

TEMA 4. CADENAS DE MARKOV

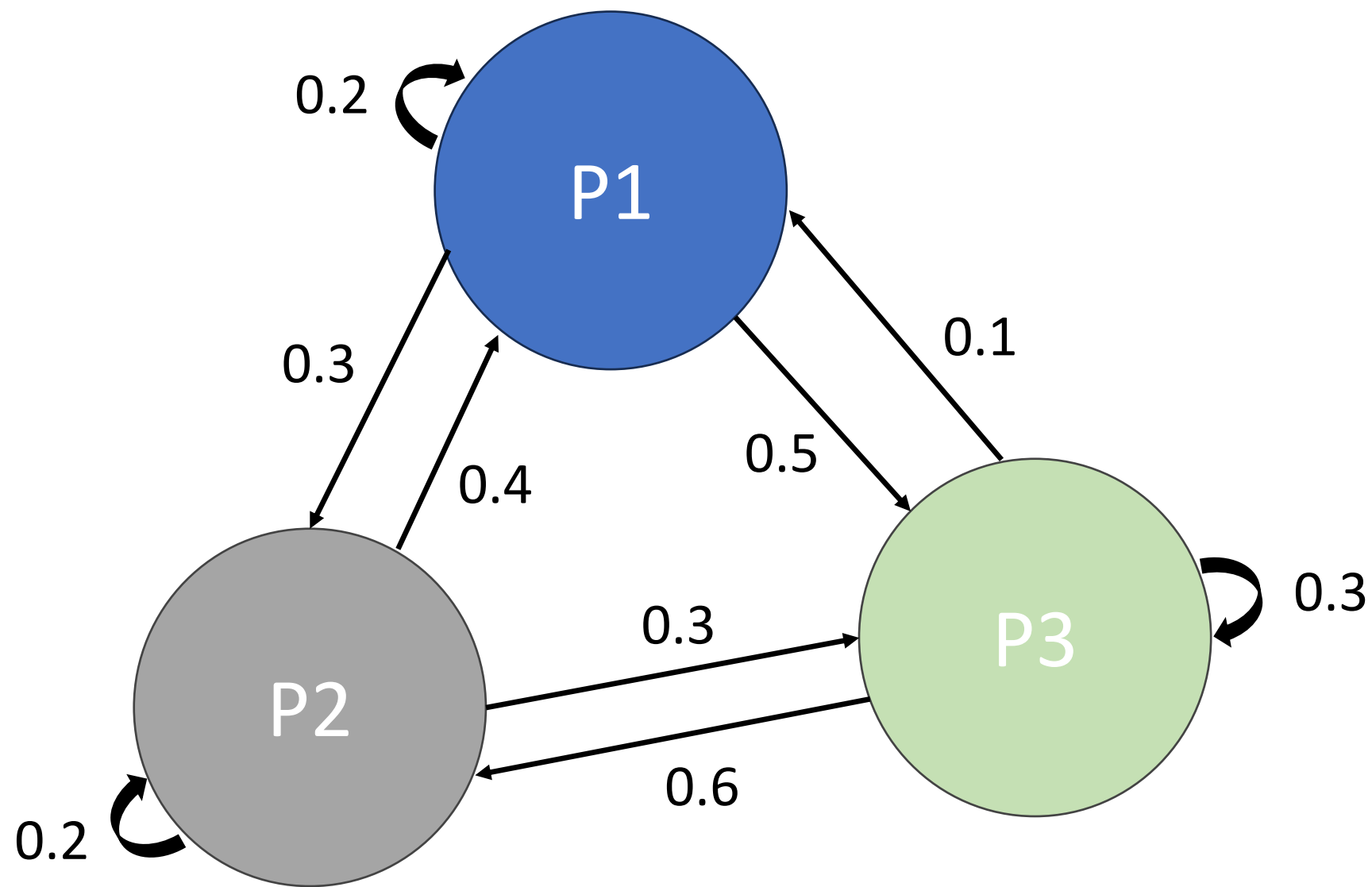
CADENAS DE MARKOV

Número finito de estados

Probabilidad de ocurrencia de un evento depende del suceso inmediatamente anterior

Las probabilidades permanecerán constantes en el tiempo

CADENAS DE MARKOV



MATRIZ DE TRANSICIÓN

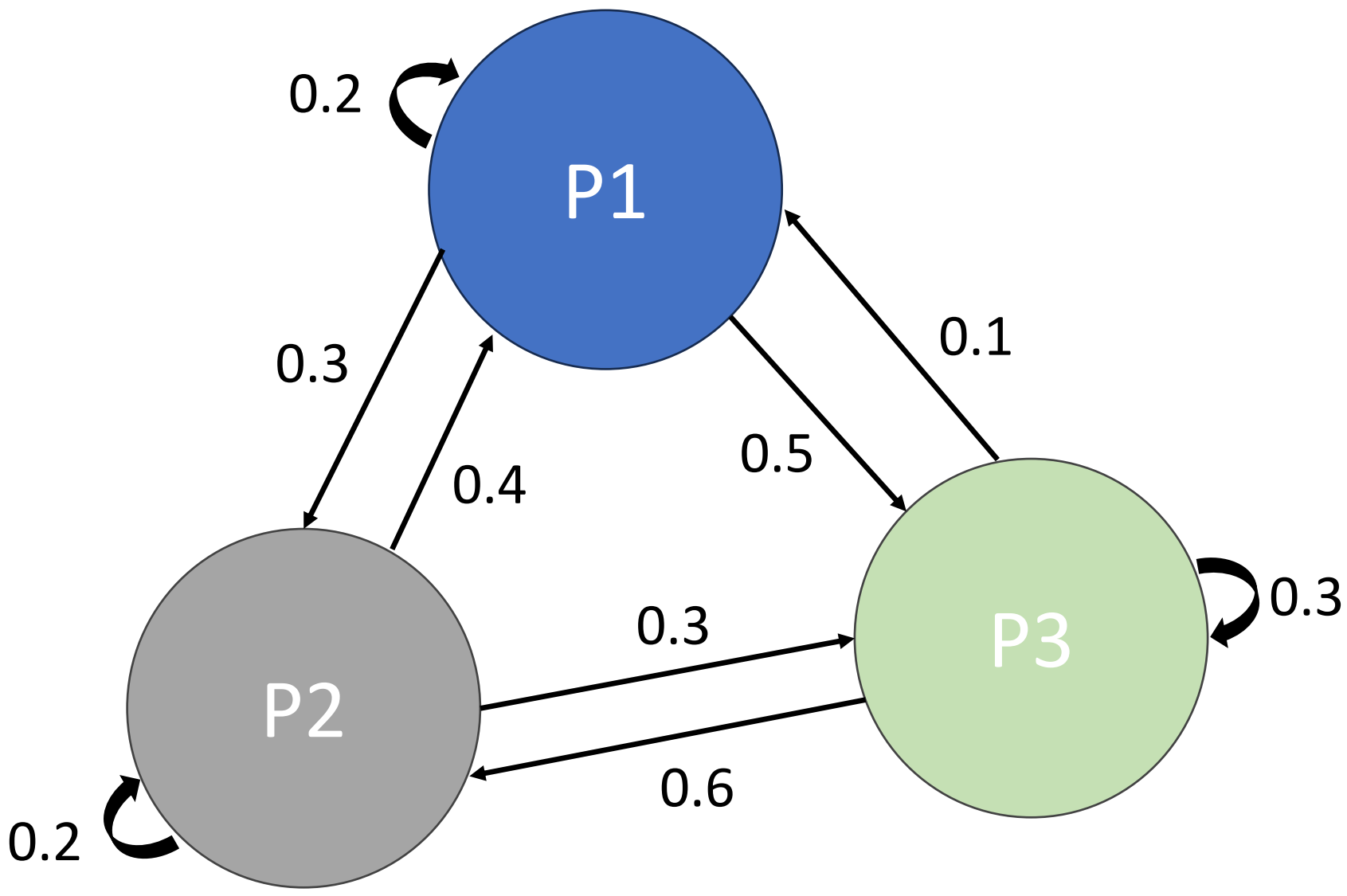
	P1	P2	P3
P1	2	3	5
P2	4	2	4
P3	1	6	3

ESTADO INICIAL

M_0

M_1

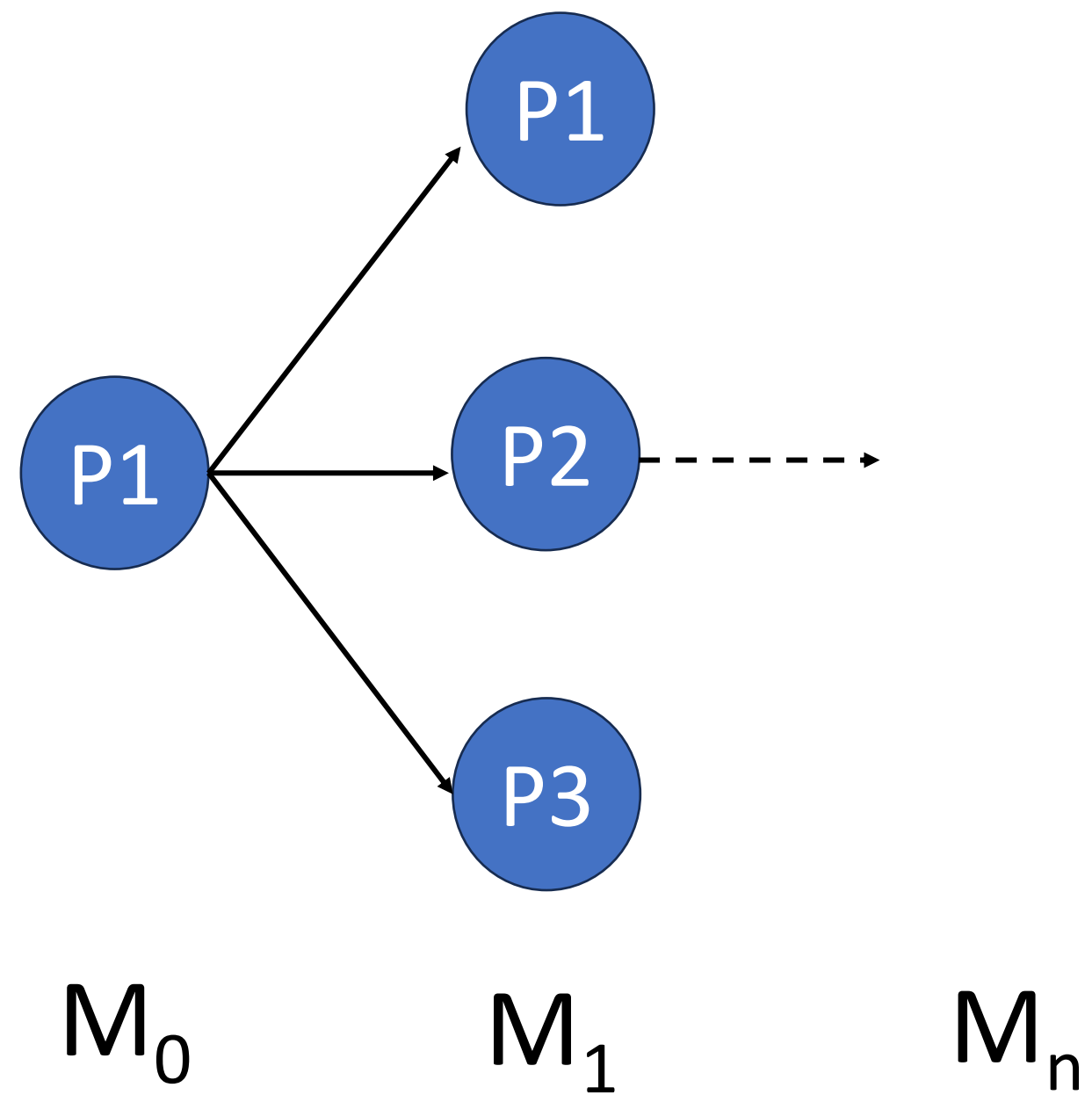
CADENAS DE MARKOV



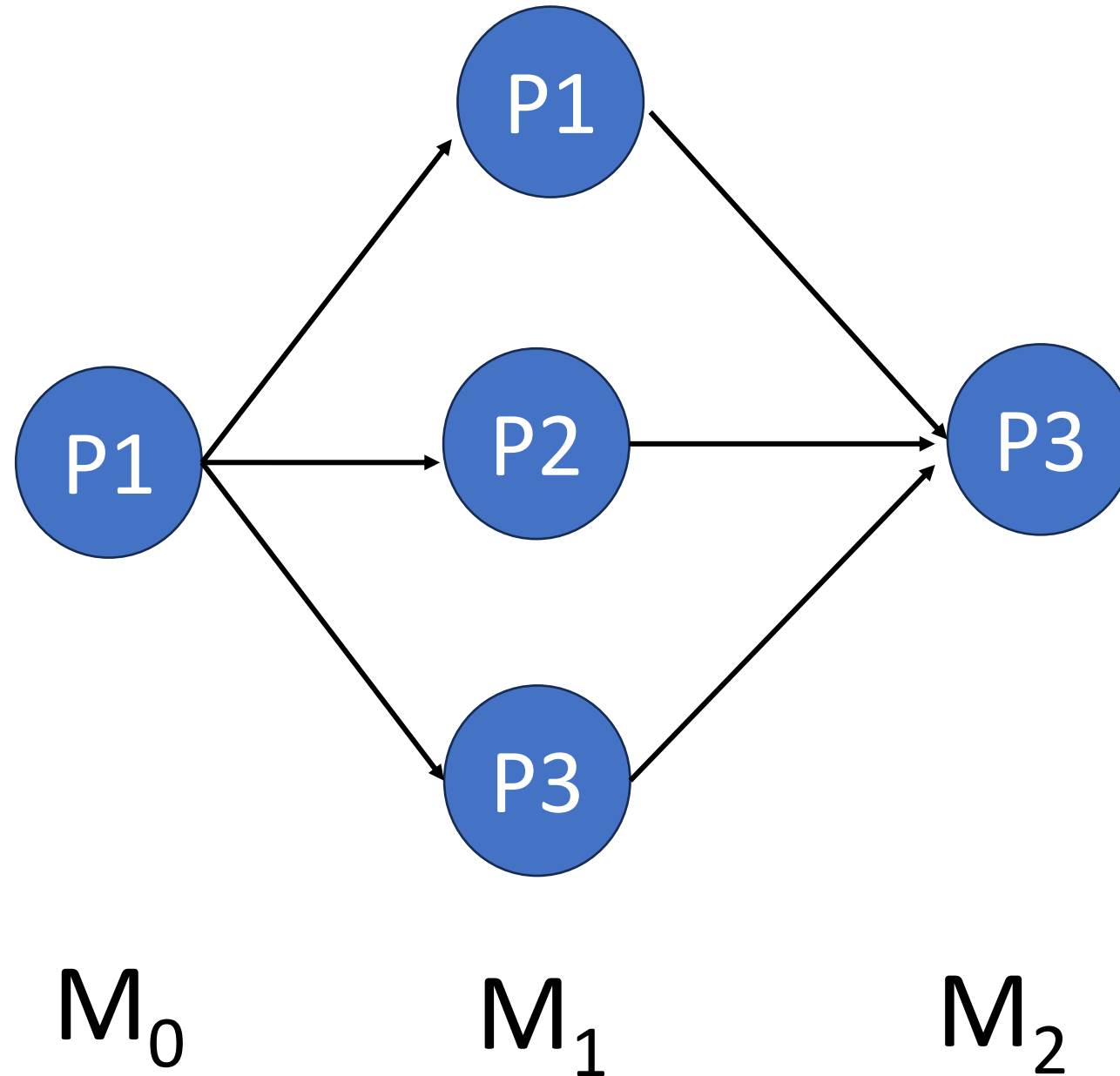
	P1	P2	P3
P1	2	3	5
P2	4	2	4
P3	1	6	3

<i>P1P1</i>	<i>P1P2</i>	<i>P1P3</i>
<i>P2P1</i>	<i>P2P2</i>	<i>P2P3</i>
<i>P3P1</i>	<i>P3P2</i>	<i>P3P3</i>

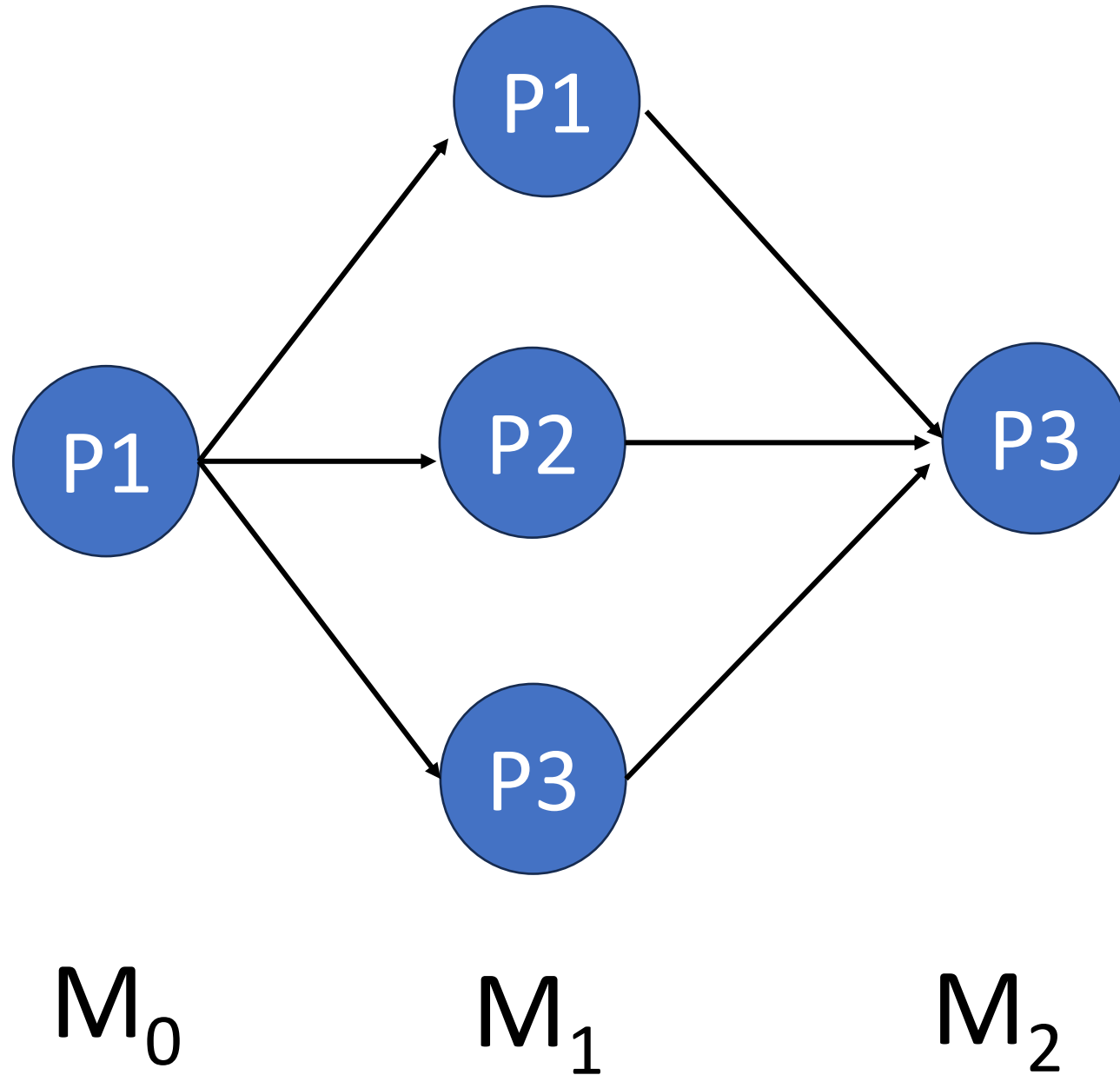
CADENAS DE MARKOV



MATRIZ DE DOS PASOS



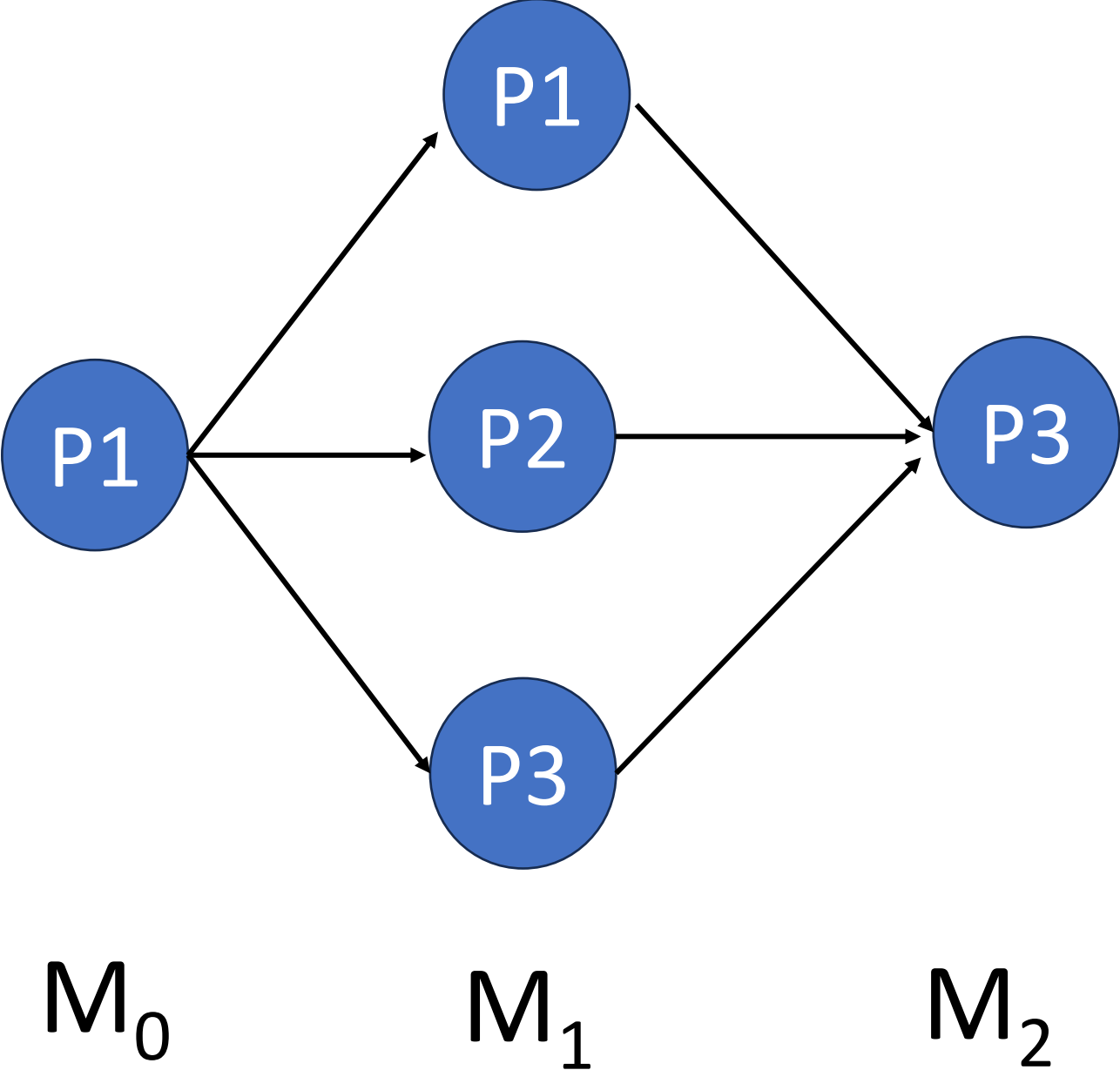
MATRIZ DE DOS PASOS



$P1P1$	$P1P2$	$P1P3$
$P2P1$	$P2P2$	$P2P3$
$P3P1$	$P3P2$	$P3P3$

$P1P1+P1P2+P1P3+P1P3+P2P3+P3P3$

MATRIZ DE DOS PASOS



$P1P1$ $P1P2$ $P1P3$
 $P2P1$ $P2P2$ $P2P3$
 $P3P1$ $P3P2$ $P3P3$

$P1P1+P1P2+P1P3+P1P3+P2P3+P3P3$

$P1P1$	$P1P2$	$P1P3$
$P2P1$	$P2P2$	$P2P3$
$P3P1$	$P3P2$	$P3P3$

MATRIZ DE DOS PASOS

	P1	P2	P3
P1	2	3	5
P2	4	2	4
P3	1	6	3

*

	P1	P2	P3
P1	2	3	5
P2	4	2	4
P3	1	6	3

$$2(2)+3(4)+5(1) = 21$$

$$2(3)+3(2)+5(6) = 42$$

$$2(5)+3(4)+5(3) = 37$$

21	42	37
—	—	—
—	—	—

MATRIZ DE TRANSICIÓN

	P1	P2	P3			P1	P2	P3	
P1	2	3	5			P1	2	3	5
P2	4	2	4	*		P2	4	2	4
P3	1	6	3			P3	1	6	3

MATRIZ DE DOS PASOS

	P1	P2	P3	
P1	2	3	5	*
P2	4	2	4	
P3	1	6	3	

	P1	P2	P3
P1	2	3	5
P2	4	2	4
P3	1	6	3

$$2(2)+3(4)+5(1)=21$$

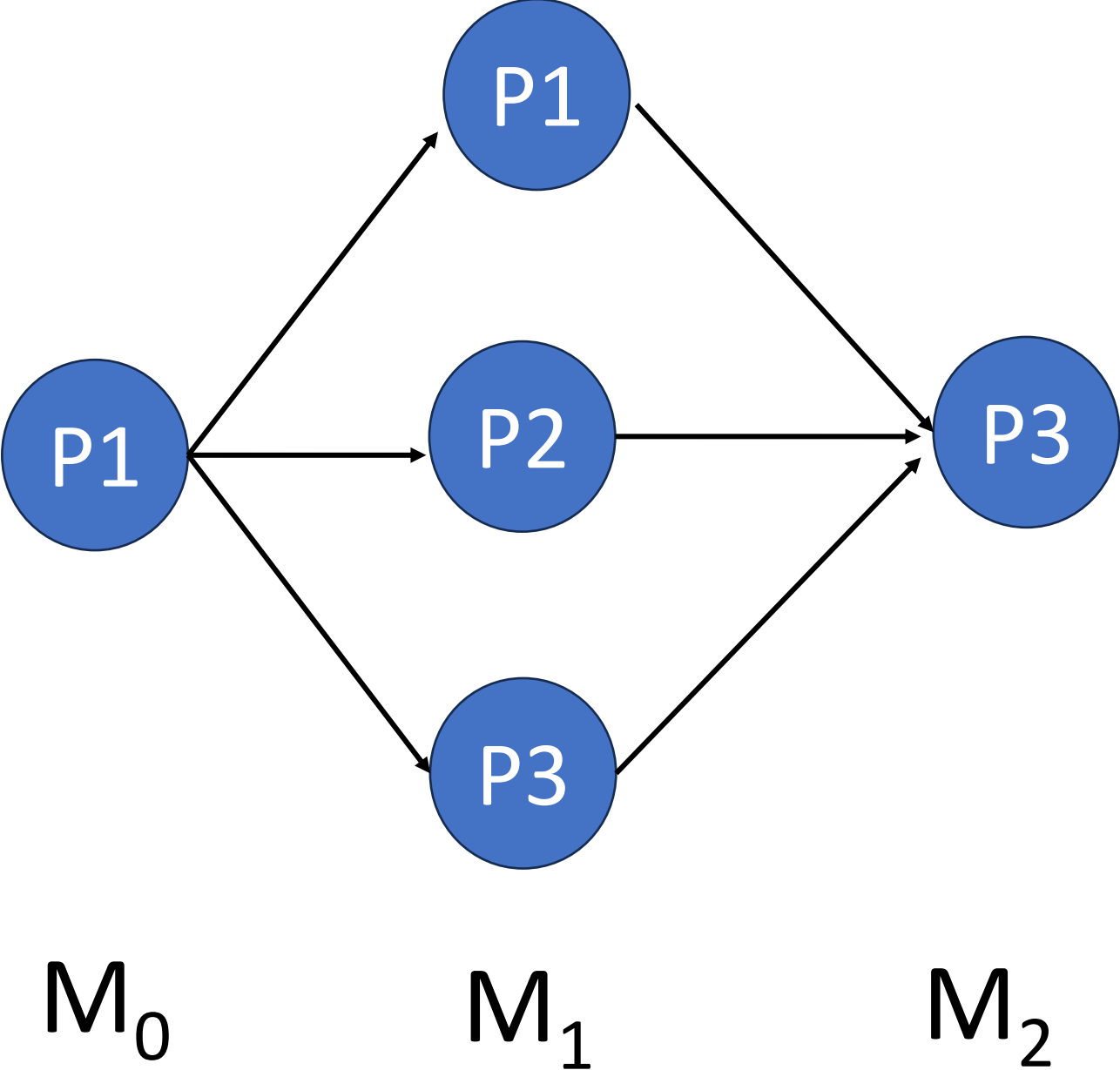
$$2(3)+3(2)+5(6)=42$$

$$2(5)+3(4)+5(3)=37$$

21	42	37
20	40	40
30	33	38

$$M_n = [M1]^n$$

MATRIZ DE DOS PASOS

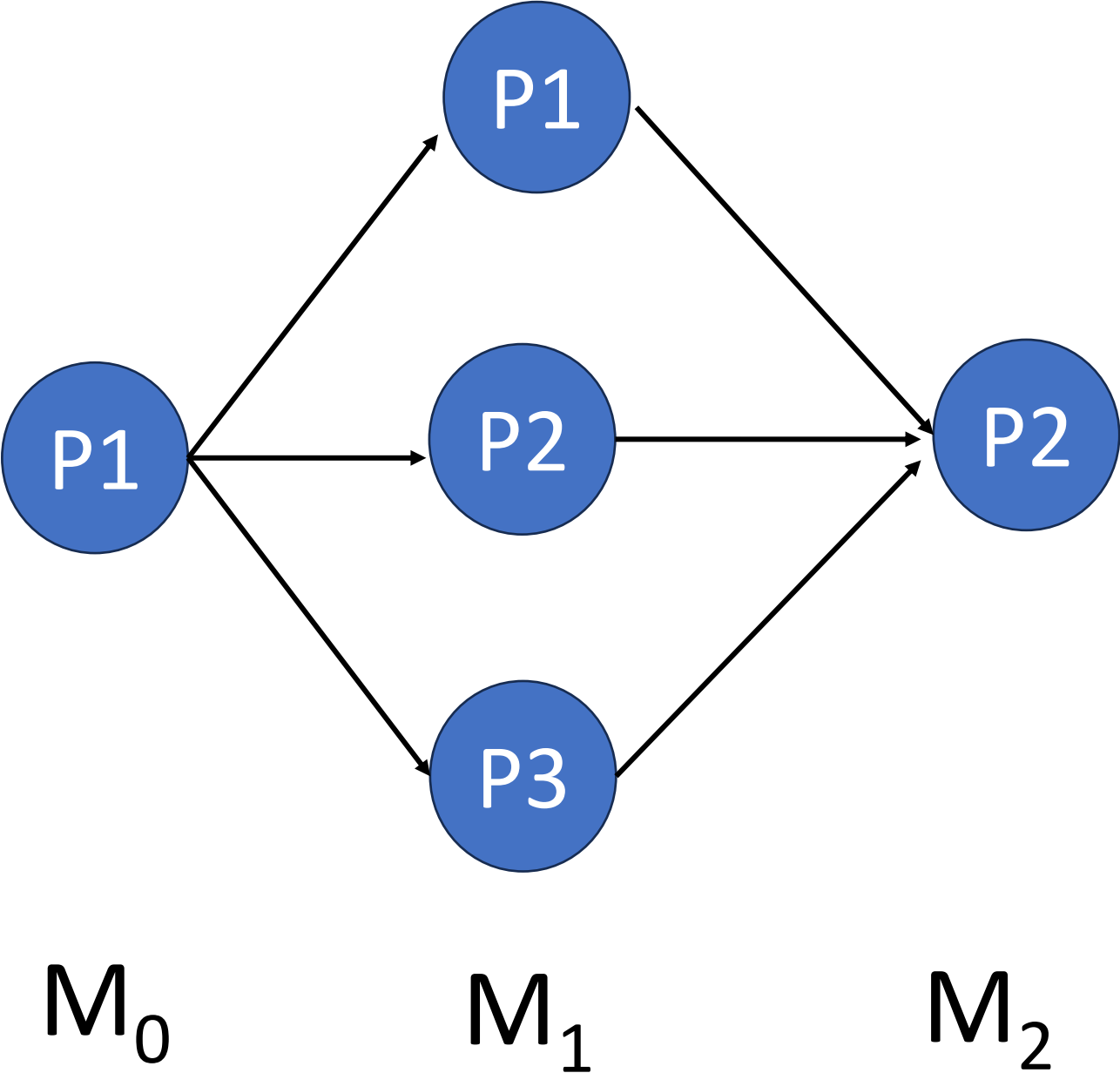


$P1P1$	$P1P2$	$P1P3$
$P2P1$	$P2P2$	$P2P3$
$P3P1$	$P3P2$	$P3P3$

$P1P1+P1P2+P1P3+P1P3+P2P3+P3P3$

21	42	37
20	40	40
30	33	38

MATRIZ DE DOS PASOS

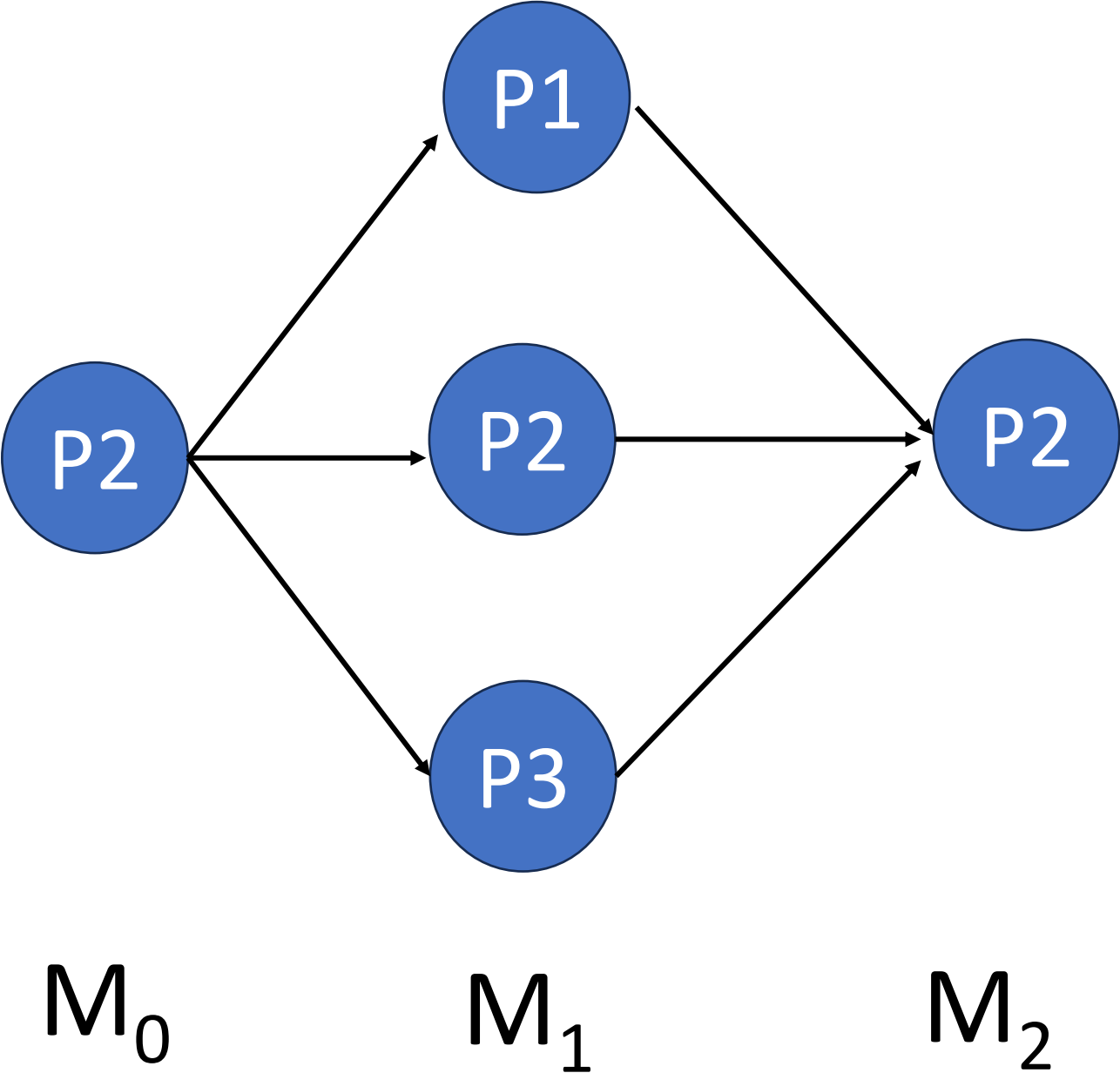


$P1P1$	$P1P2$	$P1P3$
$P2P1$	$P2P2$	$P2P3$
$P3P1$	$P3P2$	$P3P3$

$P1P1+P1P2+P1P3+P1P2+P2P2+P3P2$

21	42	37
20	40	40
30	33	38

MATRIZ DE DOS PASOS



P_1P_1	P_1P_2	P_1P_3
P_2P_1	P_2P_2	P_2P_3
P_3P_1	P_3P_2	P_3P_3

$P_2P_1 + P_2P_2 + P_2P_3 + P_1P_2 + P_2P_2 + P_3P_2$

21	42	37
20	40	40
30	33	38

