

Motivation of choice

In this exercise we decided to use an `AdaptableHeapPriorityQueue` because it was the only data structure that allowed us to have a maximum logarithm complexity for the most expensive operations, i.e. `remove_min`, `add` and `update`, thus allowing us to achieve the best performance.

Computational Complexity

For the computation complexity calculation we will consider only the portion of code inside the `while(true)`.

In the first part of the function the only operations that have a time complexity greater than $O(1)$ are the `add()` and the `remove_min()` method of the `AdaptableHeapPriorityQueue`, that have a complexity of $O(\log(n))$.

In the second part (when we update the priority of the jobs) there is an for-loop on the n elements of the queue. In this loop there is also the update method of the priority queue that has an computation complexity of $O(\log(n))$. So, this loop has a complexity of $O(n \cdot \log(n))$.

Therefore, the whole algorithm has an computational complexity equal to:

$$O(\log(n)) + O(n \cdot \log(n)) = O(n \cdot \log(n))$$

If we also consider the cycles of the CPU, the computational complexity of the algorithm will be multiplied by the sum of the length of all the jobs. As a result we will have:

$$O(n \cdot \log(n)) * \sum_{i=1}^n apq_data[i] _value.length$$