

# hw1

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## Problem 2

Looking to solve:

- $P(c = 0 \mid X1 = X2)$
- $P(c = 1 \mid X1 = X2)$
- $P(c = 2 \mid X1 = X2)$

### 0 Collisions

$$P(c = 0 \mid X1 = X2) = P(c = 0 \mid X1 = X2 = 1) + P(c = 0 \mid X1 = X2 = 2)$$

$$P(c = 0 \mid X1 = X2 = 1) = P(X1 = X2 = 1 \text{ and } c = 0) / P(X1 = X2 = 1)$$

$$\begin{aligned} P(X1 = X2 = 1) &= P(X1 = 1) * P(X2 = 1 \mid X1 = 1) \\ &= 2p(1-p) + [P(X2 = 1 \mid \text{no activation}) + P(X2 = 1 \mid \text{activation})] \\ &= 2p(1-p) * [(1-p)(1-q)] + p(1-p)q + (1-p)pq \\ &= 0.24192 \end{aligned}$$