

# HW2

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## R Markdown

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see <http://rmarkdown.rstudio.com>.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
# summary(cars)
```

## Including Plots

You can also embed plots, for example:

Note that the `echo = FALSE` parameter was added to the code chunk to prevent printing of the R code that generated the plot.

## Problem 1

1.

$$\text{Var}(X - Y) = \text{Var}[X + (-Y)] = \text{Var}(X) + \text{Var}(Y) - 2\text{Cov}(X, Y) \quad (\text{mailing tube (3.73)})$$

Let  $X$  and  $Y$  be independent random variables. Then,  $E(XY) = E(X) * E(Y)$ .

By definition,  $\text{Cov}(U, V) = E(UV) - E(U) * E(V)$  (mailing tube (3.72)).

$$\begin{aligned} \text{Thus, in this problem, } \text{Cov}(X, Y) &= E(XY) - E(X) * E(Y) \\ &= E(XY) - E(XY) \\ &= 0 \end{aligned}$$

Thus, when  $X$  and  $Y$  are independent, then  $\text{Var}(X - Y) = \text{Var}(X) + \text{Var}(Y)$

2.

## Problem 4

1. The values the random variable can take are  $\{(1,1), (1,2), (1,3), (1,4), (2,1), (2,2), (2,3), (2,4), (3,1), (3,2), (3,3), (3,4), (4,1), (4,2), (4,3), (4,4)\}$
2. The PMF is:

X	2	3	4	5	6	7	8
P(x)	1/16	2/16	3/16	4/16	3/16	2/16	1/16

3. The Expected value of X is:

$$E(x) = x \cdot f(x) = 2 \cdot (1/16) + 3 \cdot (2/16) + 4 \cdot (3/16) + 5 \cdot (4/16) + 6 \cdot (3/16) + 7 \cdot (2/16) + 8 \cdot (1/16) = 80/16$$

## Problem 5

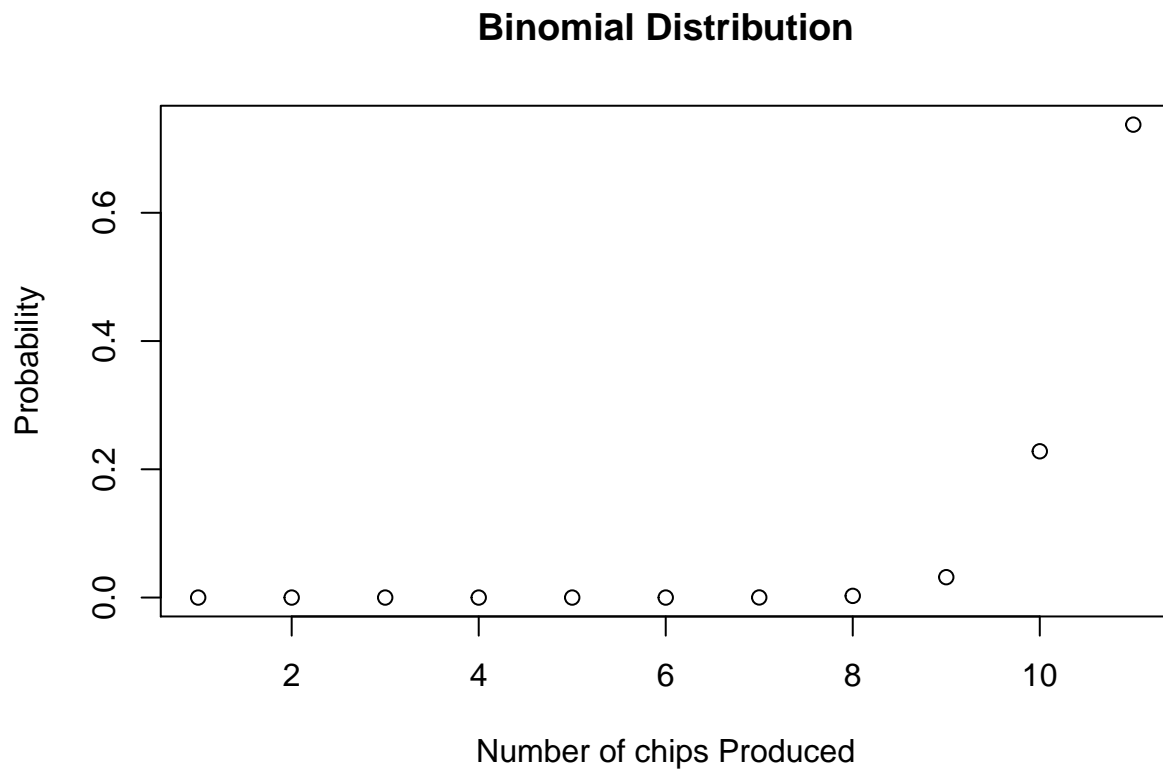
1.

The PMF of x:

$$P(x = X) = nCx \cdot p^x \cdot (1-p)^{n-x}$$

$$P = 0.97, n = 10$$

```
X <- 0:10  
  
plot(dbinom(X,10,0.97), col="black", main = "Binomial Distribution", xlab = "Number of chips Produced",
```



2.

The rate of failure  $p' = 1 - 0.97 = 0.03$

```
1-pbinom(1,10,0.03)
```

```
## [1] 0.03450656
```