn: code for "Conformal time-series forecasting", NeurIPS 2021
- crepes: Conformal Regressors and Conformal Predictive Systems
- EasyVVUQ: verification, validation and uncertainty quantification in high performance computing
- EnbPI: Ensemble batch prediction intervals
- EnCQR: ensemble conformalized quantile regression (EnCQR)
- MAPIE: scikit-learn-compatible module for estimating prediction intervals
- mystic: highly-constrained non-convex optimization and uncertainty quantification
- OpenTURNS (Open source initiative to Treat Uncertainties, Risks'N Statistics)
- PySloth: Probabilistic Prediction
- UncertaintyToolbox: predictive uncertainty quantification, calibration, metrics, and visualization
- UQpy: UQpy (Uncertainty Quantification with python) is a general purpose Python toolbox for modeling uncertainty in physical and mathematical systems

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- bootComb: Combine Parameter Estimates via Parametric Bootstrap

7.45 Visualization and reporting

Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- Algviz is an algorithm visualization tool for your Python code
- appmode: Jupyter extension that turns notebooks into web applications
- Best of Streamlit
- clustergram: Visualization and diagnostics for cluster analysis in Python
- dash: framework for building ML and data science web apps
- dash-extensions:extensions to the Plotly Dash framework
- D-tale:Visualizer by Man Group for pandas data structures
- FlameScope: visualization ny Netflix for exploring different time ranges as Flame Graphs.
- HyperTools: toolbox for gaining geometric insights into high-dimensional data
- ipyslides: Create Interactive Slides in Jupyter Notebook with all kind of rich content
- itables: Pandas DataFrames as Interactive DataTables
- Lux: automate the visualization and data analysis process
- Markdown: Python implementation of markdown
- matplotlib: omprehensive library for creating static, animated, and interactive visualizations
- mpl-animators: interative animation framework for matplotlib
- Orange: Interactive data analysis
- plotly: graphing library makes interactive, publication-quality graphs
- Plotly Resampler: Visualize large time-series data in plotly
- plotnine: A grammar of graphics for Python
- plottable: Beautifully customized tables with matplotlib
- psyplot: interactive data visualization
- PyGraphistry: quickly load, shape, embed, and explore big graphs with the GPU-accelerated Graphistry visual graph analyzer
- PyMetis: Python wrapper around Metis, a graph partitioning package
- PyShiny: Shiny for Python
- pyvis: visualizing interactive network graphs
- seaborn: statistical data visualization
- seaborn analyzer: data analysis and visualization tool using Seaborn library
- streamlit: fastest way to build and share data apps
- tensorboard: TensorFlow's Visualization Toolkit
- torchsde: Differentiable SDE solvers with GPU support and efficient sensitivity analysis

- tourr: Tour Methods for Multivariate Data Visualisation
- Vega-Altair is a declarative statistical visualization library for Pytho
- VisPy: interactive scientific visualization in Python
- visdom: lexible tool for creating, organizing, and sharing visualizations of live, rich data

R software implementations

List of packages and/or codes and/or frameworks and/or links:

- apexcharter: Create Interactive Chart with the JavaScript 'ApexCharts' Library
- autoplotly: Automatic Generation of Interactive Visualizations for Statistical Results
- classmap: Visualizing Classification Results
- cleanrmd: Clean Class-Less 'R Markdown' HTML Documents
- clustree: Visualise Clusterings at Different Resolutions
- ComplexUpset: Create Complex UpSet Plots Using 'ggplot2' Components
- condformat: Conditional Formatting in Data Frames
- conductor: Create Tours in 'Shiny' Apps Using 'Shepherd.js'
- d3po: Fast and Beautiful Interactive Visualization for 'Markdown' and 'Shiny'
- DataVisualizations: Visualizations of High-Dimensional Data
- descriptr: Generate Descriptive Statistics
- DT: A Wrapper of the JavaScript Library 'DataTables'
- echarty: Minimal R/Shiny Interface to JavaScript Library 'ECharts'
- esquisse: Explore and Visualize Your Data Interactively
- fmtr: Easily Apply Formats to Data
- ggalluvial: Alluvial Plots in 'ggplot2'
- GGally: Extension to 'ggplot2'
- gganimate: A Grammar of Animated Graphics
- ggbreak: Set Axis Break for 'ggplot2'
- ggcharts: Shorten the Distance from Data Visualization Idea to Actual Plot
- ggcorrplot: Visualization of a Correlation Matrix using 'ggplot2'
- ggcorset: The Corset Plot
- ggdag: Analyze and Create Elegant Directed Acyclic Graphs
- ggdist: Visualizations of Distributions and Uncertainty
- ggDoubleHeat: A Heatmap-Like Visualization Tool
- ggeffects: Create Tidy Data Frames of Marginal Effects for 'ggplot' from Model Outputs
- ggESDA: Exploratory Symbolic Data Analysis with 'ggplot2'

- ggfocus: Scales that Focus Specific Levels in your ggplot
- ggforce: Accelerating 'ggplot2'
- ggformula: Formula Interface to the Grammar of Graphics
- ggfortify: Data Visualization Tools for Statistical Analysis Results
- gghdr: Visualisation of Highest Density Regions in 'ggplot2'
- ggheatmap: Plot Heatmap
- gghighlight: Highlight Lines and Points in 'ggplot2'
- ggh4x: Hacks for 'ggplot2'
- ggiraph: Make 'ggplot2' Graphics Interactive
- ggmatplot: Plot Columns of Two Matrices Against Each Other Using 'ggplot2'
- ggmice: Visualizations for 'mice' with 'ggplot2'
- ggmosaic: Mosaic Plots in the 'ggplot2' Framework
- ggmulti: High Dimensional Data Visualization
- ggnetwork: Geometries to Plot Networks with 'ggplot2'
- ggpattern: 'ggplot2' Pattern Geoms
- ggpie: pie, donut and rose pie plots with ggplot2
- ggplot2: Create Elegant Data Visualisations Using the Grammar of Graphics
- ggplotify: Convert Plot to 'grob' or 'ggplot' Object
- ggpmisc: Miscellaneous Extensions to 'ggplot2'
- ggpubr: 'ggplot2' Based Publication Ready Plots
- ggpval: Annotate Statistical Tests for 'ggplot2'
- ggquickeda: Quickly Explore Your Data Using 'ggplot2' and 'table1' Summary Tables
- ggside extends 'ggplot2' by allowing users to add graphical information about one of the main panel's axis using a familiar 'ggplot2' style API with tidy data
- ggsignif: Significance Brackets for 'ggplot2'
- ggstance: Horizontal 'ggplot2' Components
- ggstar: Multiple Geometric Shape Point Layer for 'ggplot2'
- ggstatsplot: 'ggplot2' Based Plots with Statistical Details
- ggthemes: Extra Themes, Scales and Geoms for 'ggplot2'
- ggtrace: Provides ggplot2 geoms that allow groups of data points to be outlined or highlighted for emphasis
- gluedown: Wrap Vectors in Markdown Formatting
- gridstackeR: easy way to create responsive layouts with just a few lines of code using gridstack.js
- gt: Easily Create Presentation-Ready Display Tables
- gtExtras: additional functions for creating tables with gt

- gtsummary: Presentation-Ready Data Summary and Analytic Result Tables
- heatmaply: Interactive Cluster Heat Maps Using 'plotly' and 'ggplot2'
- heplots: Visualizing Hypothesis Tests in Multivariate Linear Models
- htmlTable: Advanced Tables for Markdown/HTML
- huxtable: Easily Create and Style Tables for LaTeX, HTML and Other Formats
- jjAnno: An Annotation Package for 'ggplot2' Output
- kableExtra: Construct Complex Table with 'kable' and Pipe Syntax
- listdown: Create R Markdown from Lists
- loon: Interactive Statistical Data Visualization
- loon.ggplot: A Grammar of Interactive Graphics
- magick: Advanced Graphics and Image-Processing in R
- memoiR: R Markdown and Bookdown Templates to Publish Documents
- ndtv: Network Dynamic Temporal Visualizations
- numform: Tools to Format Numbers for Publication
- performance: Assessment of Regression Models Performance
- plot.matrix: Visualizes a Matrix as Heatmap
- presenter: Present Data with Style
- prompter: Add Tooltips in 'Shiny' Apps with 'Hint.css'
- psre: Presenting Statistical Results Effectively
- quarto: R Interface to 'Quarto' Markdown Publishing System
- r2resize: In-Text Resizing for Containers, Images and Data Tables in 'Shiny', 'Markdown' and 'Quarto' Documents
- r3js: allow WebGL-based 3D plotting using the three.js library
- reactR: Make it easy to use 'React' in R with 'htmlwidget' scaffolds
- reporter: Creates Statistical Reports
- rheroicons: A Zero Dependency 'SVG' Icon Library for 'Shiny'
- rhino: A Framework for Enterprise Shiny Applications
- rintrojs: Wrapper for the 'Intro.js' Library
- rmarkdown: Dynamic Documents for R
- rsvg: Render SVG Images into PDF, PNG, (Encapsulated) PostScript, or Bitmap Arrays
- semantic.dashboard: Dashboard with Fomantic UI Support for Shiny
- shapviz: visualize SHapley Additive exPlanations (SHAP) - waterfall, force, importance, dependence plots
- shiny: Web Application Framework for R
- shinyChakraUI: A Wrapper of the 'React' Library 'Chakra UI' for 'Shiny'

- shinydlplot: Add a Download Button to a 'shiny' Plot or 'plotly'
- shinyHugePlot: Efficient Plotting of Large-Sized Data
- shinyMobile: Mobile Ready 'shiny' Apps with Standalone Capabilities
- shinySelect: A Wrapper of the 'react-select' Library
- shiny.semantic: Semantic UI Support for Shiny
- shinytest: Test Shiny Apps
- shinyWidgets: Custom Inputs Widgets for Shiny
- starry: Explore Data with Plots and Tables
- statsExpressions: Tidy Dataframes and Expressions with Statistical Details
- sugrrants: Supporting Graphs for Analysing Time Series
- tidybayes: Tidy Data and 'Geoms' for Bayesian Models
- tidycharts: Generate Tidy Charts Inspired by 'IBCS'
- tidyHeatmap: A Tidy Implementation of Heatmap
- tourr: Tour Methods for Multivariate Data Visualisation
- tornado: Plots for Model Sensitivity and Variable Importance
- trelliscopejs: Create Interactive Trelliscope Displays
- tsviz: Easy and Interactive Time Series Visualization
- UpSetR: A More Scalable Alternative to Venn and Euler Diagrams for Visualizing Intersecting Sets
- visNetwork: Network Visualization using 'vis.js' Library
- visStatistics: Automated Visualization of Statistical Tests
- vtable: Variable Table for Variable Documentation
- xaringan: Presentation Ninja
- yardstick: Tidy Characterizations of Model Performance

8 Codes for QWIM (Quantitative Wealth and Investment Management)

8.1 Collections of resources

List of links:

- Curated list of practical financial machine learning tools and applications
- EliteQuant: online resources for quantitative modeling, trading, portfolio management

8.2 Research studies with code

Ardia et al. ("RiskPortfolios: Computation of Risk-Based Portfolios in R," 2017)

Boileau et al. ("cvCovEst: Cross-validated covariance matrix estimator selection and evaluation in R," 2021)

Brugiere (*Quantitative Portfolio Management with Applications in Python*, 2020)

Bryzgalova et al. ("Forest Through the Trees: Building Cross-Sections of Stock Returns," 2021)

Cajas ("Entropic Portfolio Optimization: a Disciplined Convex Programming Framework," 2021)

Cajas ("OWA Portfolio Optimization: a Disciplined Convex Programming Framework," 2021)

Chen and Zimmermann ("Open Source Cross-Sectional Asset Pricing," 2022)

Chib (*R package czfactor*, 2020)

Chib and Zhao (*R package czzg*, 2020)

Coqueret and Guida (*Machine Learning for Factor Investing: R Version*, 2020)

Coqueret (*Perspectives in sustainable equity investing (website version)*, 2022)

de Carvalho and Rua ("Real-time nowcasting the US output gap: Singular spectrum analysis at work," 2017)

Ding et al. ("A Python package for multi-stage stochastic programming," 2020)

Dixon et al. (*Machine Learning in Finance: from theory to practice*, 2020)

Dixon and Polson ("Deep Fundamental Factor Models," 2020)

Dong et al. ("Anomalies and the expected market return," 2022)

Guijarro-Ordonez et al. ("Deep Learning Statistical Arbitrage," 2021)

Gurdogan and Kercheval ("Multi Anchor Point Shrinkage for the Sample Covariance Matrix (Extended Version)," 2021)

Ho et al. ("Moving beyond P values: data analysis with estimation graphics," 2019)

Irlam ("Multi Scenario Financial Planning via Deep Reinforcement Learning AI," 2020)

Irlam (*AI Planner*, 2020)

Irlam ("Machine learning for retirement planning," 2020)

Jansen (*Machine Learning for Algorithmic Trading (Second Edition)*, 2020)

Kakushadze and Yu ("Statistical Risk Models," 2016)

Kakushadze and Yu ("Open Source Fundamental Industry Classification," 2017)

Kakushadze and Yu ("Betas, Benchmarks, and Beating the Market," 2018)

Kakushadze and Yu ("Decoding stock market with quant alphas," 2018)

Kakushadze and Yu ("Machine learning risk models," 2019)

Kakushadze and Yu ("Machine learning treasury yields," 2020)

Lai et al. ("TODS: An Automated Time Series Outlier Detection System," 2021)

Lettau and Pelger ("Factors That Fit the Time Series and Cross-Section of Stock Returns," 2020)

Li et al. ("FinRL-Podracer: High Performance and Scalable Deep Reinforcement Learning for Quantitative Finance," 2021)

Liu et al. ("FinRL: Deep Reinforcement Learning Framework to Automate Trading in Quantitative Finance," 2021)

Liu et al. ("FinRL-Meta: A Universe of Near-Real Market Environments for Data-Driven Deep Reinforcement Learning in Quantitative Finance," 2022)

Marinescu ("Risk-Based Optimal Portfolio Strategies: A Compendium," 2022)

Martin ("PyPortfolioOpt: portfolio optimization in Python," 2021)

Marwood and Minnen ("Safely Boosting Retirement Income by Harmonizing Drawdown Paths," 2020)

McIndoe ("A Data Driven Approach to Market Regime Classification," 2020)

Micheli and Neuman ("Evidence of Crowding on Russell 3000 Reconstitution Events," 2022)

Milevsky (*Retirement Income Recipes in R: From Ruin Probabilities to Intelligent Drawdowns*, 2020)

Qian et al. ("Combining forecasts for universally optimal performance," 2022)

Rao and Jelvis (*Foundations of Reinforcement Learning with Applications in Finance*, 2022)

Sarmas et al. (*Multicriteria Portfolio Construction with Python*, 2020)

Sharma et al. ("DoWhy: Addressing Challenges in Expressing and Validating Causal Assumptions," 2021)

Shi et al. ("Deep Learning Algorithms for Hedging with Frictions," 2022)

Siebert et al. ("A systematic review of Python packages for time series analysis," 2021)

Simos et al. ("Time-varying Black–Litterman portfolio optimization using a bio-inspired approach and neuronets," 2021)

Snow ("Machine learning in asset management," 2019)

Snow ("Machine Learning in Asset Management Part 1: Portfolio Construction Trading Strategies," 2020)
Snow ("Machine Learning in Asset Management - Part 2: Portfolio Construction - Weight Optimization," 2020)
Tatsat et al. (*Machine Learning and Data Science Blueprints for Finance: From Building Trading Strategies to Robo-Advisors Using Python*, 2020)
Tuck et al. ("Portfolio Construction Using Stratified Models," 2022)
Ungolo et al. ("affine_mortality: A Github repository for estimation, analysis, and projection of affine mortality models," 2021)
Vamossy and Skog ("EmTract: Investor Emotions and Market Behavior," 2021)
Vinod ("R Package GeneralCorr Functions for Portfolio Choice," 2021)
Yang et al. ("FinBERT: A Pretrained Language Model for Financial Communications," 2020)
Yu et al. ("An AI approach to measuring financial risk," 2020)

8.3 Python software implementations

List of packages and/or codes and/or frameworks and/or links:

- alive-progress: new kind of Progress Bar, with real-time throughput, ETA, and very cool animations
- alphalens: Performance analysis of predictive (alpha) stock factors
- AlphaPy: Automated Machine Learning [AutoML] with Python, scikit-learn, Keras, XGBoost, LightGBM, and CatBoost
- auquantoolbox: Backtesting toolbox for trading strategies
- azapy: Financial Portfolio Optimization Algorithms
- bt: flexible backtesting framework
- btgym: Scalable, event-driven, deep-learning-friendly backtesting library
- Clairvoyant: identify and monitor social/historical cues for short term stock movement
- CVXPortfolio: Portfolio optimization and simulation
- cyanure: Toolbox for Empirical Risk Minimization
- Elegant-FinRL: algorithmic strategies using Reinforcement Learning
- Empyrial: AI and data-driven quantitative portfolio management for risk and performance analytics
- empyrical: Common financial risk and performance metrics
- EmTract: Extracting Emotions from Social Media Text Tailored for Financial Contexts
- ffn: Financial functions for Python
- FinDataPy: download market data via Bloomberg, Eikon, Quandl, Yahoo etc.
- FinMarketPy: backtesting trading strategies and analyzing financial markets
- finnhub-python: Finnhub Python API Client to provide financial data(real-time stock price, global fundamentals, global ETFs holdings and alternative data)
- FinRL: Deep Reinforcement Learning for Quantitative Finance
- FinRL-Meta: Universe of Near-Real Market Environments for Data-Driven Financial Reinforcement Learning
- fredapi is a Python interface to the Federal Reserve Economic Data (FRED) and ALFRED databases
- lifelib: Actuarial models in Python
- lifelines: Survival analysis in Python, including Kaplan Meier, Nelson Aalen and regression

- lrsm_portfolio: Portfolio Construction using Stratified Models
- Machine Learning and Data Science Blueprints for Finance (codes for the book)
- Machine Learning fior asset management
- Machine Learning for Algorithmic Trading (codes for the book)
- MLFinLab: Machine Learning Financial Laboratory
- momentum: Running mean, variance, skew, and kurtosis
- Multicriteria Portfolio Construction with Python
- okama: investment portfolio analyzing and optimization tools
- OpenBBTerminal: modern Python-based integrated environment for investment research
- OptimalPortfolio: portfolio optimization
- QuantAxis: Quantitative Financial FrameWork
- QuantEcon: quantitative economics
- Pandas TA: Technical Analysis Indicators
- portfolio-backtest: backtest portfolio asset allocation
- precise: online covariance and precision forecasting, portfolios, and model ensembles
- predictionrevisited: implements the core statistical concepts from the book "Prediction Revisited: The Importance of Observation"
- pyfinance: general financial and security returns analysis
- pyfolio: Portfolio and risk analytics in Python
- pyhrp: hierarchical risk parity algorithms
- PyPortfolioOpt: Financial portfolio optimisation
- Qlib: Microsoft AI-oriented quantitative investment platform
- QuantEcon.py: quantitative economics
- QuantLib: Python bindings for the QuantLib library
- QuantResearch: Quantitative analysis, strategies and backtests
- Quantropy: Financial pipeline for the data-driven investor to research, develop and deploy robust strategie
- QuantStats: Portfolio analytics for quants
- Riskfolio-Lib: Portfolio Optimization and Quantitative Strategic Asset Allocation
- Robust Risk-aware reinforcement learning
- stocksight: Stock market analyzer and predictor using Elasticsearch, Twitter, News headlines, NLP and sentiment analysis
- ta: Technical Analysis Library using Pandas and Numpy
- TA-lib: Python wrapper for TA-Lib Technical Analysis Library
- Tax-Calculator: USA Federal Individual Income and Payroll Tax Microsimulation Model
- tf-quant-finance: High-performance TensorFlow library by Google for quantitative finance.
- vectorbt: Supercharged backtesting and technical analysis for quants
- zipline: Algorithmic Trading Library

8.4 R software implementations

List of packages and/or codes and/or frameworks and/or links:

- ASSA: Applied Singular Spectrum Analysis
- AssetAllocation: Backtesting Simple Asset Allocation Strategies
- BEKKs: Multivariate Conditional Volatility Modelling and Forecasting
- crseEventStudy: A Robust and Powerful Test of Abnormal Stock Returns in Long-Horizon Event Studies
- DOSPortfolio: Dynamic Optimal Shrinkage Portfolio
- ExtremeRisks: Extreme Risk Measures
- FFdownload: Download Data from Kenneth French's Website
- FinnTS: Microsoft Finance Time Series Forecasting Framework
- finreportr: Financial Data from U.S. Securities and Exchange Commission
- fHMM: Fitting Hidden Markov Models to Financial Data
- FinnTS: Microsoft Finance Time Series Forecasting Framework
- fitHeavyTail: Mean and Covariance Matrix Estimation under Heavy Tails
- fixedincome: Fixed Income Models, Calculations, Data Structures and Instruments
- generalCorr: Generalized Correlations, Causal Paths and Portfolio Selection
- greeks: Sensitivities of Prices of Financial Options
- HDShOP: High-Dimensional Shrinkage Optimal Portfolios
- HierPortfolios: Hierarchical Clustering-Based Portfolio Allocation Strategies
- highOrderPortfolios: Design of High-Order Portfolios via Mean, Variance, Skewness, and Kurtosis
- imputeFin: Imputation of Financial Time Series with Missing Values and/or Outliers
- MarkowitzR: Statistical Significance of the Markowitz Portfolio
- MortCast: Estimation and Projection of Age-Specific Mortality Rates
- parma: Portfolio Allocation and Risk Management Applications
- pbo: Probability of Backtest Overfitting
- pec: Prediction Error Curves for Risk Prediction Models in Survival Analysis
- pedquant: Public Economic Data and Quantitative Analysis
- PerformanceAnalytics: Econometric Tools for Performance and Risk Analysis
- PortfolioAnalytics: Portfolio Analysis, Including Numerical Methods for Optimization of Portfolios
- portfolioBacktest: Automated Backtesting of Portfolios over Multiple Datasets
- portvine: portfolio level risk estimates using ARMA-GARCH and vine copulas
- priceR: Economics and Pricing Tools
- qlcal: R Bindings to the Calendaring Functionality of 'QuantLib'

- qrmtools: Tools for Quantitative Risk Management
- quantmod: Quantitative Financial Modelling Framework
- RcppQuantuccia: R Bindings to the Calendaring Functionality of 'QuantLib'
- riskParityPortfolio: Design of Risk Parity Portfolios
- RiskPortfolios: Computation of Risk-Based Portfolios
- riskRegression: Risk Regression Models and Prediction Scores for Survival Analysis with Competing Risks
- RPESE: Estimates of Standard Errors for Risk and Performance Measures
- RQuantLib: R Interface to the 'QuantLib' Library
- SharpeR: Statistical Significance of the Sharpe Ratio
- sharpeRratio: Moment-Free Estimation of Sharpe Ratios
- sparseIndexTracking: Design of Portfolio of Stocks to Track an Index
- SWIM: Scenario Weights for Importance Measurement
- TextForecast: Regression Analysis and Forecasting Using Textual Data from a Time-Varying Dictionary
- tidyquant: Tidy Quantitative Financial Analysis
- Trading: CCR, Advanced Correlation & Beta Estimates, Betting Strategies
- tseries: Time Series Analysis and Computational Finance
- ufRisk: Risk Measure Calculation in Financial TS
- usincometaxes: wrapper to the NBER's TAXSIM 35 tax simulator for federal and state income taxes
- ycevo: Nonparametric Estimation of the Yield Curve Evolution
- yfR: Downloads and Organizes Financial Data from Yahoo Finance

References

Abbeel, P. and Ng, A. Y. (2017). "Inverse Reinforcement Learning." In: *Encyclopedia of machine learning and data mining*. Ed. by C. Sammut and G. I. Webb. Boston, MA: Springer US, pp. 678–682.

Aboussalah, A. M. (2021). "Topological Phase Space Reconstruction For Augmented Real-World Reinforcement Learning." In: *SSRN e-Print*.

Aboussalah, A. M., Xu, Z., and Lee, C.-G. (2022). "What is the value of the cross-sectional approach to deep reinforcement learning?" In: *Quantitative Finance*, Early View.

Adcock, C., Areal, N., Armada, M. R., Cortez, M. C., Oliveira, B., and Silva, F. (2017). "Portfolio Performance Measurement: Monotonicity with Respect to the Sharpe Ratio and Multivariate Tests of Correlation." In: *SSRN e-Print*.

Aliaga-Diaz, R., Ahluwalia, H., Zhu, V., Donaldson, S., Daga, A., and Pakula, D. (2021). *Vanguard's Life-Cycle Investing Model (VLCM): A general portfolio framework for goals-based investing*. Tech. rep. Vanguard.

Alsabah, H., Capponi, A., Ruiz Lacedelli, O., and Stern, M. (2021). "Robo-Advising: Learning Investors Risk Preferences via Portfolio Choices." In: *Journal of Financial Econometrics* 19(2), pp. 369–292.

Amin, S., Gomrokchi, M., Satija, H., van Hoof, H., and Precup, D. (2021). "A Survey of Exploration Methods in Reinforcement Learning." In: *arXiv e-Print*.

Andre, E. and Coqueret, G. (2021). "Dirichlet policies for reinforced factor portfolios." In: *arXiv e-Print*.

Ardia, D., Boudt, K., and Gagnon-Fleury, J.-P. (2017). "RiskPortfolios: Computation of Risk-Based Portfolios in R." In: *The Journal of Open Source Software* 2(10), pp. 171+.

Ardon, L., Vadori, N., Spooner, T., Xu, M., Vann, J., and Ganesh, S. (2021). "Towards a fully RL-based Market Simulator." In: *arXiv e-Print*.

Arnott, R. D., Harvey, C. R., and Markowitz, H. (2019). "A backtesting protocol in the era of machine learning." In: *The Journal of Financial Data Science* 1(1), pp. 64–74.

Arora, S. and Doshi, P. (2018). "A Survey of Inverse Reinforcement Learning: Challenges, Methods and Progress." In: *arXiv e-Print*.

Arulkumaran, K., Deisenroth, M. P., Brundage, M., and Bharath, A. A. (2017). "Deep reinforcement learning: A brief survey." In: *IEEE Signal Processing Magazine* 34(6), pp. 26–38.

Bacon, C. R. (2019). "Performance Attribution: History and Progress." In: *CFA Institute Research Foundation Publications*.

Bailey, D. H., Borwein, J. M., and Lopez de Prado, M. (2017). "Stock Portfolio Design and Backtest Overfitting." In: *Journal of Investment Management* 15(1), pp. 75–87.

Bareinboim, E. (2020). *Causal Reinforcement Learning*. URL: `https://crl.causalai.net/`.

Bargiacchi, E., Roijers, D. M., and Nowe, A. (2020). "AI-Toolbox: A C++ library for Reinforcement Learning and Planning (with Python Bindings)." In: *Journal of Machine Learning Research*.

Bartram, S. M., Branke, J., De Rossi, G., and Motahari, M. (2021). "Machine Learning for Active Portfolio Management." In: *The Journal of Financial Data Science* 3(3), pp. 9–30.

Benhamou, E. (2021). "Next Generation Robo Advisors." In: *SSRN e-Print*.

Benhamou, E., Saltiel, D., Ohana, J.-J., and Atif, J. (2021a). "Detecting and Adapting to Crisis Pattern with Context Based Deep Reinforcement Learning." In: *SSRN e-Print*.

Benhamou, E., Saltiel, D., Ohana, J.-J., Atif, J., and Laraki, R. (2021b). "Deep Reinforcement Learning (DRL) for Portfolio Allocation." In: *Joint European Conference on Machine Learning and Knowledge Discovery in Databases*, pp. 527–531.

Benhamou, E., Saltiel, D., Ohana, J.-J., Atif, J., and Laraki, R. (2021c). "Deep Reinforcement Learning (DRL) for Portfolio Allocation." In: *SSRN e-Print*.

Benhamou, E., Saltiel, D., Ohana, J.-J., Atif, J., and Laraki, R. (2021d). "DRLPS: Deep Reinforcement Learning for Portfolio Selection (Presentation Slides ECML PKDD)." In: *SSRN e-Print*.

Benhamou, E., Saltiel, D., Tabachnik, S., Wong, S. K., and Chareyron, F. (2021e). "Adaptive learning for financial markets mixing model-based and model-free RL for volatility targeting." In: *arXiv e-Print*.

Benhamou, E., Saltiel, D., Tabachnik, S., Wong, S. K., and Chareyron, F. (2021f). "Adaptive learning for financial markets mixing model-based and model-free RL for volatility targeting." In: *SSRN e-Print*.

Benhamou, E., Saltiel, D., Ungari, S., Atif, J., and Mukhopadhyay, A. (2021g). "AAMDRL: Augmented Asset Management With Deep Reinforcement Learning." In: *SSRN e-Print*.

Benhamou, E., Saltiel, D., Ungari, S., and Mukhopadhyay, A. (2020). "Time your hedge with Deep Reinforcement Learning." In: *arXiv e-Print*.
Benhamou, E., Saltiel, D., Ungari, S., and Mukhopadhyay, A. (2021h). "Bridging the Gap Between Markowitz Planning and Deep Reinforcement Learning." In: *SSRN e-Print*.
Benhamou, E., Saltiel, D., Ungari, S., and Mukhopadhyay, A. (2021i). "Bridging the gap between Markowitz planning and deep reinforcement learning (ICAPS PRL Presentation Slides 2020)." In: *SSRN e-Print*.
Bertsekas, D. P. (2018). "Feature-Based Aggregation and Deep Reinforcement Learning: A Survey and Some New Implementations." In: *arXiv e-Print*.
Bessler, W., Opfer, H., and Wolff, D. (2017). "Multi-asset portfolio optimization and out-of-sample performance: an evaluation of Black Litterman, mean-variance, and naive diversification approaches." In: *The European Journal of Finance* 23(1), pp. 1–30.
Bessler, W. and Wolff, D. (2017). "Portfolio Optimization with Industry Return Prediction Models." In: *SSRN e-Print*.
Beysolow II, T. (2019). *Applied Reinforcement Learning with Python: With OpenAI Gym, Tensorflow, and Keras*. Berkeley, CA: Apress. 112 pp.
Bjerring, T., Ross, O., and Weissensteiner, A. (2017). "Feature selection for portfolio optimization." In: *Annals of Operations Research* 256, pp. 21–40.
Boileau, P., Hejazi, N., Collica, B., Laan, M. van der, and Dudoit, S. (2021). "cvCovEst: Cross-validated covariance matrix estimator selection and evaluation in R." In: *Journal of Open Source Software* 6(63), p. 3273.
Borrageiro, G., Firoozye, N., and Barucca, P. (2021). "Reinforcement Learning for Systematic FX Trading." In: *arXiv e-Print*.
Borrageiro, G., Firoozye, N., and Barucca, P. (2022). "The Recurrent Reinforcement Learning Crypto Agent." In: *arXiv e-Print*.
Bou, A. and De Fabritiis, G. (2021). "PyTorchRL: Modular and Distributed Reinforcement Learning in PyTorch." In: *arXiv e-Print*.
Brini, A. and Tantari, D. (2022). "Deep Reinforcement Trading with Predictable Returns." In: *arXiv e-Print*.
Brockman, G., Cheung, V., Pettersson, L., Schneider, J., Schulman, J., Tang, J., and Zaremba, W. (2016). "OpenAI Gym." In: *arXiv e-Print*.
Brown, D. S., Cui, Y., and Niekum, S. (2019). "Risk-Aware Active Inverse Reinforcement Learning." In: *arXiv e-Print*.
Brown, D. S. and Niekum, S. (2019). "Machine teaching for inverse reinforcement learning: algorithms and applications." In: *Proceedings of the AAAI Conference on Artificial Intelligence* 33, pp. 7749–7758.
Brugiere, P. (2020). *Quantitative Portfolio Management with Applications in Python*. Springer International Publishing. 189 pp.
Brunel, J. L. P. (2020). "Extending the Goals-Based Framework to Comprise Both Investment and Financial Planning." In: *The Journal of Wealth Management* 22(44), pp. 21–26.
Bruni, R., Cesarone, F., Scozzari, A., and Tardella, F. (2016). "Real-world datasets for portfolio selection and solutions of some stochastic dominance portfolio models." In: *Data in Brief* 8, pp. 858–862.
Bruni, R., Cesarone, F., Scozzari, A., and Tardella, F. (2017). "On exact and approximate stochastic dominance strategies for portfolio selection." In: *European Journal of Operational Research* 259(1), pp. 322–329.
Bryzgalova, S., Huang, J., and Julliard, C. (2021a). "Bayesian solutions for the factor zoo: we just ran two quadrillion models." In: *SSRN e-Print*.
Bryzgalova, S., Pelger, M., and Zhu, J. (2021b). "Forest Through the Trees: Building Cross-Sections of Stock Returns." In: *SSRN e-Print*.
Buehler, H., Gonon, L., Teichmann, J., and Wood, B. (2019). "Deep hedging." In: *Quantitative Finance* 19 (8), pp. 1271–1291.
Cai, Q., Cui, C., Xiong, Y., Wang, W., Xie, Z., and Zhang, M. (2022). "A Survey on Deep Reinforcement Learning for Data Processing and Analytics." In: *arXiv e-Print*.
Cajas, D. (2021a). "Entropic Portfolio Optimization: a Disciplined Convex Programming Framework." In: *SSRN e-Print*.
Cajas, D. (2021b). "OWA Portfolio Optimization: a Disciplined Convex Programming Framework." In: *SSRN e-Print*.
Cao, J., Chen, J., Hull, J., and Poulos, Z. (2021). "Deep Hedging of Derivatives Using Reinforcement Learning." In: *The Journal of Financial Data Science* 3(1), pp. 10–27.

Cao, J., Chen, J., Hull, J. C., and Poulos, Z. (2020). "Deep Hedging of Derivatives Using Reinforcement Learning." In: *SSRN e-Print*.
Carbonneau, A. (2020). "Deep Hedging of Long-Term Financial Derivatives." In: *arXiv e-Print*.
Carbonneau, A. and Godin, F. (2021). "Equal risk pricing of derivatives with deep hedging." In: *Quantitative Finance* 21(4), pp. 593–608.
Cartea, A., Jaimungal, S., and Sanchez-Betancourt, L. (2022). "Deep Reinforcement Learning for Algorithmic Trading." In: *Machine Learning in Financial Markets: A guide to contemporary practices*. Ed. by A. Capponi and C.-A. Lehalle. Cambridge University Press.
Castro, P. S., Li, S., and Zhang, D. (2019). "Inverse Reinforcement Learning with Multiple Ranked Experts." In: *arXiv e-Print*.
Castro, P. S., Moitra, S., Gelada, C., Kumar, S., and Bellemare, M. G. (2018). "Dopamine: A Research Framework for Deep Reinforcement Learning." In: *arXiv e-Print*.
Cesarone, F., Moretti, J., and Tardella, F. (2018). "Why Small Portfolios Are Preferable and How to Choose Them." In: *SSRN e-Print*.
Cesarone, F., Mottura, C., Ricci, J. M., and Tardella, F. (2019). "On the stability of portfolio selection models." In: *SSRN e-Print*.
Chakraborty, S. (2019). "Deep Reinforcement Learning in Financial Markets." In: *arXiv e-Print*.
Chan, Y., Hogan, K., Schwaiger, K., and Ang, A. (2020). "ESG in Factors." In: *The Journal of Impact and ESG Investing* 1(1), pp. 26–45.
Charpentier, A., Elie, R., and Remlinger, C. (2020). "Reinforcement Learning in Economics and Finance." In: *arXiv e-Print*.
Chaudhuri, S. E. and Lo, A. W. (2019). "Dynamic Alpha: A Spectral Decomposition of Investment Performance Across Time Horizons." In: *Management Science* 65(9), pp. 4440–4450.
Chen, A. Y. and Zimmermann, T. (2022). "Open Source Cross-Sectional Asset Pricing." In: *American Finance Association Annual Meeting*.
Chhabra, A. B. (2015). *The Aspirational Investor: Taming the Markets to Achieve Your Life's Goals*. HarperBusiness. 245 pp.
Chib, S. (2020). *R package czfactor*. Tech. rep. Washington University.
Chib, S. and Zhao, L. (2020). *R package czzg*. Tech. rep. Washington University.
Coache, A. and Jaimungal, S. (2022). "Reinforcement Learning with Dynamic Convex Risk Measures." In: *arXiv e-Print*.
Cong, L., Tang, K., Wang, J., and Zhang, Y. (2022). "AlphaPortfolio: Direct Construction Through Deep Reinforcement Learning and Interpretable AI." In: *SSRN e-Print*.
Cong, L. W., Tang, K., Wang, J., and Zhang, Y. (2021). "Deep Sequence Modeling: Development and Applications in Asset Pricing." In: *The Journal of Financial Data Science* 3(1), pp. 28–42.
Coqueret, G. (2022). *Perspectives in sustainable equity investing (website version)*.
Coqueret, G. and Guida, T. (2020). *Machine Learning for Factor Investing: R Version*. Chapman and Hall/CRC. 341 pp.
Cruz Barsce, J., Palombarini, J. A., and Martinez, E. C. (2021). "Automatic tuning of hyper-parameters of reinforcement learning algorithms using Bayesian optimization with behavioral cloning." In: *arXiv e-Print*.
Cuschieri, N., Vella, V., and Bajada, J. (2021). "TD3-Based Ensemble Reinforcement Learning for Financial Portfolio Optimisation." In: *31st International Conference on Automated Planning and Scheduling*.
Cvitanic, J., Kou, S., Wan, X., and Williams, K. L. (2020). "Pi portfolio management: reaching goals while avoiding drawdowns." In: *SSRN e-Print*.
D'Eramo, C., Tateo, D., Bonarini, A., Restelli, M., and Peters, J. (2021). "MushroomRL: Simplifying Reinforcement Learning Research." In: *Journal of Machine Learning Research* 22(131), pp. 1–5.
Das, S. and Varma, S. (2020). "Dynamic Goals-Based Wealth Management using Reinforcement Learning." In: *Journal of Investment Management* 18 (2), pp. 1–20.
Das, S. R., Ostrov, D., Radhakrishnan, A., and Srivastav, D. (2020). "Dynamic portfolio allocation in goals-based wealth management." In: *Computational Management Science* 17, pp. 613–640.
Das, S. R., Ostrov, D., Radhakrishnan, A., and Srivastav, D. (2022a). "Dynamic optimization for multi-goals wealth management." In: *Journal of Banking & Finance* 140 (106192).
Das, S. R., Ostrov, D. N., Casanova, A., Radhakrishnan, A., and Srivastav, D. (2021). "Optimal Goals-Based Investment Strategies For Switching Between Bull and Bear Markets." In: *SSRN e-Print*.

Das, S. R., Ostrov, D. N., Casanova, A., Radhakrishnan, A., and Srivastav, D. (2022b). "Optimal Goals-Based Investment Strategies For Switching Between Bull and Bear Markets." In: *The Journal of Wealth Management* 24(4), pp. 8–36.
Das, S. R. and Ross, G. (2021). "The Role of Options in Goals-Based Wealth Management." In: *SSRN e-Print*.
de Carvalho, M. and Rua, A. (2017). "Real-time nowcasting the US output gap: Singular spectrum analysis at work." In: *International Journal of Forecasting* 33(1), pp. 185–198.
Deguest, R., Martellini, L., Milhau, V., Suri, A., and Wang, H. (2015). *Introducing a Comprehensive Investment Framework for Goals-Based Wealth Management*. Tech. rep. EDHEC Risk Institute.
Dempster, M. A. H., Kloppers, D., Medova, E., Osmolovsky, I., and Ustinov, P. (2016). "Lifecycle Goal Achievement or Portfolio Volatility Reduction?" In: *The Journal of Portfolio Management* 42(2), pp. 99–117.
Denault, M. and Simonato, J.-G. (2022). "A note on a dynamic goal-based wealth management problem." In: *Finance Research Letters* 46 (Part B) (102404).
Ding, L., Ahmed, S., and Shapiro, A. (2020). "A Python package for multi-stage stochastic programming." In: *Optimization Online e-Print*.
Diris, B., Palm, F., and Schotman, P. (2015). "Long-Term Strategic Asset Allocation: An Out-of-Sample Evaluation." In: *Management Science* 61(9), pp. 2185–2202.
Dixon, M. and Polson, N. (2020). "Deep Fundamental Factor Models." In: *SIAM Journal on Financial Mathematics* 11(3), SC–26–SC–37.
Dixon, M. F., Halperin, I., and Bilokon, P. (2020). *Machine Learning in Finance: from theory to practice*. Springer International Publishing. 548 pp.
Dixon, M. F. and Halperin, I. (2020). "G-Learner and GIRL: Goal Based Wealth Management with Reinforcement Learning." In: *SSRN e-Print*.
Dixon, M. F. and Halperin, I. (2021). "Goal-based wealth management with generative reinforcement learning." In: *Risk (Cutting edge)*.
Dong, L., Gao, G., Li, Y., and Wen, Y. (2021a). "Baconian: A Unified Open source Framework for Model-Based Reinforcement Learning." In: *arXiv e-Print*.
Dong, X., Li, Y., Rapach, D., and Zhou, G. (2022). "Anomalies and the expected market return." In: *Journal of Finance* 27(1), pp. 639–681.
Dong, Z., Huang, S., Ma, S., and Qian, Y. (2021b). "Factor Representation and Decision Making in Stock Markets Using Deep Reinforcement Learning." In: *arXiv e-Print*.
Du, J., Jin, M., Kolm, P. N., Ritter, G., Wang, Y., and Zhang, B. (2020). "Deep Reinforcement Learning for Option Replication and Hedging." In: *The Journal of Financial Data Science* 22(44), pp. 44–57.
Dulac-Arnold, G., Levine, N., Mankowitz, D. J., Li, J., Paduraru, C., Gowal, S., and Hester, T. (2021). "An empirical investigation of the challenges of real-world reinforcement learning." In: *arXiv e-Print*.
Fabozzi, F. J., Fabozzi, F. A., Lopez de Prado, M., and Stoyanov, S. (2021). *Asset Management: Tools and Issues*. World Scientific. 516 pp.
Fabozzi, F. J. and Lopez de Prado, M. (2018). "Being Honest in Backtest Reporting: A Template for Disclosing Multiple Tests." In: *The Journal of Portfolio Management* 45(1), pp. 141–147.
Fedus, W., Gelada, C., Bengio, Y., Bellemare, M. G., and Larochelle, H. (2019). "Hyperbolic Discounting and Learning over Multiple Horizons." In: *arXiv e-Print*.
Fischer, T. G. (2018). *Reinforcement learning in financial markets - a survey*. Tech. rep. Friedrich-Alexander University.
Fleiss, A., Kumaar, A., Rida, A., Shin, J., Lai, X., Fant, V., Chen, J., and Li, A. (2021). "Deep Reinforcement Learning and Feature Extraction For Constructing Alpha Generating Equity Portfolios." In: *SSRN e-Print*.
Forsyth, P. A., Vetzal, K. R., and Westmacott, G. (2021). "Optimal control of the decumulation of a retirement portfolio with variable spending and dynamic asset allocation." In: *arXiv e-Print*.
Francois-Lavet, V., Henderson, P., Islam, R., Bellemare, M. G., and Pineau, J. (2018). "An introduction to deep reinforcement learning." In: *Foundations and Trends in Machine Learning* 11(3-4), pp. 219–354.
Freymuth, N., Becker, P., and Neumann, G. (2021). "Versatile Inverse Reinforcement Learning via Cumulative Rewards." In: *arXiv e-Print*.
Fu, J., Tacchetti, A., Perolat, J., and Bachrach, Y. (2021). "Evaluating Strategic Structures in Multi-Agent Inverse Reinforcement Learning." In: *Journal of Artificial Intelligence Research* 71, pp. 925–951.
Fujita, Y., Kataoka, T., Nagarajan, P., and Ishikawa, T. (2021). "ChainerRL: A Deep Reinforcement Learning Library." In: *Journal of Machine Learning Research* 22(77), pp. 1–14.

Garau-Luis, J. J., Crawley, E., and Cameron, B. (2021). "Evaluating the progress of Deep Reinforcement Learning in the real world: aligning domain-agnostic and domain-specific research." In: *arXiv e-Print*.
Gasperov, B., Saric, F., Begusic, S., and Kostanjcar, Z. (2020). "Adaptive rolling window selection for minimum variance portfolio estimation based on reinforcement learning." In: *43rd International Convention on Information, Communication and Electronic Technology (MIPRO)*. IEEE.
Gašperov, B., Begušić, S., Šimović, P. P., and Kostanjčar, Z. (2021). "Reinforcement Learning Approaches to Optimal Market Making." In: *Mathematics* 9(21), p. 2689.
Glanois, C., Weng, P., Zimmer, M., Li, D., Yang, T., Hao, J., and Liu, W. (2022). "A Survey on Interpretable Reinforcement Learning." In: *arXiv e-Print*.
Grealish, A. and Kolm, P. N. (2021). "Robo-Advisory: From Investing Principles and Algorithms to Future Developments." In: *SSRN e-Print*.
Greiner, S. P. and Stoyanov, S. V. (2019). "Portfolio scoring by expected risk premium." In: *The Journal of Portfolio Management* 45(4), pp. 83–90.
Gu, S. (2021). "Deep Reinforcement Learning with Function Properties in Mean Reversion Strategies." In: *arXiv e-Print*.
Guan, M. and Liu, X.-Y. (2021). "Explainable Deep Reinforcement Learning for Portfolio Management: An Empirical Approach." In: *arXiv e-Print*.
Guidolin, M., Hansen, E., and Lozano-Banda, M. (2018). "Portfolio performance of linear SDF models: an out-of-sample assessment." In: *Quantitative Finance* 18(8), pp. 1425–1436.
Guijarro-Ordonez, J., Pelger, M., and Zanotti, G. (2021). "Deep Learning Statistical Arbitrage." In: *SSRN e-Print*.
Guo, D. (2019). "A Statistical Response to Challenges in Vast Portfolio Selection." PhD thesis. University of Waterloo.
Guo, D., Boyle, P. P., Weng, C., and Wirjanto, T. S. (2019). "When Does The 1/N Rule Work?" In: *SSRN e-Print*.
Guo, I., Langrené, N., Loeper, G., and Ning, W. (2022). "Portfolio optimization with a prescribed terminal wealth distribution." In: *Quantitative Finance*, pp. 1–15.
Gurdogan, H. and Kercheval, A. (2021). "Multi Anchor Point Shrinkage for the Sample Covariance Matrix (Extended Version)." In: *arXiv e-Print*.
Haley, M. R. (2017). "K-fold cross validation performance comparisons of six naive portfolio selection rules: how naive can you be and still have successful out-of-sample portfolio performance?" In: *Annals of Finance* 13, pp. 341–353.
Halperin, I. (2019). "The QLBS Q-Learner goes NuQLear: fitted Q iteration, inverse RL, and option portfolios." In: *Quantitative Finance* 19(9), pp. 1543–1553.
Halperin, I. and Feldshteyn, I. (2018). "Market Self-Learning of Signals, Impact and Optimal Trading: Invisible Hand Inference with Free Energy (Or, How We Learned to Stop Worrying and Love Bounded Rationality)." In: *SSRN e-Print*.
Halperin, I., Liu, J., and Zhang, X. (2022). "Combining Reinforcement Learning and Inverse Reinforcement Learning for Asset Allocation Recommendations." In: *arXiv e-Print*.
Hamadanian, P., Schwarzkopf, M., Sen, S., and Alizadeh, M. (2022). "Reinforcement Learning in Time-Varying Systems: an Empirical Study." In: *arXiv e-Print*.
Hambly, B. M., Xu, R., and Yang, H. (2021). "Recent Advances in Reinforcement Learning in Finance." In: *SSRN e-Print*.
Harvey, C. R., Liu, Y., and Saretto, A. (2020). "An Evaluation of Alternative Multiple Testing Methods for Finance Applications." In: *The Review of Asset Pricing Studies* 10(2), pp. 199–248.
Hayes, C. F., Radulescu, R., Bargiacchi, E., Kallstrom, J., Macfarlane, M., Reymond, M., Verstraeten, T., Zintgraf, L. M., Dazeley, R., Heintz, F., Howley, E., Irissappane, A. A., Mannion, P., Nowe, A., Ramos, G., Restelli, M., Vamplew, P., and Roijers, D. M. (2021). "A Practical Guide to Multi-Objective Reinforcement Learning and Planning." In: *arXiv e-Print*.
Hens, T., Schenk-Hoppe, K. R., and Woesthoff, M.-H. (2020). "Escaping the backtesting illusion." In: *The Journal of Portfolio Management* 46(4), pp. 81–93.
Heuillet, A., Couthouis, F., and Díaz-Rodríguez, N. (2021). "Explainability in deep reinforcement learning." In: *Knowledge-Based Systems* 214, p. 106685.
Hieu, L. T. (2020). "Deep Reinforcement Learning for Stock Portfolio Optimization." In: *arXiv e-Print*.
Hirsa, A., Osterrieder, J., Hadji-Misheva, B., and Posth, J.-A. (2021). "Deep reinforcement learning on a multi-asset environment for trading." In: *arXiv e-Print*.

Ho, J., Tumkaya, T., Aryal, S., Choi, H., and Claridge-Chang, A. (2019). "Moving beyond P values: data analysis with estimation graphics." In: *Nature Methods* 16(7), pp. 565–566.
Hoang, C., Sohn, S., Choi, J., Carvalho, W., and Lee, H. (2021). "Successor Feature Landmarks for Long-Horizon Goal-Conditioned Reinforcement Learning." In: *arXiv e-Print*.
Hoffman, M., Shahriari, B., Aslanides, J., Barth-Maron, G., Behbahani, F., Norman, T., Abdolmaleki, A., Cassirer, A., Yang, F., Baumli, K., Henderson, S., Novikov, A., Colmenarejo, S. G., Cabi, S., Gulcehre, C., Paine, T. L., Cowie, A., Wang, Z., Piot, B., and Freitas, N. de (2020). "Acme: A Research Framework for Distributed Reinforcement Learning." In: *arXiv e-Print*.
Homescu, C. (2014). "Many risks, one (optimal) portfolio." In: *SSRN e-Print*.
Homescu, C. (2015). "Better Investing Through Factors, Regimes and Sensitivity Analysis." In: *SSRN e-Print*.
Honchar, A. (2019). *AI for portfolio management: from Markowitz to Reinforcement Learning*. URL: `https://medium.com/swlh/ai-for-portfolio-management-from-markowitz-to-reinforcement-learning-cffedcbba566`.
Hsu, Y.-C., Lin, H.-W., and Vincent, K. (2017). *Do Cross-Sectional Stock Return Predictors Pass the Test without Data-Snooping Bias?* Tech. rep. Institute of Economics Academia Sinica.
Hsu, P.-H., Han, Q., Wu, W., and Cao, Z. (2018). "Asset allocation strategies, data snooping, and the 1 / N rule." In: *Journal of Banking & Finance* 97, pp. 257–269.
Hu, Y.-J. and Lin, S.-J. (2019). "Deep reinforcement learning for optimizing finance portfolio management." In: *Amity International Conference on Artificial Intelligence (AICAI)*. IEEE, pp. 14–20.
Huang, G., Zhou, X., and Song, Q. (2022). "Deep reinforcement learning for portfolio management." In: *arXiv e-Print*.
Huang, M. and Yu, S. (2020). "A new procedure for resampled portfolio with shrinkaged covariance matrix." In: *Journal of Applied Statistics* 47(44), pp. 642–652.
Huang, Z. and Tanaka, F. (2021). "A Modularized and Scalable Multi-Agent Reinforcement Learning-based System for Financial Portfolio Management." In: *arXiv e-Print*.
Hulbert, N., Spillers, S., Francis, B., Haines-Temons, J., Romero, K. G., Jager, B. D., Wong, S., Flora, K., Huang, B., and Irissappane, A. A. (2020). "EasyRL: A Simple and Extensible Reinforcement Learning Framework." In: *arXiv e-Print*.
Hwang, I., Xu, S., and In, F. (2018). "Naive versus optimal diversification: Tail risk and performance." In: *European Journal of Operational Research* 265(1), pp. 372–388.
Ielpo, F., Merhy, C., and Simon, G. (2017). *Engineering Investment Process: Making Value Creation Repeatable*. Elsevier. 430 pp.
Irlam, G. (2020a). *AI Planner*. URL: `https://www.aiplanner.com/`.
Irlam, G. (2020b). "Machine learning for retirement planning." In: *The Journal of Retirement* 8(1), pp. 32–29.
Irlam, G. (2020c). "Multi Scenario Financial Planning via Deep Reinforcement Learning AI." In: *SSRN e-Print*.
Ivanov, S. and D'yakonov, A. (2019). "Modern Deep Reinforcement Learning Algorithms." In: *arXiv e-Print*.
Jaeger, M., Krugel, S., Marinelli, D., Papenbrock, J., and Schwendner, P. (2020). "Understanding machine learning for diversified portfolio construction by explainable AI." In: *SSRN e-Print*.
Jaimungal, S. (2022). "Reinforcement learning and stochastic optimisation." In: *Finance and Stochastics* 26(1), pp. 103–129.
Jaimungal, S., Pesenti, S. M., Wang, Y. S., and Tatsat, H. (2021). "Robust Risk-Aware Reinforcement Learning." In: *SSRN e-Print*.
Jaisson, T. (2022). "Deep differentiable reinforcement learning and optimal trading." In: *arXiv e-Print*.
Janner, M., Li, Q., and Levine, S. (2021). "Reinforcement Learning as One Big Sequence Modeling Problem." In: *arXiv e-Print*.
Jansen, S. (2020). *Machine Learning for Algorithmic Trading (Second Edition)*. Packt Publishing. 820 pp.
Janssen, R., Kramer, B., and Boender, G. (2013). "Life Cycle Investing: From Target-Date to Goal-Based Investing." In: *The Journal of Wealth Management* 16(1), pp. 23–32.
Jordan, S. M., Chandak, Y., Cohen, D., Zhang, M., and Thomas, P. (2020). "Evaluating the Performance of Reinforcement Learning Algorithms." In: *Thirty-seventh International Conference on Machine Learning ICML*.
Jurczenko et al. (2020). *Machine Learning for Asset Management*. Ed. by E. Jurczenko. Wiley. 445 pp.
Kakushadze, Z. and Yu, W. (2016). "Statistical Risk Models." In: *SSRN e-Print*.
Kakushadze, Z. and Yu, W. (2017). "Open Source Fundamental Industry Classification." In: *MDPI Data* 22 (2).
Kakushadze, Z. and Yu, W. (2018a). "Betas, Benchmarks, and Beating the Market." In: *The Journal of Trading*.

Kakushadze, Z. and Yu, W. (2018b). "Decoding stock market with quant alphas." In: *Journal of Asset Management*, pp. 1–11.
Kakushadze, Z. and Yu, W. (2019). "Machine learning risk models." In: *SSRN e-Print*.
Kakushadze, Z. and Yu, W. (2020). "Machine learning treasury yields." In: *SSRN e-Print*.
Katongo, M. and Bhattacharyya, R. (2021). "The Use of Deep Reinforcement Learning in Tactical Asset Allocation." In: *SSRN e-Print*.
Kazak, E. and Pohlmeier, W. (2019). "Testing out-of-sample portfolio performance." In: *International Journal of Forecasting* 35(2), pp. 540–554.
Kazak, E. and Pohlmeier, W. (2020). *Portfolio Pretesting with Machine Learning*. Tech. rep. University of Lancaster.
Khetarpal, K., Riemer, M., Rish, I., and Precup, D. (2021). "Towards Continual Reinforcement Learning: A Review and Perspectives." In: *arXiv e-Print*.
Kim, W. C., Kwon, D.-G., Lee, Y., Kim, J. H., and Lin, C. (2020). "Personalized goal-based investing via multi-stage stochastic goal programming." In: *Quantitative Finance* 20(3) (3), pp. 515–526.
Kirk, R., Zhang, A., Grefenstette, E., and Rocktaschel, T. (2022). "A Survey of Generalisation in Deep Reinforcement Learning." In: *arXiv e-Print*.
Kolesnikov, S. and Hrinchuk, O. (2019). "Catalyst.RL: A Distributed Framework for Reproducible RL Research." In: *arXiv e-Print*.
Kolm, P. N. and Ritter, G. (2020). "Modern Perspectives on Reinforcement Learning in Finance." In: *The Journal of Machine Learning in Finance* 1(1).
Krishnan, S., Garg, A., Liaw, R., Miller, L., Pokorny, F. T., and Goldberg, K. (2016). "HIRL: Hierarchical Inverse Reinforcement Learning for Long-Horizon Tasks with Delayed Rewards." In: *arXiv e-Print*.
Kritzman, M., Kinlaw, W., and Turkington, D. (2017). *A Practitioner's Guide to Asset Allocation*. Wiley. 256 pp.
Kuntz, L.-C. (2018). "Portfolio Strategies with Classical and Alternative Benchmarks." PhD thesis. Georg August University of Gottingen.
Kuttler, H., Nardelli, N., Lavril, T., Selvatici, M., Sivakumar, V., Rocktaschel, T., and Grefenstette, E. (2019). "TorchBeast: A PyTorch Platform for Distributed RL." In: *arXiv e-Print*.
Lai, K.-H., Zha, D., Wang, G., Xu, J., Zhao, Y., Kumar, D., Chen, Y., Zumkhawaka, P., Wan, M., Martinez, D., and Hu, X. (2021). "TODS: An Automated Time Series Outlier Detection System." In: *arXiv e-Print*.
Lambert, N. O., Wilcox, A., Zhang, H., Pister, K. S. J., and Calandra, R. (2021). "Learning Accurate Long-term Dynamics for Model-based Reinforcement Learning." In: *arXiv e-Print*.
Lapan, M. (2020). *Deep Reinforcement Learning Hands-On*. 2nd ed. Packt. 826 pp.
Laskin, M., Lee, K., Stooke, A., Pinto, L., Abbeel, P., and Srinivas, A. (2020). "Reinforcement Learning with Augmented Data." In: *arXiv e-Print*.
Laskin, M., Yarats, D., Liu, H., Lee, K., Zhan, A., Lu, K., Cang, C., Pinto, L., and Abbeel, P. (2021). "URLB: Unsupervised Reinforcement Learning Benchmark." In: *arXiv e-Print*.
Lazaridis, A., Fachantidis, A., and Vlahavas, I. (2020). "Deep Reinforcement Learning: A State-of-the-Art Walkthrough." In: *Journal of Artificial Intelligence Research* 69, pp. 1421–1471.
Lehnert, L. and Littman, M. L. (2020). "Successor Features Combine Elements of Model-Free and Model-based Reinforcement Learning." In: *Journal of Machine Learning Research* 21(196138), pp. 1–53.
Lettau, M. and Pelger, M. (2020). "Factors That Fit the Time Series and Cross-Section of Stock Returns." In: *The Review of Financial Studies* 33(5), pp. 2274–2325.
Li, B., Cowen-Rivers, A., Kozakowski, P., Tao, D., Kamalakara, S., Rajkumar, N., Sezhiyan, H., Huang, S., and Gomez, A. (2019). "RL: Generic reinforcement learning codebase in TensorFlow." In: *The Journal of Open Source Software* 4(42), p. 1524.
Li, L. (2021a). "An Automated Portfolio Trading System with Feature Preprocessing and Recurrent Reinforcement Learning." In: *arXiv e-Print*.
Li, L. (2021b). "Financial Trading with Feature Preprocessing and Recurrent Reinforcement Learning." In: *arXiv e-Print*.
Li, R., Cai, Z., Huang, T., and Zhu, W. (2021a). "Anchor: The achieved goal to replace the subgoal for hierarchical reinforcement learning." In: *Knowledge-Based Systems* 225, p. 107128.
Li, S., Zang, Z., Wu, D., Chen, Z., and Li, S. Z. (2021b). "GenURL: A General Framework for Unsupervised Representation Learning." In: *arXiv e-Print*.

Li, Z., Liu, X.-Y., Zheng, J., Wang, Z., Walid, A., and Guo, J. (2021c). "FinRL-Podracer: High Performance and Scalable Deep Reinforcement Learning for Quantitative Finance." In: *ACM International Conference on AI in Finance*.

Liao, S.-L., Lin, S.-K., Kuang, X.-J., and Chen, T. (2022). "Portfolio Allocation with Dynamic Risk Preference Via Reinforcement Learning: Evidence from the Taiwan 50 Index." In: *SSRN e-Print*.

Liu, D., Alnegheimish, S., Zytek, A., and Veeramachaneni, K. (2021a). "MTV: Visual Analytics for Detecting, Investigating, and Annotating Anomalies in Multivariate Time Series." In: *arXiv e-Print*.

Liu, M., Zhu, M., and Zhang, W. (2022a). "Goal-Conditioned Reinforcement Learning: Problems and Solutions." In: *arXiv e-Print*.

Liu, X.-Y., Rui, J., Gao, J., Yang, L., Yang, H., Wang, Z., Wang, C. D., and Guo, J. (2022b). "FinRL-Meta: A Universe of Near-Real Market Environments for Data-Driven Deep Reinforcement Learning in Quantitative Finance." In: *arXiv e-Print*.

Liu, X.-Y., Yang, H., Gao, J., and Wang, C. (2021b). "FinRL: Deep Reinforcement Learning Framework to Automate Trading in Quantitative Finance." In: *SSRN e-Print*.

Llorente, F., Martino, L., Read, J., and Delgado, D. (2021). "A survey of Monte Carlo methods for noisy and costly densities with application to reinforcement learning." In: *arXiv e-Print*.

Lohre, H., Rother, C., and Schafer, K. A. (2020). "Hierarchical Risk Parity: Accounting for Tail Dependencies in Multi-asset Multi-factor Allocations." In: *Machine Learning for Asset Management: New Developments and Financial Applications*. Ed. by E. Jurczenko. Wiley, pp. 329–368.

Loon, K. W., Graesser, L., and Cvitkovic, M. (2019). "SLM Lab: A Comprehensive Benchmark and Modular Software Framework for Reproducible Deep Reinforcement Learning." In: *arXiv e-Print*.

Lopez de Prado, M. (2019). "A Data Science Solution to the Multiple-Testing Crisis in Financial Research." In: *The Journal of Financial Data Science* 1(1), pp. 99–110.

Lopez de Prado, M. (2020). *Machine learning for asset managers*. Cambridge University Press. 190 pp.

Lopez de Prado, M. and Lewis, M. J. (2019). "Detection of false investment strategies using unsupervised learning methods." In: *Quantitative Finance* 19(9), pp. 1555–1565.

Ma, Y. c. (, Wang, Z., and Fleiss, A. (2021). "Deep Q-Learning for Trading Cryptocurrency." In: *The Journal of Financial Data Science* 3(3), pp. 121–127.

Majid, A. Y., Saaybi, S., Rietbergen, T. van, Francois-Lavet, V., Prasad, R. V., and Verhoeven, C. (2021). "Deep Reinforcement Learning Versus Evolution Strategies: A Comparative Survey." In: *arXiv e-Print*.

Malavasi, M., Lozza, S. O., and Truck, S. (2021). "Second order of stochastic dominance efficiency vs mean variance efficiency." In: *European Journal of Operational Research* 290(3), pp. 1192–1206.

Marinescu, M. (2022). "Risk-Based Optimal Portfolio Strategies: A Compendium." In: *SSRN e-Print*.

Martellini, L., Milhau, V., and Mulvey, J. (2020). "Securing Replacement Income with Goal-Based Retirement Investing Strategies." In: *The Journal of Retirement* 7(4), pp. 8–26.

Martin, R. (2021). "PyPortfolioOpt: portfolio optimization in Python." In: *Journal of Open Source Software* 6(61), p. 3066.

Marwood, D. and Minnen, D. (2020). "Safely Boosting Retirement Income by Harmonizing Drawdown Paths." In: *Journal of Financial Planning* 33(11), pp. 46–60.

Marzban, S., Delage, E., Li, J. Y., Desgagne-Bouchard, J., and Dussault, C. (2021). "WaveCorr: Correlation-savvy Deep Reinforcement Learning for Portfolio Management." In: *arXiv e-Print*.

Maschner, C., Moritz, B., and Schmitz, M. (2021). "Modern Asset Management." In: *SSRN e-Print*.

McIndoe, C. (2020). "A Data Driven Approach to Market Regime Classification." MA thesis. Imperial College.

Micheli, A. and Neuman, E. (2022). "Evidence of Crowding on Russell 3000 Reconstitution Events." In: *arXiv e-Print*.

Milevsky, M. A. (2020). *Retirement Income Recipes in R: From Ruin Probabilities to Intelligent Drawdowns*. Springer International Publishing. 302 pp.

Moerland, T. M., Broekens, J., and Jonker, C. M. (2021). "Model-based Reinforcement Learning: A Survey." In: *arXiv e-Print*.

Mohammed, S., Bealer, R., and Cohen, J. (2021). "Embracing advanced AI/ML to help investors achieve success: Vanguard Reinforcement Learning for Financial Goal Planning." In: *arXiv e-Print*.

Mooney, T., Rapaka, R., and Vera, T. (2020). "Dynamic Regime Strategy for Stress Testing and Optimizing Institutional Investor Portfolios." In: *SSRN e-Print*.

Mosavi, A., Ghamisi, P., Faghan, Y., Duan, P., ardabili, sina faizollahzadeh, Salwana, E., and Band, S. (2020). "Comprehensive Review of Deep Reinforcement Learning Methods and Applications in Economics." In: *SSRN e-Print*.

Mulvey, J. M., Martellini, L., Hao, H., and Li, N. (2019). "A Factor- and Goal-Driven Model for Defined Benefit Pensions: Setting Realistic Benefits." In: *The Journal of Portfolio Management* 45 (3), pp. 165–177.

Muralidhar, A. (2020). "Asset Pricing, Asset Allocation and Risk-Adjusted Performance with Multiple Goals and Agency: The Goals and Risk-based Asset Pricing Model." In: *SSRN e-Print*.

Nachum, O., Tang, H., Lu, X., Gu, S., Lee, H., and Levine, S. (2019). "Why Does Hierarchy (Sometimes) Work So Well in Reinforcement Learning?" In: *arXiv e-Print*.

Naeem, M., Rizvi, S. T. H., and Coronato, A. (2020). "A Gentle Introduction to Reinforcement Learning and its Application in Different Fields." In: *IEEE Access* 8, pp. 209320–209344.

Nguyen, N. D., Nguyen, T. T., Nguyen, H., and Nahavandi, S. (2021). "Review, Analyze, and Design a Comprehensive Deep Reinforcement Learning Framework." In: *arXiv e-Print*.

Noguer i Alonso, M. and Srivastava, S. (2020). "Deep Reinforcement Learning for Asset Allocation in US Equities." In: *arXiv e-Print*.

Odermatt, L., Beqiraj, J., and Osterrieder, J. (2021). "Deep Reinforcement Learning for Finance and the Efficient Market Hypothesis." In: *SSRN e-Print*.

Pardo, F. (2021). "Tonic: A Deep Reinforcement Learning Library for Fast Prototyping and Benchmarking." In: *arXiv e-Print*.

Parker, F. J. (2016a). "Goal-Based Portfolio Optimization." In: *The Journal of Wealth Management* 19(3), pp. 22–30.

Parker, F. J. (2016b). "Portfolio Selection in a Goal-Based Setting." In: *The Journal of Wealth Management* 19(2), pp. 41–46.

Parker, F. J. (2020). "Allocation of wealth both within and across goals: a practitioner guide." In: *The Journal of Wealth Management* 23(1), pp. 8–21.

Parker, F. J. (2021a). "A Goals-Based Theory of Utility." In: *Journal of Behavioral Finance* 22(1), pp. 10–25.

Parker, F. J. (2021b). "Achieving Goals While Making an Impact: Balancing Financial Goals with Impact Investing." In: *The Journal of Impact and ESG Investing* 1(3), pp. 27–38.

Parker, F. J. (2021c). "Multi-Period Goals-Based Portfolio Optimization." In: *SSRN e-Print*.

Parker-Holder, J., Rajan, R., Song, X., Biedenkapp, A., Miao, Y., Eimer, T., Zhang, B., Nguyen, V., Calandra, R., Faust, A., Hutter, F., and Lindauer, M. (2022). "Automated Reinforcement Learning (AutoRL): A Survey and Open Problems." In: *arXiv e-Print*.

Perrin, S. and Roncalli, T. (2020). "Machine Learning Optimization Algorithms & Portfolio Allocation." In: *Machine Learning for Asset Management: New Developments and Financial Applications*. Ed. by E. Jurczenko. Wiley, pp. 261–328.

Pineda, L., Amos, B., Zhang, A., Lambert, N. O., and Calandra, R. (2021). "MBRL-Lib: A Modular Library for Model-based Reinforcement Learning." In: *arXiv e-Print*.

Plaat, A. (2022). "Deep Reinforcement Learning." In: *arXiv e-Print*.

Plaat, A., Kosters, W., and Preuss, M. (2021). "High-Accuracy Model-Based Reinforcement Learning, a Survey." In: *arXiv e-Print*.

Platanakis, E., Sutcliffe, C. M., and Ye, X. (2021). "Horses for Courses: Mean-Variance for Asset Allocation and 1/N for Stock Selection." In: *European Journal of Operational Research* 288(1), pp. 302–317.

Pretorius, A., Tessera, K.-a., Smit, A. P., Formanek, C., Grimbly, S. J., Eloff, K., Danisa, S., Francis, L., Shock, J., Kamper, H., Brink, W., Engelbrecht, H., Laterre, A., and Beguir, K. (2021). "Mava: a research framework for distributed multi-agent reinforcement learning." In: *arXiv e-Print*.

Pricope, T.-V. (2021). "Deep Reinforcement Learning in Quantitative Algorithmic Trading: A Review." In: *arXiv e-Print*.

Prollochs, N. and Feuerriegel, S. (2019). "ReinforcementLearning: A Package to Perform Model-Free Reinforcement Learning in R." In: *The Journal of Open Source Software* 4(38), p. 1087.

Qian, H. and Yu, Y. (2021). "Derivative-Free Reinforcement Learning: A Review." In: *arXiv e-Print*.

Qian, W., Rolling, C. A., Cheng, G., and Yang, Y. (2022). "Combining forecasts for universally optimal performance." In: *International Journal of Forecasting*.

Radovanov, B. and Marcikic, A. (2014). "Testing The Performance Of The Investment Portfolio Using Block Bootstrap Method." In: *Economic Themes* 52(2).

Rafati, J. and Marcia, R. F. (2018). "Deep Reinforcement Learning via L-BFGS Optimization." In: *arXiv e-Print*.
Raileanu, R., Goldstein, M., Yarats, D., Kostrikov, I., and Fergus, R. (2021). "Automatic Data Augmentation for Generalization in Deep Reinforcement Learning." In: *arXiv e-Print*.
Rao, A. and Jelvis, T. (2022). *Foundations of Reinforcement Learning with Applications in Finance*.
Rebonato, R. (2019). "A financially justifiable and practically implementable approach to coherent stress testing." In: *Quantitative Finance* 19(5), pp. 827–842.
Ren, T., Zhang, T., Szepesvari, C., and Dai, B. (2021). "A Free Lunch from the Noise: Provable and Practical Exploration for Representation Learning." In: *arXiv e-Print*.
Roncalli, T. (2019). "How Machine Learning Can Improve Portfolio Allocation of Robo-Advisors." In: *SwissQuant Conference*.
Roncalli, T. (2021). "Advanced Course in Asset Management." In: *SSRN e-Print*.
Sarmas, E., Xidonas, P., and Doukas, H. (2020). *Multicriteria Portfolio Construction with Python*. Springer International Publishing.
Sato, Y. (2019). "Model-Free Reinforcement Learning for Financial Portfolios: A Brief Survey." In: *arXiv e-Print*.
Schumann, E. (2019). "Backtesting." In: *SSRN e-Print*.
Schwarzer, M., Rajkumar, N., Noukhovitch, M., Anand, A., Charlin, L., Hjelm, D., Bachman, P., and Courville, A. (2021). "Pretraining Representations for Data-Efficient Reinforcement Learning." In: *arXiv e-Print*.
Seymour, A., Flint, E. J., and Chikurunhe, F. (2018). "Dynamic portfolio management strategies: A framework for historical analysis." In: *SSRN e-Print*.
Shalett, L. (2015). *An Outcomes-Oriented Approach to Alternatives*. Tech. rep. Morgan Stanley Wealth Management.
Sharma, A., Syrgkanis, V., Zhang, C., and Kiciman, E. (2021). "DoWhy: Addressing Challenges in Expressing and Validating Causal Assumptions." In: *arXiv e-Print*.
Shi, W., Song, S., Wang, Z., and Huang, G. (2020). "Self-Supervised Discovering of Causal Features: Towards Interpretable Reinforcement Learning." In: *arXiv e-Print*.
Shi, X., Xu, D., and Zhang, Z. (2022). "Deep Learning Algorithms for Hedging with Frictions." In: *arXiv e-Print*.
Siebert, J., Gross, J., and Schroth, C. (2021). "A systematic review of Python packages for time series analysis." In: *Engineering Proceedings* 5(1) (22).
Simos, T. E., Mourtas, S. D., and Katsikis, V. N. (2021). "Time-varying Black–Litterman portfolio optimization using a bio-inspired approach and neuronets." In: *Applied Soft Computing* 112, p. 107767.
Snow, D. (2019). "Machine learning in asset management." In: *SSRN e-Print*.
Snow, D. (2020a). "Machine Learning in Asset Management - Part 2: Portfolio Construction - Weight Optimization." In: *The Journal of Financial Data Science* 2 (2), pp. 17–24.
Snow, D. (2020b). "Machine Learning in Asset Management Part 1: Portfolio Construction Trading Strategies." In: *The Journal of Financial Data Science* 2(1) (1), pp. 10–23.
Soleymani, F. and Paquet, E. (2021). "Deep Graph Convolutional Reinforcement Learning for Financial Portfolio Management - DeepPocket." In: *Expert Systems with Applications*.
Staley, E. W., Rivera, C. G., and Llorens, A. J. (2021). "The AI Arena: A Framework for Distributed Multi-Agent Reinforcement Learning." In: *arXiv e-Print*.
Stapelberg, B. and Malan, K. M. (2021). "A survey of benchmarking frameworks for reinforcement learning." In: *arXiv e-Print*.
Stooke, A. and Abbeel, P. (2018). "Accelerated Methods for Deep Reinforcement Learning." In: *arXiv e-Print*.
Stooke, A. and Abbeel, P. (2019). "rlpyt: A Research Code Base for Deep Reinforcement Learning in PyTorch." In: *arXiv e-Print*.
Suhonen, A., Lennkh, M., and Perez, F. (2017). "Quantifying Backtest Overfitting in Alternative Beta Strategies." In: *The Journal of Portfolio Management* 43 (2), pp. 90–104.
Sun, H., Zhong, J., Ma, Y., Han, Z., and He, K. (2021a). "TimeTraveler: Reinforcement Learning for Temporal Knowledge Graph Forecasting." In: *arXiv e-Print*.
Sun, S., Wang, R., and An, B. (2021b). "Reinforcement Learning for Quantitative Trading." In: *arXiv e-Print*.
Suri, K., Shi, X. Q., Plataniotis, K., and Lawryshyn, Y. (2021). "TradeR: Practical Deep Hierarchical Reinforcement Learning for Trade Execution." In: *arXiv e-Print*.
Sutton, R. S. and Barto, A. G. (2018). *Reinforcement Learning: An Introduction (Second Edition)*. MIT Press. 552 pp.
Taljaard, B. H. and Maré, E. (2021). "Why has the equal weight portfolio underperformed and what can we do about it?" In: *Quantitative Finance* 21(11), pp. 1855–1868.

Tarbouriech, J., Domingues, O. D., Menard, P., Pirotta, M., Valko, M., and Lazaric, A. (2021). "Adaptive Multi-Goal Exploration." In: *arXiv e-Print*.
Tatsat, H., Puri, S., and Lookabaugh, B. (2020). *Machine Learning and Data Science Blueprints for Finance: From Building Trading Strategies to Robo-Advisors Using Python*. O'Reilly. 400 pp.
Tayali, S. T. (2020). "A novel backtesting methodology for clustering in mean–variance portfolio optimization." In: *Knowledge-Based Systems* 209, p. 106454.
Terry, J. K., Black, B., Grammel, N., Jayakumar, M., Hari, A., Sullivan, R., Santos, L., Perez, R., Horsch, C., Dieffendahl, C., Williams, N. L., Lokesh, Y., and Ravi, P. (2021). "PettingZoo: Gym for Multi-Agent Reinforcement Learning." In: *arXiv e-Print*.
Traccucci, P., Dumontier, L., Garchery, G., and Jacot, B. (2019). "A Triptych Approach for Reverse Stress Testing of Complex Portfolios." In: *Risk (Cutting Edge)*.
Tuck, J., Barratt, S., and Boyd, S. (2022). "Portfolio Construction Using Stratified Models." In: *Machine Learning in Financial Markets: A guide to contemporary practices*. Ed. by A. Capponi and C.-A. Lehalle. Cambridge University Press.
Ungari, S. and Benhamou, E. (2021). "Deep Reinforcement Learning for Portfolio Allocation." In: *Risk Magazine Global Quant Network*.
Ungolo, F., Sherris, M., and Zhou, Y. (2021). "affine_mortality: A Github repository for estimation, analysis, and projection of affine mortality models." In: *SSRN e-Print*.
Valentine, K. D., Buchanan, E. M., Scofield, J. E., and Beauchamp, M. T. (2019). "Beyond p values: utilizing multiple methods to evaluate evidence." In: *Behaviormetrika* 46(1), pp. 121–144.
Vamossy, D. and Skog, R. (2021). "EmTract: Investor Emotions and Market Behavior." In: *arXiv e-Print*.
Vanini, P. (2020). "Asset Management." In: *SSRN e-Print*.
Vincent, K., Hsu, Y.-C., and Lin, H.-W. (2018). "Analyzing the Performance of Multifactor Investment Strategies under a Multiple Testing Framework." In: *The Journal of Portfolio Management* 44(4), pp. 113–126.
Vinod, H. D. (2021). "R Package GeneralCorr Functions for Portfolio Choice." In: *SSRN e-Print*.
Vovk, V. and Wang, R. (2020). "True and false discoveries with e-values." In: *arXiv e-Print*.
Vovk, V. and Wang, R. (2021). "E-values: Calibration, combination, and applications." In: *Annals of Statistics* 49(3), pp. 1736–1753.
Wang, H. and Yu, S. (2021). "Robo-Advising: Enhancing Investment with Inverse Optimization and Deep Reinforcement Learning." In: *arXiv e-Print*.
Wang, H., Suri, A., Laster, D., and Almadi, H. (2011). "Portfolio Selection in Goals-Based Wealth Management." In: *The Journal of Wealth Management* 14(1), pp. 55–65.
Wang, T., Bao, X., Clavera, I., Hoang, J., Wen, Y., Langlois, E., Zhang, S., Zhang, G., Abbeel, P., and Ba, J. (2019). "Benchmarking Model-Based Reinforcement Learning." In: *arXiv e-Print*.
Wells, L. and Bednarz, T. (2021). "Explainable AI and Reinforcement Learning—A Systematic Review of Current Approaches and Trends." In: *Frontiers in Artificial Intelligence* 4.
Weng, J., Chen, H., Yan, D., You, K., Duburcq, A., Zhang, M., Su, H., and Zhu, J. (2022). "Tianshou: a Highly Modularized Deep Reinforcement Learning Library." In: *arXiv e-Print*.
Wiecki, T., Campbell, A., Lent, J., and Stauth, J. (2016). "All That Glitters Is Not Gold: Comparing Backtest and Out-of-Sample Performance on a Large Cohort of Trading Algorithms." In: *The Journal of Investing* 25(3), pp. 69–80.
Xing, L. (2019). "Learning and Exploiting Multiple Subgoals for Fast Exploration in Hierarchical Reinforcement Learning." In: *arXiv e-Print*.
Xiong, Z., Liu, X.-Y., Zhong, S., Yang, H., and Walid, A. (2018). "Practical Deep Reinforcement Learning Approach for Stock Trading." In: *arXiv e-Print*.
Xu, R. and Chen, Z. (2021). "A Validation Tool for Designing Reinforcement Learning Environments." In: *arXiv e-Print*.
Yaghmaie, F. A. and Ljung, L. (2021). "A Crash Course on Reinforcement Learning." In: *arXiv e-Print*.
Yang, H., Liu, X.-Y., Zhong, S., and Walid, A. (2020a). "Deep Reinforcement Learning for Automated Stock Trading: An Ensemble Strategy." In: *SSRN e-Print*.
Yang, T., Tang, H., Bai, C., Liu, J., Hao, J., Meng, Z., and Liu, P. (2022). "Exploration in Deep Reinforcement Learning: A Comprehensive Survey." In: *arXiv e-Print*.
Yang, Y., UY, M. C. S., and Huang, A. (2020b). "FinBERT: A Pretrained Language Model for Financial Communications." In: *arXiv e-Print*.

Yashaswi, K. (2021). "Deep Reinforcement Learning for Portfolio Optimization using Latent Feature State Space (LFSS) Module." In: *arXiv e-Print*.
Yekelchik, B., Tatsat, H., and Coriarty, Z. (2021). "Deep Q-Network Interpertability: Applications to ETF Trading." In: *SSRN e-Print*.
Yu, L. (2021). "Comparing Classical Portfolio Optimization and Robust Portfolio Optimization on Black Swan Events." MA thesis. University of Waterloo.
Yu, L., Hardle, W. K., Borke, L., and Benschop, T. (2020). "An AI approach to measuring financial risk." In: *SSRN e-Print*.
Yuan, M. and Zhou, G. (2022). "Why Naive 1/N Diversification Is Not So Naive, and How to Beat It?" In: *SSRN e-Print*.
Zhang, B., Rajan, R., Pineda, L., Lambert, N., Biedenkapp, A., Chua, K., Hutter, F., and Calandra, R. (2021). "On the Importance of Hyperparameter Optimization for Model-based Reinforcement Learning." In: *arXiv e-Print*.
Zhang, C., Vinyals, O., Munos, R., and Bengio, S. (2018). "A Study on Overfitting in Deep Reinforcement Learning." In: *arXiv e-Print*.
Zhang, C., Li, Y., Chen, X., Jin, Y., Tang, P., and Li, J. (2020a). "DoubleEnsemble: A New Ensemble Method Based on Sample Reweighting and Feature Selection for Financial Data Analysis." In: *IEEE International Conference on Data Mining (ICDM)*. IEEE.
Zhang, F., Guo, R., and Cao, H. (2020b). "Information Coefficient as a Performance Measure of Stock Selection Models." In: *arXiv e-Print*.
Zhang, H. and Yu, T. (2020). "Taxonomy of Reinforcement Learning Algorithms." In: *Deep Reinforcement Learning*. Springer Singapore, pp. 125–133.
Zhang, Z., Zohren, S., and Roberts, S. (2020c). "Deep Learning for Portfolio Optimization." In: *The Journal of Financial Data Science* 22(4), pp. 8–20.
Zhao, D., Zhang, L., Zhang, B., Zheng, L., Bao, Y., and Yan, W. (2019). "Deep Hierarchical Reinforcement Learning Based Recommendations via Multi-goals Abstraction." In: *arXiv e-Print*.
Zhu, Z., Lin, K., and Zhou, J. (2021). "Transfer Learning in Deep Reinforcement Learning: A Survey." In: *arXiv e-Print*.

Appendix A: Overviews of investment processes and models in QWIM

References

List of references:

Coqueret and Guida (*Machine Learning for Factor Investing: R Version*, 2020)
Dixon et al. (*Machine Learning in Finance: from theory to practice*, 2020)
Fabozzi et al. (*Asset Management: Tools and Issues*, 2021)
Grealish and Kolm ("Robo-Advisory: From Investing Principles and Algorithms to Future Developments," 2021)
Homescu ("Many risks, one (optimal) portfolio," 2014)
Homescu ("Better Investing Through Factors, Regimes and Sensitivity Analysis," 2015)
Jansen (*Machine Learning for Algorithmic Trading (Second Edition)*, 2020)
Jurczenko et al. (*Machine Learning for Asset Management*, 2020)
Kritzman et al. (*A Practitioner's Guide to Asset Allocation*, 2017)
Lopez de Prado (*Machine learning for asset managers*, 2020)
Maschner et al. ("Modern Asset Management," 2021)
Perrin and Roncalli ("Machine Learning Optimization Algorithms & Portfolio Allocation," 2020)
Roncalli ("Advanced Course in Asset Management," 2021)
Vanini ("Asset Management," 2020)

Online courses

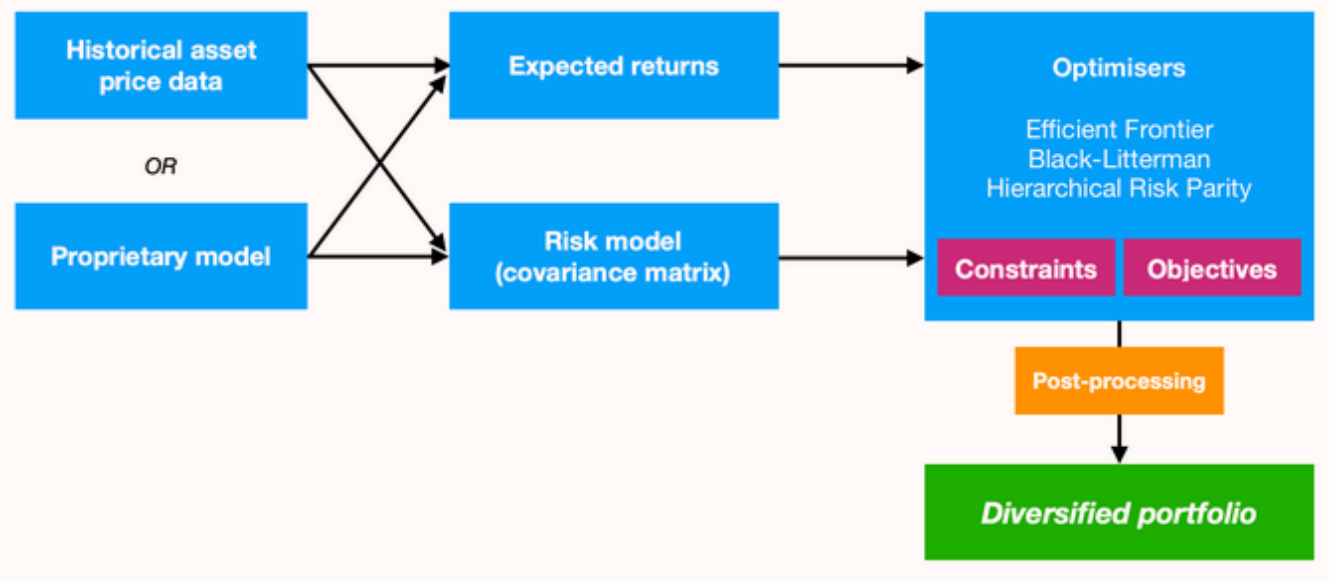
List of online courses:

- Investment Management with Python and Machine Learning Specialization
  - Introduction to Portfolio Construction and Analysis with Python
  - Advanced Portfolio Construction and Analysis with Python
  - Python and Machine Learning for Asset Management
  - Python and Machine Learning for Asset Management with Alternative Data Sets
- Machine Learning and Reinforcement Learning in Finance Specialization
  - Guided Tour of Machine Learning in Finance
  - Fundamentals of Machine Learning in Finance
  - Reinforcement Learning in Finance
  - Overview of Advanced Methods of Reinforcement Learning in Finance
- Investment Management Specialization
  - Understanding Financial Markets
  - Meeting Investors' Goals
  - Portfolio and Risk Management
  - Securing Investment Returns in the Long Run
  - Planning your Client's Wealth over a 5-year Horizon
- Investment and Portfolio Management Specialization
  - Global Financial Markets and Instruments
  - Portfolio Selection and Risk Management
  - Biases and Portfolio Selection
  - Investment Strategies and Portfolio Analysis
  - Build a Winning Investment Portfolio

Appendix C: Incorporating comparison of portfolio metrics using benchmark portfolios

For your QWIM project it is likely that you would compare investment portfolios constructed using your method(s) versus benchmark portfolios constructed using most common "optimal portfolio" types used in the industry and in academia. See below for an example of how this can be done.

Figure 7: Example of portfolio optimization process



Source: PyPortfolioOpt

Portfolio optimization methods

List of portfolio optimization methods may include (see Roncalli ("Advanced Course in Asset Management," 2021) and Perrin and Roncalli ("Machine Learning Optimization Algorithms & Portfolio Allocation," 2020) for a comprehensive overview of such methods):

- equal weighting
- mean variance optimization (Markowitz)
- minimum variance optimization
- maximum diversification
- risk budgeting/risk parity
- hierarchical risk parity
- Black-Litterman
- robust versions of some the above portfolio optimization methods

Some relevant links:

- Portfolio Optimization: A General Framework for Portfolio Choice
- Performance of risk-based asset allocation strategies
- Revisiting the Portfolio Optimization Machine Portfolio
- Construction Techniques Applied to Traditional Multi Asset Portfolios

Python and R packages/codes for portfolio optimization

- Codes mentioned in Snow ("Machine Learning in Asset Management - Part 2: Portfolio Construction - Weight Optimization," 2020)
- Empyrial
- MLFinLab
- Optimal Portfolio
- PortfolioAnalytics
- PortfolioLab
- PyPortfolioOpt
- Quantropy
- Riskfolio-Lib
- RiskPortfolios
- riskparityportfolio

Portfolio metrics

List of portfolio metrics may include some of the following (see Bacon ("Performance Attribution: History and Progress," 2019) for a comprehensive list):

- Sharpe ratio
- Sortino ratio
- Information ratio
- Maximum Drawdown
- expected shortfall
- maximum loss
- and more.

Some relevant links:

- Portfolio metrics
- Picking the Right Risk-Adjusted Performance Metric
- Risk-Adjusted Performance Measurement – State of the Art
- An Investor's Guide to the Risk Versus Return Conundrum
- How sharp is the Sharpe ratio? Risk-adjusted Performance Measures

Python and R packages/codes for portfolio metrics and performance evaluation

- bt
- empyrical
- ffn
- JFE
- MLFinLab
- PerformanceAnalytics
- portfolioBacktest
- Portfolio Optimization and Performance Evaluation
- Pyfolio
- QuantStats
- Riskfolio-Lib
- tidyquant

How to compare investment portfolios

Let us consider portfolio optimization methods (selected from the ones implemented in Python and/or R packages mentioned above, such as PyPortfolioOpt) which rely on based on expected returns and expected covariance matrix.

One would construct two portfolios (let's call them Traditional and Enhanced) using the same portfolio optimization method(s), where the only difference would be in terms of the inputs (expected returns and expected covariance matrix) to the optimization method:

As of the date of portfolio construction, expected returns and expected covariance matrix can be either calculated using only historical data or, respectively, output from your model. Then one would compare side-by-side various portfolio metrics for these two portfolios. Comparison would be done across the entire Out-Of-Sample period, and also across each market regine period.

NOTE: If you have N forecasting methods used in your coding framework, then for each optimizaton method you would end up with (1+N) optimal portfolios

To exemplifty, let's say that you want to construct portfolios at date of June 20, 2019, and you have data as below

- Range of entire dataset: January 1st, 1990 - August 1, 2020
- Range of Training dataset: January 1st, 1990- February 20, 2017
- Range of Test dataset: February 20, 2017 - August 1, 2020

For Traditional portfolio:

- vector of expected means is calculated based on historical data available at June 20, 2019 (namely from 1990 to June 19, 2019)
- expected covariance matrix is calculated based on historical data available at June 20, 2019 (namely from 1990 to June 19, 2019)

For Enhanced portfolio:

- vector of expected means is calculated based on forecasted values available at June 20, 2019 and obtained using the forecasted model trained on given training dataset (which is from 1990 to 2017)

- expected covariance matrix is calculated based on forecasted values available at June 20, 2019 and obtained using the forecasted model trained on given training dataset (which is from 1990 to 2017)

Then one would compare various portfolio metrics among the two portfolios. These metrics can be calculated on following time periods:

- from date of portfolio construction (June 20, 2019) to last date for which you have data (August 1, 2020)
- from starting date of dataset (January 1st, 1990) to last date for which you have data (August 1, 2020)
- from starting date of dataset (January 1st, 1990) to date of portfolio construction (June 20, 2019)

So you would have side-by-side comparisons of portfolio metrics for each of the above 3 time periods.

Portfolio metrics can be calculated using various Python and/or R packages mentioned above.